

Beam asymmetry Σ measurements of π^- photoproduction on neutrons

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The Σ -beam asymmetry in the photoproduction of negative pions on quasi-free neutrons in a deuterium target was measured at the Grenoble Anneau Accélérateur Laser in the energy interval 700–1500 MeV and over a wide angular range, using polarized and tagged photons. Results are compared with recent partial-wave analyses.

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I. INTRODUCTION

During the last 20 years, pseudoscalar meson photoproduction has proven to be a valid and complementary approach to hadronic reactions for the study of properties of baryon resonances. The main disadvantage of the electromagnetic probe, that is, the lower cross-section values, has been overcome thanks to the advent of a new generation of high-duty cycle electron accelerators and to the resulting high-intensity real and virtual photon beams. These beams, in combination with large-solid-angle and/or high-momentum acceptance detectors, have recently provided a large amount of high-precision data.

Pseudoscalar meson photoproduction can be described in terms of four complex CGLN [1] (or, equivalently, helicity) amplitudes, providing seven real independent quantities for each set of incident photon energy and meson polar angle in the center-of-mass (c.m.) system. To resolve the ambiguities in the context of Barker *et al.* [2], it is necessary to perform a “complete experiment.” That is, eight polarization observables (including the unpolarized differential cross section) need to be measured for each isospin channel. Waiting for such an experiment, the analysis of meson photoproduction has concentrated on a description of the reaction mechanisms in terms of intermediate states, which have definite parity and angular momentum and are therefore excited via electric and magnetic multipoles.

Polarization observables, accessible with the use of polarized photon beams and/or nucleon targets and/or measurement of the polarization of the recoil nucleon, play a special role in the disentanglement of hadron resonances contributing to the reaction [3–7].

One further complication in the study of meson photoproduction on nucleons comes from the isospin, which must be conserved at the hadronic final vertex, while it can be changed at the photon vertex. In particular, for isovector mesons, such as pions, the transition operator can be split into an isoscalar ($\Delta I = 0$) and an isovector ($\Delta I = 1$) component, giving rise to three independent matrix elements $\langle I_f, I_{f,z} | A | I_i, I_{i,z} \rangle$ describing the transitions between the initial and the final states: one isoscalar A^{IS} (with ΔI and $\Delta I_3 = 0$) and two isovector A^{IV} and A^{V3} ($\Delta I = 1$ and $\Delta I_3 = 0, \pm 1$) components. It is necessary to perform experiments on the proton and neutron for each final-state isospin channel to disentangle these transition amplitudes [8,9].

Data on the four reactions ($\gamma p \rightarrow \pi^0 p$, $\gamma p \rightarrow \pi^+ n$, $\gamma n \rightarrow \pi^0 n$, $\gamma n \rightarrow \pi^- p$) have been collected at the Grenoble Anneau Accélérateur Laser (GRAAL), with a polarized photon beam impinging on a H₂ or D₂ liquid target and with the final products detected in a large-solid-angle apparatus. This allowed, for the first time, the simultaneous extraction of the beam asymmetry values of the four reactions under the same experimental conditions and the same photon energy range (0.55–1.5 GeV) corresponding to the second and third nucleon resonance regions. Results for the first three reactions have been published by the GRAAL Collaboration [10–12], providing, for pion photoproduction on the nucleon, a very

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extensive database of high-precision data composed of 830 differential cross-section and 437 beam asymmetry points for π^0 photoproduction on free protons, about 300 beam asymmetry points for π^+n photoproduction on free protons, and 216 asymmetry points for π^0 photoproduction on both quasi-free protons and neutrons.

The last of the four reactions is the subject of the present article. Extraction of the beam asymmetry values for π^-p photoproduction on quasi-free neutrons advances the isospin study of pion photoproduction on nucleons, constraining the determination of the three isoscalar and isovector transition amplitudes.

II. EXPERIMENTAL SETUP

The GRAAL γ -ray beam at the European Synchrotron Radiation Facility (ESRF) is produced by the backward scattering in flight of laser photons on the relativistic electrons circulating in the storage ring. This technique, first used on a storage ring for the LADON beam on the ADONE at Frascati [13], produces polarized and tagged γ -ray beams with a very high polarization and good energy resolution. At its maximum energy the beam polarization is very close to one of the laser photons (linear or circular) [14] and can be easily rotated or changed with conventional optical components that change the polarization of the laser light. It remains above 74% for photon energy above 70% of its maximum. With the 6.03-GeV ESRF accelerator and the 351-nm line of an argon (ion) laser, the maximum γ -ray energy obtainable is 1487 MeV and the spectrum is almost flat over the whole tagged spectrum. The energy resolution of the tagged beam is limited by the optics of the ESRF magnetic lattice and is 16 MeV (FWHM) over the entire spectrum.

The GRAAL apparatus has been described in several papers [10–12, 15–17]. A cylindrical liquid hydrogen (or deuterium) target is located on the beam and coaxial with it. The detector covers the entire solid angle and is divided into three parts. The central part, $25^\circ < \theta \leq 155^\circ$, is covered by two cylindrical wire chambers, a barrel made of 32 plastic scintillators, and a BGO crystal ball made of 480 crystals, which is well suited for the detection of γ rays of an energy below 1.5 GeV. The chambers, the barrel, and the BGO are all coaxial with the beam and the target. The wire chambers detect and measure the positions and angles of the charged particles emitted by the target, while the scintillating barrel measures their energy loss. The BGO ball detects charged and neutral particles and measures the energy deposited by them. For neutral particles it provides a measurement of their angles by its granularity (480 crystals: 15 in the θ direction and 32 in the ϕ direction).

At forward angles, $\theta \leq 25^\circ$, the particles emitted from the target encounter, first, two-plane wire chambers that measure their angles, then, at 3 m from the center of the target, two planes of plastic scintillators, made of 26 horizontal and 26 vertical bars to measure the particle position, specific ionization, and time of flight (TOF), and then a thick (shower wall) wall made of a sandwich of scintillators and leading to detection of charged particles, γ rays, and neutrons. The TOF resolution of these scintillators is of the order of 560 ps (FWHM) for charged particles and 900 ps for neutrons. The total thickness

of the plastic scintillators is 20 cm and the detection efficiency is about 20% for neutrons and 95% for γ rays.

Backward angles, $\theta > 155^\circ$, are covered by two disks of plastic scintillators separated by 6 mm of lead to detect charged particles and γ rays escaping in the backward direction. The energy of the γ rays is provided by the tagging setup, which is located inside the ESRF shielding, attached to the ESRF vacuum system. The electrons that scatter off a laser photon and produced a γ ray have lost a significant fraction of their energy and, therefore, drift away from the equilibrium orbit of the stored electrons and, finally, hit the vacuum chamber of the storage ring. Before hitting the vacuum chamber they are detected by the tagging system, which measures their displacement from the equilibrium orbit. This displacement is a measure of the difference between their energy and that of the stored electron beam and, therefore, provides a measure of the energy of the γ ray produced. The tagging system [11] consists of 10 plastic scintillators and a 128 channel solid-state microstrip detector with a pitch of 300 μm . The plastic scintillator signals are synchronized by GaAs electronics with a radio-frequency accelerating system, and provide a timing for the entire electronics of the GRAAL apparatus with a resolution of 180 ps (FWHM). This allows clear discrimination between electrons coming from two adjacent electron bunches that are separated by 2.8 ns. The microstrips provide the position of the scattered electron and therefore the energy of the associated γ ray. Their pitch (300 μm) has been set to limit the number of tagging channels without an appreciable reduction in the γ -ray energy resolution imposed by the characteristics of the storage ring. The detector is located inside a shielding box positioned in a modified section of the ring vacuum chamber. The shielding box is positioned 10 mm from the circulating electron beam. This limits the lowest tagged γ -ray energy to about 550 MeV.

III. EVENT IDENTIFICATION AND DATA ANALYSIS

Data analysis is based on the following direct measurements: the energy E_γ of the incident photon measured by the tagging detector, the energy E_p of the proton measured in the BGO or by the TOF in the forward wall, and the polar and azimuthal angles θ_p and ϕ_p of the proton and θ_{π^-} and ϕ_{π^-} of the pion measured by the planar and cylindrical MWPCs [19]. The energy of the pion E_{π^-} is obtained by the reaction energy balance neglecting the Fermi energy of the neutron in the deuterium target ($E_{\pi^-} = E_\gamma + M_n - E_p$).

The charged particle identification in the central part of the apparatus ($25^\circ < \theta \leq 155^\circ$) was performed using a cut in the bidimensional plot of the energy lost in the barrel versus the energy measured by the BGO calorimeter [18]. In the forward direction ($\theta \leq 25^\circ$) it was obtained using the bidimensional cut on energy lost versus TOF measured by the plastic scintillator wall [18]. We also applied to each charged particle detected the condition that a coincidence of the signals from the three charged particle detectors be obtained.

Our simulation, based on GEANT3 [20] and on a realistic event generator [21], has shown that, with the preliminary selection of events obtained by the constraint that a proton and pion are the only charged particles detected in the GRAAL

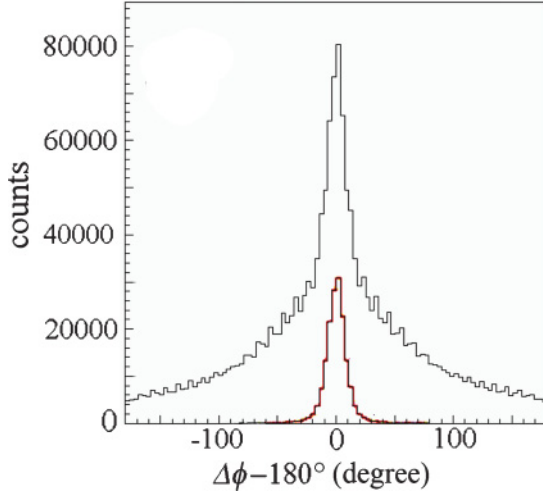


FIG. 1. (Color online) The π^- - p coplanarity before (upper curve) and after the cuts (lower curve).

apparatus, the number of events coming from other reaction channels is lower than 14%.

The quantities measured in the GRAAL experiment exceed the number required for a full kinematical reconstruction of the event in a (quasi-)two-body kinematics. Therefore it is possible to calculate all kinematic variables using only a subset of the measured ones. For example, the polar angle of the pion $\theta_{\pi^-}^{\text{calc}}$ and the energy of the proton E_p^{calc} were calculated from the other measured quantities and then compared with the results of their direct observations.

Therefore the background from the other reaction channels was drastically reduced by the following constraints.

- (i) We reject all events with additional signals from neutral particles in the BGO or in the shower wall.
- (ii) We impose coplanarity of the p and π^- by the condition $|\phi_{\pi^-} - \phi_p| - 180^\circ < 3\sigma_\phi$, where σ_ϕ is the experimental variance of the distribution indicated in Fig. 1.
- (iii) We impose the condition

$$\sqrt{\sum_i^{x,y,z} (P_{Fi} - P_{Fi}^{\text{recurs}})^2} < 10 \text{ MeV}/c, \quad (1)$$

where P_{Fi} ($i = x, y, z$) is the component of the Fermi momentum of the target nucleus calculated from the measured kinematical variables neglecting its Fermi energy; P_{Fi}^{recurs} is its value obtained at the end of a recursive process in which, at each stage, the Fermi momentum is calculated by inserting into the energy-momentum conservation equations the value of the Fermi energy derived by the value of the Fermi momentum resulting from the previous iteration. The iterations stop when the difference in the modules of the Fermi momentum in two successive iterations is less than 10 keV/ c . The cut value, 10 MeV/ c , was suggested by the simulation to minimize the loss of good events (see Fig. 2).

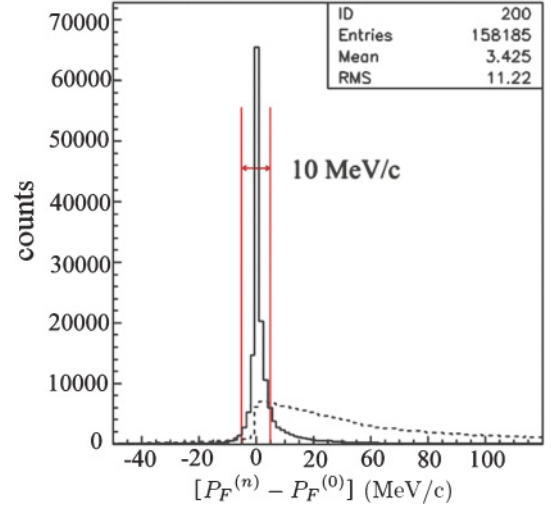


FIG. 2. (Color online) Difference between the Fermi momentum reconstruction at the n th step in the recursive method and at step 0 for the signal (solid line) and for the concurrent channels (dashed line) in the simulation.

- (iv) The last constraint is

$$\frac{(x - \mu_x)^2}{\sigma_x^2} + \frac{(y - \mu_y)^2}{\sigma_y^2} - \frac{2C(x - \mu_x)(y - \mu_y)}{\sigma_x \sigma_y} < \sigma^2, \quad (2)$$

where $x = \Delta\theta = \theta_{\pi^-}^{\text{calc}} - \theta_{\pi^-}^{\text{meas}}$, $\theta_{\pi^-}^{\text{meas}}$ is the measured angle of the π^- , while $\theta_{\pi^-}^{\text{calc}}$ is the calculated value from the angle θ_p of the proton and the γ -ray energy E_γ provided by the tagger; $y = R_p = E_p^{\text{calc}}/E_p^{\text{meas}}$, where E_p^{meas} is the measured value of the proton energy and E_p^{calc} is the calculated value from E_γ and θ_{π^-} ; μ_x , μ_y , σ_y , and σ_x are the mean values and the variances obtained by a Gaussian fit to the experimental distributions; and C is the correlation parameter obtained by a combined best fit of x and y with a bidimensional Gaussian surface (see Fig. 3). σ was empirically set at 3, after several attempts, to

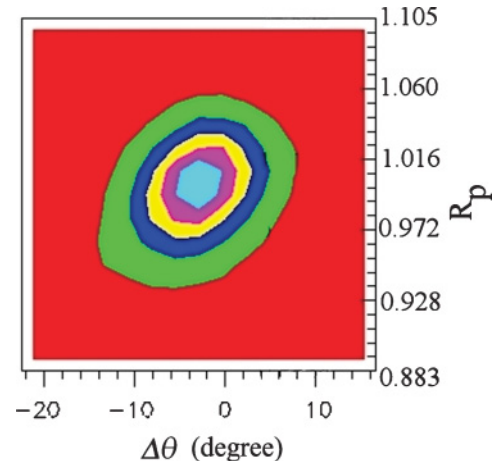


FIG. 3. (Color online) Bidimensional distribution of $\Delta\theta$ vs. R_p as defined in this article.

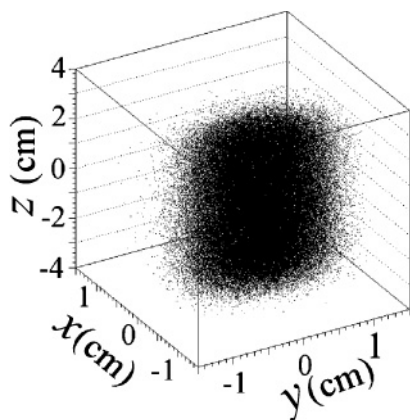


FIG. 4. Reconstructed position of the production vertex.

minimize the loss of good events and, at the same time, the acceptance of events from competing reactions. As a result, the contribution of spurious events is less than 2.3% as indicated by the simulation. Other systematic errors arise from our imperfect knowledge of the beam polarization owing to the laser optics and other minor effects and do not exceed 2% in total.

The wire chambers provide the distribution of the reaction vertex [19] inside the deuterium target. Figure 4 shows that the source of our events is well localized inside the liquid D_2 .

To check the invariance of our results with respect to the selection criteria in an independent analysis, we (i) plotted alternatively $\Delta\theta$ vs. $\Delta\phi - 180^\circ$, which has the advantage that the physical quantities are not correlated as shown in Fig. 5; (ii) applied an independent cut on the variable R_p ; and (iii) introduced a cut for $P_F \leq 250$ MeV/c instead of condition 3: inequality [Eq. (1)]. The results of the two procedures are consistent within 1 standard deviation [22].

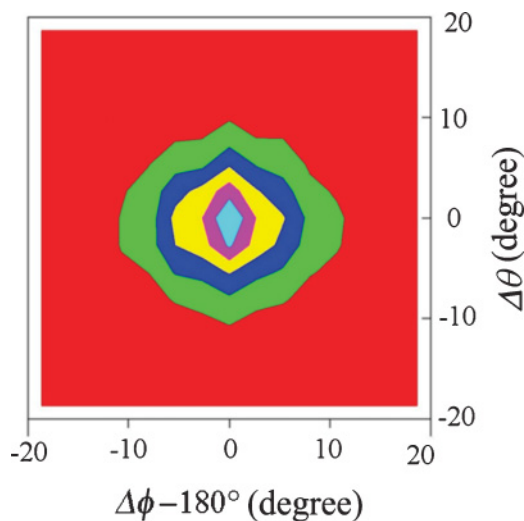
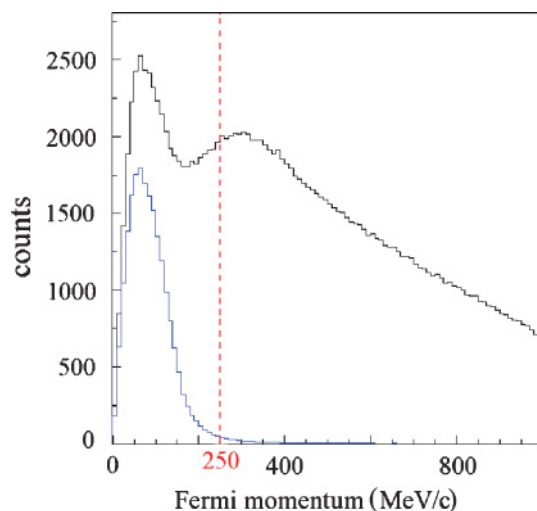
FIG. 5. (Color online) Bidimensional distribution of $\Delta\theta$ vs. $\Delta\phi - 180^\circ = |\phi_{\pi^-} - \phi_p| - 180^\circ$ as defined in this article.

FIG. 6. (Color online) Fermi momentum of the neutron calculated before (upper curve) and after (lower curve) the cuts.

As a further check we plotted (see Fig. 6) the Fermi momentum calculated for all events (spurious included) and that calculated for the “good” events (those that have passed our selection).

The effect of the cuts on the degree of coplanarity of the reaction products and on the Fermi momentum is indicated in Figs. 1 and 6, respectively.

Our simulation data show that the Gaussian fit of the difference between the Fermi momentum reconstructed by our detectors and the one generated using the Paris potential [23] present a σ of about 16.9 MeV/c. The cuts provide a distribution of the Fermi momentum consistent with our knowledge of the structure of the deuteron excluding the spurious events that would require an anomalously high Fermi momentum to satisfy a quasi-two-body kinematic. Figure 7 compares the experimental and simulated Fermi momentum distributions. For the simulation we used the Paris potential

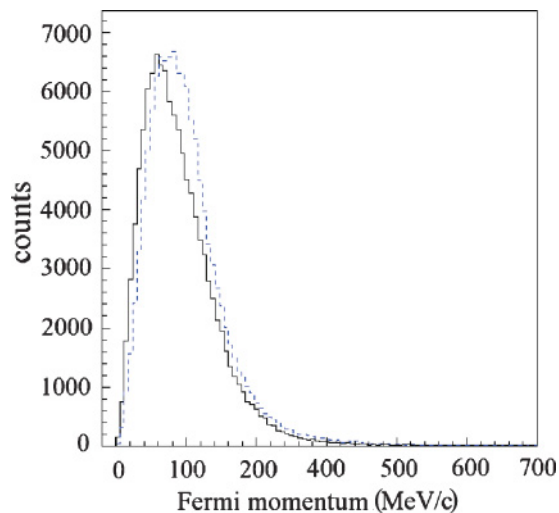


FIG. 7. (Color online) Fermi momentum (dashed line) of the neutron after the cuts (data) and Fermi momentum (solid line) generated using the Paris potential.

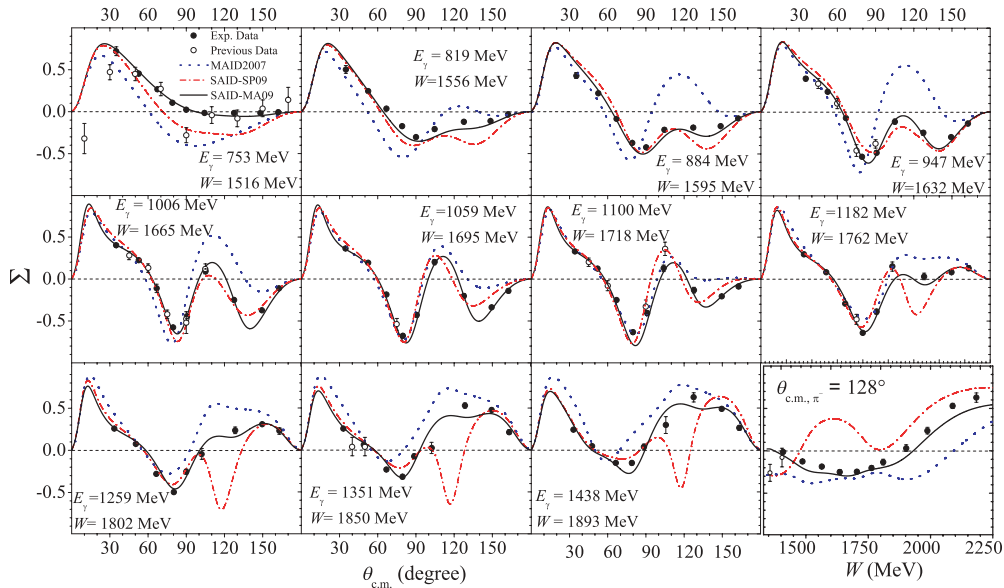


FIG. 8. (Color online) Beam polarization asymmetries for $\gamma n \rightarrow \pi^- p$ versus pion center-of-mass scattering angle. The photon energy is shown. Solid (dash-dotted) lines correspond to the SAID MA09 (SP09 [26]) solution. Dotted lines give the MAID2007 [27] predictions. Experimental data are from the current (filled circles) and previous [24,25] (open circles) measurements. Plotted points from previously published experimental data are data points within 4 MeV of the photon energy indicated in each panel. Plotted uncertainties are statistical. In the last panel the asymmetries are plotted versus the γ -ray energy for the c.m. angle of 128° . The MA09 includes in its database the GRAAL asymmetries for the $\gamma n \rightarrow \pi^- p$ and $\gamma n \rightarrow \pi^0 n$ [12] reactions. SP09 and MAID2007 do not include these data.

[23] and processed the simulated events through the same analysis software of our data.

The beam polarization asymmetries were calculated as we did in Refs. [11], [12], and [16], using the symmetry of the central detector around the beam axis. The various checks performed to verify the stability of our results are indicated in the same references. More than 99% of the events that survived the cuts produce a reconstructed Fermi momentum lower than 250 MeV/c. For this reason the results presented in Fig. 8 and in Table I were obtained without any direct cut on the reconstructed Fermi momentum distribution. We refer to Ref. [11] for a discussion of possible sources of systematic errors; in particular, we have shown that we obtain the same asymmetries, in the overlapping region, using the Green or UV laser lines. These lines produce γ -ray beams with different spectra and polarizations, and their comparison eliminates one main source of systematic errors.

IV. RESULTS AND DISCUSSION

In this paper, we report the first tagged measurement of the $\gamma n \rightarrow \pi^- p$ reaction by the GRAAL Collaboration in the energy range from 753 to 1438 MeV. The available statistics allowed the determination of the angular σ -beam asymmetry for 11 bins in the incident-photon energy and 9 angular bins.

Our results for the asymmetries are shown in Fig. 8 together with previous results [25] and some theoretical models. The GRAAL data and the results of previous untagged measurements [25] appear to agree well in the overlapping energies. As we have shown in Ref. [12] and also in this analysis, we

have obtained the same asymmetries using independently two different sets of criteria for the event selection. Moreover, the close similarity between the asymmetries measured on the free proton (in hydrogen) and those on the quasi-free proton (in deuterium) encourages the assumption that the asymmetries measured on the quasi-free neutron (in deuterium) could be close to those on free neutrons.

Multipole amplitude analyses provide a powerful tool for extracting information about the reaction process in a manner as nearly model independent as possible [26]. This approach, in turn, facilitates the identification of s -channel resonances involved in the reaction process.

SAID-MA09 is the solution that includes our results and recent GRAAL results for $\gamma n \rightarrow \pi^0 n$ [12] in the best fit, while SAID-SP09 does not include both of them [26]. The earlier MAID2007 solution [27] is also included in Fig. 8 for comparison. The status of the MAID database for the MAID2007 solution is the same as that for SAID-SP09. The overall χ^2 /GRAAL data are 483, 2634, and 8793 per 99 GRAAL Σ s for the SAID-MA09, SAID-SP09, and MAID2007 solutions, respectively.

The SAID-SP09 solution is consistent with our data in the forward angular region where previous results constrained the fit. In the backward region and at energies above 1100 MeV, the agreement becomes satisfactory only after inclusion of our data. The MAID2007 solution agrees with our data in the forward region. Both the SAID-SP09 and the MAID2007 results exhibit structures not seen in the data and that explain the poor χ^2 for both cases.

Neutron multipoles from the SAID-MA09 fit are compared to the earlier SAID-SP09 determinations in Fig. 9. Both MA09

TABLE I. Beam asymmetry Σ values for photon energies E_γ ranging from 753 to 1438 MeV. Errors are statistical only.

$\theta_{c.m.}$ (deg)	$E_\gamma = 753$ MeV	$\theta_{c.m.}$ (deg)	$E_\gamma = 820$ MeV	$\theta_{c.m.}$ (deg)	$E_\gamma = 884$ MeV	$\theta_{c.m.}$ (deg)	$E_\gamma = 947$ MeV
35.1	0.721 ± 0.053	35.0	0.504 ± 0.046	35.2	0.431 ± 0.034	35.1	0.396 ± 0.026
52.6	0.453 ± 0.026	52.5	0.244 ± 0.015	52.5	0.219 ± 0.016	52.5	0.237 ± 0.012
67.2	0.267 ± 0.022	66.9	0.034 ± 0.014	66.9	-0.087 ± 0.017	66.7	-0.074 ± 0.017
79.3	0.106 ± 0.019	79.1	-0.173 ± 0.019	79.3	-0.369 ± 0.016	79.5	-0.534 ± 0.020
89.9	0.023 ± 0.018	90.0	-0.301 ± 0.019	90.3	-0.426 ± 0.022	90.6	-0.485 ± 0.024
104.2	-0.013 ± 0.021	104.5	-0.209 ± 0.023	104.6	-0.218 ± 0.026	105.2	-0.114 ± 0.029
127.5	-0.014 ± 0.019	127.8	-0.123 ± 0.021	127.3	-0.189 ± 0.021	127.4	-0.250 ± 0.028
148.2	-0.018 ± 0.014	148.5	-0.109 ± 0.010	148.7	-0.174 ± 0.012	149.2	-0.299 ± 0.014
162.1	-0.007 ± 0.025	162.3	-0.033 ± 0.029	162.4	-0.080 ± 0.022	162.5	-0.137 ± 0.026
$\theta_{c.m.}$ (deg)	$E_\gamma = 1006$ MeV	$\theta_{c.m.}$ (deg)	$E_\gamma = 1059$ MeV	$\theta_{c.m.}$ (deg)	$E_\gamma = 1100$ MeV	$\theta_{c.m.}$ (deg)	$E_\gamma = 1182$ MeV
35.0	0.400 ± 0.021	34.7	0.364 ± 0.016	34.3	0.329 ± 0.017	33.8	0.297 ± 0.023
52.5	0.226 ± 0.014	52.5	0.192 ± 0.011	52.2	0.123 ± 0.011	51.1	0.083 ± 0.011
66.7	-0.112 ± 0.014	66.7	-0.185 ± 0.013	66.7	-0.253 ± 0.016	66.2	-0.292 ± 0.011
79.6	-0.577 ± 0.017	79.7	-0.676 ± 0.024	79.8	-0.636 ± 0.024	79.9	-0.642 ± 0.018
90.7	-0.447 ± 0.021	90.7	-0.429 ± 0.026	90.8	-0.406 ± 0.027	90.7	-0.388 ± 0.030
105.1	0.094 ± 0.026	104.5	0.201 ± 0.031	104.0	0.127 ± 0.039	103.2	0.149 ± 0.054
127.5	-0.248 ± 0.021	127.8	-0.201 ± 0.025	127.7	-0.133 ± 0.034	128.1	0.032 ± 0.039
149.4	-0.374 ± 0.012	149.5	-0.336 ± 0.011	149.6	-0.204 ± 0.014	149.6	0.079 ± 0.017
162.6	-0.113 ± 0.018	162.7	-0.141 ± 0.024	162.9	-0.088 ± 0.026	163.0	0.131 ± 0.031
$\theta_{c.m.}$ (deg)	$E_\gamma = 1259$ MeV	$\theta_{c.m.}$ (deg)	$E_\gamma = 1351$ MeV	$\theta_{c.m.}$ (deg)	$E_\gamma = 1438$ MeV		
33.6	0.259 ± 0.013	33.2	0.253 ± 0.012	33.0	0.243 ± 0.011		
50.3	0.073 ± 0.013	49.0	0.065 ± 0.008	47.6	0.045 ± 0.009		
66.5	-0.280 ± 0.017	66.6	-0.236 ± 0.017	66.3	-0.152 ± 0.014		
80.0	-0.493 ± 0.021	79.5	-0.318 ± 0.027	78.9	-0.156 ± 0.023		
90.0	-0.255 ± 0.030	88.6	-0.074 ± 0.026	88.5	0.035 ± 0.036		
102.1	-0.042 ± 0.064	102.3	0.024 ± 0.067	105.6	0.297 ± 0.100		
128.4	0.238 ± 0.040	128.5	0.529 ± 0.030	127.5	0.628 ± 0.055		
149.4	0.310 ± 0.017	149.5	0.476 ± 0.021	149.3	0.489 ± 0.021		
163.1	0.229 ± 0.039	163.4	0.214 ± 0.026	163.4	0.264 ± 0.029		

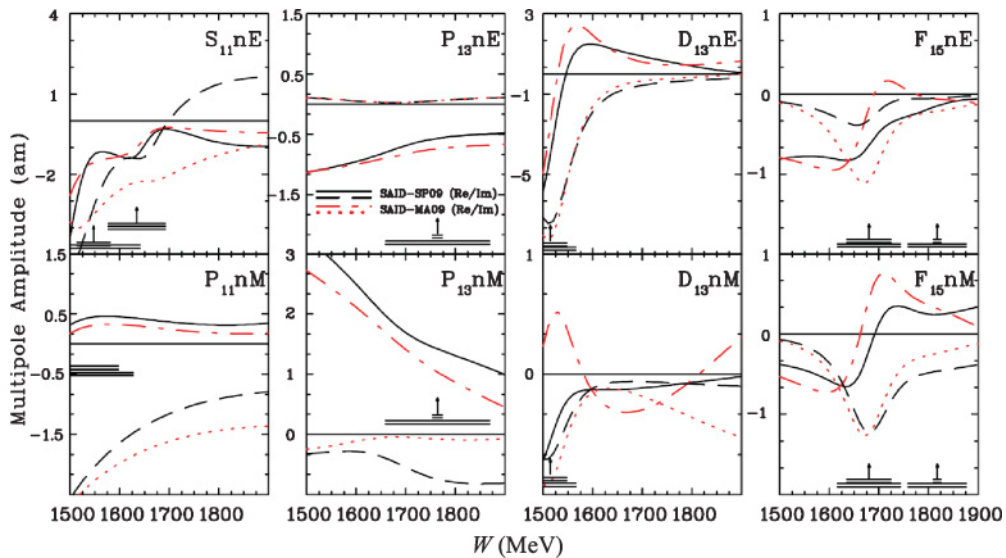


FIG. 9. (Color online) Multipole amplitudes from $W = 1500$ to $W = 1900$ MeV for isospin 1/2. Solid (dashed) lines correspond to the real (imaginary) part of the MA09 solution. Dashed-dotted (dotted) lines give the real (imaginary) part of the SP09 [26] solution. Vertical arrows indicate the position of the considered resonance, while horizontal bars show full Γ and partial widths for $\Gamma_{\pi N}$ associated with the SAID πN solution SP06 [28].

and SP09 are quite similar, but significant differences in magnitude (e.g., S_{11} , D_{13} , and F_{15}) are seen between them. With the addition of the GRAAL π^-p and π^0n asymmetries, the SAID solution is now far more reliable than in previously published analyses.

Extending our knowledge of the asymmetry to the backward direction, the results of this experiment constrain the models in the angular region where they had the largest variations and the major differences among themselves.

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