Update on α -particle and nucleon widths in ¹⁹F and ¹⁹Ne

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We present updated information and analysis for several states in ¹⁹F and ¹⁹Ne and correct a mistake in an earlier article.

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This short article concerns α -particle and/or nucleon widths for several states in ¹⁹F and ¹⁹Ne. It addresses questions arising from new experiments or calculations. Many of the states involved are of interest in connection with reaction-rate calculations in astrophysics. For each state, or set of states, we discuss the new information in the context of what was previously known.

Our recent article [1] concerned states above 6.5 MeV in ¹⁹F. Except for one of those states, the present article primarily involves only states below 6.5 MeV. Unless otherwise noted, our energies and J^{π} values are from the latest compilation. [2]

I. 19 F (3.91)/ 19 Ne (4.03)

We have made several attempts [3–5] to determine the α width of this $3/2^+$ state in ¹⁹Ne by using α transfer to its mirror in ¹⁹F. The calculated width depends somewhat on the number of oscillator quanta q assumed for the (core + α) relative motion. For the states discussed in this article, all of which have positive parity, the only reasonable values of q are 7 and 9. The $(sd)^3$ states have q = 7, while the *a*-cluster states are dominated by q = 9. Some other states could contain mixtures of the two. If the structure of a state is such that one value of q is clearly indicated, we present calculations only for that q. If ambiguity exists, or the state likely contains both q = 7 and q = 9, we give results for both.

In an α -transfer experiment, the spectroscopic factor S_{α} is proportional to $\sigma_{exp}/\sigma_{DWBA}$, while the α width is given by $\Gamma_{\alpha} = S_{\alpha} \Gamma_{sp}$. Calculations of σ_{DWBA} and Γ_{sp} involve what some have called "nuisance parameters"—such as the number of quanta q or the geometrical parameters of the α -particle well. Because σ_{DWBA} and Γ_{sp} behave similarly with changes in these parameters, the dependence on them of Γ_{α} nearly vanishes. Some authors have claimed—incorrectly—that α widths extracted from α -transfer experiments can be wrong by an order of magnitude. There is no evidence for that statement. If care is taken to do a consistent calculation, the uncertainty in the data can be much larger. This point is treated more fully in Refs. [3,4]. The uncertainty in the procedure is

especially small if there is a "normalizing state"—a state in the same or a nearby nucleus that is reached by the same L transfer, has a similar Q value, is strong in α transfer, and has a known α width [5]. This is the case for states discussed here.

Whenever appropriate, we quote results for both values of q so that if a nuclear structure model provides a specific mixture of q = 7 and 9, then the width can be computed. A simple average of the results for q = 7 and 9 would not be appropriate. For q = 7, the ¹⁵N(⁶Li,d) results [3,4] led to an α spectroscopic factor $S_{\alpha} = 0.076$ for ¹⁹F(3.91) and (assuming equal S_{α} in ¹⁹F and ¹⁹Ne) an α width of 11 μ eV for ¹⁹Ne(4.03) (Table I). That analysis involved subtracting a nondirect [presumably compound-nucleus (CN)] contribution to the cross section. Reference [4] estimated the uncertainty in the width as about 15%. In ¹⁵N(⁷Li,t), the result [5] was $S_{\alpha} = 0.052$ and $\Gamma_{\alpha} = 7.5 \mu eV$ without subtracting any CN cross section. If some CN contribution is present in (⁷Li,t) (but not subtracted out), the width will be somewhat smaller. If q = 9, rather than q = 7, is appropriate, the width is about 82% of the values quoted earlier. The α width of this level is so small that the total width is virtually identical to the gamma width. Thus the value of $\omega \gamma = 2 \Gamma_{\alpha} \Gamma_{\gamma} / \Gamma$ that is needed for astrophysics reaction-rate calculations will be essentially just $\omega \gamma = 2 \Gamma_{\alpha}$. Of course, if the total width and the $\alpha/(\alpha + \gamma)$ branching ratio (BR) were known, then Γ_{α} and $\omega\gamma$ could be easily computed. Several measurements of the lifetime of ¹⁹Ne(4.03) have been made. Three recent results for the mean life are (all in fs, all 1σ uncertainties) 13^{+9}_{-6} [6], 11^{+4}_{-3} [7], and $6.9 \pm 1.5 \pm 0.7$ [8] (see Table I). The latter is the combined value for decays to two separate states. The two values are [8] 7.1[19(6)] (to gs) and $6.6^{+2.4}_{-2.1} \pm 0.7$ (to 1.54 MeV) fs. We have combined the separate values [6-8] to get 7.9(15) fs, which we use. Most attempts [9,10] to determine the Γ_{α}/Γ BR resulted only in upper limits. But the most recent article [11] has a value of $2.9(21) \times 10^{-4}$. Previous upper limits are consistent with this value. Combining this BR with the average mean life gives Γ_{α} [¹⁹Ne(4.03)] = 24(18) μ eV. These are very difficult experiments, but we await future reduction in the BR uncertainty. The new excitation energy [6] of 4034.5(8) keV is within the uncertainty of the old value of 4032.9(24), but the increase in the central value causes an increase of 4% in our α width.

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TABLE I. ¹⁹F(3.91) and ¹⁹Ne(4.03).

Quantity measured	Measured value	$\Gamma_{\alpha} [{}^{19}\text{Ne}(4.03)] (\mu eV)$	Ref.
$S[^{15}N(^{6}Li,d)]$	0.076 ^a	11.0(16)	[3,4]
$S[^{15}N(^{7}Li,t)]$	0.052 ^b	7.5(13)	[<mark>5</mark>]
$\tau(^{19}\text{Ne})^{c}$ (fs)	13^{+9}_{-6}		[<mark>6</mark>]
	11^{+4}_{-3}		[<mark>7</mark>]
	$6.9 \pm 1.5 \pm 0.7$		[<mark>8</mark>]
Γ_{α}/Γ (¹⁹ Ne) ^c	$2.9(21) \times 10^{-4}$	$24(18)^{d}$	[11]

^aAfter subtracting a CN cross-sectional component of 18(2)%.

^bNo CN subtracted.

^cOne σ uncertainty.

^dCombining τ 's to get 7.9 \pm 1.5 fs, and then combining with BR.

II. WEAK L = 3 STATES IN ¹⁹F

If α widths are computed from a single-particle width and a spectroscopic factor extracted from results of an α -transfer reaction [e.g., $({}^{6}\text{Li},d)$ or $({}^{7}\text{Li},t)$], one source of uncertainty is from the determination of the fraction of the experimental cross section that corresponds to direct one-step α transfer. The only competing process for which the cross sections add is a CN reaction mechanism. For other possibilities, the amplitudes must be added. For strong states, this uncertainty is small, but it can be large for weak states—as in this section. States that are weak but that are connected by a strong E2transition to a state that is abnormally strong in α transfer could possess an amplitude of inelastic scattering preceding or following α transfer. None of the states discussed here fit this category. Whenever appropriate, we estimate the uncertainty in subtracting the CN component. Throughout, the quoted uncertainties include those from all sources, except the one involving q.

We tried to estimate the reliability of extracting S_{α} for very weak states [12] by comparing results of (⁷Li,t) (at bombarding energies of 15, 20 [12] and 28 [13] MeV) and the (⁶Li,*d*) reaction at 22 MeV [3,4] for three states with small values of S_{α} . The values of S_{α} from the various reactions were in approximate agreement, but only at about the 50% level for the two weakest states, and only after correcting for a nondirect component in the cross sections. Goerres [14] has questioned the α widths derived from those S_{α} 's, and it does appear that a numerical mistake of a factor 2–3 was made [12] in converting S_{α} to Γ_{α} . After considerable scrutiny and checking against calculations with other computer codes, we conclude that the S_{α} 's were correctly extracted, but the published α widths are too large. Corrected values are listed in Table II. We have recomputed many of the α *sp* widths we have published in other articles, and we have found no other errors. Goerres [14] has also checked a number of our published numbers and has found no other mistakes.

III. WEAK L = 3 STATES IN ¹⁹Ne

The three weak L = 3 states in ¹⁹F discussed in the previous section all have identified mirror states in ¹⁹Ne, which are listed in Table III. Using S_{α} 's from ¹⁹F and Γ_{sp} 's calculated for ¹⁹Ne, we have computed the expected α widths in ¹⁹Ne, also listed in Table III. The first two of these states have recently had their lifetimes measured [6]. Because the very small BR is poorly known for the 4.379 MeV level, we use our calculated α width and the new lifetime to compute the expected BR, for which we get $1.14^{+.82}_{-0.65} \times 10^{-3}$, to be compared with three measured values of 16(5), 44(32), and <3.9 (all $\times 10^{-3}$) (Table III). All of the three are larger than our calculated value, but the upper-limit measurement is intriguingly close. The published upper limit is at a 90% confidence level (CL). The 68% CL upper limit is 2.6×10^{-3} [15]. The large uncertainty on the calculated BR comes primarily from the uncertainty in the lifetime. The uncertainty on the calculated α width is 40%.

For the 4.600 MeV (5/2⁺) state, the BR is reliably known [9,16], the average being 0.285(28). In this case, we use the BR and our calculated α width to compute the mean life, for which we get 2.0(5) fs—to be compared with the new measurements of 7^{+5}_{-4} fs [6] and $7.6^{+2.1}_{-2.0} \pm 0.9$ fs [8].

For the third state, S_{α} in ¹⁹F is only an upper limit. Combined with Γ_{sp} in ¹⁹Ne, the upper limit on the α width in ¹⁹Ne is 0.35 eV. Combining with the measured BR of 0.90(5) [9] leads to a lifetime limit of $\tau > 1.6$ fs, probably not an interesting limit. The γ branch of 0.10(5) leads to an upper limit on the gamma width of 62 meV.

IV. ¹⁹F(5.337)/¹⁹Ne(5.351)

The $1/2^+$ state at 5.337 MeV in ¹⁹F has a very large S_{α} . Its measured α width [17] is 1.3(5) keV, and the α width computed from $S_{\alpha}(^7\text{Li},t) = 0.64(7)$ is $\Gamma_{\alpha} = 1.9(2)$ keV [5]. Again, assuming equality of S_{α} for mirror states, this value of S_{α} , together with the *sp* width of 12 keV in ¹⁹Ne, leads to a

TABLE II. Weak L = 3 states in ¹⁹F.

$\overline{E_x (MeV)}$	E_{α} (MeV)	\mathbf{J}^{π}	$S_{\alpha}{}^{a}$	Γ_{sp}^{b} (eV)	$\Gamma_{\alpha}{}^{c}$ (eV)	$\omega \gamma^{\rm d} ({\rm eV})$
4.378	0.364	$7/2^{+}$	0.008(3)	1.8×10^{-7e}	$1.4(5) \times 10^{-9}$	$5.8(19) \times 10^{-9}$
4.550	0.536	$5/2^{+}$	0.12(3)	2.5×10^{-4e}	$3.0(8) \times 10^{-5}$	$9.0(22) \times 10^{-5}$
5.107	1.093	$5/2^+$	< 0.005	5.6	< 0.028	< 0.084

^aFrom column 8 of Table I of Ref. [12].

^bUsing r_0 , a = 1.40, 0.60 fm for q = 7.

$$^{c}\Gamma_{\alpha}=S_{\alpha}\ \Gamma_{sp}.$$

 ${}^{d}\omega\gamma = (2 \mathrm{J} + 1) \Gamma_{\alpha}\Gamma_{\gamma}/(2\Gamma).$

^eReference [14] gets 1.6×10^{-7} and 2.2×10^{-4} for these two quantities.

E_x (MeV)	\mathbf{J}^{π}	$S_{\alpha}{}^{a}$	$\Gamma_{sp}^{\mathbf{b}}$ (eV)	Γ_{α} (meV)	В	BR	τ (fs)
					Exp.	Calc. ^f	Exp.	Calc. ⁱ
4.379	7/2+	0.008(3)	0.019	0.15(6)	$16(5) \times 10^{-3c}$ $44(32) \times 10^{-3d}$ $< 3.9 \times 10^{-3e}$	$1.14^{+.82}_{65} \times 10^{-3}$	5^{+3g}_{-2}	_
4.600	(5/2+)	0.12(3)	0.80	96(24)	$0.32(4)^{e}$ $0.25(4)^{d}$	_	7^{+5g}_{-4} 7.6(21) ^h	2.0(5) ^j
5.092	5/2+	< 0.005	70	<350	$0.90(5)^{e}$	_	_	>1.6

TABLE III. Weak L = 3 states in ¹⁹Ne.

^aFrom ¹⁹F (Table II).

^bFor q = 7.

^cReference [10].

^dReference [16].

^eReference [9]. Number given is for 90% CL for 4.379 MeV state; 68% CL limit is $<2.6 \times 10^{-3}$ [15].

^fPresent. Computed from Γ_{α} and τ .

^gReference [6].

^hReference [8].

ⁱPresent. Computed from Γ_{α} and BR.

^jPresent. Computed from Γ_{α} and average of two BR values in column 6.

prediction of $\Gamma_{\alpha} = 7.7(8)$ keV for the state at 5.351 MeV in ¹⁹Ne. We use the expression $\Gamma_{calc} = S_{\alpha}\Gamma_{sp}$ and have calculated Γ_{sp} for q = 9 in this case [18]. Throughout, we have used r_0 , a = 1.40, 0.60 fm for the geometry of the α potential well, where $R = r_0(15)^{1/3}$. A very recent measurement [19] using a beam of ¹⁵O incident on a He gas target yielded the result $\Gamma_{\alpha}(^{19}\text{Ne}) = 3.2(16)$ keV. Again, the uncertainties are large, but these are extremely difficult experiments. Results are summarized in Table IV. For all our computations, we carry an extra significant digit and round at the end. This procedure may occasionally make it appear (as in Table IV) that the percentage uncertainty is (slightly) smaller in a derived quantity than in the experimental number. Before rounding, this was not the case.

V. ¹⁹F(6.497, 3/2⁺)

The result [5] of the reaction ${}^{15}N({}^{7}Li,t)$ gave a value of $S_{\alpha} = 0.07(1)$ and $\Gamma_{\alpha} = 23(4)$ keV for this state, using q = 9. Because this state was not observed in ${}^{15}N(\alpha,\alpha)$ [20], and a state with that width should have been [20,21], we have

TABLE IV. ¹⁹F(5.337) and ¹⁹Ne(5.351).

$\Gamma_{\alpha}(^{19}\mathrm{F})$	$S_{\alpha}(^{19}F)$	$\Gamma_{\alpha}(^{19}\text{Ne})$
1.3(5) keV ^a	0.44(17) ^b	5.3(20) keV ^c
1.9(2) keV ^d	0.64(7) ^e	7.7(8) keV ^f
Direct measurement		3.2(16) keV ^g

^aDirect measurement [17].

^bFrom measured width [17] and ¹⁹F sp width [18].

^cFrom S_{α} and ¹⁹Ne sp width (present).

^dComputed from S_{α} in column 2 for q = 9.

^eFrom analysis of (⁷Li, t) [5].

^fCalculated, assuming same S_{α} in ¹⁹F and ¹⁹Ne.

^gReference [19].

reexamined that analysis. The $3/2^+$ state is not resolved from a nearby $11/2^+$ state at 6.500 MeV, whose direct α -transfer cross section should be small, as discussed later. The cross section for the doublet, at 20 MeV and 15° , is 48 μ b/sr. In Ref. [5], the analysis attributed all the cross section to the $3/2^+$ level. The $9/2^+$ state at 6.59 MeV and the $11/2^+$ at 6.50 MeV both require L = 5 in α transfer, expected to be considerably weaker than L = 1 and 3 at the 20 MeV beam energy involved in this study. [Within the gs band, the $7/2^+$ state (L = 3) at 5.47 MeV is 13 times as strong as the $9/2^+$ (L = 5) at 2.78 MeV.] The $3/2^+$ state at 6.497 MeV is probably to be identified with the second $3/2^+(sd)^3$ shell-model state, predicted to occur at 6.6 MeV. It is seen in ${}^{18}F(d, p)$ [22] with reasonably large $\ell = 0$ and 2 spectroscopic factors, and in $^{18}O(d,n)$ [23] with C²S(d3/2) = 0.13. So, q = 7 may be more appropriate (see later).

In what follows, we try to unravel the contributions to the (⁷Li,t) cross section for the 6.5- MeV $3/2^+/11/2^+$ doublet, making use of the results from other states in the same region of excitation energy. For the present purposes, we can estimate the upper limit on a possible CN contribution by looking at the results for the 6.55 MeV $7/2^+$ and 7.11 MeV $5/2^+$ states, both of which are reached via L = 3 and have quite different S_{α} 's—0.05 and 0.25, respectively [18]. [The state at 7.11 MeV is listed as $7/2^+$ in the latest compilation. It has L = 3 in (α, α) , requiring $5/2^+$ or $7/2^+$. Reference [18] first suggested

TABLE V. ¹⁹F(6.497, 3/2⁺).

Assumption	S_{α}	Γ_{α} (keV)
All cross section is 3/2 ⁺	0.07(1) ^a	23(4) ^a
Subtracting doublet CN and $11/2^+$ direct	$0.05(2)^{b}$	16(6) ^b
As one row above, but $q = 7$	0.07(3)	20(8)

^aReference [5], q = 9.

^bPresent, q = 9.

$\overline{\mathrm{E}_{x}(^{19}\mathrm{Ne})~(\mathrm{MeV})}$	\mathbf{J}^{π}	Assumed mirror in ¹⁹ F (MeV)	Comment
7.42 ^a	7/2 ^a	7.56	Leads to $S_p(\ell = 2) = 8$ [1]
7.42	1/2 ^b	8.138	Large $S_p(\ell = 0)$ provides large energy shift; we expect $\Gamma_p \approx 75(15)$ keV

TABLE VI. ¹⁹Ne(7.42).

^aReference [26] (but not observed by Ref. [27]).

^bSuggested here. Not relevant if the state does not exist in ¹⁹Ne.

it should be $5/2^+$, from a consideration of $L = 3 \alpha$ -cluster widths. The clear $\ell = 2$ angular distribution in ¹⁸O(d,n) [23] confirms the $5/2^+$ assignment.] The conclusion is that the upper limit to any CN contribution to the 6.50 MeV doublet is 19 μ b/sr, with a reasonable value being about half that, that is, $\sigma_{\rm CN} \sim 10 \ \mu$ b/sr, with a large uncertainty. This value includes $\sigma_{\rm CN}$ for both $3/2^+$ and $11/2^+$ states.

We can put a limit on any direct cross section to the $11/2^+$ state by using the $9/2^+$ state at 6.59 MeV, which also has L = 5. Its α width is known [2] to be 7.3(17) eV, which gives $S_{\alpha} = 0.021(5)$. The α width for the $11/2^+$ state is not known, but $\omega\gamma$ is known [24]— $\omega\gamma = 6 \Gamma_{\alpha}\Gamma_{\gamma}/\Gamma = 2.3(4) \text{ eV}.$ Following ¹²C(¹¹B, α), which favors high-J states, the limit on the branching ratio of the doublet is $\Gamma_{\gamma}/\Gamma > 0.18$ [25]. Even though this limit is for the doublet, it seems a safe lower limit for the $11/2^+$ state, which should have a larger value of Γ_{γ}/Γ than the 3/2⁺ state. Combining the value of $\omega\gamma$ with the BR limit results in a limit on the α width of $\Gamma_{\alpha} \leq 2.5 \,\text{eV}.$ (And, of course, $\Gamma_{\alpha} \geq 0.31 \,\text{eV}$ from $\omega \gamma$.) Any direct α transfer cross section to the $11/2^+$ state is thus (by comparison with the $9/2^+$ state) in the range 1.3–10 μ b/sr. Putting all this together, a reasonable lower limit for the $3/2^+$ cross section is $48 - 19 - 10 = 19 \ \mu \text{b/sr}$, and a likely value is 32 μ b/sr—quite a wide range. The lower value results in a lower limit on S_{α} of 0.03, with a likely value of 0.05. We suggest $S_{\alpha} = 0.05(2)$ [replacing 0.07(1)], giving $\Gamma_{\alpha} =$ 16(6) keV, again for q = 9. For q = 7, we have S = 0.07(3)and $\Gamma_{\alpha} = 20(8)$ keV. We may have over-estimated the CN cross section, so it is difficult to see how the width could be less than 10 keV. It would be interesting to obtain a rigorous upper limit on the width from the ${}^{15}N(\alpha, \alpha)$ analysis. The present analysis is summarized in Table V.

VI. ¹⁹Ne(7.42)

In [1] we pointed out that, for this state, if the J^{π} assignment [26] of $7/2^+$ and the measured widths were correct, the proton spectroscopic factor was about 8-a very unwelcome value. It would thus appear that the proton width and/or the J^{π} is incorrect, or at least two states are present. A large proton width might imply $\ell = 0$, that is, $J^{\pi} = 1/2^+$ or $3/2^+$. In searching for a mirror candidate in ¹⁹F, we were immediately drawn to the $1/2^+$ state at 8.1 MeV in ¹⁹F that has a large S_n in ${}^{18}F(d,p)$ [22]. The spectroscopic factor of 0.32(6) becomes even larger, 0.45(9), if our bound-state geometry is used in the analysis [21]. This large 2s1/2occupancy would cause a large downward shift from ¹⁹F to ¹⁹Ne (estimated to be about 410(80) keV for this component of the wave function). This suggestion is summarized in Table VI. If our suggestion is correct, the proton width should be about 75(15) keV for a state at 7.42 MeV. If this is not the mirror of the 8.14 MeV state, another strong $1/2^+$ resonance should exist in ¹⁹Ne not very far away. However, a recent paper [27] on ${}^{18}F(p,p)$ and ${}^{18}F(p,\alpha)$ did not observe this state.

In conclusion, we have presented updated information and analyses for several states in ¹⁹F and ¹⁹Ne and have corrected a mistake in the Γ_{α} values of Ref. [12].

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