

Quasi-elastic neutrino charged-current scattering off ^{12}C

A. V. Butkevich

Institute for Nuclear Research, Russian Academy of Sciences, 60th October Anniversary Prosp. 7A, Moscow RU-117312, Russia

(Received 17 April 2009; published 31 July 2009)

The charged-current quasielastic scattering of muon neutrino on a carbon target is calculated for neutrino energy up to 2.8 GeV using the relativistic distorted-wave impulse approximation with relativistic optical potential, which was earlier successfully applied to describe the electron-nucleus data. We studied both neutrino and electron processes and have shown that the reduced exclusive cross sections for neutrino and electron scattering are similar. The nuclear and axial vector mass effects on the shape of Q^2 distribution have also been studied. The comparison of the (anti-)neutrino total cross sections per (proton)neutron, calculated for the carbon and oxygen targets, shows the cross sections for oxygen to be lower than those for carbon. A significant nuclear model dependence of inclusive and total cross sections for energy about 1 GeV was found.

DOI: [10.1103/PhysRevC.80.014610](https://doi.org/10.1103/PhysRevC.80.014610)

PACS number(s): 25.30.Bf, 25.30.Pt, 13.15.+g

I. INTRODUCTION

The goals of the current and upcoming accelerator-based neutrino experiments [1–7] are the precision measurements of the neutrino-mass-squared difference Δm_{23}^2 by measuring muon neutrino disappearance and searching for the last unmeasured leptonic mixing angle θ_{13} through the muon to electron neutrino transition. The last oscillation channel, if it occurs, opens the possibility of observing the matter/antimatter asymmetries in neutrinos and determination of the ordering of the neutrino mass states. The data of these experiments will greatly extend the statistics due to the extreme intensity of the neutrino beamline.

To study the neutrino oscillation effects on the terrestrial distance scale, the neutrino beams cover the energy range from a few hundred MeV to several GeV. In this energy range, the dominant contribution to the neutrino-nucleus cross section comes from the charged-current (CC) quasielastic (QE) reactions and resonance production processes. The cross-section data in this energy range are rather scarce and were taken on targets not used in the neutrino oscillation experiments (i.e., water, iron, lead, or plastic). In this situation, the statistical uncertainties should be negligible compared to systematic errors in the incident neutrino flux, neutrino interaction model, and the detector effects on the neutrino events selection and the neutrino energy reconstruction. Apparently, these uncertainties produce the systematic errors in the extraction of the oscillation parameters.

Many experiments try to reduce these uncertainties by using a near detector. One of the options for the near detector design is to make the detector more segmented and as fine-grained as possible using a scintillator (carbon) as a target and detecting material. This strategy means that one must try to measure the fluxes and cross sections as independently as possible and then use this information to constrain the detector simulation so that the information is correctly extrapolated to the far detector. The concern with this strategy is that the detector simulation must accurately predict the detector response. Because the near and far detectors are not necessarily of the same target material, a part of the near detector must include some of the same target material, so that nuclear effects on the cross sections (QE

and non-QE) can be taken into account. Among the proposed experiments, MINERvA [4] and ND280 detector [8] will be able to make precise measurements in a wide range of energies and for various nuclear targets.

To model the QE neutrino scattering from a nuclei, most neutrino oscillation experiments employ a Monte Carlo (MC) event generators [9] based on the relativistic Fermi gas model (RFGM) [10] with Pauli blocking, in which the nucleus is described as a system of quasi-free nucleons with a flat nucleon momentum distribution up to the same Fermi momentum p_F and nuclear binding energy ϵ_b . But this model does not take into account the nuclear shell structure, the final-state interaction (FSI) between the outgoing nucleon and the residual nucleus, and the presence of short-range nucleon-nucleon (NN) correlations, leading to the appearance of a high-momentum and high-energy component in the nucleon momentum-energy distribution in the target.

The comparison with the high-precision electron-scattering data has shown [11] that the accuracy of the RFGM prediction becomes poor at low squared four-momentum transfer Q^2 , where the nuclear effects are the largest. The modern quasielastic neutrino-scattering data (the CC QE event distribution as a function of Q^2) [1,12] also reveals the inadequacies in the present neutrino cross-section simulations. The data/MC disagreement shows the data deficit in the low- Q^2 [$Q^2 \leq 0.2$ (GeV/c) 2] region.

There are many calculations for the QE neutrino charged-current and neutral-current scattering cross sections on the nucleus, which go beyond the simple RFGM and use more realistic description of nuclear dynamics. In the calculations of Refs. [13,14] within the plane-wave impulse approximation (PWIA), the short range NN correlations were included using the description of the nuclear dynamics, based on nuclear many-body theory. Charged current and/or neutral current neutrino-nucleus cross sections were studied within the relativistic distorted-wave impulse approximation (RDWIA) in Refs. [15–24], using the relativistic shell-model approach and taking into account the FSI effects. In Refs. [21,22] the contribution of short-range correlations (SRC) was also considered. The FSI effects were studied within the framework of the random-phase approximation

[25–28], within the superscaling approach [29–33], and in the Giessen Boltzmann-Uehling-Uhlenbeck (GiBUU) model [34].

In this article, we calculate the single-nucleon knockout contribution to the exclusive, inclusive, and total cross sections of the charged-current QE (anti-)neutrino scattering from ^{12}C using various approximations (PWIA and RDWIA) and the Fermi gas model. We employ the LEA code [35] that was adopted for neutrino reactions. In our approach, the effect of the SCR in the carbon ground state is evaluated in the PWIA [36,37] and the FSI effect on the inclusive cross sections in the presence of the NN correlations is estimated according to Ref. [21]. The aims of this work are (a) calculation the RDWIA CC QE $\nu^{12}\text{C}$ cross sections, (b) investigation of the nuclear effects on the Q^2 dependence of the (anti-)neutrino cross section, and (c) comparison of the total cross sections, scaled with the number of neutrons/protons in the target for (anti-)neutrino scattering on the oxygen and carbon targets.

The outline of this article is as follows. In Sec. II we present briefly the formalism for the CC QE-scattering process and the RDWIA model. The results are presented and discussed in Sec. III. Our conclusions are summarized in Sec. IV.

II. FORMALISM OF QUASIELASTIC SCATTERING AND RDWIA

We consider electron and neutrino charged-current QE exclusive

$$l(k_i) + A(p_A) \rightarrow l'(k_f) + N(p_x) + B(p_B), \quad (1)$$

and inclusive

$$l(k_i) + A(p_A) \rightarrow l'(k_f) + X \quad (2)$$

scattering off nuclei in the one-photon (W-boson) exchange approximation. Here l labels the incident lepton [electron or muon (anti-)neutrino], and l' represents the scattered lepton (electron or muon), $k_i = (\varepsilon_i, \mathbf{k}_i)$ and $k_f = (\varepsilon_f, \mathbf{k}_f)$ are the initial and final lepton momenta, $p_A = (\varepsilon_A, \mathbf{p}_A)$, and $p_B = (\varepsilon_B, \mathbf{p}_B)$ are the initial and final target momenta, $p_x = (\varepsilon_x, \mathbf{p}_x)$ is the ejectile nucleon momentum, $q = (\omega, \mathbf{q})$ is the momentum transfer carried by the virtual photon (W-boson), and $Q^2 = -q^2 = \mathbf{q}^2 - \omega^2$ is the photon (W-boson) virtuality.

A. CC QE neutrino-nucleus cross sections

In the laboratory frame, the differential cross section for the exclusive electron (σ^{el}) and (anti-)neutrino CC QE (σ^{cc}) scattering, in which only a single discrete state or narrow resonance of the target is excited, can be written as

$$\frac{d^5\sigma^{\text{el}}}{d\varepsilon_f d\Omega_f d\Omega_x} = R \frac{|\mathbf{p}_x| \varepsilon_x}{(2\pi)^3} \frac{\varepsilon_f}{\varepsilon_i} \frac{\alpha^2}{Q^4} L_{\mu\nu}^{(\text{el})} W^{\mu\nu(\text{el})} \quad (3a)$$

$$\frac{d^5\sigma^{\text{cc}}}{d\varepsilon_f d\Omega_f d\Omega_x} = R \frac{|\mathbf{p}_x| \varepsilon_x}{(2\pi)^5} \frac{|\mathbf{k}_f|}{\varepsilon_i} \frac{G^2 \cos^2 \theta_c}{2} L_{\mu\nu}^{(\text{cc})} W^{\mu\nu(\text{cc})}, \quad (3b)$$

where Ω_f is the solid angle for the lepton momentum, Ω_x is the solid angle for the ejectile nucleon momentum, R is the recoil factor, $\alpha \simeq 1/137$ is the fine-structure constant, $G \simeq 1.16639 \times 10^{-11} \text{ MeV}^{-2}$ is the Fermi constant, θ_c is

the Cabbibo angle ($\cos \theta_c \approx 0.9749$), $L_{\mu\nu}$ is the lepton tensor and $W_{\mu\nu}^{(\text{el})}$ and $W_{\mu\nu}^{(\text{cc})}$ are the electromagnetic and weak CC nuclear tensors, respectively. The energy ε_x is the solution to the equation

$$\varepsilon_x + \varepsilon_B - m_A - \omega = 0, \quad (4)$$

where $\varepsilon_B = \sqrt{m_B^2 + \mathbf{p}_B^2}$, $\mathbf{p}_B = \mathbf{q} - \mathbf{p}_x$, $\mathbf{p}_x = \sqrt{\varepsilon_x^2 - m^2}$, and m_A , m_B , and m are masses of the target, recoil nucleus, and nucleon, respectively. The missing momentum p_m and missing energy ε_m are defined by

$$\mathbf{p}_m = \mathbf{p}_x - \mathbf{q} \quad (5a)$$

$$\varepsilon_m = m + m_B - m_A. \quad (5b)$$

The leptonic tensor is separated into symmetrical and antisymmetrical components that are written as in Ref. [21]. The electromagnetic and weak CC hadronic tensors, $W_{\mu\nu}^{(\text{el})}$ and $W_{\mu\nu}^{(\text{cc})}$ are given by bilinear products of the transition matrix elements of the nuclear electromagnetic or CC operator $J_{\mu}^{(\text{el})(\text{cc})}$ between the initial nucleus state $|A\rangle$ and the final state $|B_f\rangle$ as

$$W_{\mu\nu}^{(\text{el})(\text{cc})} = \sum_f \langle B_f, p_x | J_{\mu}^{(\text{el})(\text{cc})} | A \rangle \langle A | J_{\nu}^{(\text{el})(\text{cc})\dagger} | B_f, p_x \rangle, \quad (6)$$

where the sum is taken over undetected states.

In the inclusive reactions (2) only the outgoing lepton is detected, and the differential cross sections can be written as

$$\frac{d^3\sigma^{\text{el}}}{d\varepsilon_f d\Omega_f} = \frac{\varepsilon_f}{\varepsilon_i} \frac{\alpha^2}{Q^4} L_{\mu\nu}^{(\text{el})} \mathcal{W}^{\mu\nu(\text{el})}, \quad (7a)$$

$$\frac{d^3\sigma^{\text{cc}}}{d\varepsilon_f d\Omega_f} = \frac{1}{(2\pi)^2} \frac{|\mathbf{k}_f|}{\varepsilon_i} \frac{G^2 \cos^2 \theta_c}{2} L_{\mu\nu}^{(\text{cc})} \mathcal{W}^{\mu\nu(\text{cc})}, \quad (7b)$$

where $\mathcal{W}^{\mu\nu}$ is the inclusive hadronic tensor. The expressions for the exclusive (3) and inclusive (7) lepton-scattering cross sections in terms of response functions are given in Ref. [21].

It is also useful to define a reduced cross section

$$\sigma_{\text{red}} = \frac{d^5\sigma^{(\text{el})(\text{cc})}}{d\varepsilon_f d\Omega_f d\Omega_x} / K^{(\text{el})(\text{cc})} \sigma_{IN}, \quad (8)$$

where $K^{\text{el}} = R p_x \varepsilon_x / (2\pi)^3$ and $K^{\text{cc}} = R p_x \varepsilon_x / (2\pi)^5$ are phase-space factors for electron and neutrino scattering and σ_{IN} is the corresponding elementary cross section for the lepton scattering from the moving free nucleon.

B. Models

We describe the lepton-nucleon scattering in the impulse approximation (IA), in which only one nucleon of the target is involved in the reaction, and the nuclear current is written as a sum of single-nucleon currents. Then, the nuclear matrix element in Eq. (6) takes the form

$$\langle p, B | J_{\mu} | A \rangle = \int d^3r \exp(it \cdot \mathbf{r}) \bar{\Psi}^{(-)}(\mathbf{p}, \mathbf{r}) \Gamma^{\mu} \Phi(\mathbf{r}), \quad (9)$$

where Γ^{μ} is the vertex function, $\mathbf{t} = \varepsilon_B \mathbf{q} / W$ is the recoil-corrected momentum transfer, $W = \sqrt{(m_A + \omega)^2 - \mathbf{q}^2}$ is the invariant mass, and Φ and $\Psi^{(-)}$ are relativistic bound-state and outgoing wave functions.

For the electron scattering, we use the CC2 electromagnetic vertex function for a free nucleon [38]

$$\Gamma^\mu = F_V^{(\text{el})}(Q^2)\gamma^\mu + i\sigma^{\mu\nu}\frac{q_\nu}{2m}F_M^{(\text{el})}(Q^2), \quad (10)$$

where $\sigma^{\mu\nu} = i[\gamma^\mu, \gamma^\nu]/2$, $F_V^{(\text{el})}$ and $F_M^{(\text{el})}$ are the Dirac and Pauli nucleon form factors. The single-nucleon charged current has $V-A$ structure $J^{\mu(\text{cc})} = J_V^\mu + J_A^\mu$. For the free-nucleon vertex function $\Gamma^{\mu(\text{cc})} = \Gamma_V^\mu + \Gamma_A^\mu$ we use the CC2 vector current vertex function

$$\Gamma_V^\mu = F_V(Q^2)\gamma^\mu + i\sigma^{\mu\nu}\frac{q_\nu}{2m}F_M(Q^2) \quad (11)$$

and the axial current vertex function

$$\Gamma_A^\mu = F_A(Q^2)\gamma^\mu\gamma_5 + F_P(Q^2)q^\mu\gamma_5. \quad (12)$$

The weak vector form factors F_V and F_M can be expressed in terms of the corresponding electromagnetic factors for proton $F_{i,p}^{(\text{el})}$ and neutron $F_{i,n}^{(\text{el})}$ as follows

$$F_i = F_{i,p}^{(\text{el})} - F_{i,n}^{(\text{el})}. \quad (13)$$

For the electromagnetic and weak CC vector vertexes we employ the de Forest prescription [38] (because the bound nucleons are off shell) and the Coulomb gauge. For the Dirac and Pauli nucleon form factors we use the approximation from Ref. [39] and the dipole approximation for the axial F_A and pseudoscalar F_P form factors

$$F_A(Q^2) = \frac{F_A(0)}{(1 + Q^2/M_A^2)^2}, \quad F_P(Q^2) = \frac{2mF_A(Q^2)}{m_\pi^2 + Q^2}, \quad (14)$$

where $F_A(0) = 1.267$ and m_π , M_A are the pion and axial mass, respectively.

In Ref. [40], a formalism was developed for the $A(e, e'N)B$ reaction that describes the channel coupling in the FSI of the $N + B$ system. In this work the independent particle shell model (IPSM) is assumed for the nuclear structure. The model space for $^{12}\text{C}(l, l'N)$ consists of $1s_{1/2}$ and $1p_{3/2}$ nucleon-hole states in the ^{11}B and ^{11}C nuclei. The $1s_{1/2}$ state is regarded as a discrete state even though its spreading width is actually appreciable.

In the independent particle shell-model the relativistic bound-state functions Φ in Eq. (9) are obtained within the Hartree–Bogoliubov approximation in the $\sigma - \omega$ model [41]. The upper component of the bound-state wave function Φ is used for evaluation of the shell nucleons spectral function in the PWIA calculations. We use the nucleon bound-state functions calculated by the TIMORA code [42] with the normalization factors $S(\alpha)$, relative to full occupancy of the IPSM orbitals of ^{12}C : $S(1p_{3/2}) = 84\%$, $S(1s_{1/2}) = 100\%$, and an average factor of about 89%. These estimations of the depletion of hole states follow from the RDWIA analysis of $^{12}\text{C}(e, e'p)$ for $Q^2 < 2$ (GeV/c) 2 [43] and are consistent with a direct measurement of the spectral function using $^{12}\text{C}(e, e'p)$ in the parallel kinematics [44], which observed approximately 0.6 protons in a region with $p_m \geq 240$ MeV/c and $\varepsilon_m \geq 50$ MeV, attributable to a single-nucleon knockout from the correlated cluster. Similar estimates of the depletion of hole states are available from the self-consistent Green's

function method [45], the correlated basis function theory [46], and other methods.

In the RDWIA the ejectile wave function Ψ in Eq. (9) is obtained by following the direct Pauli reduction method [47,48]. It is known that the Dirac spinor

$$\Psi = \begin{pmatrix} \Psi_+ \\ \Psi_- \end{pmatrix} \quad (15)$$

can be written in terms of its positive energy component Ψ_+ as

$$\Psi = \begin{pmatrix} \Psi_+ \\ \frac{\boldsymbol{\sigma} \cdot \mathbf{p}}{E+M+S-V}\Psi_+ \end{pmatrix}, \quad (16)$$

where $S = S(r)$ and $V = V(r)$ are the scalar and vector potentials for the nucleon with energy E . The upper component Ψ_+ can be related to the Schrödinger-like wave function ξ by the Darwin factor $D(r)$, i.e.,

$$\Psi_+ = \sqrt{D(r)}\xi. \quad (17)$$

The two-component wave function ξ is the solution of the Schrödinger equation containing equivalent central and spin-orbit potentials, which are functions of the scalar and vector potentials S and V that are energy dependent. We use the LEA program [35] for the numerical calculation of the distorted-wave functions with EDAD1 SV relativistic optical potential [49] for carbon.

In the plane-wave impulse approximation (PWIA) the final-state interaction between the outgoing nucleon and the residual nucleus is neglected, and the nonrelativistic PWIA exclusive cross section has a factorized form [50]

$$\frac{d^5\sigma}{d\varepsilon_f d\Omega_f d\Omega_x} = K^{(\text{el})(\text{cc})}\sigma_{IN}\mathcal{P}(E, \mathbf{p}) \quad (18)$$

where $\mathcal{P}(E, \mathbf{p})$ is the nuclear spectral function.

According to the JLab data [44,51], the occupancy of the independent particle shell-model orbitals of ^{12}C equals on average about 89%. In this work we assume that the missing strength (11%) can be attributed to the short-range NN correlations in the ground state, leading to the appearance of the high-momentum (HM) and high-energy nucleon distributions in the target. The inclusive cross sections with the FSI effects in the presence of the short-range NN correlations was calculated using the approach was proposed in Ref. [21]. In this approach the contribution of the NN -correlated pair $(d^2\sigma/d\varepsilon_f d\Omega_f)_{\text{HM}}$ is evaluated in the PWIA model. We use the general expression for the high-momentum and high-energy part of the spectral function from Ref. [37] with the parametrization for the nucleon high-momentum distribution $n_{\text{cor}}(\mathbf{p})$ from Ref. [36], which was renormalized to value of 11%. The FSI effect for the high-momentum component is estimated by scaling $(d^2\sigma/d\varepsilon_f d\Omega_f)_{\text{HM}}$ with $\Lambda(\varepsilon_f, \Omega_f)$ function determined in Ref. [21].

III. RESULTS AND ANALYSIS

A. Electron scattering

The LEA code was successfully tested against $^{12}\text{C}(e, e'p)$ data. For illustration, Fig. 1 shows measured JLab [51] reduced cross sections for the removal of protons from the $1s$ and

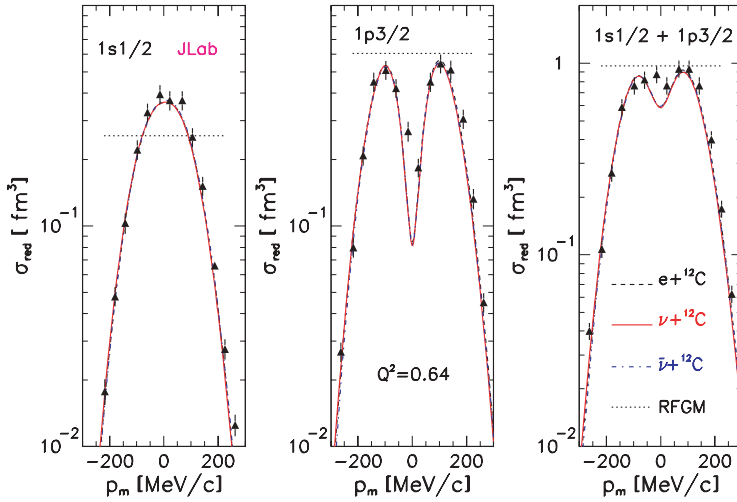


FIG. 1. (Color online) Comparison of the RDWIA and the RFGM calculations for electron, neutrino, and antineutrino reduced cross sections for the removal of nucleons from $1p$ and $1s$ shells of ^{12}C as functions of the missing momentum. JLab data [51] for beam energy $E_{\text{beam}} = 2.455$ GeV, proton kinetic energy $T_p = 350$ MeV, and $Q^2 = 0.64$ (GeV/c)². The RDWIA calculations are shown for electron scattering (dashed line) and neutrino (solid line) and antineutrino (dashed-dotted line) scattering; and the RFGM results are shown for the reduced cross sections (dotted line) for the JLab kinematics.

$1p$ shells of ^{12}C as functions of missing momentum p_m as compared with LEA code calculations. It should be noted that negative values of p_m correspond to $\phi = \pi$ and positive ones to $\phi = 0$, where ϕ is the angle between the scattering ($\mathbf{k}_i, \mathbf{k}_f$) and reaction ($\mathbf{p}_x, \mathbf{p}_B$) planes. The data for beam energy $E_{\text{beam}} = 2.445$ GeV and $Q^2 = 0.6, 1.2$, and 1.8 (GeV/c)² were measured in the quasiperpendicular kinematics with constant (ω, \mathbf{q}) . The detailed data analysis [43] for $^{12}\text{C}(e, e'p)$ with $Q^2 \leq 2$ (GeV/c)² using the RDWIA, based on Dirac-Hartree wave functions, has shown that the $1p$ normalization extracted from data for $Q^2 \geq 0.6$ (GeV/c)² is equals approximately 0.87, independent of Q^2 , which is close to 0.84 used in our calculation.

The electron and neutrino scattering off the nuclei are closely interrelated and one can treat both processes within the same formalism. In the nonrelativistic PWIA, σ_{red} is a nuclear spectral function and should be similar for electron and (anti-)neutrino scattering, except the small distinctions that can be attributed to the Coulomb distortion on the electron wave function. The small difference between neutrino and antineutrino is due to the difference in the FSI of the proton and neutron with the residual nucleus. This effect is neglected at the beam energy higher than 1 GeV. There is an overall good agreement between the cross sections calculated in the RDWIA and data. Apparently, the RFGM predictions (with the Fermi momentum $p_F = 221$ MeV/ c and binding energy $\epsilon_b = 25$ MeV) overestimate the values of cross sections and completely off the exclusive data. This is due to the uniform momentum distribution of the Fermi gas model and neglecting the FSI effects. Therefore, the RFGM cannot predict well enough the momentum distribution of the outgoing protons in simulation of the CC QE two-track events at momentum transfer $|\mathbf{q}| \leq |\mathbf{p}_m|$, i.e., at low Q^2 .

A complex relativistic optical potential with a nonzero imaginary part generally produces an absorption of flux. However, for the inclusive reaction, the total flux must be conserved. Currently there is no fully consistent solution to this problem, and different approaches are used. In Refs. [15,52] it was shown that the inclusive CC cross sections calculated with only the real part of the optical potential are almost identical to those of the Green's function approach, in which the FSI effect

in the inclusive reactions is treated by means of a complex optical potential and the total flux is conserved. In this work, to calculate the inclusive and total cross sections, we use the approach in which only the real part of the optical potential EDAD1 is included.

To test our approach, we calculated the inclusive $^{12}\text{C}(e, e')$ cross sections and compared them with the data from SLAC [53–55], Saclay [56], and JLab [57]. Figures 2 and 3 show

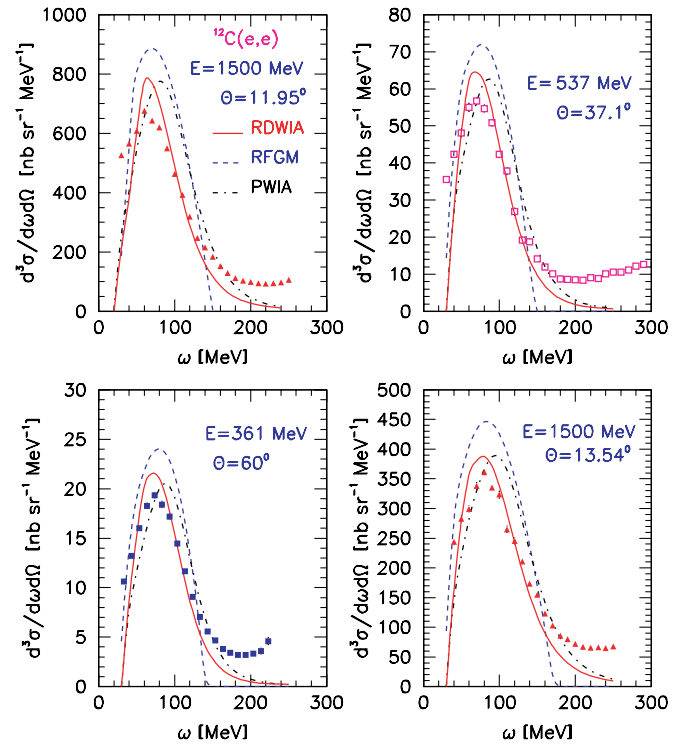


FIG. 2. (Color online) Inclusive cross section versus energy transfer ω for electron scattering on ^{12}C . The data are from Ref. [53] (filled triangles), Ref. [54] (open squares), and Ref. [56] (filled squares). In Ref. [53] data are for the electron beam energy $E_e = 1500$ MeV, and scattering angles $\theta_e = 11.95^\circ, 13.54^\circ$; in Ref. [54] data are for $E_e = 537$ MeV and $\theta_e = 37.1^\circ$; in Ref. [56] data are for $E_e = 361$ MeV and $\theta_e = 60^\circ$.

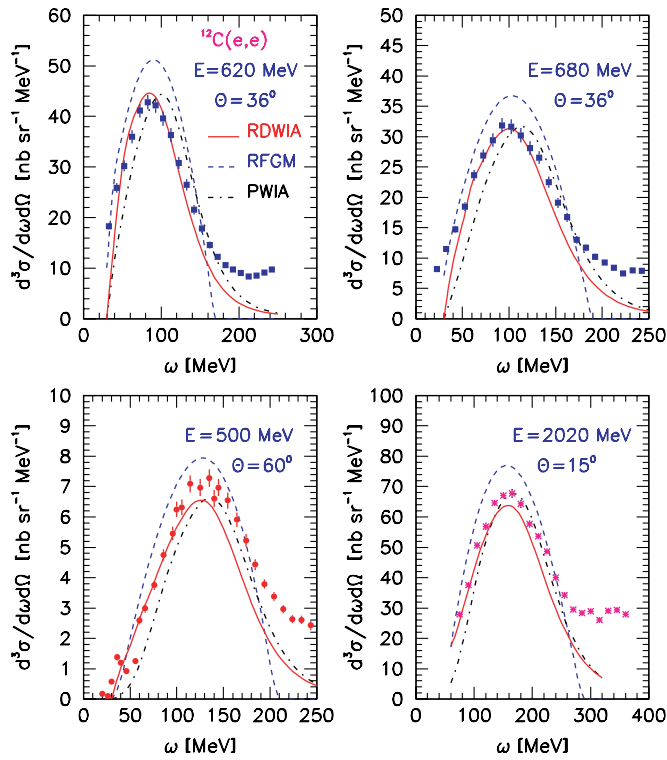


FIG. 3. (Color online) Same as Fig. 2, but the data are from Ref. [56] (filled squares) for $E_e = 620$ MeV, $\theta_e = 36^\circ$ and $E_e = 680$ MeV, $\theta_e = 36^\circ$; Ref. [55] (filled circles) for $E_e = 500$ MeV, $\theta_e = 60^\circ$; Ref. [57] (stars) for $E_e = 2020$ MeV, $\theta_e = 15^\circ$.

measured inclusive cross sections as functions of energy transfer as compared to the RDWIA, PWIA, and RFGM calculations. These data cover the range of the three-momentum transfer (around the peak) from $|q| \approx 310$ MeV/c (beam energy $E_e = 1500$ MeV and scattering angle $\theta = 11.95^\circ$) up to $|q| \approx 530$ MeV/c ($E_e = 2020$ MeV, $\theta = 15^\circ$). We note that relative to the PWIA results, the generic effect of the FSI with the real part of the optical potential reduces the cross-section value around the peak and shifts the peak toward the lower value energy transfer. The inclusion of the high-momentum component increases the inclusive cross section in the high-energy transfer region and improves the agreement with data. The peak in the RDWIA calculation occurs at the same energy loss as the data, and the value of the calculated cross sections generally agree with data within $\pm 12\%$. For the RFGM results this difference decreases with $|q|$ from about 20% at $|q| \approx 310$ MeV/c down to $\approx 13\%$ at $|q| \approx 510$ MeV/c. These results demonstrate a strong nuclear-model dependence of the inclusive cross sections at low-momentum transfer.

B. Neutrino scattering

The charged-current QE event distributions as functions of Q^2 were measured in K2K [12,58] and MiniBooNE [1] experiments. The shape of the Q^2 distribution, which is weakly dependent on the flux uncertainties, was analyzed. High-statistic data show a disagreement with the RFGM predictions. The data samples exhibit significant deficit in the

region of low $Q^2 \leq 0.2(\text{GeV}/c)^2$ (so-called low- Q^2 problem). In Ref. [1] it was shown that the data/MC disagreement is not due to mismodeling of the incoming neutrino energy spectrum but due to the inaccuracy in the simulation of the CC QE interactions. To tune the Fermi gas model to the low Q^2 , an additional parameter κ was introduced that reduced the phase-space volume of the nucleon Fermi gas at low-momentum transfer. This parameter controls the Q^2 distribution in the low Q^2 region only.

In the region of high Q^2 the data excess is observed, and the value of the axial vector mass M_A obtained from a fit to the measured data, is higher than the results of the previous experiments. The formal averaging of M_A values from several experiments, which are very wide spread from 0.7 to 1.3 GeV, was done in Ref. [59]: $M_A = 1.026 \pm 0.021$. This result is also known as the world average value of axial mass. K2K obtained the value of 1.2 ± 0.12 from the SciFi detector [12] using the water-aluminum mixture as a target and the preliminary result of 1.14 ± 0.11 from the SciBar detector [58] using a scintillator target. The MiniBooNE experiment (scintillator target) found that the data were better described with an adjustment of two parameters $M_A = 1.23 \pm 0.20$ GeV and $\kappa = 1.019 \pm 0.011$ [1].

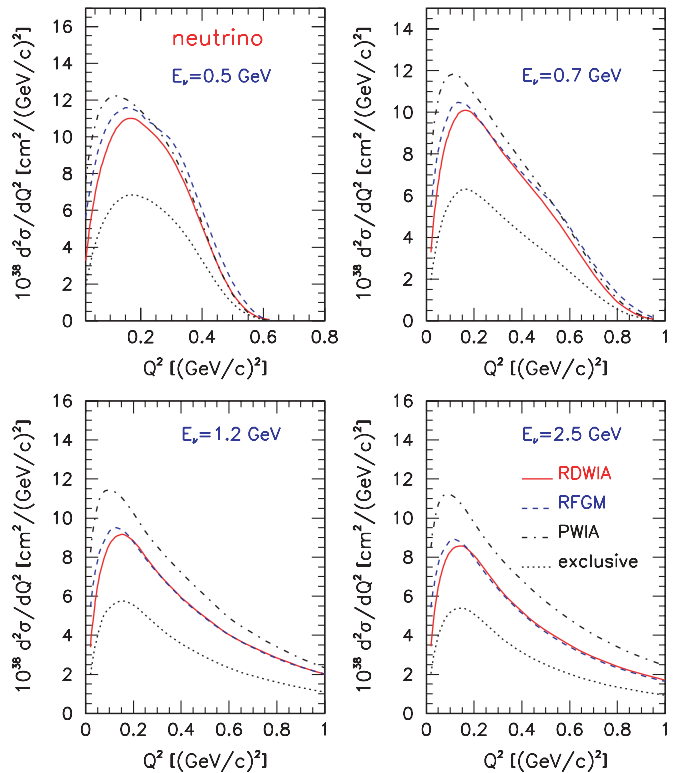


FIG. 4. (Color online) Inclusive cross section vs. the four-momentum transfer Q^2 for neutrino scattering off ^{12}C and for the four values of incoming neutrino energy: $\varepsilon_\nu = 0.5, 0.7, 1.2,$ and 2.5 GeV. The solid line is the RDWIA calculation, whereas the dashed and dash-dotted lines are the RFGM and PWIA calculations, respectively. The dotted lines are the cross sections for the exclusive reaction.

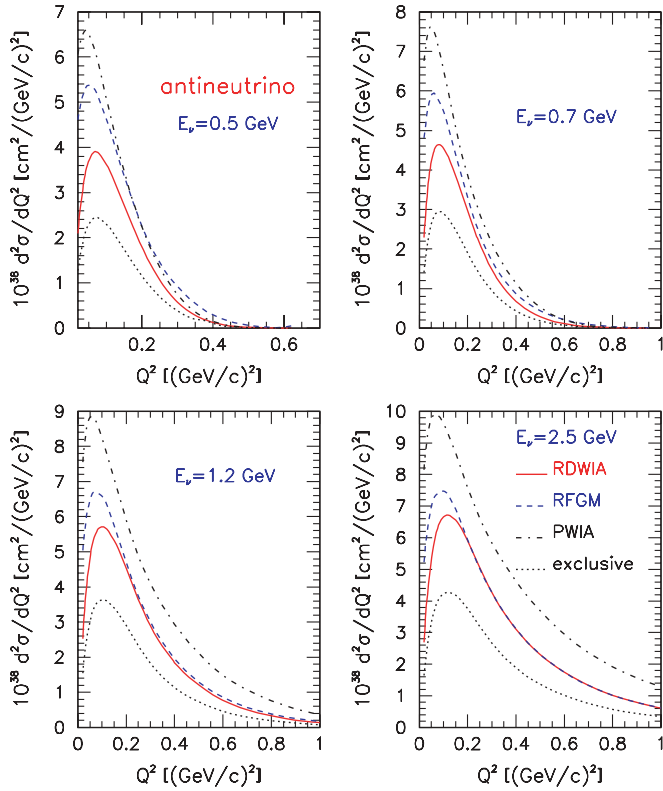


FIG. 5. (Color online) Same as Fig. 4 but for antineutrino scattering.

Recently, the NOMAD experiment [60] extracted the value of $M_A = 1.05 \pm 0.02 \pm 0.06$ GeV using a carbon target, which is in agreement with the world average value. This result was obtained from the analysis of a measured $\nu^{12}\text{C}$ total CC QE cross section for neutrino energy above ≈ 4 GeV, where the cross section “plateau” is reasonably well-known. It should be noted that both approaches, i.e., analysis of the shape of the Q^2 distribution and the direct measurement of the total cross section assume, that the vector form factors are well known from the electron-scattering experiments. Actually, at $Q^2 \geq 3$ (GeV/c) 2 the values of the neutron form factors are much less known than those of the proton [61], and the relative contribution from this region to the total cross section increases with neutrino energy.

To study the nuclear effects on the Q^2 distribution, we calculated (with $M_A = 1.032$ GeV) the inclusive cross sections $d\sigma/dQ^2$ for neutrino energies $\varepsilon_\nu = 0.5, 0.7, 1.2$ and 2.5 GeV and compared them with those for neutrino scattering on a free nucleon. The results for neutrino and antineutrino scattering on carbon are presented in Figs. 4 and 5, respectively, which show $d\sigma/dQ^2$ as functions of Q^2 . Here, the results obtained in the RDWIA are compared with cross sections calculated in the PWIA and RFGM. The cross sections for the exclusive reaction are shown as well. In the region $Q^2 < 0.2$ (GeV/c) 2 the Fermi gas model results for neutrino (antineutrino) are higher than those obtained within the RDWIA. At $Q^2 = 0.1$ (GeV/c) 2 this discrepancy equals 12% (28%) for $\varepsilon_\nu = 0.5$ GeV and decreases to 7% (12%) for $\varepsilon_\nu = 2.5$ GeV. The contribution of ($\nu, \mu N$) channels to the inclusive cross sections is about 60%.

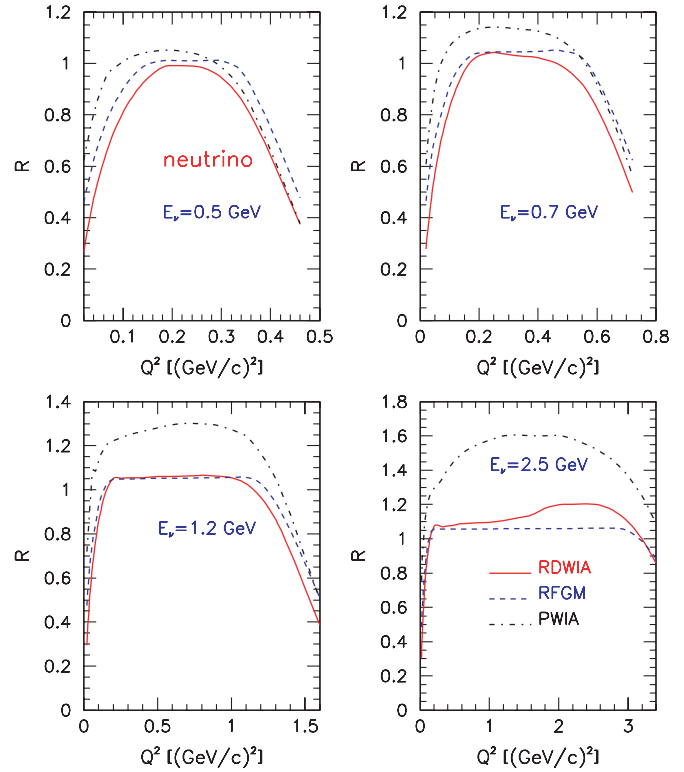


FIG. 6. (Color online) Ratio $R(\varepsilon_\nu, Q^2)$ vs. the four-momentum transfer Q^2 for neutrino scattering off ^{12}C and for the four values of incoming neutrino energy: $\varepsilon_\nu = 0.5, 0.7, 1.2$, and 2.5 GeV. As shown in the key, the cross sections were calculated with the RDWIA, PWIA, and RFGM.

Nuclear effects on the shape of the four-momentum transfer Q^2 distribution, i.e., the ratio $R(\varepsilon_\nu, Q^2) = (d\sigma/dQ^2)_{\text{nuc}} / (d\sigma/dQ^2)_{\text{free}}$, where $(d\sigma/dQ^2)_{\text{nuc}}$ is the cross section scaled with number of neutrons/protons in the target and $(d\sigma/dQ^2)_{\text{free}}$ is the cross section for (anti-)neutrino scattering off the free nucleon, are presented in Fig. 6 for neutrino and in Fig. 7 for antineutrino as functions of Q^2 . Here, the results obtained in the RDWIA for energies $\varepsilon_\nu = 0.5, 0.7, 1.2$ and 2.5 GeV are compared with those calculated in the PWIA and Fermi gas model. The nuclear effects are seen at low Q^2 ; the tail of the momentum distribution at high Q^2 , an overall suppression, and a slight change in the slope in the middle region at $\varepsilon_\nu \geq 1$ GeV is also observed. The range of Q^2 where $R \approx \text{const.}$, i.e. nuclear effects are negligible and therefore cannot modify the value of M_A , increases with incoming neutrino energy. At energies higher than 1 GeV, the range $0.3 \leq Q^2 \leq 1$ (GeV/c) 2 can be used for M_A extraction from Q^2 shape-only fit.

We calculated $d\sigma/dQ^2$ cross sections at energy of 700 MeV in the RDWIA and Fermi gas model with $M_A = 1.032$ and 1.32 GeV. The results are shown in Fig. 8 as functions of Q^2 . Apparently, at low $Q^2 \leq 0.1$ (GeV/c) 2 the cross sections depend weakly on the value of the axial mass and Q^2 distributions are controlled by nuclear effects.

The inclusive neutrino and antineutrino cross sections for energies $\varepsilon_\nu = 0.5, 0.7, 1.2$, and 2.5 GeV are presented in Figs. 9 and 10, which show $d\sigma/d\varepsilon_\mu$ as a function of

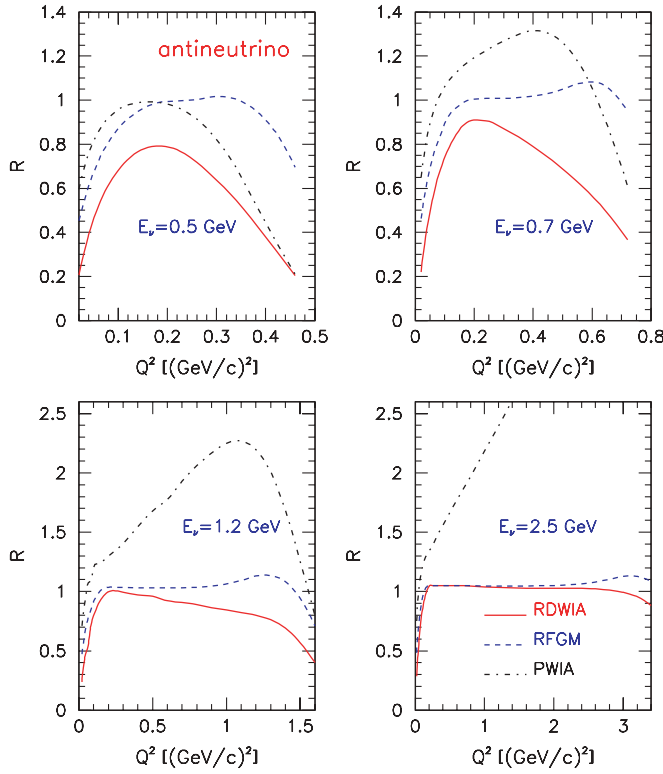


FIG. 7. (Color online) Same as Fig. 7 but for antineutrino scattering.

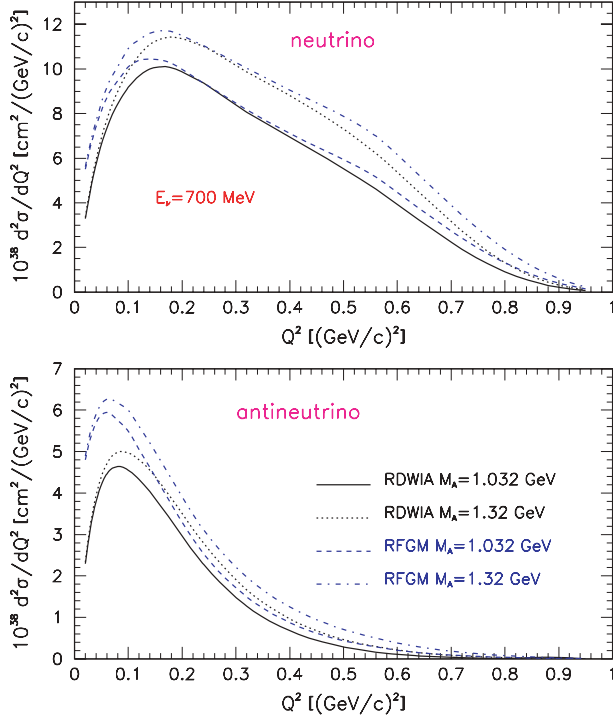


FIG. 8. (Color online) Inclusive cross section vs. the four-momentum transfer Q^2 for neutrino (upper panel) and antineutrino (lower panel) scattering off ^{12}C with energy $\varepsilon_\nu = 0.7$ GeV and for the two values of axial mass $M_A = 1.032$ and 1.32 GeV. As shown in the key, cross sections were calculated within the RDWIA and Fermi gas model.

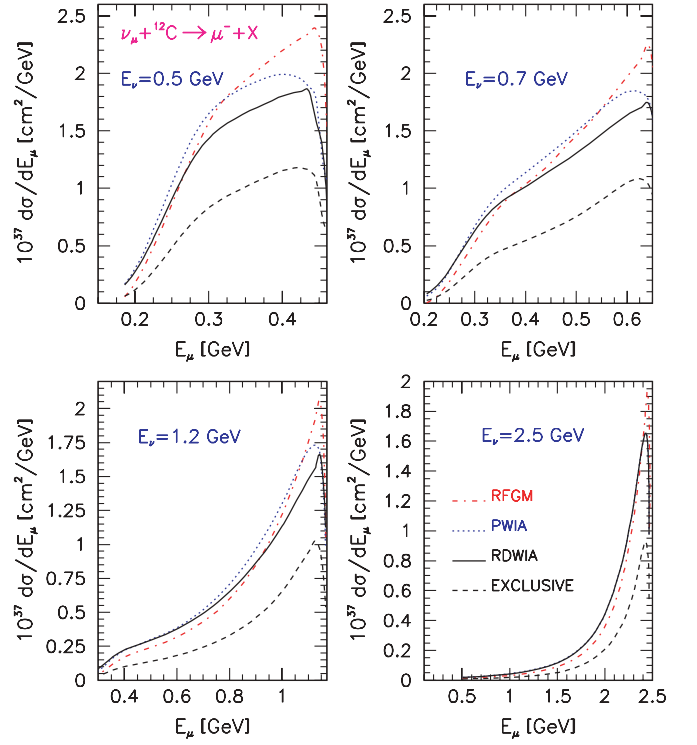


FIG. 9. (Color online) Inclusive cross section vs. the muon energy for neutrino scattering on ^{12}C and for the four values of incoming neutrino energy: $\varepsilon_\nu = 0.5, 0.7, 1.2,$ and 2.5 GeV. As shown in the key, the cross sections were calculated with the RDWIA, PWIA, RFGM, and RDWIA for the exclusive reaction.

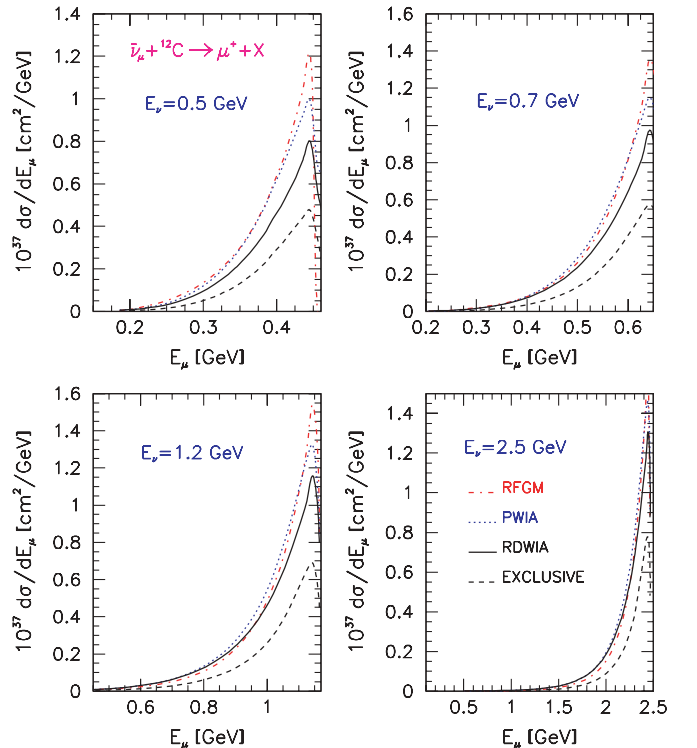


FIG. 10. (Color online) Same as Fig. 9 but for antineutrino.

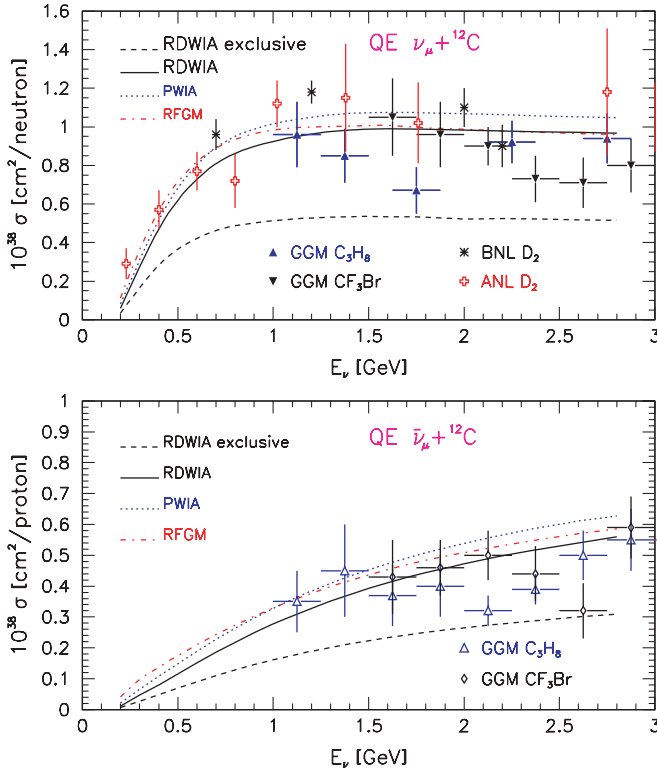


FIG. 11. (Color online) Total cross section for the CC QE scattering of muon neutrino (upper panel) and antineutrino (lower panel) on ^{12}C as a function of incoming (anti-)neutrino energy. The solid line is the RDWIA result while the dashed-dotted and dotted lines are the RFGM and PWIA results, respectively. The dashed line is the RDWIA result for exclusive reaction. Data points for different targets are from Refs. [62–65].

muon energy. Here, the results obtained in the RDWIA with $M_A = 1.032$ GeV are compared with the inclusive cross sections calculated in the PWIA, RFGM, and RDWIA for the exclusive reaction. The cross-section values obtained in the RFGM are higher than those obtained within the RDWIA. For neutrino (antineutrino) cross sections in the region close to the maximum this discrepancy is about 25%(49%) for $\varepsilon_\nu = 0.5$ GeV and 23%(29%) for $\varepsilon_\nu = 2.5$ GeV. The contribution of $(\nu, \mu N)$ channels to the inclusive cross sections is about 60%.

The neutrino and antineutrino total cross sections, calculated with $M_A = 1.032$ GeV up to a neutrino energy of 2.8 GeV, are shown in Fig. 11 together with data of Refs. [62–65]. Also shown are the results obtained in the RFGM, PWIA as well as the contribution of the exclusive channels to the total cross sections. The cross sections are scaled with the number of neutrons/protons in the target. The ratio between the neutrino cross sections calculated in the RFGM and RDWIA decreases with neutrino energy from about 1.15 for $\varepsilon_\nu = 0.5$ GeV to 1.02 for $\varepsilon_\nu = 2.6$ GeV. For the antineutrino cross sections this ratio is about 1.5 for $\varepsilon_\nu = 0.5$ GeV, and 1.05 for $\varepsilon_\nu = 2.6$ GeV. The contribution of the exclusive channels is about 60%. The results presented in Fig. 11 show significant nuclear-model dependency for energies less than 1 GeV.

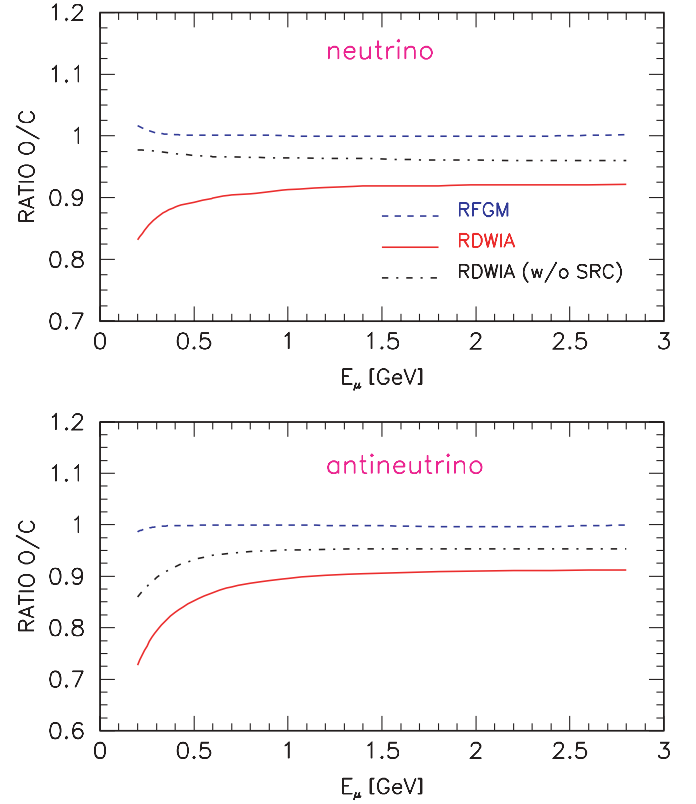


FIG. 12. (Color online) Ratio of the total cross sections per neutrons/protons $R = O/C$ for CC QE scattering of muon neutrino (upper panel) and antineutrino (lower panel) scattering on ^{16}O and ^{12}C vs. incoming (anti-)neutrino energy. The solid line is the RDWIA result, while the dashed and dashed-dotted lines are, respectively, the RFGM and RDWIA without contributions of the short-range correlations.

The RDWIA prediction for the CC QE flux-averaged total cross section is compared with the experimental result from the LSND Collaboration at Los Alamos for the $^{12}\text{C}(\nu_\mu, \mu^-)$ reaction [66]. The mean energy of the neutrino flux above threshold is 156 MeV. The calculated value of 10.14×10^{-40} cm 2 is in a good agreement with measured value of $(10.46 \pm 0.3 \pm 1.8) \times 10^{-40}$ cm 2 .

To compare the CC QE total cross sections for (anti-)neutrino scattering on the oxygen [21] and carbon targets, we calculated the $R(\varepsilon_\nu) = (\sigma_{\text{tot}}^O)_{\text{nucl}} / (\sigma_{\text{tot}}^C)_{\text{nucl}}$ ratio where the cross sections $(\sigma_{\text{tot}}^i)_{\text{nucl}}$ are scaled with the number of neutrons/protons in the targets. The results obtained in the RFGM and RDWIA are shown in Fig. 12. The Fermi gas model predicts almost identical values of $(\sigma_{\text{tot}}^i)_{\text{nucl}}$ for ^{16}O and ^{12}C . In the RDWIA approach the cross section calculated for oxygen is lower than that for carbon. For the neutrino (antineutrino) scattering this ratio is 0.90(0.88) at $\varepsilon_\nu = 0.7$ GeV and 0.92(0.91) at $\varepsilon_\nu = 2.6$ GeV.

To study the NN -correlation effects, we calculated the ratio $R(\varepsilon_\nu)$ without the NN -correlation contribution, i.e., with $S_\alpha = 1$ for all bound nucleon states in the oxygen and carbon targets. The difference between the results obtained with and without the high-momentum component contribution is about 5% for $\varepsilon_\nu \geq 1$ GeV. In Ref. [21] it was shown that

the NN -correlation effect reduces the total cross section in proportion to the missing strength in the nuclear ground state, which is about 25% for ^{16}O and 11% for ^{12}C .

Therefore, in the long-baseline neutrino oscillation experiments a part of the near detector must include some of the same target material, as the far detector to reduce the systematic uncertainty due to nuclear effects on the CC QE total cross section.

IV. CONCLUSIONS

In this article, we study electron and CC quasielastic (anti-)neutrino scattering on a carbon target in different approximations (PWIA, RDWIA, RFGM) placing particular emphasis on the nuclear-model dependence of the results. In RDWIA, the LEA program, adapted to neutrino interactions, was used to calculate the differential and reduced exclusive cross sections. We found that the reduced cross sections for (anti-)neutrino scattering are similar to those of electron scattering and the latter are in good agreement with the electron data. In calculating the inclusive and total cross sections, the imaginary part of a relativistic optical potential was neglected and the SRC effect in the target ground state was taken into account. This approach was tested against electron-carbon inclusive scattering data. This test revealed an overall agreement with the data, with the differences between the calculated and the measured cross sections in the peak region less than 12%.

We calculated $d\sigma/dQ^2$ cross sections for different neutrino energies and estimated the range of Q^2 where nuclear effects

on the shape of Q^2 distribution are negligible. Also, it was shown that at low $Q^2 < 0.1$ (GeV/c) 2 the cross sections depend weakly on the values of the axial mass.

The CC QE total cross sections predicted by the RFGM are higher than the corresponding values obtained in the RDWIA and this difference decreases with neutrino energy. The flux-averaged total cross section was calculated within the RDWIA approach and compared with the experimental result from the LSND collaboration. The calculated cross section is in good agreement with the data. We compared the CC QE total cross sections (scaled with the number of neutrons/protons in the target) for (anti-)neutrino scattering on the oxygen and carbon targets and found that the cross sections calculated within the RDWIA for oxygen are lower than those calculated for carbon and the SRC effects increase this difference.

We conclude that the data favor the results obtained in the RDWIA model, which has been modified with phenomenological spectroscopic factors and nucleon high-momentum components in the target. This indicates that the use of this model in Monte Carlo simulations of the neutrino detector response would allow one to reduce the systematic uncertainty in neutrino oscillation parameters.

ACKNOWLEDGMENTS

The author greatly acknowledges S. Kulagin, J. Morfin, G. Zeller, N. Jachowicz, M. Wascko, R. Gran, and V. Takhistov for fruitful discussions at different stages of this work.

-
- [1] A. A. Aguilar-Arevalo *et al.* (MiniBooNE Collaboration), *Phys. Rev. Lett.* **100**, 032301 (2008).
 - [2] A. K. Hiraide *et al.* (SciBooNE Collaboration), *Phys. Rev. D* **78**, 112004 (2008).
 - [3] P. Adamson *et al.* (MINOS Collaboration), *Phys. Rev. D* **77**, 072002 (2008).
 - [4] K. S. McFarland *et al.* (MiNERvA Collaboration), *Nucl. Phys. B, Proc. Suppl.* **159**, 107 (2006).
 - [5] T. Nakadaira *et al.* (T2K Collaboration), *Nucl. Phys. B, Proc. Suppl.* **149**, 303 (2006).
 - [6] G. Rosa *et al.* (OPERA Collaboration), *Nucl. Phys. B, Proc. Suppl.* **145**, 98 (2005).
 - [7] D. S. Ayres *et al.* (NOvA Collaboration), arXiv:hep-ex/0503053.
 - [8] A. Vacheret *et al.* (T2K Collaboration), *AIP Conf. Proc.* **967**, 66 (2007).
 - [9] G. P. Zeller, arXiv:hep-ex/0312061.
 - [10] R. A. Smith and E. J. Moniz, *Nucl. Phys.* **B43**, 605 (1972).
 - [11] A. V. Butkevich and S. P. Mikheyev, *Phys. Rev. C* **72**, 025501 (2005).
 - [12] R. Gran *et al.* (K2K Collaboration), *Phys. Rev. D* **74**, 052002 (2006).
 - [13] O. Benhar, N. Farina, H. Nakamura, M. Sakuda, and R. Seki, *Phys. Rev. D* **72**, 053005 (2005).
 - [14] O. Benhar and D. Meloni, *Nucl. Phys.* **A789**, 379 (2004).
 - [15] A. Meucci, C. Giusti, and F. D. Pacati, *Nucl. Phys.* **A739**, 277 (2004).
 - [16] A. Meucci, C. Giusti, and F. D. Pacati, *Nucl. Phys.* **A744**, 307 (2004).
 - [17] A. Meucci, C. Giusti, and F. D. Pacati, *Phys. Rev. C* **77**, 034606 (2008).
 - [18] C. Maieron, M. C. Martinez, J. A. Caballero, and J. M. Udias, *Phys. Rev. C* **68**, 048501 (2003).
 - [19] M. C. Martinez, P. Lava, N. Jachowicz, J. Ryckebusch, K. Vantournhout, and J. M. Udias, *Phys. Rev. C* **73**, 024607 (2006).
 - [20] N. Jachowicz, P. Vancraeyveld, P. Lava, C. Praet, and J. Ryckebusch, *Phys. Rev. C* **76**, 055501 (2007).
 - [21] A. V. Butkevich and S. A. Kulagin, *Phys. Rev. C* **76**, 045502 (2007).
 - [22] A. V. Butkevich, *Phys. Rev. C* **78**, 015501 (2008).
 - [23] K. S. Kim, B. G. Yu, M. K. Cheoun, T. K. Choi, and M. T. Chung, *J. Phys. G* **34**, 2643 (2007).
 - [24] K. S. Kim, M. K. Cheoun, and B. G. Yu, *Phys. Rev. C* **77**, 054604 (2008).
 - [25] J. Nieves, J. E. Amaro, and M. Valverde, *Phys. Rev. C* **70**, 055503 (2004).
 - [26] J. Nieves, M. Valverde, and M. J. Vicente Vacas, *Phys. Rev. C* **73**, 025504 (2006).
 - [27] M. S. Athar, S. Chauhan, S. K. Singh, and M. J. Vicente Vacas, arXiv:0808.1437 [nucl-th].
 - [28] M. S. Athar, S. Chauhan, and S. K. Singh, arXiv:0808.2103 [nucl-th].
 - [29] J. A. Caballero, J. E. Amaro, M. B. Barbaro, T. W. Donnelly, C. Maieron, and J. M. Udias, *Phys. Rev. Lett.* **95**, 252502 (2005).
 - [30] J. A. Caballero, *Phys. Rev. C* **74**, 015502 (2006).

- [31] J. E. Amaro, M. B. Barbaro, J. A. Caballero, and T. W. Donnelly, *Phys. Rev. Lett.* **98**, 242501 (2007).
- [32] J. E. Amaro, M. B. Barbaro, J. A. Caballero, T. W. Donnelly, and J. M. Udias, *Phys. Rev. C* **75**, 034613 (2007).
- [33] M. C. Martinez, J. A. Caballero, T. W. Donnelly, and J. M. Udias, *Phys. Rev. C* **77**, 064604 (2008).
- [34] T. Leitner, O. Buss, L. Alvarez-Ruso, and U. Mozel, *Phys. Rev. C* **79**, 034601 (2009).
- [35] J. J. Kelly, <http://www.physics.umd.edu/enp/jjkelly/LEA>.
- [36] Ciofi degli Atti and S. Simula, *Phys. Rev. C* **53**, 1689 (1996).
- [37] S. A. Kulagin and R. Petti, *Nucl. Phys.* **A765**, 126 (2006).
- [38] T. de Forest, *Nucl. Phys.* **A392**, 232 (1983).
- [39] P. Mergell, U.-G. Meissner, and D. Drechsel, *Nucl. Phys.* **A596**, 367 (1996).
- [40] J. J. Kelly, *Phys. Rev. C* **59**, 3256 (1999).
- [41] B. Serot and J. Walecka, *Adv. Nucl. Phys.* **16**, 1 (1986).
- [42] C. J. Horowitz, D. P. Murrack, and Brian D. Serot, in *Computational Nuclear Physics I: Nuclear Structure*, edited by K. Langanke, J. A. Maruhn, and Steven E. Koonin (Springer-Verlag, Berlin, Heidelberg, 1991), p. 129.
- [43] J. J. Kelly, *Phys. Rev. C* **71**, 064610 (2005).
- [44] D. Rohe *et al.*, *Nucl. Phys. B, Proc. Suppl.* **159**, 152 (2006).
- [45] T. Frick, K. S. A. Hassaneen, D. Rohe, and H. Müther, *Phys. Rev. C* **70**, 024309 (2004).
- [46] O. Benhar, A. Fabrocini, and S. Fantoni, *Phys. Rev. C* **41**, R24 (1990).
- [47] J. M. Udias, P. Sarriguren, E. Moya de Guerra, E. Garrido, and J. A. Caballero, *Phys. Rev. C* **51**, 3246 (1995).
- [48] M. Hedayati-Poor, J. I. Johansson, and H. S. Sherif, *Phys. Rev. C* **51**, 2044 (1995).
- [49] E.D. Cooper, S. Hama, B. C. Clark, and R. L. Mercer, *Phys. Rev. C* **47**, 297 (1993).
- [50] S. Frullani and J. Mougey, *Adv. Nucl. Phys.* **14**, 1 (1984).
- [51] D. Dutta *et al.*, *Phys. Rev. C* **68**, 064603 (2003).
- [52] A. Meucci, F. Capuzzi, C. Giusti, and F. D. Pacati, *Phys. Rev. C* **67**, 054601 (2003).
- [53] D. Baran *et al.*, *Phys. Rev. Lett.* **61**, 400 (1988).
- [54] J. S. O'Connell *et al.*, *Phys. Rev. C* **35**, 1063 (1987).
- [55] R. R. Whitney, I. Sick, J. R. Ficenec, R. D. Kephart, and W. P. Trower, *Phys. Rev. C* **9**, 2230 (1974).
- [56] P. Barreau *et al.*, *Nucl. Phys.* **A402**, 515 (1983).
- [57] D. Day *et al.*, *Phys. Rev. C* **48**, 1849 (1993).
- [58] X. Espinal and F. Sanchez, *AIP Conf. Proc.* **967**, 117 (2007).
- [59] V. Bernard, L. Elouadrhiri, and U. G. Meissner, *J. Phys. G* **28**, R1 (2002).
- [60] V. Lyubushkin *et al.*, (NOMAD Collaboration), arXiv:0812.4543 [hep-ex].
- [61] H. Budd, A. Bodek, and J. Arrington, arXiv:hep-ex/0308005.
- [62] W. A. Mann *et al.*, *Phys. Rev. Lett.* **31**, 844 (1973).
- [63] N. J. Baker *et al.*, *Phys. Rev. D* **23**, 2499 (1981).
- [64] M. Pohl *et al.*, *Lett. Nuovo Cimento* **26**, 332 (1979).
- [65] J. Brunner *et al.*, *Z. Phys. C* **45**, 551 (1990).
- [66] L. B. Auerbach *et al.*, *Phys. Rev. C* **66**, 015501 (2002).