Interference Between Direct Nuclear Reactions and Coulomb Excitation with Alpha Particles on 154 Sm, 166 Er, and 182 W[†]

C. E. Bemis, Jr., P. H. Stelson, F. K. McGowan, W. T. Milner, J. L. C. Ford, Jr., R. L. Robinson, and W. Tuttle* Oak Ridge National Laboratory, Oak Ridge, Tennessee 37830 (Received 25 June 1973)

> Striking destructive interference effects have been observed in the ⁴He excitation of the 2^+ and 4^+ ground-state band rotational states in deformed even- A ¹⁵⁴Sm, ¹⁶⁶Er, and ¹⁸²W. The E2 and E4 transitio moments and charge deformation parameters, β_{20}^c and β_{40}^c are given.

NUCLEAR REACTIONS 154 Sm(α , α'), E=11-19 MeV; 166 Er(α , α'), E=12.5-19.5 MeV, 182 W(α , α'), E = 13-21 MeV; measured $\sigma(E_{\alpha}; \theta = 150^{\circ})$; deduced $B(E2)$, $B(E4)$. Enriched targets. Extracted model-dependent deformations, β_{20} and β_{40} .

I. INTRODUCTION

At incident projectile energies sufficiently below the Coulomb barrier so that the projectile is well outside the range of nuclear forces, the elastic and inelastic scattering processes are completely described by Coulomb-excitation theory.¹ Since the cross sections for Coulomb excitation are a strong function of projectile energy, it is desirable to perform such experiments at the highest possible "safe" bombarding energy. ^A central experimental problem in Coulomb excitation is the continuing development of criteria for "safe" bombarding energies. When both Coulomb excitation and direct nuclear excitation contribute to the target excitation, the amplitudes are coherent and interference occurs. This interference markedly affects the experimental results if the experiments are analyzed under the assumptions of pure Coulomb excitation.

The interference between Coulomb excitation and direct nuclear excitation has been explored using α particles by several workers²⁻⁴ and also investigated using heavy-ion projectiles.⁵ In the recent action of μ work of Brückner *et al*.,⁴ the α -particle excitation probabilities of the 2^+ and 4^+ ground-state band rotational states in 152 Sm were investigated in an energy range spanning the classical Coulomb barrier. The results from the sub-Coulomb barrier region were analyzed using Coulomb-excitation theory to yield the electric transition matrix elements $M_{02}(E2)$ and $M_{04}(E4)$ and corresponding charge deformation parameters β_{20}^c and β_{40}^c . The experimental results at higher energies, in the region of the interference minima and above the Coulomb barrier, were analyzed with a deformed optical-model theory for the direct reactions including the effects of Coulomb excitation. The pronounced influence of direct nuclear excitation on Coulomb excitation at energies well below the

classical Coulomb barrier has prompted us to investigate this effect for three even-mass targets spanning the rare-earth deformed region, 154 Sm, 166 Er, and 182 W, in a manner similar to that of Brückner et al .⁴ We were particularly interested in the sensitivity of the derived electric quadrupole and hexadecapole transition moments to projectile energy as well as the influence of the sign of the hexadecapole charge deformation parameter β_{40}^c on the Coulomb-nuclear interference effect.

II. EXPERIMENTAL METHOD AND RESULTS

Elastically and inelastically scattered 'He ions at a laboratory angle of 150° from thin (25 μ g/cm²) isotopically pure targets of 154 Sm, 166 Er, and 182 W on carbon backings (40 μ g/cm²) were observed by means of an Enge split-pole magnetic spectrometer at the Oak Ridge EN tandem Van de Graaff accelerator. These targets were prepared using an electromagnetic isotope separator as described previously.⁶ Scattered particles were detected in the spectrometer focal plane with a gas-flow position-sensitive proportional counter in a manner identical to that previously reported by us in studies of the quadrupole and hexadecapole charge deformations of even-mass deformed nuclei in the $transurarium region.⁶ Excitation functions were$ measured in 0.5- or 1.0-MeV steps in the energy range 11.0 to 21.0 MeV which spans the classical Coulomb barrier region for these targets.

A representative spectrum is shown in Fig. 1 for the excitation of ¹⁶⁶Er with 18.5-MeV α particles. Excitation probabilities for the 2^+ , 4^+ , and higher states were determined relative to the elastic scattering by integration of the appropriate peak areas. In general, the experimental ratios $d\sigma_{a^+}/d\sigma_{el}$ were determined to an accuracy of 0.5 to 1% and the ratios $d\sigma_{4}$ +/d σ_{el} to an accuracy of 3 to 5%.

The excitation probabilities using the lowest

1934

 $\frac{8}{5}$

FIG. 1. Spectrum observed for the scattering of 18.5-MeV α particles from ¹⁶⁶Er at an angle of 150° (lab).

energy data for the 2^+ and 4^+ members of the ground-state bands as well as higher 2' states were analyzed using the semiclassical coupledchannels Coulomb -excitation code of Winther and deBoer⁷ which was modified to include $E1$, $E3$, and $E4$ excitations. Rotational $E2$ and $E4$ static and transition moments were used for the intra-groundstate band transitions and the calculations included all possible $E2$ and $E4$ excitations up to and including the 6' state. The influences of the higher 2^+ , 4^+ , and 3^- states on the ground-state band excitation probabilities are very small but they were included in the calculations. We have applied the second-order quantum mechanical corrections to the calculated semiclassical 4' excitation probabilities for the pure double $E2$ excitation using the calculations of Alder, Roesel, and Morf. ' These corrections reduced the calculated semiclassical excitation probability for the double E2 process by -5% for the cases studied here.

The matrix elements $\langle 2^* \| \mathfrak{M}(E2) \| 0^* \rangle$ and $\langle 4^* \Vert m(E4) \Vert 0^* \rangle$ and the E2 elements for observed higher states were extracted from the 11.0-MeV data for 154 Sm, the 12.5-MeV data for 166 Er, and the 13.0-MeV data for ^{182}W . The experimental excitation probabilities for the 4' states exceeded the calculated probabilities by $\neg 6\%$ for 166 Er and

¹⁸²W and \sim 20% for ¹⁵⁴Sm if only E2 excitations were considered. The excess 4' excitation was interpreted as due to the presence of E4 excitations.

In the analyses, we have used the sign convention for $\langle 2^* \| \mathfrak{M}(E2) \| 0^* \rangle$ and all other E2 intraground-state band rotational matrix elements which correspond to the prolate quadrupole shape $(\beta_{20} > 0)$. Theory^{9,10} and previous experimental information both from (α, α') inelastic scatterinformation both from (α, α') inelastic scatter-
ing^{11,12} and from recent Coulomb excitation experiments¹³⁻¹⁶ support the prolate quadrupole shape $(\beta_{\infty} > 0)$ and indicate that the hexadecapole deformation β_{40} is positive for ¹⁵⁴Sm, nearly zero for 166 Er, and negative for 182 W. We have, in a similar fashion, derived the E4 transition moments $\langle 4^* \vert \sin(E4) \vert \vert 0^* \rangle$ assuming $\beta_{40} > 0$ for ¹⁵⁴Sm and ¹⁶⁶Er and β_{40} < 0 for ¹⁸²W.

The matrix elements $\langle 2^+ \|\mathfrak{M}(E2)\|0^+$ and $\langle 4^+ \|\mathfrak{M}(E4) \| 0^+ \rangle$ as derived above are listed in Table I together with the charge deformation parameters β_{20}^c and β_{40}^c for the uniform or homogeneous distribution and for the deformed Fermi distribution (modified " c " distribution). The matrix elements are related to the volume integral via

$$
\langle I_f = \lambda \left\| \Re(\mathbf{E}\lambda) \right\| I_i = 0 \rangle = \int r^{\lambda} Y_{\lambda 0}(\theta) \rho(r, \theta) d\tau \qquad (1)
$$

using $R(\theta) = R_0[1+\beta_{20}Y_{20}(\theta) + \beta_{40}Y_{40}(\theta)]$ for the shape of the nuclear surface. For the uniform charge distribution,

$$
\rho(r,\,\theta) = \frac{3Ze}{4\pi (r_0 A^{1/3})^3} \quad \text{for } r \leq R(\theta) \tag{2}
$$

using r_0 = 1.2 fm and for the deformed Fermi distribution,

$$
\rho(r,\,\theta) = \frac{\rho_0}{e^x + 1} \quad , \tag{3}
$$

where

$$
x=\frac{r-R(\theta)}{a}
$$

TABLE I. Experimental transition moments and charge deformation parameters derived from Coulomb-excitation measurements with 4 He ions for 164 Sm, 166 Er, and 182 W. Errors include in addition to the usual statistical uncertainties, an uncertainty corresponding to $a \pm 50$ keV possible error in the incident beam energy.

	$ \mathfrak{M}(E2) 0^{+}\rangle$ (2^{+}) (e _b)	$\langle 4^+ $ $\Re(E4) $ $\langle 0^+ \rangle$ (e b ²)	Uniform distribution ^a		Deformed Fermi distribution ^a	
			$\beta_{2.0}$	β_{40}	β_{20}	β_{40}
154 Sm $166_{\rm Er}$ 182W	2.063 ± 0.015	$+0.58 \pm 0.14$	0.274 ± 0.012	$+0.112 \pm 0.039$	0.301 ± 0.012	$+0.112 \pm 0.040$
	2.378 ± 0.011	$+0.32 \pm 0.16$	0.301 ± 0.011	$+0.020 \pm 0.039$	0.329 ± 0.012	$+0.019 \pm 0.040$
	2.053 ± 0.015	$-0.63\substack{+0.34 \\ -0.63\substack{+0.34 \\ -0.63\substack{+$	0.266 ± 0.009	-0.181 ± 0.060	0.290 ± 0.010	-0.187 ± 0.062

^a See text for explanation of the deformed charge distributions and the relationship to the measured transition moments.

and

$$
\rho_0 = Ze \bigg/ \int \frac{d\tau}{1+\exp[(r-r_0A^{1/3})/a]};
$$

we have used $a=0.6$ fm and $r_0=1.1$ fm. The deformation parameters β_{20} and β_{40} were determined by evaluating Eq. (1) using an iterative numerical procedure until the measured moments were reproduced. The central charge density was held constant at the value it would have had for zero deformation and $R_0 = r_0 A^{1/3}$ was adjusted slightly in order to conserve total nuclear charge for the deformed shape.

FIG. 2. Energy dependence of the ratios of experimental 2^+ and 4^+ excitation probabilities for ⁴He ions to the calculated excitation probability expected for pure Coulomb excitation for 154 Sm, 166 Er, and 182 W. Measurements were performed at 150° (lab) and the curves connecting the experimental data points have been drawn to guide the eye.

III. DISCUSSION

Our $E2$ and $E4$ transition moments for 154 Sm, 166 Er, and E2 transition moment for 182 W compare reasonably well with the results of previous α particle Coulomb-excitation experiments.¹³⁻¹⁷ It should be emphasized, however, that the relatively small differences in the $\langle 2^* || \mathfrak{M}(E2) || 0^* \rangle$ values between the various experiments listed above could well be explained by small uncertainties in the incident 4 He ion energy. For example, a 50-keV error in the absolute 4 He ion energy at 11 MeV would introduce a systematic error of 1.6% in the $B(E2, 0^+ \rightarrow 2^+)$ value for ¹⁵⁴Sm. Since the derivation of the E4 transition moments depends sensitively on the $B(E2)$ values, the difference in the E4 moments between the various workers may well be due to this effect also. Our $E2$ and $E4$ transition moments listed in Table I include the uncertainty associated with a possible ± 50 keV uncertainty in the incident 4 He ion energy. We have also derived $B(E2, 0^+ \rightarrow 2^{+\prime})$ values of 0.142 ± 0.005 $e^2 b^2$ and 0.124 ± 0.010 e^2b^2 for the 787- and 1221-keV states in 166 Er and 182 W, respectively, from these experiments.

Using the matrix elements given in Table I, the excitation probabilities for the 2^+ and 4^+ states, assuming only Coulomb excitation, were calculated and compared to the experimental excitation probabilities for the higher energy measurements. This comparison is shown in Fig. 2 for the 2^+ and 4^* states in 154 Sm, 166 Er, and 182 W where we have plotted the ratios of excitation probabilities $(d\sigma/d\sigma_{\rm el})_{\rm expt.}/(d\sigma/d\sigma_{\rm el})_{\rm calc.}$ as a function of the ⁴He bombarding energy. Deviations from pure Coulomb excitation and the onset of contributions from direct nuclear excitations are immediately obvious from these figures. As the bombarding energy is increased, the experimental excitation probability decreases below that expected for pure Coulomb excitation due to the interference with the direct nuclear excitations. The experimental excitation probability eventually exceeds that expected from Coulomb excitation for the highest energies where direct nuclear excitations are the dominant excitation mechanism. We have observed similar inter
ference effects for the 787-keV 2⁺ state in ¹⁶⁶Er ference effects for the 787-keV 2^+ state in $^{166}\rm{Er}$ and the 1221-keV 2^+ state in 182 W. These effects are qualitatively similar to those observed for the 2' ground-state band states although with much poorer statistical accuracy.

Several qualitative features about the curves shown in Fig. 2 are of interest. Deviations from pure Coulomb excitation $(1-2\%)$ can occur at quite low bombarding energies which correspond to a distance d of \sim 8 fm between the surfaces of the projectile and target if we assume spherical surfaces

with radii of $1.2 A^{1/3}$ fm. The distance d is given by the following relation:

$$
d(\text{fm}) = 0.7199 \left(1 + \frac{A_1}{A_2} \right) \frac{Z_1 Z_2}{E(\text{MeV})_{\text{lab}}} \left[1 + \csc\left(\frac{1}{2} \theta_{\text{c.m.}}\right) \right]
$$

$$
- \left[r_0 (A_1^{1/3} + A_2^{1/3}) \right]. \tag{4}
$$

The maximum interference effect for the 2' states occurs at an average distance of 3.8 fm between the surfaces while the distance d for the interference minima for the 4' states appears to depend upon the strength of the direct nuclear ezcitations leading to the 4' states. In the case of 154 Sm, the 4⁺ excitation via the direct nuclear mechanism far exceeds that of Coulomb excitation only 2-3 MeV above the interference minimum for the 2' state. In this case, the interference minimum for the 4' state occurs at a lower energy (greater separation distance) than the 2^+ state. For 182 W, the opposite appears to be true. Here, the excitation of the 4' state via the direct nuclear mechanisms appears to be somewhat weaker and the interference minimum occurs at a higher energy (smaller separation distance) than the 2'

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state. The depth of the destructive interference minimum is very much larger in the ^{182}W case than for 154 Sm or 166 Er. The 4⁺ interference minimum for 166 Er occurs at approximately the same energy as for the 2' state.

Our results for 154 Sm, 166 Er, and 182 W are significantly different than the results obtained by Brückner et al.⁴ for 152 Sm. While the interference for the 2^+ states appear similar to that of 152 Sm. we observe substantial interference for the 4' states which appears unlike that observed for 152 Sm. Moreover, we observe substantial differences between the three cases studied here for the 4' excitation curves which are most probably related to the magnitude and sign of the hexadecapole deformation parameter β_{40} . For ¹⁵⁴Sm β_{40} is large and positive, for $^{166}\text{Er } \beta_{40} \text{~}^{\circ}$ 0, and for $^{182}\text{W }\beta_{40}$ is large and negative which could explain the large interference effect observed for the 4^+ state in 182 W. Theoretical studies using a coupled-channels reaction code are in $progress¹⁸$ and should shed considerable light on the nature of the interference effect between Coulomb and direct nuclear excitations for these cases.

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