

Radiative decay of the dynamically generated open and hidden charm scalar meson resonances $D_{s0}^*(2317)$ and $X(3700)$

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We present the formalism for the decay of dynamically generated scalar mesons with open- or hidden charm and give results for the decay of $D_{s0}^*(2317)$ to γD_s^* plus that of a hidden charm scalar meson state predicted by the theory around 3700 MeV decaying into $\gamma J/\psi$.

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I. INTRODUCTION

The discovery of charmed scalar meson resonances at BABAR, Belle, and CLEO [1–4] has stimulated a fruitful line of research, suggesting that their structure is much richer than what one might guess assuming the $q\bar{q}$ picture, which has proved quite successful in other areas [5]. Some authors have suggested a $qq\bar{q}\bar{q}$ structure [6,7] or mixing between the usual $q\bar{q}$ structure and four quark [8]. Also there have been suggestions that these states might be molecular states of the pseudoscalar mesons [9–13]. Similar to these latter works, but with subtle differences that we shall discuss later on, are the pictures where these states appear as dynamically generated in the context of unitarized chiral perturbation theory [14–17]. The works in Refs. [14–16] rely upon Lagrangians based on heavy quark symmetry, while the Lagrangian in Ref. [17] starts from an extension of the SU(3) chiral Lagrangian to SU(4) which is largely broken due to the implicit vector meson exchange characterizing the Weinberg-Tomozawa term of the chiral Lagrangian [18]. Because of this, the terms of the Lagrangian used in Ref. [17] are suppressed by the ratio of the light to heavy mass squared of the vector mesons. SU(4) Lagrangians with covariant derivatives adapted to include weak interactions are used in Ref. [19]. The Lagrangian in Ref. [17] contains the Lagrangian used in Refs. [14] and [16], which is suited for the study of open charm resonances like the $D_{s0}^*(2317)$, but it also contains other terms that allow one to study the hidden charm states. The comparison of the results using this Lagrangian with another one using a chiral symmetry breaking extension to SU(N) of the SU(3) results [20] allows one to have an idea of the uncertainties in the results. The stability of the $D_{s0}^*(2317)$ was confirmed, while the $X(3700)$ state could sometimes become a cusp instead of a bound state, but experimentally it would lead to a bump in the mass distributions in any case. Hence one can be confident that the new state should also be found.

The radiative decay of resonances has been usually suggested as a test for their nature [21,22]. In the present case, we are interested in the decays $D_{s0}^*(2317) \rightarrow D_s^* \gamma$ and $X(3700) \rightarrow \gamma J/\psi$. The first of these decays has been evaluated assuming varied structures for the resonance within quark models, vector meson dominance, light cone QCD sum rules, etc., [23–32] and more recently from the point of view of the $D_{s0}^*(2317)$ as a molecular state [33]. The $X(3700)$ has also been predicted in Ref. [34] as a molecular state assuming a reasonable interaction Lagrangian between the D and \bar{D} states. The radiative decay of this predicted state is reported here for the first time.

II. FORMULATION FOR THE RADIATIVE DECAY

In a picture of the scalar mesons as dynamically generated one needs to couple the photon to the meson components of the coupled channels. Here the reactions studied are

$$\begin{aligned} D_{s0}^*(2317) &\rightarrow \gamma D_s^* \\ X(3700) &\rightarrow \gamma J/\psi, \end{aligned}$$

and the technical way to evaluate them is considering the loop diagrams of Fig. 1.

These are the same diagrams used in the evaluation of the radiative decay of the $D_{s0}^*(2317)$ as a DK molecule in Ref. [33]. The differences are that here we do not need the wave function of the $D_{s0}^*(2317)$, we only need the couplings of the resonance to the $P\bar{P}$ channels, which are obtained in the study of these resonances as dynamically generated in Ref. [17]. Another difference is that we have more channels than DK , and this has some numerical effects on the results because of cancellations of terms in the most important channels D^+K^0 , D^0K^+ . Finally, although it provides a small contribution in Ref. [33], there is a term where the photon couples to the D_s^* . This term involves a transition $D_{s0}^*(2317) \rightarrow D_s^*$ that is allowed for a virtual D_s^* as would be the case here. Such terms mix the longitudinal part of the vector meson propagator with the scalar meson. However, to prevent the appearance of a pole of a scalar in the vector meson propagator, in a covariant formalism like the one we use, this transition amplitude must

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vanish for $P^2 = m_S^2$, with P and m_S being the total momentum and the mass of the scalar meson, respectively [35,36]. This is discussed in a related work on the radiative decay of axial vector mesons [37], but we address the problem in detail in the Appendix. There is also a diagram with the photon attached to the scalar resonance (for charged states) that is shown to vanish in the amplitude in Ref. [33] because of the Lorentz condition of the vector meson.

The two diagrams discussed above, together with those considered in Fig. 1, provide a set of gauge invariant terms, as shown explicitly in Ref. [33]. The two terms with the photon coupling to the external particles in the loop diagram play a role in the gauge invariant test of the theory, as shown in Ref. [33], but they vanish in the radiative decay amplitude, as we show in the Appendix.

The procedure to evaluate the radiative decay followed here for the dynamically generated scalar resonances has been tested with success in the decays $\phi \rightarrow f_0(980)\gamma$ and $\phi \rightarrow a_0(980)\gamma$ [38–40] with the f_0 and a_0 resonances dynamically generated from the interaction of the lowest order meson-meson chiral Lagrangian [41]. The present reaction is the time reversal reaction, in the charmed sector, of the radiative ϕ decay into a scalar and a photon. The same ideas presented here are used in the study of the radiative decay of the $f_0(980)$ and $a_0(980)$, as dynamically generated resonances, into $\gamma\rho$ and $\gamma\omega$ in Ref. [22].

The channels to which the $D_{s0}^*(2317)$ and the $X(3700)$ resonances have appreciable couplings in Ref. [17] are the

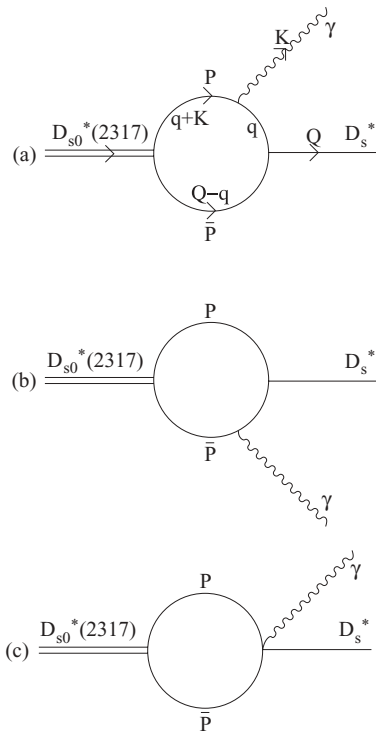


FIG. 1. Diagrams considered in the evaluation of the radiative decay $D_{s0}^*(2317) \rightarrow \gamma D_s^* P$ and \bar{P} are the pseudoscalar mesons that couple to the $D_{s0}^*(2317)$.

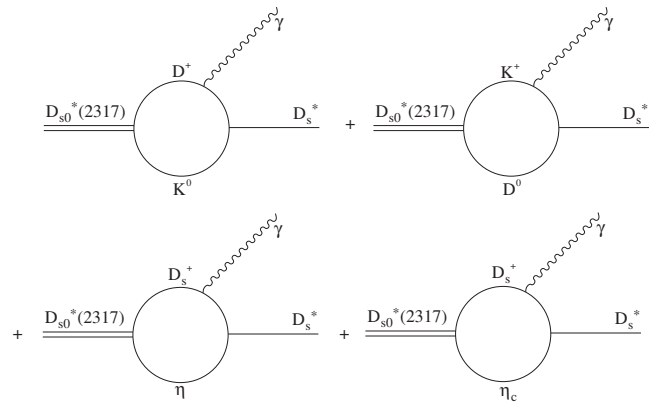


FIG. 2. Diagrams needed in the evaluation of the $D_{s0}^*(2317)$ radiative decay.

following:

$$D_{s0}^*(2317) : D^+ K^0, \quad D^0 K^+, \quad D_s^+ \eta, \quad D_s^+ \eta_c$$

$$X(3700) : D^+ D^-, \quad D^0 \bar{D}^0, \quad D_s^+ D_s^-.$$

We shall demonstrate that, using arguments of gauge invariance, we can overcome the evaluation of Diagram (c) of Fig. 1 and, as a consequence, we must only evaluate the diagrams of Fig. 2 for the $D_{s0}^*(2317)$ and of Fig. 3 for the $X(3700)$.

Let us proceed to the explicit evaluation of the diagrams. The amplitude of the diagram of Fig 2(a) is readily evaluated as

$$-iT = \int \frac{d^4q}{(2\pi)^4} (-i) g_{D_{s0}^*(2317) \rightarrow P\bar{P}} \times \frac{i}{(q+K)^2 - m_1^2 + i\epsilon} \frac{i}{q^2 - m_1^2 + i\epsilon} \times \frac{i}{(Q-q)^2 - m_2^2 + i\epsilon} (-i) e Q_1 \epsilon_\nu(\gamma) (q+q+K)^\nu \times (+i) \frac{1}{\sqrt{2}} \frac{M_V G_V}{f_\pi f_D} \epsilon_\mu(D_s^*) (q-Q+q)^\mu \lambda_\nu, \quad (1)$$

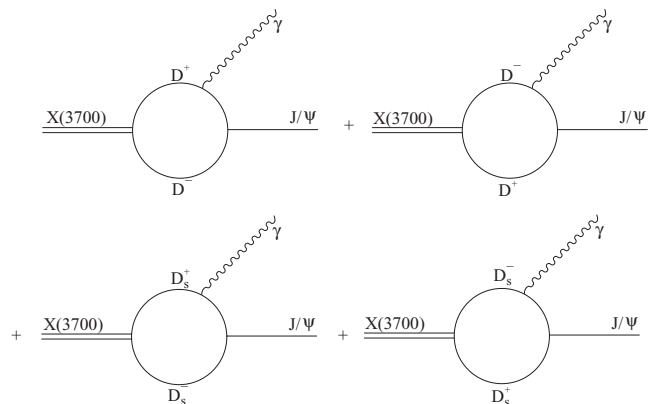


FIG. 3. Diagrams needed in the evaluation of the $X(3700)$ radiative decay.

TABLE I. Couplings of the resonances to the pseudoscalars.

Resonance	Channel	$g_{R \rightarrow P \bar{P}}$ (MeV)
$D_{s0}^*(2317)$	$D^+ K^0$	-7358
	$K^+ D^0$	-7358
	$D_s^+ \eta$	5993
	$D_s^+ \eta_c$	1541
X(3700)	$D^+ D^-$	7353
	$D^- D^+$	7353
	$D_s^+ D_s^-$	6740
	$D_s^- D_s^+$	6740

where m_1 and m_2 are the masses of the upper and lower pseudoscalar mesons in the loop diagram, eQ_1 is the charge ($e > 0$) of the upper pseudoscalar meson, M_V is the mass of the vector meson, and G_V is the VPP coupling ($G_V = 55$ MeV). The constant $g_{D_{s0}^*(2317) \rightarrow D^+ K^0}$ provides the coupling of the resonance to the $D^+ K^0$. In Table I we show the calculated couplings for the poles from Ref. [17] located at 2317.25 MeV and (3718.93-i0.06) MeV. For this last one we have neglected its imaginary part.

The coupling of the vector meson to the pseudoscalars is obtained from the SU(4) generalization (see Ref. [17]) of the ordinary SU(3) Lagrangian.

$$\mathcal{L}_{PPV} = \frac{-ig}{\sqrt{2}} \text{Tr}([\partial_\mu \phi, \phi] V^\mu), \quad (2)$$

with $g = -M_V G_V / f^2$ and the SU(4) matrices ϕ and V^μ given by

$$\phi = \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} + \frac{\eta_c}{\sqrt{12}} & \pi^+ & K^+ & \bar{D}^0 \\ \pi^- & \frac{-\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} + \frac{\eta_c}{\sqrt{12}} & K^0 & D^- \\ K^- & \bar{K}^0 & \frac{-2\eta}{\sqrt{6}} + \frac{\eta_c}{\sqrt{12}} & D_s^- \\ D^0 & D^+ & D_s^+ & \frac{-3\eta_c}{\sqrt{12}} \end{pmatrix} \quad (3)$$

$$V^\mu = \begin{pmatrix} \frac{\rho_\mu^0}{\sqrt{2}} + \frac{\omega_\mu}{\sqrt{6}} + \frac{J/\psi_\mu}{\sqrt{12}} & \rho_\mu^+ & K_\mu^{*+} & \bar{D}_\mu^{*0} \\ \rho_\mu^{*-} & \frac{-\rho_\mu^0}{\sqrt{2}} + \frac{\omega_\mu}{\sqrt{6}} + \frac{J/\psi_\mu}{\sqrt{12}} & K_\mu^{*0} & D_\mu^{*-} \\ K_\mu^{*-} & \bar{K}_\mu^{*0} & \frac{-2\omega_\mu}{\sqrt{6}} + \frac{J/\psi_\mu}{\sqrt{12}} & D_{s\mu}^{*-} \\ D_\mu^{*0} & D_\mu^{*+} & D_{s\mu}^{*+} & \frac{-3J/\psi_\mu}{\sqrt{12}} \end{pmatrix}. \quad (4)$$

In Eq. (1) we have chosen to substitute f^2 in the denominator by $f_\pi f_D$ following the prescription in Ref. [17] of associating f_π (the pion decay constant, $f_\pi = 93$ MeV) to

TABLE II. Coefficients λ_V for the coupling of the vector meson to the pseudoscalars.

Vector meson	Channel	λ_V
D_s^*	$D^+ K^0$	1
	$K^+ D^0$	-1
	$D_s^+ \eta$	$-2/\sqrt{6}$
	$D_s^+ \eta_c$	$2/\sqrt{3}$
J/ψ	$D^+ D^-$	$-2/\sqrt{3}$
	$D^- D^+$	$2/\sqrt{3}$
	$D_s^+ D_s^-$	$-2/\sqrt{3}$
	$D_s^- D_s^+$	$2/\sqrt{3}$

the light pseudoscalars and $f_D = 165$ MeV to the charmed pseudoscalars.

All the other diagrams are easily obtained by changing the couplings of the resonance to the channel and the constant λ_V to account for the different VPP vertices. The different values of λ_V are given in Table II.

By using the Lorentz condition for the photon and the vector meson,

$$\epsilon_\mu(D^{*+})Q^\mu = 0 \quad (5)$$

$$\epsilon_\nu(\gamma)K^\nu = 0, \quad (6)$$

the amplitude of Eq. (1) is simplified and we obtain

$$\begin{aligned} \mathcal{T} &= -ig_{D_{s0}^*(2317) \rightarrow P \bar{P}} e Q_1 \lambda_V \frac{4}{\sqrt{2}} \frac{M_V G_V}{f_\pi f_D} \epsilon_\mu(D_s^*) \epsilon_\nu(\gamma) \\ &\times \int \frac{d^4 q}{(2\pi)^4} \frac{1}{(q+K)^2 - m_1^2 + i\epsilon} \frac{1}{q^2 - m_1^2 + i\epsilon} \\ &\times \frac{1}{(Q-q)^2 - m_2^2 + i\epsilon} q^\mu q^\nu. \end{aligned} \quad (7)$$

Upon integration of the q variable one has the expression

$$\mathcal{T} = T^{\mu\nu} \epsilon_\mu(V) \epsilon_\nu(\gamma), \quad (8)$$

and Lorentz covariance provides the most general form for $T^{\mu\nu}$ as

$$\begin{aligned} T^{\mu\nu} &= a g^{\mu\nu} + b Q^\mu Q^\nu + c Q^\mu K^\nu \\ &+ d K^\mu Q^\nu + e K^\mu K^\nu. \end{aligned} \quad (9)$$

The Lorentz condition of Eqs. (5) and (6) removes the contributions of the b , c , and e terms, such that only the a and d terms contribute. In addition, gauge invariance (which is guaranteed when all the terms in Fig. 1 are accounted for) $T^{\mu\nu} K_\nu = 0$, implies $b = 0$ and $a + d Q \cdot K = 0$; so,

$$a = -d Q \cdot K, \quad (10)$$

such that only one term is needed in the evaluation. We choose to evaluate the d term because it is finite and only comes from the diagrams of Figs. 2 and 3. The procedure outlined here has been used before in the evaluation of the $\phi \rightarrow \gamma K^0 \bar{K}^0$ decay [42,43].

The amplitude \mathcal{T} is now easily written as

$$\mathcal{T} = -d(Q \cdot K g^{\mu\nu} - K^\mu Q^\nu) \epsilon_\mu(V) \epsilon_\nu(\gamma). \quad (11)$$

The evaluation of d is straightforward following the Feynman formalism. We write

$$\frac{1}{abc} = 2 \int_0^1 dx \int_0^x dy \frac{1}{(a + (b-a)x + (c-b)y)^3}, \quad (12)$$

with

$$a = (Q - q)^2 - m_2^2 \quad (13)$$

$$b = q^2 - m_1^2 \quad (14)$$

$$c = (q + k)^2 - m_1^2. \quad (15)$$

Upon a transformation $q = q' + Q(1-x) - Ky$, we are left with the integral

$$\int \frac{d^4 q'}{(2\pi)^4} \frac{(q' + Q(1-x) - Ky)^\mu}{(q'^2 + s + i\epsilon)^3} (q' + Q(1-x) - Ky)^\nu, \quad (16)$$

with $s = Q^2 x(1-x) + 2Q \cdot K(1-x)y - m_2^2 + (m_2^2 - m_1^2)x$, which shows that the contribution to the d term comes from

$$\int \frac{d^4 q'}{(2\pi)^4} \frac{K^\mu Q^\nu (1-x)y}{(q'^2 + s + i\epsilon)^3}, \quad (17)$$

where two powers of q' have disappeared from the integral and hence it is convergent. The q' integral is also readily obtained following the Feynman formalism

$$\int \frac{d^4 q'}{(2\pi)^4} \frac{1}{(q'^2 + s + i\epsilon)^3} = \frac{i\pi^2}{(2\pi)^4} \frac{1}{2} \frac{1}{s + i\epsilon}, \quad (18)$$

and the d coefficient is readily obtained as

$$d = -g_{D_{s_0}^*(2317) \rightarrow P\bar{P}e} Q_1 \lambda_\nu \frac{M_V G_V \sqrt{2}}{f_\pi f_D} \frac{1}{8\pi^2} \times \int_0^1 dx \int_0^x dy \frac{(1-x)y}{s + i\epsilon}. \quad (19)$$

As mentioned above, one can see, following the same procedure, that the diagram in Fig. 1(c) only contributes to the $ag^{\mu\nu}$ term of Eq. (9) and thus we do not need to calculate it.

The finiteness of the results is also noted in Ref. [33] where the wave function is governed by a range parameter Λ , and the results remain finite in the limit of $\Lambda \rightarrow \infty$.

One must sum coherently the contribution of each term of the diagrams in Fig. 2 to the d coefficient and then the radiative decay width is given finally by

$$\Gamma = \frac{1}{8\pi} \frac{1}{m_{D_{s_0}^*(2317)}^2} |\vec{K}| 2(K \cdot Q)^2 |d|^2, \quad (20)$$

where $|\vec{K}|$ is photon three-momentum in the rest frame of the $D_{s_0}^*(2317)$.

The decay of the $X(3700)$ proceeds identically through the same lines using the appropriate couplings and masses in the diagrams of Fig. 3.

III. RESULTS

In Table III we show the results for the d coefficient from each term in Fig. 2.

TABLE III. Results.

Diagram	d (fm)	Γ (KeV)
$K^+ D^0$	0.01284	2.518
$D^+ K^0$	-0.00529	0.427
$D_s^+ \eta$	-0.00197	0.059
$D_s^+ \eta_c$	0.00007	0.000
Total	0.00565	0.488

As we can see, the largest contribution comes from the $K^+ D^0$ intermediate state. The $D^+ K^0$ is smaller than the $K^+ D^0$ because it involves two heavy pseudoscalar propagators instead of two light ones. Next and weaker than the others is the contribution of the $D_s^+ \eta$ channel, and finally the $D_s^+ \eta_c$ channel provides a negligible contribution.

Note that the contribution from the two charge partners in the isospin $I = 0$ DK channel is destructive. Had the $D_{s_0}^*(2317)$ been an isospin $I = 1$ resonance, the relative couplings to the two channels would have been opposite, making thus a constructive interference, and we would have obtained a width of 4 KeV instead of 0.488 KeV, a factor eight times bigger. Furthermore, because of the destructive interference, the effect of the $D_s^+ \eta$ channel, which is quite small by itself, becomes relevant. Indeed, if we neglect the channels with the D_s^+ meson, the width obtained is $\Gamma = 0.872$ KeV, a factor 1.8 times bigger than when one takes them into account. Then, one can see that the consideration of all the coupled channels of the approach is quite relevant, which introduces one novel element with respect to the ordinary molecular picture [33] where only the dominant KD channel is taken into account.

The results for the $X(3700)$ radiative decay are shown in Table IV. We see that this radiative decay is considerably larger than for the $D_{s_0}^*(2317)$. In this case all the terms add constructively.

Next we perform an analysis of the uncertainties in the results. The fact that we have obtained a very small width, because of strong cancellations, indicates that it should be rather sensitive to uncertainties in the input used for the evaluation.

To evaluate the uncertainties we follow the same procedure used in Ref. [17]. We take a random generated ensemble of sets for the input parameters within a physical allowed range and calculate the radiative decay for each set of parameters in the ensemble. The uncertainties in the results are then given

TABLE IV. Results.

Diagram	d (fm)	Γ (KeV)
$D^+ D^-$	-0.00314	3.709
$D^- D^+$	-0.00314	3.709
$D_s^+ D_s^-$	-0.00129	0.622
$D_s^- D_s^+$	-0.00129	0.622
Total	-0.00886	29.481

by the standard deviation from the mean value calculated:

$$\sigma^2 = \frac{\sum_{i=1}^N (\bar{\Gamma} - \Gamma_i)^2}{N-1} \quad (21)$$

$$\bar{\Gamma} = \frac{1}{N} \sum_{i=1}^N \Gamma_i. \quad (22)$$

Because the radiative decay of the $D_{s_0}^*(2317)$ is very small and the uncertainties are of the same order of magnitude, we separately calculate the standard deviation above and under the mean value. The parameters generated are within the following ranges [17]:

$$\begin{aligned} M_V &= 2060 \pm 52 \text{ MeV} \\ f_D &= 182 \pm 36 \text{ MeV} \\ f_\pi &= 100 \pm 15 \text{ MeV} \\ m_{D_{s_0}^*(2317)} &= 2316 \pm 39 \text{ MeV} \\ g_{D_{s_0}^*(2317) \rightarrow DK} &= -6420 \pm 1790 \text{ MeV} \\ g_{D_{s_0}^*(2317) \rightarrow D_s \eta} &= 5250 \pm 1430 \text{ MeV} \\ g_{D_{s_0}^*(2317) \rightarrow D_s \eta_c} &= 1450 \pm 470 \text{ MeV} \\ m_{X(3700)} &= 3698 \pm 35 \text{ MeV} \\ g_{X(3700) \rightarrow D^+ D^-} &= 8089 \pm 3125 \text{ MeV} \\ g_{X(3700) \rightarrow D_s^+ D_s^-} &= 5339 \pm 2100 \text{ MeV}. \end{aligned} \quad (23)$$

When we do the exercise for $N = 500$ randomly generated parameter sets, we obtain

$$\Gamma_{D_{s_0}^*(2317)} = 0.475_{-0.290}^{+0.831} \text{ KeV} \quad (24)$$

and

$$\Gamma_{X(3700)} = 18.45 \pm 13.00 \text{ KeV}. \quad (25)$$

It is instructive to compare our results with those of Ref. [33] for the $D_{s_0}^*(2317)$. They are rather similar. In Ref. [33] the results vary from 0.47 KeV in some approximations to 1.41 KeV in other approximations. Our uncertainties stem from different sources, couplings, masses, etc., but the range of values obtained is very similar. A comparison of these results with those of different quark models is made in Ref. [33] and we refer the reader to Table III of this reference. The results obtained with the present picture are in general smaller than those obtained in quark models or other pictures. The destructive interference between the two components of the main isospin channel is the main reason for it. Precise experiments on this rate should help us understand better the nature of this resonance. As for the $X(3700)$, a search for it as a peak in some reactions would be a first step. The search for its radiative decay could follow and, given the large rate predicted, the investigation of this decay channel does not look particularly difficult, specially when the ratio of the radiative decay of the $D_{s_0}^*(2317) \rightarrow \gamma D_s^*$ to the $D_{s_0}^*(2317) \rightarrow \pi^0 D_s^*$ has already been measured [4].

IV. CONCLUSIONS

We have presented here the evaluation of the radiative decay of the open and hidden charm scalar mesons that are

dynamically generated from the interaction of two pseudoscalar mesons. The calculations have been done for the $D_{s_0}^*(2317)$ open charm scalar state and for the predicted hidden charm state $X(3700)$, not yet observed. We found very different results for the two states. While the $D_{s_0}^*(2317)$ decay into γD_s^* has a width of around 0.5 KeV, the $X(3700)$ has a width into $\gamma J/\psi$ of the order of 20 KeV, a factor 40 times bigger. One of the reasons, but not the only one, is the large cancellation between the two charge partners of the isospin component of the DK $I = 0$ state. With the obvious similarities, we also found subtle differences between the DK molecular picture for the $D_{s_0}^*(2317)$ state and the dynamically generated picture. The latter one, including more channels than just the DK channel, showed sensitive effects from the $D_s \eta$ state, particularly because of the large cancellation found between the dominant $D^+ K^0$ and $K^+ D^0$ states. Yet, within the theoretical uncertainties, the final result obtained in the two pictures are rather similar.

We also presented a different technical way to evaluate the amplitudes that makes the formalism simpler and shows immediately the finiteness of the results using arguments of gauge invariance.

Concerning the $X(3700)$ state and its radiative decay, the large width obtained for the decay into $\gamma J/\psi$ should make its observation easy, in principle, and we also recalled that the predictions on this state were rather solid so that it should be observed as a bound state or a strong cusp, in both of which cases the radiative decay could be investigated. The observation of this state with its relatively large radiative width would provide a boost to the idea of the low energy scalar mesons with open charm and some particular hidden charm scalar states as dynamically generated resonances.

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APPENDIX: PHOTON COUPLING TO EXTERNAL LINES

In addition to the diagrams considered in Fig. 1, one should also include two extra diagrams; for the case of the decay of charged particles, where the photon couples to the external lines, see Fig. 4.

These two diagrams are explicitly considered in Ref. [33] and shown to be relevant in the test of gauge invariance. However, we show here that they vanish in the amplitude for on-shell $D_{s_0}^*(2317)$ and D_s^* .

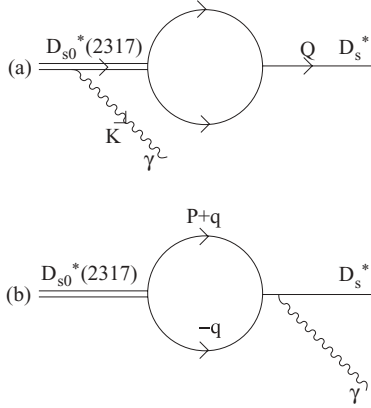


FIG. 4. Diagrams with the photon connected to the external lines.

To prove this we first evaluate the loop function in Fig. 4:

$$J(P^2)P^\mu\epsilon_\mu(D_s^*) = i \int \frac{d^4q}{(2\pi)^4} \frac{g_{D_s^*DK}}{(P+q)^2 - m_1^2 + i\epsilon} \times \frac{g_{D_s^*DK}}{q^2 - m_2^2 + i\epsilon} (P+2q)^\mu \epsilon_\mu(D_s^*). \quad (\text{A1})$$

Both diagrams in Fig. 4 imply vector-scalar mixing, which appears through the longitudinal part of the vector meson propagator. Indeed, let us consider the diagrams of Fig. 5 for the vector meson propagator.

We have

$$i\mathcal{D}^{(a)}(P) = i \sum_\lambda \frac{\epsilon^\mu(D_s^*)\epsilon^\nu(D_s^*)}{P^2 - M^2 + i\epsilon} \quad (\text{A2})$$

$$\mathcal{D}^{(a)}(P) = \left(-g^{\mu\nu} + \frac{P^\mu P^\nu}{P^2}\right) \frac{1}{P^2 - M^2 + i\epsilon} + \frac{P^\mu P^\nu}{P^2 M^2}, \quad (\text{A3})$$

where in Eq. (A3) we separated explicitly the propagator into its transverse (first) and longitudinal (second) components. Analogously, Fig. 5(b) provides a contribution to the D_s^*

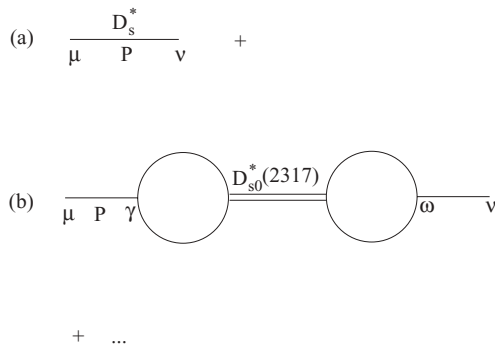


FIG. 5. Diagrams for the renormalization of the vector meson propagator.

propagator given by

$$i\mathcal{D}^{(b)}(P) = i \sum_\lambda \frac{\epsilon^\mu(D_s^*)\epsilon^\nu(D_s^*)}{P^2 - M^2 + i\epsilon} (-i)J(P^2)P_\gamma i\tilde{\mathcal{D}}_{D_{s_0}^*(2317)}(P) \times (-i)J(P^2)P_\omega i \sum_{\lambda'} \frac{\epsilon^\omega(D_s^*)\epsilon^\nu(D_s^*)}{P^2 - M^2 + i\epsilon}, \quad (\text{A4})$$

where $\tilde{\mathcal{D}}_{D_{s_0}^*(2317)}(P)$ is the propagator of the scalar particle.

One can see that the presence of $P_\gamma P_\omega$ in Eq. (A4) eliminates the contribution of the transverse part of the vector meson propagator; hence, only the longitudinal part contributes, and we obtain

$$\mathcal{D}^{(b)}(P) = \frac{P^\mu P^\nu}{M^4} J(P^2)^2 \frac{1}{P^2 - m_{D_{s_0}^*(2317)}^2}. \quad (\text{A5})$$

The iteration of the last diagram of Fig. 5 and the sum of all these terms lead to a geometrical series that renormalizes the longitudinal part of the vector propagator and leads to

$$\frac{P^\mu P^\nu}{P^2 M^2} \rightarrow \frac{P^\mu P^\nu}{P^2 M^2} \left(\frac{1}{1 - \frac{P^2}{M^2} J(P^2)^2 \frac{1}{P^2 - m_{D_{s_0}^*(2317)}^2}} \right) = \frac{P^\mu P^\nu}{P^2 M^2} \frac{P^2 - m_{D_{s_0}^*(2317)}^2}{P^2 - m_{D_{s_0}^*(2317)}^2 - \frac{P^2}{M^2} J(P^2)^2}. \quad (\text{A6})$$

Now comes an important renormalization condition that is the physical requirement that the longitudinal part of the vector meson propagator does not contain a pole of the scalar meson [35,36]. This condition is only fulfilled if

$$J(P^2 = m_{D_{s_0}^*(2317)}^2) = 0. \quad (\text{A7})$$

Next we evaluate the two terms in the amplitude of Fig. 4.

$$-i\mathcal{T}^{(a)} = -ie(2Q+K)^\mu \epsilon_\mu(\gamma) i\tilde{\mathcal{D}}_{D_{s_0}^*(2317)}(Q) \times (-i)J(Q^2)Q^\nu \epsilon_\nu(D_s^*). \quad (\text{A8})$$

This term is zero because of the Lorentz condition on the vector meson, $Q^\nu \epsilon_\nu(D_s^*) = 0$. This has already been realized and used in Ref. [33].

Next we look at the diagram that contributes to the amplitude in Fig. 4(b):

$$-i\mathcal{T}^{(b)} = -iJ(P^2)P^\mu \epsilon_\mu(D_s^*) \dots \quad (\text{A9})$$

As we can see, independently of the γVV coupling, the term $\mathcal{T}^{(b)}$ is proportional to $J(P^2 = m_{D_{s_0}^*(2317)}^2)$, which we have shown before to be zero due to the renormalization condition of the longitudinal part of the vector meson propagator.

Our procedure to evaluate the amplitude, hence, relies upon the following:

- (i) The whole set of diagrams is gauge invariant.
- (ii) The diagrams of Fig. 4 do not give contribution to the amplitude.
- (iii) Only the set of diagrams of Fig. 1 give contribution.
- (iv) Using gauge invariance and the procedure followed through Eqs. (9)–(11), only the d term has to be evaluated, to which only the diagrams of Figs. 1(a) and 1(b) contribute.

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