Measurement of the $B(E2, 0_1^+ \rightarrow 2_1^+)$ in the N = 16 nucleus ²⁶Ne

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Differential cross section of the inelastic scattering of a 54 MeV/nucleon ²⁶Ne beam on a lead target has been measured by detecting the deexcitation γ -rays. Analysis of the first 2⁺ state angular distribution of the inelastically scattered nuclei shows that the process cannot be considered as a pure Coulomb excitation, and nuclear contribution must be taken into account. The charge deformation deduced, $\beta_2^C = 0.392 \pm 0.024$, corresponds to a $B(E2) = 141 \pm 18 \ e^2 \ fm^2$ in agreement with a N = 16 subshell closure.

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Nuclei with a closed shell play a special role in nuclear physics. They can be recognized among others from the relatively high excitation energy of their first excited state, a low value of the quadrupole electromagnetic transition probability $B(E2, 0_1^+ \rightarrow 2_1^+)$, sudden change in the binding energy or the nuclear radius when crossing a shell closure. The subshell closure at N = 16 was already revealed from the analysis [1] of the 1985 nuclear mass evaluation [2]. Recently, the change of nuclear radii at N = 16 has also been observed [3]. Nonobservation of bound excited states in ²⁴O is an indication for its doubly magic character and confirms the N = 16 subshell closure at the neutron drip-line [4]. On the other hand, the subshell closure at N = 14 was found to persist in neutron-rich oxygen isotopes [4–7].

For the neon isotopes, the relatively high energy of the first 2⁺ state in ^{24,26}Ne and the relatively small values of their $B(E2, 0_1^+ \rightarrow 2_1^+)$ transition probabilities [8] were considered as signatures of the survival of the N = 14,16 subshell closures at Z = 10. Recently, the $B(E2, 0_1^+ \rightarrow 2_1^+)$ transition probability has been remeasured for ²⁸Ne [9] with a precision higher than in [8]. The observed value turned out to be even smaller than the accepted one for ^{24,26}Ne. As a consequence, the trend of the B(E2) values shows a permanent decrease as a function of the neutron number from ²⁰Ne to ²⁸Ne, thus the signs of the N = 16 subshell closure seem to disappear, which contradicts the conclusion that was drawn from the systematic behavior of the energy of the 2_1^+ states.

As a byproduct of a search for low-lying dipole strength in 26 Ne [10], we have remeasured the B(E2) value in 26 Ne.

The experiment was performed at the RIPS facility [11] in RIKEN. A secondary ²⁶Ne beam was produced by fragmentation of a 95 MeV/nucleon ⁴⁰Ar primary beam impinging on a 2-mm-thick ⁹Be target. A typical intensity of the primary beam was 60 pnA. An aluminum wedge of 3.3° with a mean thickness of 700 mg/cm² was used to improve the isotopic purity of the secondary beam. The ²⁶Ne beam was produced with an energy of 58 MeV/nucleon and of 80% purity. The main contaminants were ²⁷Na (\approx 5%) and ²⁹Mg (\approx 15%). The average beam rate was 10⁴ pps with a momentum spread of 2%.

The particle identification of the incident beam was carried out event-by-event using the magnetic-rigidity time-of-flight (TOF) method. The TOF was determined by the time difference between the cyclotron radio frequency signal and a 0.2 mm-thick plastic scintillator placed at the first focal plane of the RIPS separator. The incident beams were unambiguously identified.

The incident beam profile was monitored by two parallelplate avalanche counters [12] placed in a chamber at the next focal plane of the RIPS at a distance of 148 cm and 118 cm upstream of the secondary natural Pb target of 230 mg/cm² (alternatively with a 130 mg/cm² ²⁷Al target). The beam spot size and the beam angular spread at the target position were extrapolated to be 19 mm and 1.4° (FWHM) in the horizontal direction and 22 mm and 1.2° (FWHM) in the vertical direction, respectively. The beam line section under vacuum was terminated by a 25 μ m kapton window 2 cm before the secondary target.

The identification of the scattered particles as well as the measurement of their energy and scattering angle were performed using eight silicon telescopes placed 1.2 m downstream of the target. They were at air but inside an aluminum chamber to protect them from ambient light. The entrance window of the chamber was made of 7 μ m aluminized Mylar to minimize

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interactions with the incoming charged particles. A telescope was composed of two layers of silicon strip detectors (SSD) and one layer of lithium drifted silicon [Si(Li)] crystal. The two first layers of SSD were arranged in a 3×3 matrix, with the middle one removed to avoid silicon detectors being hit directly by the beam. Each SSD had a $50 \times 50 \text{ mm}^2$ active area and an 0.5 mm thickness. They were divided into ten strips of 5 mm each. The first layer measured the horizontal position of the outgoing heavy ions and the second layer measured the vertical one. The back sides of SSDs were used for energy loss (ΔE) measurement. The residual energy was measured by the 3-mm-thick Si(Li) detectors from the MUST array [13]. Due to a bigger active area of 55×55 mm², their positions were chosen to minimize the dead zones and the eight detectors were shared among two layers of four units each, having overlapping dead zones. All nuclei of interest stopped in the Si(Li) detectors, allowing a total energy measurement with a resolution better than 1%. The particle identification was unambiguously done using the $\Delta E - E$ technique. This set of eight telescopes allowed a very good angular coverage between 1° and 5° . The geometrical acceptance was deduced from simulation, taking into account both beam spread and straggling.

In order to minimize reactions of the beam particles with air we inflated a helium bag between the target and the silicon detector. Its entrance and exit windows were made of 16 μ m Mylar. The pressure of the He gas inside was kept around 1 atm.

Gamma rays produced in the secondary target were detected using the DALI2 array surrounding the target. It consisted of 152 NaI(TI) and had a resolution (FWHM) of ~9% at 662 keV [14]. The energy and efficiency calibrations of the NaI(TI) detectors were made by using standard ²²Na, ⁶⁰Co, ¹³⁷Cs, and Am-Be sources. The absolute efficiency and the line shape of the γ -peak was reproduced by simulation using the GEANT3 code [15]. The angular information was used for Doppler correction for γ -ray emitted from fast moving nuclei ($\beta = 0.3$). For 2 MeV γ rays the obtained resolution is 145 keV (FWHM) with an efficiency of 13% ± 1.3%.

 γ -decay of ²⁶Ne. The Doppler corrected energy spectrum for γ multiplicity strictly equal to 1 measured in coincidence with ²⁶Ne scattered particles identified in the silicon telescope is presented in Fig. 1. The spectrum obtained with an empty target frame has been subtracted from the spectra with lead target after normalization to the same number of incident particles. The ²⁶Ne γ ray from the decay of the 2⁺₁ state measured here at 2022 ± 62 keV is clearly visible in it.

In order to investigate the feeding of the 2_1^+ state through the decay of higher lying excited states, we examined the $\gamma\gamma$ correlations. By gating on γ -ray energies between 1950 keV and 2090 keV, we observed a peak at 1683 \pm 60 keV (inset of Fig. 1) assigned to the cascade from the adopted 3691.2(3) keV state through the 2018.2(1) keV 2_1^+ state to the ground state. We estimated the ratio of the intensities of the 1667 keV/ 2018.2 keV lines to be $10 \pm 5\%$. In the following, this contribution to the 2 MeV γ -ray cross section will be taken into account.

B(E2) extraction using coupled channel equation code. To extract the B(E2) value from the 2^+_1 excitation cross



FIG. 1. Doppler corrected gamma energy distribution in coincidence with ²⁶Ne. Inset: γ -ray energy spectrum, obtained with γ -multiplicity strictly equal to 2 and in coincidence with $E(\gamma) = 2020$ keV transition.

section a distorted wave calculation was performed. Here we used the coupled channel equation code ECIS97 [16] with optical potential parameters extracted from a ²⁰Ne (40 MeV/nucleon)+²⁰⁸Pb reaction [17]. In the hypothesis that no nuclear interaction is involved (corresponding to a null nuclear deformation parameter $\beta_2^N = 0$) we deduced that a Coulomb deformation parameter $\beta_2^C = 0.523 \pm 0.031$ reproduces our 68 ± 8 mb cross section. This corresponds to a $B(E2) = 250 \pm 30 \ e^2 \ fm^2$ in good agreement with the one of $228(41) \ e^2 \ fm^2$ extracted with the same assumption (equivalent photon method) from the ²⁶Ne(41.7 MeV/nucleon)+Au inelastic scattering [8].

However, at these incident energies, a contribution from nuclear processes to the cross section may also be present. To check the validity of the assumption on pure Coulomb excitation we measured the angular distribution of inelastically scattered ²⁶Ne in coincidence with the $2020 \pm 150 \text{ keV}$ gamma rays, presented in Fig. 2, where the background is removed by subtracting from the angular distribution gated by the 2020 keV peak the angular distribution gated on the adjacent area with the same $\pm 150 \text{ keV}$ width. Note that the result is similar if we build the angular distribution from the number of 2 MeV counts (above background) for a given angle.

The experimental data are compared with the theoretical calculations convoluted by our detector response obtained using GEANT3 simulations. The result is displayed in Fig. 2. The dashed line represents the case where pure Coulomb was assumed and the solid line is for the case with nuclear deformation included, with the hypothesis that its deformation length (i.e., the product $\beta \cdot \text{radius}$) is equal to that of the electromagnetic one. Our resolution makes it difficult to deduce independently the nuclear and the Coulomb part of the excitation, but from Fig. 2, it can be seen that by taking into account the nuclear contribution the experimental data are better reproduced especially at small angles. The deduced deformation parameters are $\beta_2^N = 0.403 \pm 0.025$ and $\beta_2^C = 0.392 \pm 0.024$ which gives a $B(E2) = 141 \pm 18 e^2$ fm². Note that the $\beta_2^N = \beta_2^C$ hypothesis gives a similar result.



FIG. 2. (Color online) The angular distribution for the first 2_1^+ excited state of ²⁶Ne on a lead target is compared to an ECIS97 calculation, convoluted by the detector response. We used the ²⁰Ne(40 MeV/nucleon) + ²⁰⁸Ne optical potential parameters. The solid line represents the case where a nuclear contribution is added, $\beta_2^N = 0.403$, $\beta_2^C = 0.392$ whereas the dashed line represents the pure Coulomb case with $\beta_2^N = 0$, $\beta_2^C = 0.523$. $R_{N,C}$ are the nuclear and the Coulomb radii, respectively.

In order to test our choice of optical potential we extracted the same quantities using parameters from the reaction 40 Ar(41 MeV/nucleon)+ 208 Pb [18]. For both the pure Coulomb case and that calculated by including the nuclear excitation we deduced a B(E2) only ~8% greater than with the previous 20 Ne potential. These values are therefore perfectly compatible—similarly to the study on 28 Ne [9]—and by checking also that the corresponding angular distribution reproduces our data we conclude that the 20 Ne+ 208 Pb optical potential is a reasonable choice.

In the following we compare our extracted value of $141 \pm 18 \ e^2 \ \text{fm}^2$ with the experimental systematics of 2^+_1 energies and reduced transition probabilities both presented in Fig. 3. The open diamonds are the excitation energies and the open circles are the previously accepted B(E2) values. Our result for the ²⁶Ne B(E2) and the recent extracted value for the ²⁸Ne [9] are plotted with closed circle and closed triangle respectively. These last two analysis took into account the nuclear induced excitation and hence gave lower values than those measured previously, thus changing the overall trend. Before, the transition probability had a minimum for A = 24and presented a constant increase with neutron richness, hardly compatible with the N = 16 subshell closure. Now the tendencies show a low plateau from A = 24 to A = 28 while the excitation energy is maximum for ²⁶Ne. This combination is hence in agreement with the already accepted N = 16subshell closure.

Nature of the 3.7 MeV excited state. In addition to the 2_1^+ state, another excited state at 3691 keV was populated in ²⁶Ne. Earlier, a 0⁺ spin-parity was assigned to a state at 3750 keV observed in the pion charge exchange reaction [19]. This spin assignment was retained to the 3691 keV in the β -decay study of ²⁶F [20], although the presumably 1⁺ ground state



FIG. 3. Experimental 2_1^+ energy and $B(E2; 0_1^+ \rightarrow 2_1^+)$ value for even neon isotopes. Open diamonds and open circles are previous experimental results for energy and transition probability respectively whereas the closed circle and the closed triangle are recent results. Lines (dashed and solid) are here to guide the eye only.

of ²⁶F can decay to a 2⁺ state, too, with the same probability. Here a 0⁺(g.s.) \rightarrow 0⁺ excitation is hardly compatible with our observed amount of 7.2 ± 4.2 mb of γ production cross section for the 3.7 MeV state.

This is especially true for the inelastic scattering on an Al target measured in the same experiment, where a 3 times larger cross section was observed. One might assume that the ground state and the second 0^+ state are strongly mixed in ²⁶Ne. However, this assumption clearly contradicts the shell model calculations. As another possibility to explain the large excitation cross sections, we can consider giving up the 0^+ spin assignment to this state. The excitation of the 2^+_2 state has the next largest cross section in the coupled channel calculations (7 mb) in good agreement with the observation. From the present experiment this spin assignment seems to be a more reliable one. We mention that both the Monte Carlo shell model calculations [21] and the recent USD05 (a and b) interactions [22] push the second 0^+_2 state to much higher energies (4.5, 4.7, and 5.7 MeV, respectively) than the present value of 3.7 MeV whereas their 2^+_2 is located at 3.4, 3.7, and 3.8 MeV, respectively, in good agreement with the experiments.

Summarizing our results, we have measured the differential cross section of inelastic scattering of an intermediate energy radioactive ²⁶Ne beam on a Pb target. From the coupled channel analysis of the inelastically scattered Ne nuclei we deduced the reduced transition probability for exciting the first 2_1^+ state to be $B(E2) = 141 \pm 18 \ e^2 \ fm^2$, in agreement with a N = 16 subshell closure. We also propose assigning a 2^+ spin-parity value to the 3.7 MeV second excited state.

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