Neutron capture cross section of ²³²Th measured at the n_TOF facility at CERN in the unresolved resonance region up to 1 MeV

G. Aerts,¹ U. Abbondanno,² H. Álvarez,³ F. Alvarez-Velarde,⁴ S. Andriamonje,¹ J. Andrzejewski,⁵ P. Assimakopoulos,⁶ G. Aerts,¹ U. Abbondanno,² H. Álvarez,³ F. Alvarez-Velarde,⁴ S. Andriamonje,¹ J. Andrzejewski,⁵ P. Assimakopoulos,⁶ L. Audouin,⁷ G. Badurek,⁸ P. Baumann,⁹ F. Bečvář,¹⁰ E. Berthoumieux,¹ F. Calviño,¹¹ D. Cano-Ott,⁴ R. Capote,^{12,13} A. Carrillo de Albornoz,¹⁴ P. Cennini,¹⁵ V. Chepel,¹⁶ E. Chiaveri,¹⁵ N. Colonna,¹⁷ G. Cortes,¹¹ A. Couture,¹⁸ J. Cox,¹⁸ M. Dahlfors,¹⁵ S. David,⁹ I. Dillman,⁷ R. Dolfini,¹⁹ C. Domingo-Pardo,²⁰ W. Dridi,¹ I. Duran,³ C. Eleftheriadis,²¹ M. Embid-Segura,⁴ L. Ferrant,²² A. Ferrari,¹⁵ R. Ferreira-Marques,¹⁶ L. Fitzpatrick,¹⁵ H. Frais-Koelbl,²³ K. Fujii,² W. Furman,²⁴ I. Goncalves,¹⁶ E. Gonzalez-Romero,⁴ A. Goverdovski,²⁵ F. Gramegna,²⁶ E. Griesmayer,²³ C. Guerrero,⁴ F. Gunsing,^{1,*} B. Haas,²⁷ R. Haight,²⁸ M. Heil,⁷ A. Herrera-Martinez,¹⁵ M. Igashira,²⁹ S. Isaev,²² E. Jericha,⁸ F. Käppeler,⁷ Y. Kadi,¹⁵ D. Karadimos,⁶ D. Karamanis,⁶ M. Kerveno,⁹ V. Ketlerov,^{15,25} P. Koehler,³⁰ V. Konovalov,^{15,24} E. Kossionides,³¹ M. Krtička,¹⁰ C. Lamboudis,²¹ H. Leeb,⁸ A. Lindote,¹⁶ I. Lopes,¹⁶ M. Lozano,¹³ S. Lukic,⁹ J. Marganiec,⁵ L. Marques,¹⁴ S. Marrone,¹⁷ P. Mastinu,²⁶ A. Mengoni,^{15,23} P. M. Milazzo,² C. Moreau,² M. Mosconi,⁷ F. Neves,¹⁶ H. Oberhummer,⁸ S. O'Brien,¹⁸ M. Oshima,³² J. Pancin,¹ C. Papachristodoulou,⁶ C. Papadopoulos,³³ C. Paradela,³ N. Patronis,⁶ A. Pavlik,³⁴ P. Pavlopoulos,³⁵ L. Perrot ¹ M. T. Pigni,⁸ R. Plag,⁷ A. Plompen,³⁶ A. Plukis,¹ A. Poch,¹¹ C. Pretel,¹¹ I. Ouesada,¹³ S. O Brien, ¹⁶ M. Osnima,²⁵ J. Pancin,⁴ C. Papachristodoulou,⁹ C. Papadopoulos,³⁵ C. Paradela,⁹ N. Patronis,⁶ A. Pavlik,⁴¹ P. Pavlopoulos,³⁵ L. Perrot,¹ M. T. Pigni,⁸ R. Plag,⁷ A. Plompen,³⁶ A. Plukis,¹ A. Poch,¹¹ C. Pretel,¹¹ J. Quesada,¹³ T. Rauscher,³⁷ R. Reifarth,²⁸ M. Rosetti,³⁸ C. Rubbia,¹⁹ G. Rudolf,⁹ P. Rullhusen,³⁶ J. Salgado,¹⁴ L. Sarchiapone,¹⁵ I. Savvidis,²¹ C. Stephan,²² G. Taliente,¹⁷ J. L. Tain,²⁰ L. Tassan-Got,²² L. Tavora,¹⁴ R. Terlizzi,¹⁷ G. Vannini,³⁹ P. Vaz,¹⁴ A. Ventura,³⁸ D. Villamarin,⁴ M. C. Vincente,⁴ V. Vlachoudis,¹⁵ R. Vlastou,³³ F. Voss,⁷ S. Walter,⁷ H. Wendler,¹⁵ M. Wiescher,¹⁸ and K. Wisshak⁷ (n_TOF Collaboration) ¹CEA/Saclay-DSM/DAPNIA, Gif-sur-Yvette, France ²Istituto Nazionale di Fisica Nucleare, Trieste, Italy ³Universidade de Santiago de Compostela, Spain ⁴Centro de Investigaciones Energeticas Medioambientales y Technologicas, Madrid, Spain ⁵University of Lodz, Lodz, Poland ⁶University of Ioannina, Greece ⁷Forschungszentrum Karlsruhe GmbH (FZK), Institut für Kernphysik, Germany ⁸Atominstitut der Österreichischen Universitäten, Technische Universität Wien, Austria ⁹Centre National de la Recherche Scientifique/IN2P3-IReS, Strasbourg, France ¹⁰Charles University, Prague, Czech Republic ¹¹Universitat Politecnica de Catalunya, Barcelona, Spain ¹²International Atomic Energy Agency, NAPC/Nuclear Data Section, Vienna, Austria ¹³Universidad de Sevilla, Spain ¹⁴Instituto Tecnológico e Nuclear (ITN), Lisbon, Portugal ¹⁵CERN, Geneva, Switzerland ¹⁶LIP-Coimbra & Departamento de Fisica, Universidade de Coimbra, Portugal ¹⁷Istituto Nazionale di Fisica Nucleare, Bari, Italy ¹⁸University of Notre Dame, Notre Dame, USA ¹⁹Università degli Studi Pavia, Pavia, Italy ²⁰Instituto de Física Corpuscular, CSIC-Universidad de Valencia, Spain ²¹Aristotle University of Thessaloniki, Greece ²²Centre National de la Recherche Scientifique/IN2P3-IPN, Orsay, France ²³International Atomic Energy Agency (IAEA), Nuclear Data Section, Vienna, Austria ²⁴ Joint Institute for Nuclear Research, Frank Laboratory of Neutron Physics, Dubna, Russia ²⁵Institute of Physics and Power Engineering, Kaluga Region, Obninsk, Russia ²⁶Istituto Nazionale di Fisica Nucleare (INFN), Laboratori Nazionali di Legnaro, Italy ²⁷Centre National de la Recherche Scientifique/IN2P3-CENBG, Bordeaux, France ²⁸Los Alamos National Laboratory, New Mexico, USA ²⁹Tokyo Institute of Technology, Tokyo, Japan ³⁰Oak Ridge National Laboratory, Physics Division, Oak Ridge, USA ³¹NCSR, Athens, Greece ³² Japan Atomic Energy Research Institute, Tokai-mura, Japan ³³National Technical University of Athens, Greece ³⁴Institut für Isotopenforschung und Kernphysik, Universität Wien, Austria ³⁵Pôle Universitaire Léonard de Vinci, Paris La Défense, France ³⁶CEC-JRC-IRMM, Geel, Belgium ³⁷Department of Physics and Astronomy, University of Basel, Basel, Switzerland

³⁸ENEA, Bologna, Italy

³⁹Dipartimento di Fisica, Università di Bologna, and Sezione INFN di Bologna, Italy (Received 31 January 2006; published 31 May 2006)

We have measured the neutron capture reaction yield of ²³²Th at the neutron time-of-flight facility n_TOF at CERN in the energy range from 1 eV to 1 MeV. The average capture cross section has been extracted in the energy range from 4 keV up to 1 MeV with an overall accuracy better than 4%. An independent IAEA evaluation shows good agreement with the data. The average cross section has been expressed in terms of average resonance parameters using the partial waves $\ell = 0, 1, \text{ and } 2$.

DOI: 10.1103/PhysRevC.73.054610

I. INTRODUCTION

Accurate knowledge of neutron-nucleus reaction cross sections is of primary importance in studies of stellar nucleosynthesis [1,2] and fundamental symmetries [3,4], and in applications of nuclear technology [5-8]. In addition, important information on level densities, a key ingredient in many nuclear structure and reaction models, can be obtained directly from high-resolution neutron resonance spectroscopy. Research activities related to, for example, neutron capture stellar nucleosynthesis or neutron-induced symmetry breaking reactions, as well as to applications such as the transmutation of nuclear waste, accelerator-driven systems, and the thorium-based nuclear fuel cycle, have pointed out that for many nuclides the experimental information is of insufficient accuracy or sometimes lacking. Neutron cross section data are available from compilations of experimental data [9,10] or through evaluated nuclear data libraries such as BROND, ENDF, JEFF, and JENDL [11]. The necessary updating of these neutron cross section libraries relies on the availability of accurate measurements obtainable at advanced neutron sources.

The low-energy *p*-wave resonances in ²³²Th have received little attention since they do not contribute significantly to multigroup cross sections. However, large paritynonconservation effects have been observed in *p*-wave resonances of several isotopes, measured by the asymmetry of the neutron transmission of polarized neutrons on unpolarized nuclei [3,12]. These effects, on the order of 10^{-7} in nucleonnucleon interactions, were found to be up to 10% for ²³²Th in transmission experiments [13,14]. A more precise knowledge of the *p*-wave neutron widths Γ_n may improve the extraction of the parity-nonconserving matrix elements.

The use of thorium in the nuclear fuel cycle for either critical or subcritical systems is now a topic of great interest. This cycle is based on the fertile ²³²Th and the fissile ²³³U, formed by neutron capture on ²³²Th and the subsequent β decays of ²³³Th and ²³³Pa. An interesting advantage in using this fuel cycle, as compared to the conventional uranium/plutonium cycle currently used in all operating power plants, is related to its low production of high-mass actinides. In the uranium cycle, the fuel contains a large fraction of ²³⁸₉₂U, which is the seed for the production of higher actinides by successive neutron captures and fast β decays. The use of the lighter nucleus ²³²₉₀Th significantly reduces the radiotoxicity of the spent fuel by the much lower buildup of heavy transuranium isotopes, in particular plutonium, americium, and curium.

The cross section of the ²³²Th neutron capture reaction is a crucial input parameter for the design of any nuclear system based on the thorium fuel cycle. The presently available nuclear data libraries for the 232 Th (n, γ) cross section are mainly based on less recent and discrepant experiments [15-23]. This situation prompted new neutron capture experiments to be performed recently. Most of them have been performed using the neutron time-of-flight technique. Baek et al. [24] investigated γ -ray multiplicity and capture cross section in the energy region between 21.5 and 215 eV. Grigoriev et al. [25] measured the average cross section in the energy region between 10 eV and 10 keV. In the unresolved resonance region, Borella et al. [26] measured the cross section between 5 and 150 keV. The measurement of Wisshak et al. [27] covered the region between 5 and 225 keV. Finally, Karamanis et al. [28] used the activation technique to measure the capture cross section between 60 keV and 2 MeV. Although considerable improvements could be achieved, the discrepancies in the 232 Th (n, γ) cross section below the fission threshold, i.e., in the important energy range below 1 MeV, could not be removed.

In order to study neutron-induced reactions for nuclear technology, nuclear astrophysics, and nuclear structure and reaction physics, a new neutron time-of-flight facility, n_TOF, has been recently constructed at CERN, Geneva. This facility has a very high instantaneous neutron flux, which results in a favorable signal-to-noise ratio for neutron capture experiments on radioactive isotopes. This is a major advantage for a measurement of the 232 Th (n,γ) cross section. In fact, the high-energy γ rays going up to 2.6 MeV, originating from the β decay of the daughter product ²⁰⁸Tl, were severely hindering the accuracy of previous capture measurements. This component of the background is strongly reduced in the n_TOF setup. The second advantage of the n_TOF facility is the low duty cycle with a large spacing in time between consecutive time-of-flight bursts, which allows us to measure a wide energy range in a single experiment.

We have measured in a single experiment the neutron capture cross section of 232 Th in the neutron energy range from 1 eV to 1 MeV. The analysis procedure and the type of results for the resolved and unresolved resonance region is very different. Therefore, the resolved resonance part will be described separately in a later paper [29]. In this paper, we give the average cross section in the unresolved resonance region from 4 keV up to 1 MeV. No other measurement has covered

PACS number(s): 25.40.Lw, 25.40.Ny, 28.20.Fc

^{*}Corresponding author: F. Gunsing, gunsing@cea.fr

this wide of an energy range in a single experiment. This work has been part of a Ph.D. thesis [30].

II. EXPERIMENTAL DETAILS

A. The n_TOF beam and capture setup

The n_TOF facility, based on an idea by Rubbia *et al.* [31], became fully operational in May 2002, when the scientific program started. A detailed description of its performances can be found elsewhere [32]. Here we will mention the basic characteristics of the facility. At n_TOF, neutrons are produced by spallation reactions induced by a pulsed, 6 ns wide, 20 GeV/*c* proton beam with up to 7×10^{12} protons per pulse, impinging on a $80 \times 80 \times 60$ cm³ lead target. A 5 cm water slab surrounding the lead target serves as both a coolant and a moderator of the initially fast neutron spectrum, providing a wide energy spectrum from 1 eV to about 250 MeV with a nearly 1/E isolethargic flux dependence up to 1 MeV. An evacuated neutron beamline leads to the experimental area with the capture sample position at 185.2 m from the lead target.

Two collimators are present in the neutron beam, one with a diameter of 13.5 cm placed at 135 m from the lead target and one at 175 m with a diameter of 2 cm for the capture measurements. This collimation results in a nearly symmetric Gaussian-shaped beam profile at the sample position, with an energy-dependent standard deviation, which is about 0.77 cm at low neutron energies [33].

At a distance of 145 m, a 1.5 T magnet is placed in order to remove the residual charged particles going along the neutron beamline. A previously observed background due to negative muon capture has been drastically reduced by means of a 3 m thick iron shielding located after the sweeping magnet [34,35]. The neutron beamline extends for an additional 12 m beyond the experimental area to minimize the background from back-scattered neutrons. The repetition period of the proton pulses of 2.4 s on average is low enough to prevent any overlapping of neutrons in subsequent cycles.

At the sample position located at a flight length of 185.2 m, two disc-shaped thorium samples with a diameter of 1.5 cm, a total mass of 2.8037 g, and a purity of 99.5% were put together and placed inside a remotely controlled carbon fiber vacuum sample changer. With this sample thickness, some low-energy resonances are saturated, thereby allowing us to obtain an absolute normalization of the capture yields. The samples were mounted on thin kapton foils stretched over a carbon fiber frame that was much larger than the neutron beam, thus avoiding neutron scattering from the support. In addition to the thorium samples, we have measured under the same conditions samples of gold (1.33 g) to verify the analysis procedure and of natural lead (2.04 g) to estimate the background due to in-beam photons scattered from the sample. All samples were 15 mm in diameter. The scattered photon spectrum arose mainly from 2.23 MeV γ rays from neutron capture on hydrogen in the water moderator and coolant surrounding the neutron spallation target.

The sample was viewed by two in-house-developed γ -ray detectors [36], each one consisting of about 1 liter of

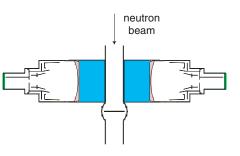


FIG. 1. (Color online) Schematic view of the horizontal plane of detectors and sample geometry in the ²³²Th(n, γ) measurement. Neutrons going through the 5.8 cm inner diameter beam tube are incident on the sample placed in the beam. Two C₆D₆ detectors, each consisting of a scintillator cell 12.7 cm in diameter and 7.62 cm high coupled to a photomultiplier, are placed 9.2 cm upstream of the sample center.

C₆D₆ liquid scintillator contained in a cylindrical low-mass carbon fiber housing, 12.7 cm in diameter and 7.62 cm high. Both carbon and deuterium have a very low neutron capture cross section and therefore do not significantly contribute to the background from sample-scattered neutron capture in the detector material. The scintillator was coupled directly, without the intermediate quartz window usually present in this type of detector, to an EMI-9823QKB photomultiplier tube. The detectors were placed perpendicular to the beam, 9.2 cm upstream from the sample center in order to reduce the background due to scattered photons. This geometrical configuration also allows us to reduce the effects of the angular distribution from primary neutron capture γ rays following neutron capture in $\ell = 1$ *p*-wave resonances with spin 3/2. The setup of the sample-detector geometry is sketched in Fig. 1. An in-beam neutron flux monitor [37], consisting of a ⁶Li deposit on a Mylar foil and four off-beam silicon detectors measuring the particles from the ${}^{6}\text{Li}(n, \alpha)\text{T}$ reaction, was located about 3 m upstream of the sample position.

The energy density of the number of neutrons crossing the plane perpendicular to the beam at the sample position at 185.2 m for a standard burst of 7×10^{12} protons of 20 GeV/*c* is shown in Fig. 2 as a function of neutron energy. This quantity will be called neutron flux in the following and

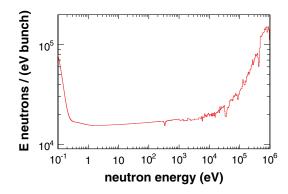


FIG. 2. (Color online) Energy density, multiplied by kinetic energy, of the total number of neutrons *n* incident on the sample plane for a standard burst of 7×10^{12} protons as a function of neutron energy. Energy density is given as $dn/d \ln(E) = E dn/dE$.

is given in isolethargic units of $d\Phi(E)/d\ln E$. These data are based on a measurement performed with a ²³⁵U loaded parallel plate fission ionization chamber from the Physikalisch-Technische Bundesanstalt in Braunschweig [38]. The raw counting spectra resulting from this flux measurement have statistical uncertainties between 1 and 1.8% per bin (20 bins per decade) in the neutron energy range from 1 keV to 1 MeV. At neutron energies below 1 keV, we used the data from the ⁶Li-based in-beam neutron flux monitor [37], with much lower statistical uncertainties. In our analysis of the ²³²Th cross section measurement, the absolute normalization of the capture yields is obtained independently from a low-energy saturated resonance. Therefore, the absolute value of the flux is not necessary but only its relative energy dependence from approximately 1 eV up to 1 MeV is used in the analysis. We estimate this value to be 2% at maximum based on the matching of the flux obtained from the ⁶Li neutron monitor and the ²³⁵U fission chamber around 1 keV. The electric signals from the photomultipliers of the detectors were sampled with a frequency of 0.5 GHz, during 16 ms after each proton pulse, with 8 bit resolution using an Acgiris Cougar 2010-4 flash analog-to-digital(ADC). The raw data for each pulse were transferred to the CERN central data recording system for off-line analysis. The pulse repetition interval was at minimum 1.2 s. For each event, the pulse height, proportional to the deposited energy in the C_6D_6 detector, and the neutron time-of-flight were extracted from the recorded signals. An effective threshold of 160 keV detected energy resulted from the pulse extraction for this case. More details on the data acquisition system can be found in Ref. [39].

The use of flash ADCs for the data acquisition reduces the dead time to an effective value of about 25 ns, related to the software for pulse extraction. The effect does not exceed 2% below 500 keV, except for large local count rates as in the peaks of large resonances. In the off-line event processing, we applied a fixed dead time of 30 ns, for which the count rate was corrected. When an event was observed in one of the two detectors, all events occurring within 30 ns in both detectors were discarded in order to eliminate coincidence counting.

B. Determination of the capture yield

The capture yield $Y(E_n)$, which is the fraction of the number of incident neutrons $\Phi(E_n)$ with energy E_n incident on the sample that leads to a capture event, cannot be determined in a straightforward way from the observed time-of-flight spectra $C_{obs}(E_n)$. In fact, without considering background, this is given by

$$C_{\rm obs}(E_n) = \Phi(E_n)Y(E_n)\epsilon_c,\tag{1}$$

where the efficiency ϵ_c for detecting the capture event depends in a complex way on the emitted γ -ray spectrum when using a low-efficiency detector like the C₆D₆ detectors of this experiment. The γ -ray spectrum is different for each isotope; and for a given isotope, it differs from one resonance to another. The neutron capture event is characterized by the deexcitation of the compound nucleus by emission of one or more γ rays. A calculation with a simulation code [40] indicates that the multiplicity of the ²³³Th compound decay is \approx 3 and goes through a cascade onto the several tens of thousands of available levels, like most medium and heavy mass nuclei. To circumvent this problem it is preferable to have the detector efficiency proportional to the γ -ray energy E_{γ} and a detection efficiency low enough to detect at most one γ ray of the cascade. In that case, the efficiency for the cascade can be shown to be proportional to the total γ energy released in the capture event $\epsilon_c = kE_c$ with proportionality k, and it is therefore independent from the details of the γ decay path. The γ -ray efficiency is related to the detector response function r_{γ} by $\epsilon_{\gamma} = \int r_{\gamma}(E_d) dE_d$. The energy deposited in the detector E_d is in general not proportional to E_{γ} but this can be introduced artificially by modifying the response function using a weighting function $W(E_d)$ such that

$$\epsilon_{\gamma} = \int W(E_d) r_{\gamma}(E_d) dE_d = k E_{\gamma}.$$
 (2)

This method, known as the pulse height weighting technique (PHWT), is described extensively elsewhere [41–43]. The weighting function can be accurately derived using Monte Carlo simulations of the detector response to different monoenergetic γ rays. In the measurement, the detector response function to the neutron capture γ -ray cascade $r_{\gamma}(E_d)$ is estimated by the measured count rate spectrum $R(E_d)$. Therefore, the weighted count rate spectrum can be written as

$$C_W(E_n) = \int R_{\gamma}(E_d) W(E_d) dE_d = \Phi(E_n) Y(E_n) E_c, \quad (3)$$

taking the proportionality constant equal to 1 in inverse units of energy. After correction for background, the capture yield can be determined from the weighted count rate spectrum.

The pulse height distribution of the C₆D₆ detectors were calibrated regularly during the experiment using the radioactive sources ¹³⁷Cs, ⁶⁰Co, and a composite source of the α -emitter ²³⁸Pu and carbon, giving a 6.13 MeV γ -ray through the ¹³C(α ,n)¹⁶O^{*} reaction.

C. Determination of the background

Several components contribute to the background level in our capture measurement. A time-independent background comes mainly from the radioactivity of the sample and has been measured with the neutron beam switched off. With the high instantaneous flux of the n_TOF installation, this background is relevant only at low neutron energies and can be easily subtracted or fitted with the data.

The main source of background in the keV region of neutron energies is generated by the γ rays present in the beam, which are scattered from the sample and detected in the C₆D₆ detectors. The majority of these γ rays originated from neutron captures on hydrogen in the water moderator, but other γ -ray components are present with relative intensities that vary slightly with time of flight. In order to quantitatively measure this background component, we performed a series of measurements with a 30 mm thick aluminum neutron blackresonance filter. These filters remove the neutrons from the beam at specific energies, corresponding to large resonances with zero transmission. The level of the background in a measurement with a black-resonance filter corresponds then to the level of the valleys in the count rate at the filter resonance energies.

The neutron filter also attenuates the in-beam photons that are scattered from the sample. In order to obtain the background level in the measurement without filters, we corrected for the attenuation of the in-beam γ rays by the filters. This is done by assuming that the shape of the scattered photon background $B_{\gamma}(t)$ as a function of time of flight *t* is independent of the sample, an assumption that we confirmed by Monte Carlo simulations for the present cases. The shape of this background component was determined by measuring, under the same conditions, a sample of natural lead. The nat Pb(n, γ) capture cross section is very low, and the reaction rate in the keV neutron energy region is almost entirely due to in-beam sample scattered photons.

Measurements of a lead sample were taken with and without the filters in the beam. After subtraction of the expected capture yield, which is small compared to the background, we obtained the background for the lead samples. The shape of the background for the lead sample without filters B_{Pb} is given by the two exponentials in brackets in Eq. (4). From the ratio of the background spectra obtained for the lead sample with (B_{PbAl}) and without (B_{Pb}) filters, we determined the attenuation of the γ rays $k_2(E_n) = B_{PbAl}/B_{Pb}$. The energy dependence of k_2 reflects the fact that the relative intensities of the in-beam γ rays change with the time of flight.

For the black resonance of Al at 34.8 keV, all neutrons are removed from the beam and the remaining part is the background. A clear dip is visible in the spectrum. We determined the level of the dip caused by the black resonance in the spectrum of thorium with the Al filter by fitting the expected shape of the resonance as a perturbation on a smooth reaction yield. The expected shape was calculated as a transmission using the total cross section of Al without the potential scattering contribution. In Fig. 3, the spectrum B_{ThAl} of the Th sample with the Al filter, in the beam in the vicinity of the 34.8 keV resonance of Al is shown together with the fit. From the ratio $k_1 = B_{ThAl}(34.8)/B_{Pb}(34.8)$ of this level and the level of the background of lead without a

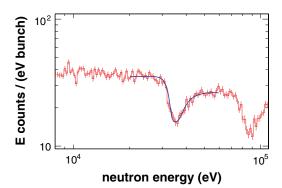


FIG. 3. (Color online) Part of the counting spectrum of the Th sample with the Al filter in the neutron beam together with the fit of the 34.8 keV black resonance of Al. Energy density of the number of counts is given as $1/d \ln(E) = E/dE$.

filter, we determined the background for the sample of thorium without the filter. The uncertainty for the normalization of this background component, obtained from the fit and the variation from different binnings, is 2.5%.

At lower energies, a time-of-flight dependent background could be determined in good approximation in between the resonances where the capture yield is very low compared to the background. A small residual background will be fitted together with the resonance shapes. The total background obtained in this way, in counts per unit time of flight, could be parametrized as a function of the neutron time of flight t by

$$B(t) = a_1 t^{b_1} + \frac{k_1}{k_2(t)} [a_2 \exp(b_2 t) + a_3 \exp(b_3 t)], \quad (4)$$

where the first term corresponds to the low-energy background and the exponents represent the photon-induced background, with a_i and b_i suitably determined constants and with the k_1 and $k_2(E_n)$ scaling factors explained previously in the text.

While our range of interest is below 1 MeV and is therefore below the fission threshold for ²³²Th, contributions from the inelastic scattering channels, which are present from the first excited state of ²³²Th at 49.4 keV, are a supplementary source of background. Although the detected energy of the γ decay of this state and even of the next state is below the signal threshold of 160 keV, states with spins and parities allowing inelastic scattering become an important source of background from about 700 keV. Indeed, the γ rays from fission or inelastic scattering cannot be distinguished from the γ rays from neutron capture with C₆D₆ detectors.

In order to exclude these background γ rays, we repeated the analysis procedure applying a γ -ray threshold of 1 MeV. This removed the background contributions from the $(n, n'\gamma)$ reaction channels up to a neutron energy of 1 MeV at the expense of a reduction of the counting statistics. The count rate spectra and the backgrounds are shown in Fig. 4 for the two thresholds of 160 and 1000 keV.

Setting such a high threshold as 1 MeV may put the validity of the weighting function technique into question. However, the derived capture yields obtained using thresholds of 160 keV and 1 MeV, and after normalization at the low-energy

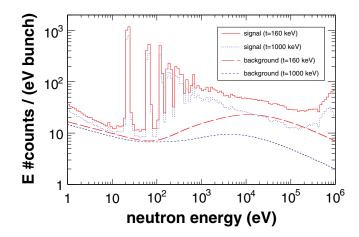


FIG. 4. (Color online) Measured count rate of 232 Th (n, γ) reaction per bunch of 7×10^{12} protons and derived background applying γ -ray thresholds of 160 and 1000 keV.

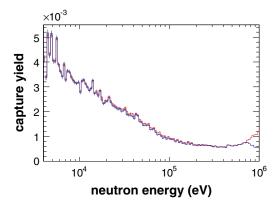


FIG. 5. (Color online) Derived capture yields using spectra with γ -ray thresholds of 160 and 1000 keV. Yields are identical within their uncertainties up to a neutron energy of about 700 keV. Beyond that energy, γ rays from inelastic scattering become visible as a background that is eliminated only with the high threshold.

saturated resonances, turned out to be essentially identical within their error bars up to about 700 keV. As shown in Fig. 5, above 700 keV the γ rays from inelastic scattering start to contribute to the background if a low threshold of 160 keV is applied, while this background is absent with the high threshold of 1 MeV. We explain this by the fact that the average γ -decay spectra for the thorium resonances are very similar because of the high level density and therefore the high number of states available for the γ -decay cascade. Since the measurement is self-normalized and hence not dependent on a reference measurement, any effect of a high γ -ray threshold propagates in the same manner to the entire energy range. It is clear that this method of eliminating γ rays from inelastically scattered neutrons may not be as straightforward when a reference measurement with a different isotope is used.

III. RESULTS IN THE UNRESOLVED RESONANCE REGION

A. The capture cross section derived from the capture yield

The capture reaction yield as a function of neutron energy E_n is related to the capture cross section σ_{γ} and the total cross section σ_T by

$$Y(E_n) = \mu(E_n)(1 - e^{-n\sigma_T(E_n)})\frac{\sigma_\gamma(E_n)}{\sigma_T(E_n)},$$
(5)

where $\mu(E_n)$ is the energy-dependent multiple scattering correction. In the resolved resonance region, the cross section is described by individual resonance parameters by means of the *R*-matrix formalism. In the unresolved resonance region, resonances are overlapping and one measures an average capture yield $\langle Y(E_n) \rangle$, which can be related to the average capture cross section by

$$\langle Y(E_n) \rangle = f(E_n) n \langle \sigma_{\gamma}(E_n) \rangle,$$
 (6)

where *n* is the sample thickness in atoms per barn and $f(E_n)$ is the correction that accounts for self-absorption and

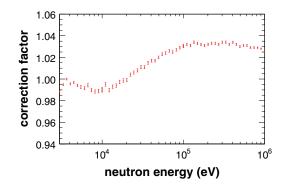


FIG. 6. (Color online) Correction factor $f(E_n)$ due to selfabsorption and multiple scattering calculated with the code SESH [44].

multiple scattering effects. This correction is in general not analytically determinable but can be obtained by Monte Carlo simulations. We used the code SESH [44] to calculate $f(E_n)$ by generating individual resonances according to user-supplied level densities and neutron strength functions. The result of these calculations are shown in Fig. 6. The energyaveraged cross section obtained in this way is reported in Table I. In Fig. 7, the cross section is plotted, multiplied by $\sqrt{E_n}$ in order to appreciate the data in the entire energy range.

B. Comparison with existing data

The present measurement, covering the full energy range from 4 keV to 1 MeV (well above the inelastic scattering threshold), can be compared to existing measurements in the overlapping energy regions. The prompt γ -ray data from Borella *et al.* [26] and the activation data from Lindner *et al.* [16] agree with the present results within the stated uncertainties. Also the data of Poenitz and Smith [18] correspond reasonably well. The activation data from Karamanis *et al.* [28]

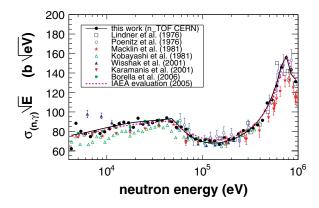


FIG. 7. (Color online) Neutron capture cross section 232 Th (n, γ) multiplied by the square root of the neutron energy, showing the measured data and an average parameter fit, compared to several other experimental data sets. To keep the figure readable, data covering energy bins are represented by points and uncertainties for some data sets are omitted.

TABLE I. Measured capture cross section of 232 Th (n, γ) reaction averaged over neutron energy intervals E_{low} to E_{high} . Quoted uncertainties are statistical only. An overall uncertainty of 3.3% should be applied to the cross section values in the entire neutron energy range (see text for detailed discussion).

E _{low} (keV)	$E_{ m high}$ (keV)	Cross section (b)	Uncertainty (b)
3.994	4.482	0.958	0.020
4.482	5.028	1.281	0.021
5.028	5.642	1.097	0.016
5.642	6.331	1.004	0.014
6.331	7.103	0.912	0.013
7.103	7.970	0.919	0.013
7.970	8.942	0.848	0.013
8.942	10.033	0.817	0.012
10.033	11.257	0.800	0.012
11.257	12.631	0.787	0.012
12.631	14.172	0.761	0.012
14.172	15.902	0.729	0.011
15.902	17.842	0.685	0.011
17.842	20.019	0.613	0.010
20.019	22.461	0.641	0.010
22.461	25.202	0.566	0.009
25.202	28.277	0.545	0.009
28.277	31.728	0.513	0.008
31.728	35.599	0.497	0.009
35.599	39.943	0.468	0.009
39.943	44.816	0.456	0.009
	50.285		
44.816		0.413	0.007
50.285	56.421	0.365	0.006
56.421	63.305	0.346	0.006
63.305	71.029	0.318	0.006
71.029	79.696	0.275	0.005
79.696	89.421	0.248	0.005
89.421	100.332	0.229	0.005
100.332	112.574	0.220	0.004
112.574	126.310	0.204	0.004
126.310	141.722	0.192	0.004
141.722	159.016	0.172	0.003
159.016	178.418	0.179	0.003
178.418	200.188	0.165	0.003
200.188	224.614	0.158	0.003
224.614	252.022	0.159	0.003
252.022	282.773	0.156	0.002
282.773	317.277	0.147	0.002
317.277	355.990	0.144	0.002
355.990	399.428	0.141	0.002
399.428	448.165	0.140	0.002
448.165	502.849	0.158	0.002
502.849	564.207	0.154	0.002
564.207	633.051	0.164	0.001
633.051	710.294	0.178	0.001
710.294	796.963	0.179	0.001
796.963	894.207	0.156	0.001
894.207	991.452	0.135	0.001

show the same the shape but are systematically lower than the present results in the overlapping energy range. The prompt

 γ -ray data from Wisshak *et al.* [27] are discrepantly higher up to about 40% below 10 keV and slightly lower around 100 keV. Macklin and Winters [45] and Kobayashi *et al.* [19] used freshly isotopically separated ²³²Th samples, reducing largely the background due to the radioactivity of the daughter nuclei of the decay chain. These data still show differences with the present results ranging up to more than 10%, probably because of normalization problems. The data from these experiments are also shown in Fig. 7. Additional data, including resonance data, can be found elsewhere [15,17,20–25,46].

We believe that many of the discrepancies with previous experiments, when exceeding the reported systematic uncertainties, could be explained by unrecognized errors in the normalization procedures, affecting the whole data set in the same way, or by insufficient corrections to background estimations, applied weighting functions, or flux determinations.

In addition to these experimental data, we have added to the figure a calculated cross section coming from a full evaluation of the neutron-induced reactions on 232 Th up to 60 MeV [47] using the EMPIRE code system [48]. The calculation is based on the dispersive coupled-channel optical model potential recently developed for thorium [49] and employed a combination of the Hauser-Feshbach theory and exciton model to describe the decay of the compound nucleus. Although this calculation is not based on the measurement, the good agreement is striking. The data are also in good agreement with a recent evaluation by Maslov *et al.* [50].

C. Average parameter description of the capture cross section

The measured cross section shown in Fig. 7 has been fitted by an average parameter description, also shown in the figure. A different way to describe average cross sections, as a complement to optical model calculations, is to use R-matrix theory, which is usually used for resolved resonances. This procedure corresponds to a Hauser-Feshbach calculation with width fluctuations [51]. In the unresolved resonance region, fictitious resonances can be generated to describe the average cross section. These resonances enable the calculation of not only the average cross sections but also self-shielding factors in a consistent way. Therefore it is important to employ an average resonance parameter description.

The resonances in the unresolved resonance region have an average reduced neutron width $\langle g \Gamma_n^{\ell} \rangle$ related to the neutron strength function S_{ℓ} by

$$S_{\ell} = \frac{1}{2\ell + 1} \frac{\left\langle g \Gamma_n^{\ell} \right\rangle}{D_{\ell}},\tag{7}$$

where D_{ℓ} is the level spacing for neutron resonances of orbital momentum ℓ . In a similar way, the average radiation width $\langle \Gamma_{\gamma} \rangle$ is included. The partial cross section for a reaction from the ingoing channel *c* to the outgoing channel *c'* is then related to the average collision matrix elements $U_{cc'}$ describing the reaction by

$$\langle \sigma_{cc'} \rangle = \pi \lambda_c^2 g_c \langle (\delta_{cc'} - U_{cc'})^2 \rangle. \tag{8}$$

The collision matrix elements $U_{cc'}$ are in their turn related to the *R* matrix containing the level properties, i.e., level energies and decay amplitudes of the resonances (widths). The capture cross section can be described in this way with only a few average parameters for each partial wave.

We used the code FITACS [52] as included in SAMMY [53] to fit the average capture cross section with average resonance parameters from a Hauser-Feshbach calculation with width fluctuations. In the code, the parameters that can be varied are the neutron strength functions S_{ℓ} , level spacings D_{ℓ} , and average radiation width $\langle \Gamma_{\gamma} \rangle_{\ell}$. The energy dependence of these parameters and the competitive widths from inelastic scattering are also taken into account. The level information for the inelastic channels has been taken from the ENSDF database [54]. The contributions from the first three partial waves are sufficient up to 1 MeV.

Much care has to be taken when trying to fit these parameters from the data, since the parameters are largely correlated, in particular the parameters for the same partial wave. In addition, the parameters are sensitive in a different way to the total or partial cross sections. The best way to constrain the fit to the most physical values of the parameters is to include data sets for different reaction cross sections in a simultaneous fit. In this work, however, we used only the present capture data.

It may be instructive to see the contributions of each partial wave to the capture cross section as shown in Fig. 8. While letting free many combinations of parameters, we found that it was in many cases possible to obtain a good overall fit of the capture data alone. This indicates that the parameters are strongly correlated. The plot in Fig. 8 has been obtained with fixed values $D_0 = 17.2$ eV for the level spacing and other parameters as given hereafter. Variations of D_0 from 16.6 to 17.6 eV did not practically influence the following results. The values for D_1 and D_2 were scaled to D_0 by the number of allowed spin states, assuming a 2J + 1 spin dependence of the level density. Values $S_0 = 0.87 \times 10^{-4}$ and $S_1 = 1.9 \times 10^{-4}$ for the neutron strength functions were taken from Ref. [49]. The fitted values resulting from the code FITACS were

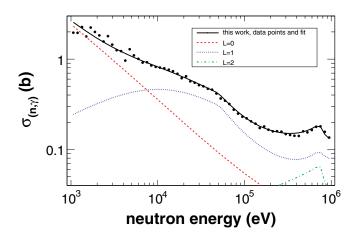


FIG. 8. (Color online) Measured cross section and a description with average resonance parameters using the code FITACS. Partial wave contributions for $\ell = 0, 1$, and 2 are also shown.

 $S_2 = 0.89 \times 10^{-4}$, $\langle \Gamma_{\gamma} \rangle_0 = \langle \Gamma_{\gamma} \rangle_2 = 18.8$ meV, and $\langle \Gamma_{\gamma} \rangle_1 = 20.6$ meV. These values of the average γ width are comparable but slightly lower than those found in the resolved resonance analysis and as found in, for example, [9]. We repeated the fit as before but now kept all γ widths fixed to $\langle \Gamma_{\gamma} \rangle_{\ell} = 24.3$ meV. The resulting fitted strength functions were in that case $S_0 = 0.68 \times 10^{-4}$, $S_1 = 1.4 \times 10^{-4}$, and $S_2 = 0.43 \times 10^{-4}$.

IV. DISCUSSION OF UNCERTAINTIES

Only uncorrelated or statistical uncertainties are given in Table I with the result on the measured cross section. The total uncertainty in the cross section consists of several contributions that can be identified from the analysis procedure. The main sources come from the background determination and from the absolute neutron flux determination. The uncertainty related to the influence of the weighting function is rather small in this case since the measurement is not relative to a different isotope, but it is self-normalized to the saturated resonances we used at 21.79 and 23.46 eV. The γ -ray spectra are quite similar for the different resonances because of the large number of levels available for decay after capture. The influence of the threshold may play a role, but the resulting cross sections with low or high thresholds give statistically coherent results. From these considerations, we could assign an uncertainty of 0.5% from the application of the PHWT.

The uncertainty due to background subtraction is the most delicate to estimate. The absolute level of the background requires the determination of the level of the black resonance as explained in detail above. We applied several combinations of fits and binnings of the spectra, and we estimate the uncertainty in the background subtraction at the level of 2.5%. This value is also in agreement with the maximum difference in cross section obtained with a threshold of 160 and 1000 keV.

The correction resulting from a simulation with the code SESH for self-absorption above 4 keV is at most about 4%. Although we had no other independent calculation to compare the correction against and derive a possible uncertainty, we believe that the uncertainty in the correction is small, and we did not include it in the error balance.

For the estimation of the uncertainty of the shape of the neutron flux, we adopted an uncertainty of 2%. An uncertainty in the absolute level of the flux is not relevant since we normalized the yield on the saturated resonances.

Adding up these components gives a total correlated or systematic uncertainty of 3.3%, as listed in Table II. A detailed

TABLE II. Different components of estimated systematic or correlated uncertainty in the measured cross section.

Component	Uncertainty (%)	
PHWT	0.5	
Normalization	0.5	
Background	2.5	
Flux shape	2.0	
Total	3.3	

covariance propagation for the present analysis procedure and within the given assumptions on the uncertainty contributions is described in a separate report [55].

V. CONCLUSION

A new set of self-normalized ²³²Th neutron capture yield data has been obtained in a large energy range from 1 eV to 1 MeV from a measurement at n_TOF at CERN. The cross section in the unresolved resonance region from 4 keV to 1 MeV has been extracted, and the results have been fitted in terms of average resonance parameters. The point-wise data have been reported in logarithmically equidistant energy bins with 20 bins per energy decade. A comparison with existing data has solved an important discrepancy in the 10 keV region and increased the present knowledge of the capture cross section up to 1 MeV.

- [1] G. Wallerstein et al., Rev. Mod. Phys. 69, 995 (1997).
- [2] F. Käppeler, Prog. Part. Nucl. Phys. 43, 419 (1999).
- [3] G. E. Mitchell, J. D. Bowman, and H. A. Weidenmüller, Rev. Mod. Phys. 71, 445 (1999).
- [4] Y. Masuda et al., Nucl. Phys. A721, 485c (2003).
- [5] M. Salvatores, I. Slessarev, and A. Tchistiakov, Nucl. Sci. Eng. 130, 309 (1998).
- [6] W. Gudowski, Nucl. Phys. A654, 436c (1999).
- [7] S. David, A. Billebaud, M. E. Brandan, R. Brissot, A. Giorni, D. Heuer, J. M. Loiseaux, O. Meplan, H. Nifenecker, J. B. Viano *et al.*, Nucl. Instrum. Methods Phys. Res. A 443, 510 (2000).
- [8] A. Bidaud, Ph.D. thesis, University of Paris XI, Orsay, 2005.
- [9] S. F. Mughabghab, M. Divadeenam, and N. E. Holden, Neutron Cross Sections: Neutron Resonance Parameters and Thermal Cross Sections. Z = 1-60 (Academic Press, New York, 1981).
- [10] S. I. Sukhoruchkin, Z. N. Soroko, and V. V. Deriglazov, Low Energy Neutron Physics, Vol. 1/16B, Tables of Neutron Resonance Parameters (Springer, Landolt-Börnstein, 1998).
- [11] See, for example, the International Atomic Energy Agency (IAEA), www-nds.iaea.org; or the OECD Nuclear Energy Agency, www.nea.fr.
- [12] G. E. Mitchell, J. D. Bowman, S. I. Pentillä, and E. I. Sharapov, Phys. Rep. 354, 157 (2001).
- [13] S. L. Stephenson et al., Phys. Rev. C 58, 1236 (1998).
- [14] J. D. Bowman, G. T. Garvey, M. B. Johnson, and G. E. Mitchell, Annu. Rev. Nucl. Part. Sci. 43, 829 (1993).
- [15] F. Rahn et al., Phys. Rev. C 6, 1854 (1972).
- [16] M. Lindner, R. J. Nagle, and J. H. Landrum, Nucl. Sci. Eng. 59, 381 (1976).
- [17] R. L. Macklin and J. Halperin, Nucl. Sci. Eng. 64, 849 (1977).
- [18] W. P. Poenitz and D. L. Smith, Nucl. Sci. Eng. 59, 381 (1976).
- [19] K. Kobayashi, Y. Fujita, and N. Yamamuro, J. Nucl. Sci. Tech. 18, 823 (1981).
- [20] R. L. Macklin, Nucl. Sci. Eng. 79, 118 (1981).
- [21] D. K. Olsen, R. W. Ingle, and J. L. Portney, Nucl. Sci. Eng. 82, 289 (1982).
- [22] R. B. Perez, G. de Saussure, R. L. Macklin, J. Halperin, and N. W. Hill, Nucl. Sci. Eng. 80, 189 (1982).
- [23] K. Kobayashi et al., Ann. Nucl. Energy 15, 381 (1988).

PHYSICAL REVIEW C 73, 054610 (2006)

The present measurement covers a large energy range including both the endpoints of other time-of-flight measurements and the starting energies of activation measurements.

Without giving details that go beyond the scope of this paper, it is clear that the accurate knowledge of this cross section is of great importance to a thorium-based nuclear fuel cycle. In addition, the precisely measured cross section puts severe constraints on optical model calculations predicting cross sections for this nucleus. Additional information is expected from the analysis of the resolved resonances below 4 keV.

ACKNOWLEDGMENTS

This work has been supported by the European Commission's 5th Framework Programme under Contract Number FIKW-CT-2000-00107 (n_TOF-ND-ADS Project).

- [24] W. Y. Baek, G. N. Kim, M. H. Cho, I. S. Ko, W. Namkung, Y. V. Grigoriev, H. Faikov-Stanczyk, V. N. Shvetshov, and W. I. Furman, Nucl. Instrum. Methods Phys. Res. B 168, 453 (2000).
- [25] Y. V. Grigoriev et al., J. Nucl. Sci. Tech. Suppl. 2, 350 (2002).
- [26] A. Borella, K. Volev, A. Brusegan, G. Lobo, P. Schillebeeckx, F. Corvi, N. Koyumdjieva, N. Janeva, and A. A. Lukyanov, Nucl. Sci. Eng. 152, 1 (2006).
- [27] K. Wisshak, F. Voss, and F. Käppeler, Nucl. Sci. Eng. 137, 183 (2001).
- [28] D. Karamanis et al., Nucl. Sci. Eng. 139, 282 (2001).
- [29] G. Aerts et al. (in preparation).
- [30] G. Aerts, Ph.D. thesis, University of Paris XI, Orsay, 2005.
- [31] C. Rubbia et al., Tech. Rep. CERN/LHC/98-02, 1998.
- [32] U. Abbondanno et al., Tech. Rep. CERN-SL-2002-053 ECT, 2003.
- [33] J. Pancin *et al.*, Nucl. Instrum. Methods Phys. Res. A **524**, 102 (2004).
- [34] U. Abbondanno et al., Tech. Rep. CERN/INTC 2001-038, 2001.
- [35] A. Ferrari, C. Rubbia, and V. Vlachoudis, Tech. Rep. CERN-SL-EET-2001-036, 2002.
- [36] R. Plag et al., Nucl. Instrum. Methods Phys. Res. A 496, 425 (2003).
- [37] S. Marrone *et al.*, Nucl. Instrum. Methods Phys. Res. A 517, 389 (2004).
- [38] C. Borcea *et al.*, Nucl. Instrum. Methods Phys. Res. A **513**, 524 (2003).
- [39] U. Abbondanno *et al.*, Nucl. Instrum. Methods Phys. Res. A **538**, 692 (2005).
- [40] F. Bečvář, Nucl. Instrum. Methods Phys. Res. A 417, 434 (1998).
- [41] F. Corvi et al., Nucl. Sci. Eng. 107, 272 (1991).
- [42] J. N. Wilson, B. Haas, S. Boyer, D. Dassié, G. Barreau, M. Aiche, S. Czajkowski, C. Grosjean, and A. Guiral, Nucl. Instrum. Methods Phys. Res. A 511, 388 (2003).
- [43] U. Abbondanno *et al.*, Nucl. Instrum. Methods Phys. Res. A 521, 454 (2004).
- [44] F. H. Fröhner, SESH computer code, GA-8380, Gulf General Atomic, 1968.
- [45] R. L. Macklin and R. R. Winters, Nucl. Sci. Eng. 78, 110 (1981).
- [46] G. Baldwin and G. Knoll, Nucl. Sci. Eng. 88, 121 (1984).

- [47] R. Capote, M. Sin, and A. Trkov, (in preparation).
- [48] M. Herman *et al.*, Nuclear reaction model code EMPIRE v.2.19, www-nds.iaea.org/empire/.
- [49] E. S. Soukhovitskii, R. Capote, J. M. Quesada, and S. Chiba, Phys. Rev. C 72, 024604 (2005).
- [50] V. M. Maslov *et al.*, Tech. Rep. INDC(BLR)-016, International Atomic Energy Agency, 2003.
- [51] F. H. Fröhner, Nucl. Sci. Eng. 103, 119 (1989).

- [52] F. H. Fröhner, B. Goel, and U. Fischer, FITACS computer code, Rep. ANL-83-4, Argonne National Laboratory, 1983.
- [53] N. M. Larson, SAMMY computer code, Rep. ORNL/TM-9179/R7, Oak Ridge National Laboratory, 2006.
- [54] See, for example, www.nndc.bnl.gov.
- [55] H. Leeb and M. Pigni, Tech. Rep. ATI-NDC-2004-03, Technische Universität Wien, 2005.