Dynamical effects in multifragmentation at intermediate energies

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The fragmentation of a quasiprojectile is studied with the INDRA multidetector for different colliding systems and incident energies in the Fermi energy range. Different experimental observations show that a large part of the fragmentation is not compatible with the statistical fragmentation of a fully equilibrated nucleus. The study of internal correlations is a powerful tool, especially to evidence entrance channel effects. These effects have to be included in the theoretical descriptions of nuclear multifragmentation.

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I. INTRODUCTION

The physical characteristics (shapes, excitation energies, angular momentum, radial flow, ...) of the hot nuclei formed in nucleus-nucleus collisions are obtained by comparisons between models and data. Statistical decay models are widely used and dedicated to describe the decay of hot fully equilibrated systems, defined as systems having reached energy, shape, and isospin equilibrium [1–9]. However, other experimental works show strong effects of the entrance channel on the decay models of the formed hot systems [10–23]. These effects, which are not taken into account in the statistical decay models, can provide complementary information on the nuclei such as the characteristics of the nucleon-nucleon interaction [24–27] and/or the viscosity of the nuclear matter.

Up to now, these entrance channel effects have been studied by tracking deviations from the standard fission process in the quasiprojectile breakup [13,14,18,19,22]. Such deviations have been seen on the angular distributions, which show the focusing of the breakup axis along the quasiprojectile velocity direction. Associated with this focusing, highly asymmetrical breakups have also been observed, whereas symmetrical breakups were expected. The corresponding relative velocities were higher than the value predicted by the Viola systematics [28]. These aligned breakups represent up to 75% of the binary breakup for the Xe+Sn system [13]. In this paper, we will extend these studies performed for binary breakup to higher fragment multiplicities to test to what extent these effects are present for other exit channels. We will present systematic studies on experimental data only, over a wide range of system sizes, incident energies, and

projectile/target asymmetries. There will be no attempt to compare these data to theoretical calculations.

We have studied the decay of different quasiprojectiles formed in several projectile-target collisions from 25*A* to 90*A* MeV. In the first section, we present the experimental setup, the studied systems, and the selections that have been applied on the data. In the second section the charge distributions, the associated velocity, and angular distributions obtained for the different systems are shown. The third section is devoted to the evolutions of some experimental observables as a function of the breakup asymmetry of the quasiprojectile. In the last section our conclusions are given.

II. THE EXPERIMENTAL SETUP

The experiments were performed at the GANIL facility with the INDRA detector. The different systems that will be presented in this paper are Ni+Ni at 52A and 90A MeV, Xe+Sn from 39A to 50A MeV, Ta+Au at 33A and 39A MeV, Ta+U at 33A and 39A MeV, and U+U at 24A MeV. Target thicknesses were, respectively, 193 μ g/cm² of Au for the experiment with the Au target, $179 \,\mu \text{g/cm}^2$ of Ni for the Ni + Ni experiment, and $330 \ \mu g/cm^2$ of Sn for the Xe + Sn experiment. The $100 \ \mu g/cm^2$ uranium target was deposited between two 20 μ g/cm² carbon foils. We will show afterwards the method used to separate the events corresponding to the uranium target from those corresponding to the carbon backing. Typical beam intensities were $3 \times 10^7 - 4 \times 10^7$ pps. Events were registered when at least four charged particle detectors fired (eight for the collisions with the Ta projectile).

The INDRA detector [29,30] can be schematically de-



FIG. 1. Correlation between the charge Z and the velocity component parallel to the beam V_z in the center of mass frame for the Ta+Au collisions at 39.6A MeV and for events having a total linear momentum greater than 80% of the incident linear momentum. The shading of gray is darker for the high cross sections.

scribed as a set of 17 detection rings centered on the beam axis. In each ring the detection of charged products was provided with two or three detection layers. The most forward ring, $2^{\circ} \leq \theta_{lab} \leq 3^{\circ}$, is made of phoswich detectors (plastic scintillators NE102 + NE115). Between 3° and 45° eight rings are constituted by three detector layers: ionization chambers, silicon, and ICs(Tl). Beyond 45°, the eight remaining rings are made of double layers: ionization chambers and ICs(Tl). The total number of detection cells is 336 and the overall geometrical efficiency of INDRA detector corresponds to 90% of 4π . Isotopic separation is achieved up to Z=3-4 in the last layer [ICs(Tl)] over the whole angular range $(3^\circ \le \theta_{lab} \le 176^\circ)$. The charge resolution in the forward region $(3^{\circ} \le \theta_{lab} \le 45^{\circ})$ is one unit up to $Z \approx 50$. In the backward region ($\theta_{lab} \ge 45^\circ$) a charge resolution of one unit is obtained up to $Z \approx 20$. The energy resolution is about 5% for ICs(Tl) and ionization chambers and better than 2% for silicon detectors.

The binary character of the collisions is clearly seen in Fig. 1, which plots the correlation between the charge Z and the velocity component parallel to the beam V_z of each detected fragment. The fragments are roughly distributed around two areas: one around the quasiprojectile velocity and charge ($V_z \approx 4$ cm/ns and $Z \approx 75$) and one around the quasitarget velocity ($V_z \approx -4$ cm/ns). Due to the experimental thresholds, the fragments emitted by the quasi-target are not detected efficiently. Then, for this analysis, only the fragments produced by the quasiprojectile are taken into account. Due to the quasisymmetry of most of the studied systems, a fragment ($Z \approx 3$) is assumed to be emitted by the quasiprojectile if its velocity component parallel to the beam axis is higher than the velocity of the center of mass $V_{c.m.}$.

In order to have enough information to perform our studies, only events for which more than 80% of the incident

TABLE I. Grazing angles in the laboratory frame for different systems.

System	Incident energy (MeV)	$ heta_{grazing} \ (ext{deg})$
$\overline{U + U}$	24A	8
U + C	24A	0.7
Ta + U	33A	6
Ta + Au	33A	5
Ta + C	33A	0.5
Ta + U	39.6A	5
Ta + Au	39.6A	4
Ta + C	39.6A	0.4

linear momentum was detected are selected $(\Sigma Z_i V_i^z) > 0.8 Z_{proj} V_{proj}^z$ where Z_i and Z_{proj} are the charge of the fragment *i* and the charge of the projectile, respectively, and V_i^z and V_{proj}^z their velocity components parallel to the beam axis in the laboratory frame).

The events are sorted according to the multiplicity M_{imf} of fragments ($Z \ge 3$) emitted by the quasiprojectile.

The use of a 4π multidetector gives a very good coverage of the quasiprojectile emissions. The angular, charge and velocity or energy distributions are precisely obtained. This allows the study of the internal correlations in one event such as the correlation between the fragments relative velocities and the breakup direction. It will be shown later that this is a powerful tool to distinguish different reaction mechanisms.

As said previously, uranium was deposited between two carbon layers. Thus, for the systems with this target, there will be a mixing of reactions on the backing (C) and on the target (U). The separation between these two reactions is done by using the angular distribution of the quasiprojectile. For a fixed incident energy, the grazing angle for the heavy



FIG. 2. Distribution of θ_{QP} for the Ta+C,U system at 33A MeV (full line) and the Ta+Au system at 33A MeV (dashed line).



FIG. 3. Distribution of θ_{QP} for the Ta+C,U system at 39.6A MeV (full line) and the Ta+Au system at 39.6A MeV (dashed line).

target is larger that the grazing angle for the light one. The values of this angle are summarized in Table I.

Two contributions are then expected for the quasiprojectile diffusion angle θ_{QP} . The quasiprojectile (QP) is reconstructed with the fragments whose velocities are greater than $V_{c.m.}$. Such distributions are shown in Figs. 2–4. In the first two figures, the dashed line corresponds to the system with the Ta projectile and the Au target and the full line corresponds to the system with the Ta projectile and the U target and C backing. Reactions on the C backing clearly show up at small angles, while the distributions at large angles, from



FIG. 4. Distribution of θ_{OP} for the U+C,U system at 24A MeV.



FIG. 5. Definition of the angles $\theta_{F/QP}$ and θ_{QP} .

their similarities with those arising from Ta+Au, can be attributed to reaction on U only. A clear selection of Ta+U reactions is ensured by selecting events with $\theta_{QP} > 10^{\circ}$. For the U+C,U system (Fig. 4), the two contributions (U target and C backing) are better separated due to the larger difference between the values of the grazing angles. The same cut $(\theta_{QP}=10^{\circ})$ was applied to separate the contributions from the uranium target and the carbon backing. For this system, the contribution of the uranium target at small angles is weaker compared to the Ta+C,U systems.



FIG. 6. Charge (uppermost row), parallel velocity (middle row), and $\cos(\theta_{F/QP})$ (lowermost row) distributions for the Ta+Au system at 33A MeV. The columns correspond to different fragment multiplicities (from $M_{imf}=2$ to $M_{imf}=4$ from left to right). The shading of the distribution darkens according to the rank of the fragment in the event (the lightest shading corresponds to the heaviest fragment in the event).



FIG. 7. Same as Fig. 6, but for the Ta+Au system at 39.6A MeV.



FIG. 9. Same as Fig. 6, but for the Xe+Sn system at 45A MeV.



FIG. 8. Same as Fig. 6, but for the Xe+Sn system at 39A MeV.



FIG. 10. Same as Fig. 6, but for the Xe+Sn system at 50A MeV.



FIG. 11. Same as Fig. 6, but for the Ni+Ni system at 52A MeV.



FIG. 13. Same as Fig. 6, but for the Ta+U system at 33A MeV $(\theta_{QP} > 10^{\circ})$.



FIG. 12. Same as Fig. 6, but for the Ni+Ni system at 90A MeV.



FIG. 14. Same as Fig. 6, but for the Ta+U system at 39.6A MeV ($\theta_{QP} > 10^{\circ}$).



FIG. 15. Same as Fig. 6, but for the Ta+C,U system at 33A MeV (all θ_{QP}).



FIG. 17. Same as Fig. 6, but for the U+U system at 24A MeV ($\theta_{QP} > 10^{\circ}$).



FIG. 16. Same as Fig. 6, but for the Ta+C,U system at 39.6A MeV (all θ_{QP}).



FIG. 18. Same as Fig. 6, but for the U+C system at 24A MeV ($\theta_{QP} \leq 10^{\circ}$).



FIG. 19. Schematic view of the fragmentation scenario leading to the "hierarchy effect." The shading darkens according to the charge ranking of the fragments.

III. SIZE AND VELOCITY HIERARCHY

We will first look at simple and direct observables such as the fragment charge distributions, the corresponding distributions of the velocity component parallel to the beam (V_z) , and the angular distributions for the different systems. The angle $\theta_{F/QP}$ is the angle between the velocity of the fragment in the quasiprojectile (QP) frame and the velocity of the quasiprojectile in the center of mass frame (see Fig. 5). The events are sorted according to the multiplicity M_{imf} of the forward fragments ($V_z > V_{c.m.}$). In each event, the fragments are sorted according to their charge.

Charge V_z and $\cos(\theta_{F/QP})$ distributions are shown in Fig. 6. The uppermost row corresponds to the charge distribution, the middle row to the V_z distribution, and the lowermost row to $\cos(\theta_{F/QP})$ distribution. The different columns correspond to the different fragment multiplicities (from $M_{imf}=2$ to $M_{imf}=4$ from left to right). On each panel, the shading of the distribution darkens according to the rank of the fragment in the event.

One spectacular observation is that the velocity distributions are strongly correlated to the charge sorting: the heaviest fragment is in average the fastest one, the second heaviest fragment is the second fastest one, and so on. For the $\cos(\theta_{F/QP})$ distributions, the distribution of the heaviest fragment is peaked at forward angles $[\cos(\theta_{F/QP})\approx 1]$: the emission direction of this fragment is close to the quasiprojectile



FIG. 20. $\cos(\theta_{prox})$ distributions for the Ta+Au system at 33A MeV. The columns correspond to the different fragment multiplicities from 2 to 5. The rows correspond to different ranges for the charge Z_1 of the heaviest fragment: the most symmetrical breakups (low Z_1 values) correspond to the uppermost row and the most asymmetrical breakups (high Z_1 values) correspond to the lowermost row.



FIG. 21. Same as Fig. 20, but for the Ta+Au system at 39.6A MeV.

velocity direction. Such pictures were not expected in case of a fragmentation of a fully equilibrated quasiprojectile, for which the fragments are emitted in all directions without a particular hierarchy for the velocities. This hierarchy effect [the ranking in charge induces on average the ranking in V_z and the $\cos(\theta_{F/QP})$ distribution of the heaviest fragment is forward peaked] suggests an entrance channel effect.

Similar results are observed for the corresponding distributions for most of other systems. The heaviest fragment is the fastest one and its direction of emission is close to the quasiprojectile velocity direction, whatever the system size and whatever the incident energy. The hierarchy between the size of the fragment and its velocity is observed for the Ta + Au (Figs. 6 and 7), Xe+Sn (Figs. 8–10), and Ni+Ni systems (Figs. 11 and 12). This effect is strong on the Ta+Au system and is slightly weaker for the Xe+Sn and the Ni+Ni systems. For the Xe+Sn system, the anisotropy of the heaviest fragment angular distribution increases slightly with the incident energy.

For the Ta+U system (events with $\theta_{QP} > 10^{\circ}$, Figs. 13 and 14), the same hierarchy effect is observed as for the Ta+Au system. For the Ta + C,U system (Figs. 15 and 16), this hierarchy effect is still observed for high multiplicities $(M_{imf} \ge 3)$, but is not present for $M_{imf} = 2$. This is due to the mixing between the carbon backing and the uranium target mentioned in the preceding section. For $M_{imf} = 2$, the two fragments have almost the same charges, the velocities are similar, and the whole range of $\cos(\theta_{F/OP})$ is covered. The contribution of the Ta+C collisions becomes stronger as M_{imf} decreases. This contribution is especially seen for $M_{imf}=2$ (compare leftmost columns of Figs. 13 and 15 for 33A MeV and Figs. 14 and 16 for 39A MeV) where the distributions are completely different. The Ta+C collisions lead to the formation of an incomplete fusion nucleus, which decays through fission. In this case, no hierarchy in velocities or no privileged angles of the heaviest fragment are expected.

For the U+U system (Fig. 17, events with $\theta_{OP} > 10^{\circ}$) the hierarchy effect is observed for $M_{imf} \ge 3$ but is not observed for $M_{imf} = 2$. Due to the high fissility of uranium, the M_{imf} =2 events correspond mainly to the fission process. However, events for which the charge of the heaviest fragment is close to 80 are still present. They correspond to asymmetric binary breakups that are not expected for the fission of such a heavy nucleus. These asymmetric breakups are not present for the U+C system (Fig. 18, leftmost column, $\theta_{OP} < 10^{\circ}$) and no hierarchy effect is seen: these observations are consistent with the fission of a fully equilibrated nucleus. For $M_{imf} \ge 3$, the velocities of the two heaviest fragments are similar and their $\cos(\theta_{F/OP})$ distributions are flat. For the other fragments, the hierarchy effect is present. This could be due to a two-step process in which the hierarchy effect is present at the early stage of the collision, followed by the fission of the heaviest fragment due to the high value of its charge.

To summarize this section, a hierarchy effect [the ranking



FIG. 22. $E_{t12}/E_{c.m.}$ distributions (in percent) for the Ta+Au system at 39.6A MeV. The columns correspond to the different fragment multiplicities from 2 to 5. The rows correspond to different ranges for the charge Z_1 of the heaviest fragment: the most symmetrical breakups (low Z_1 values) correspond to the uppermost row and the most asymmetrical breakups (high Z_1 values) correspond to the lowermost row.

in charge induces the ranking in V_z and the $\cos(\theta_{F/QP})$ distribution of the heaviest fragment is forward peaked] is seen for many system sizes and incident energies. These observations are not consistent with the decay of a fully equilibrated nucleus for which no hierarchy effect is expected. This "hierarchy effect" is consistent with a strong deformation of QP or QT during the collision, which is followed by the breakup of these elongated nuclei in two or more fragments (neck formation and breakup, see Fig. 19). The fragments emitted by this neck reflect its internal structure: its size at the center of mass is on average thinner than close to the quasiprojectile or quasitarget, and the velocity moduli in the center of mass are smaller than those of nucleons close to the quasitarget or to the quasiprojectile.

This leads to the "hierarchy effect" observed experimentally. The velocity gradient can be tracked by studying the relative velocities between the heaviest fragment and the others. In the proposed scenario, this relative velocity is expected to be larger than the one obtained from the decay of a fully equilibrated nucleus. For the heaviest systems, the standard fission process superimposes on the neck formation and breakup. The two contributions are clearly seen for Ta and U projectiles. In these cases, deviations from the standard fission can be easily tracked.

IV. INTERNAL CORRELATIONS

In the preceding section, we have evidenced a "hierarchy effect," indicating a strong entrance channel influence on the fragmentation of the quasiprojectile. We will study in this section correlations between some observables to verify whether the fragmentation scenario proposed above resists a more detailed analysis. If an elongated quasiprojectile is formed and breaks quickly, the relative velocities between the fragments should be higher along the QP velocity direction than in any other direction, because the incident energy is not fully damped in internal degrees of freedom in such a process. Within this assumption, the heaviest fragment focused along the QP velocity has a high velocity because it is a remnant of the projectile. In the case of the fragmentation of a fully equilibrated QP, the relative velocity should be independent of the breakup direction.

For $M_{imf}=2$, the relative velocity between the two fragments can be easily determined, while it is not the case for higher multiplicities. We have seen in the preceding section



FIG. 23. Evolutions of the average relative velocity V_{rel} with $\cos(\theta_{prox})$ for the Ta+Au system at 39.6A MeV. The columns correspond to the different fragment multiplicities from 2 to 5. The rows correspond to different ranges for the charge Z_1 of the heaviest fragment: the most symmetrical breakups (low Z_1 values) correspond to the uppermost row and the most asymmetrical breakups (high Z_1 values) correspond to the low-ermost row.

that the heaviest fragment has the same properties whatever the value of M_{imf} : it is the fastest one and it is focused in the direction of the quasiprojectile in the center of mass frame. We can use this property to define the breakup direction θ_{prox} as the direction of the heaviest fragment with respect to the quasiprojectile velocity, and the relative velocity \vec{V}_{rel} as the difference of the velocity of the heaviest fragment \vec{V}_1 and the velocity of the center of mass of all other fragments detected with a velocity greater than $V_{c.m.}$. They are determined as follows:

$$\vec{V}_{rel} = \vec{V}_1 - \frac{\sum_{i=2}^{M_{imf}} Z_i \vec{V}_i}{\sum_{i=2}^{M_{imf}} Z_i},$$
(1)

where Z_i is the charge of the *i*th fragment $(Z_i > Z_{i+1})$ and $\overline{V_i}$ its velocity,

$$\cos(\theta_{prox}) = \frac{(\vec{V}_1 - \vec{V}_{QP}) \cdot \vec{V}_{QP}}{|\vec{V}_1 - \vec{V}_{QP}| |\vec{V}_{QP}|},$$
(2)

where V_{QP} is the velocity of the quasiprojectile. All the velocities in formulas (1)–(3) are expressed in the center of mass frame. With this definition, θ_{prox} is identical to $\theta_{F/QP}$ of the heaviest fragment (see Fig. 5),

$$\vec{V}_{QP} = \frac{\sum_{i=1}^{M_{imf}} Z_i \vec{V}_i}{\sum_{i=1}^{M_{imf}} Z_i}.$$
(3)

Let us study the behavior of the $\cos(\theta_{prox})$ distributions. The experimental distributions are shown in Figs. 20 and 21 for the Ta + Au system at 33A and 39.6A MeV, respectively. On each figure, the columns correspond to different values of M_{imf} and the rows to different ranges in charge of the heaviest detected fragment Z_1 . This cut in Z_1 was done due to the particular behavior of the heaviest fragment. It is also correlated to the asymmetry of the breakup as in fission: the highest values of Z_1 correspond to the more asymmetric breakups (one big fragment and small other ones) and the lowest values of Z_1 correspond to the most symmetric breakups (equal size fragments). It can be seen in these figures that



FIG. 24. Same as Fig. 23, but for the U+U system at 24A MeV ($\theta_{QP} > 10^{\circ}$).

the $\cos(\theta_{prox})$ distributions are in most cases peaked at 1 (emission along the direction of the QP velocity). The most forward peaked $\cos(\theta_{prox})$ distributions are obtained for the most asymmetric breakups (high values of Z_1), and this for all values of M_{imf} . This is not expected in the case of a fragmentation of a fully equilibrated nucleus. An angular momentum effect would lead to a forward-backward symmetry in angular distributions.

For the most symmetric breakups (low values of Z_1) and the greater IMF multiplicities, the distribution becomes less forward peaked. In this case, the fragments having almost the same charge, the ranking in charge is meaningless. Consequently, the memory of the direction of the QP in the fragmentation process is blurred. Another possible scenario could be the occurrence of the fragmentation of a fully equilibrated QP. It will be seen later that the cut at $V_{c.m.}$ can also influence these distributions.

Is there a connection between the strength of the anisotropy of the $\cos(\theta_{prox})$ distributions and the violence of the collisions? The latter has been estimated by using the sum of the transverse energies E_{t12} of light charge particles ($Z \leq 2$). This global variable has been widely used as an impact parameter selector in previous studies [12,13]. The low values of transverse energies correspond to peripheral collisions and the high values to the most violent collisions. The reduced transverse energy distributions $(E_{t12}/E_{c.m.})$ where $E_{c.m.}$ is the energy available in the center of mass) are presented in Fig. 22 for Ta+Au collisions at 39.6A MeV. The shapes of these distributions depend weakly on the value of M_{imf} and strongly on that of Z_1 . This is in agreement with Z_1 being the remnant of the QP. The average E_{t12} value decreases when going from symmetrical (first row) to asymmetrical breakups (last row), as already shown for the lighter Ar+Ni system [31]. The last row corresponds to the most asymmetrical and aligned breakups (see Fig. 21). The transverse energies of the associated particles are low and correspond to peripheral collisions. The first row corresponds to the most symmetrical breakups and to more wider $\cos(\theta_{prox})$ distributions. The transverse energies of the associated particles are high and correspond to more central collisions.

It is interesting to observe low E_{t12} values for the highest IMF multiplicities (last row, rightmost panel of Fig. 22). In this case, the excitation energy of the QP is low and low evaporated IMF multiplicities are expected. This observation, combined with the "hierarchy effect" and the strongly peaked $\cos(\theta_{prox})$ distributions, strongly suggests that these



FIG. 25. Same as Fig. 23, but for the U+C system at 24A MeV ($\theta_{QP} \leq 10^{\circ}$).

fragmentations are only due to entrance channel effects. For the binary breakups (first column), the very asymmetrical breakups (last row) are not expected for the standard fission of a quasi-Ta. Nevertheless, this is the dominant decay channel for $M_{imf}=2$. The second and third panels of the first column ($M_{imf}=2$) correspond to more symmetrical breakups ($Z_1 \approx 37$) and the standard fission process is expected. In this case the transverse energy distributions are wider. It seems that two contributions could be considered, as already suggested by the the $\cos(\theta_{prox})$ distributions. These observations are also made on the other systems.

Let us now come to the correlation between the relative velocities of the fragment V_{rel} and $\cos(\theta_{prox})$. They are presented in Fig. 23 for Ta+Au collisions at 39.6A MeV, in Fig. 24 for the U+U collisions at 24A MeV, and in Fig. 25 for the U+C collisions at 24A MeV. As in Figs. 20 and 21, the columns correspond to different IMF multiplicities and the rows to different values of Z_1 . For the most asymmetric breakup of the Ta + Au collisions (two lowest rows for Fig. 23), a strong variation of V_{rel} with $\cos(\theta_{prox})$ is seen. The value of V_{rel} increases from 2.3 cm/ns at $\cos(\theta_{prox}) = -1$ up to ≈ 3.5 cm/ns at around $\cos(\theta_{prox}) = 0.8$ and then decreases. The variation is weaker for the more symmetric breakups (two first rows). This variation is also observed for the U+U collisions but its amplitude is smaller. For the U+C system (Fig. 25), no evolution is seen whatever the IMF multiplicity and the charge of the heaviest fragment. For the U+C system, no "hierarchy effect" was seen (see Fig. 18). Within our interpretation of the "hierarchy effect," no modulation is expected for this system. On all other systems, the same correlation is observed: a modulation of V_{rel} with $\cos(\theta_{prox})$ is seen when the "hierarchy effect" is observed. So the modulation of V_{rel} with $\cos(\theta_{prox})$ is correlated to the observation of a "hierarchy effect."

The decrease of V_{rel} at the smallest angles $[\cos(\theta_{prox})$ =1] is not compatible with the expected behavior of V_{rel} resulting from our interpretation on the "hierarchy effect." But due to the selection of the fragments in this analysis $(V_z > V_{c.m.})$, the highest values of V_{rel} cannot be reached. We have tested the effect of this velocity cut on our analysis with the help of a simple simulation. For the sake of simplicity, we have only verified the effect of the velocity cut for $M_{imf} = 2$. The basic ingredients of this simulation are the following: a QP with a charge Z_{OP} , a velocity V_{OP} , and an angle θ_{OP} is considered. This QP splits in two fragments of charges Z_1 and Z_2 , the axis of the breakup being isotropically distributed and the relative velocity between the fragments ranging from 0 cm/ns to 10 cm/ns. For each case, the event is taken into account in this analysis if both fragments have a V_z greater than $V_{c.m.}$. The velocities \vec{V}_1 and \vec{V}_2 of the two fragments are calculated the following way:

$$\vec{V}_{1} = \vec{V}_{QP} + \left(1 - \frac{Z_{1}}{Z_{QP}}\right)\vec{V}_{rel},$$
(4)



FIG. 26. First column: simulation of the accessible range of V_{rel} as a function of $\cos(\theta_{prox})$ for the Ta+Au system at 39.6A MeV and for $M_{imf}=2$. The two other columns display the correlation between V_{rel} and $\cos(\theta_{prox})$ for two different systems. See text for more details.

$$\vec{V}_{2} = \vec{V}_{QP} - \frac{Z_{1}}{Z_{OP}} \vec{V}_{rel}.$$
(5)

The first column of Fig. 26 corresponds to the result of the simulation; the second column shows the experimental bidimensional plots of V_{rel} versus $\cos(\theta_{prox})$ for the Ta + Au collisions at 39.6A MeV; the third column shows the same plots for the U + C collisions at 24A MeV ($\theta_{OP} < 10^{\circ}$). The plots corresponding to events with an IMF multiplicity equal to 2 are displayed. The rows correspond to different selections on the charge of the heaviest fragment Z_1 , the uppermost row corresponding to the lowest Z_1 values and the lowermost row to the highest Z_1 values. For each plot of the simulation (leftmost column), the values of V_{QP} , θ_{QP} , and the ratio Z_1/Z_{OP} have been chosen according to the average experimental values for the Ta+Au collisions at 39.6A MeV for a given IMF multiplicity and for a fixed Z_1 range. The shaded areas (leftmost column) correspond to the events selected in our analysis. One can see that the velocity cut (V_z) $>V_{c.m.}$) systematically removes the events with the highest V_{rel} values when the fragmentation axis is aligned on the QP velocity direction. For $\cos(\theta_{prox})=1$, this effect is always present. This could explain the decrease of V_{rel} for high $\cos(\theta_{prox})$ values observed in Figs. 23 and 24. This is confirmed by the bidimensional plot (second column) which was used to obtain Fig. 23. The effect of the velocity cut is clearly seen for the highest Z_1 values. The agreement between data and simulation is good, showing that the velocity cut limits the range of accessible V_{rel} values. For higher M_{imf} values, similar conclusions are obtained. Another interesting observation is that the V_{rel} distribution for $\cos(\theta_{prox})$ ≈ -1 is narrow, its average value $V_{rel} = 2.3$ cm/ns corresponds to the Viola systematics [28] and is not affected by the velocity cut at $V_{c.m.}$. When $\cos(\theta_{prox})$ increases, the width of the V_{rel} distribution and its average value increase while the velocity cut has no influence, i.e., for $\cos(\theta_{prox})$ values below 0.8. Above $\cos(\theta_{prox}) = 0.8$, high values of V_{rel} cannot be reached and then its average value decreases. For the U+C system rightmost column, it can be seen that the V_{rel} distributions are always narrow and centered around the Viola systematics value whatever the $\cos(\theta_{prox})$ value. For these collisions, our experimental cut does not affect the evolutions of V_{rel} with $\cos(\theta_{prox})$.

The observations made in this section confirm the scenario proposed in the preceding section. For the U+C system, all observations are compatible with the decay of a fully equilibrated nucleus: no modulation of V_{rel} with $\cos(\theta_{prox})$ is seen while at the same time the "hierarchy effect" is absent or very weak. For the systems with a heavy target, the variation of V_{rel} with $\cos(\theta_{prox})$ is observed. This indicates that a strongly deformed QP or a neck of matter is formed at the early stage of the collision, and breaks quickly into several fragments. In such a process, the incident kinetic energy is not fully damped, and the fragments keep the memory of the formation of the neck and/or deformed QP. Within this interpretation, the heaviest fragment is a remnant of the projectile. This scenario seems to occur for a wide range of system sizes and incident energies. For the heaviest systems, such as U+U for which the fissility of the QP is high, it competes with the fission process.

V. CONCLUSIONS

The study of the parallel velocity distributions of the fragments forward emitted as a function of their charge exhibits a "hierarchy effect": the ranking in charge induces in average a ranking in the average parallel velocity, the heaviest fragment is the fastest and is focused in the forward direction relative to the QP recoil velocity. This "hierarchy effect" is stronger when the size of the target is large, when the fissility of the QP is limited (Z < 80) and when the incident energy is high. This effect is observed for all systems, whatever the multiplicity of fragments. These observations are compatible with the formation of a neck of matter in-between the quasiprojectile and the quasitarget. The neck may or may not be attached to the QP (or QT) remnant. In any case, its breakup is fast enough to keep the memory of the entrance channel.

This mechanism is predominant for asymmetric breakups that mainly correspond to peripheral collisions. For the most peripheral collisions, the asymmetry observed for the binary breakups is not compatible with the result of a standard fission, and for the highest multiplicities, the high focusing of the heaviest fragment at forward angles is inconsistent with the fragmentation of a fully equilibrated nucleus.

The observed variation of the fragments relative velocity with the emission angle of the heaviest fragment strengthens the previous statement. This internal correlation study is a powerful tool to clearly establish the degree of equilibration of the studied ensemble. Up to now, the comparisons of models to data were mainly made on global observations only (size distributions, multiplicity distributions, kinetic energy distributions, and so on). The study of such internal correlations is a more accurate tool to test the pertinence of the models.

In order to have a full understanding of the fragmentation process, the models have to reproduce the effects of the entrance channel. A first step could be to mock up these effects in effective parameters in the statistical decay approaches. It will be certainly worth to use dynamical approaches [15,32–39] to test the presence of such a hierarchy effect. But in all cases, the models have to reproduce the global observations and the internal correlations as well.

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