

## Mixed-symmetry strength in $^{114}\text{Cd}$

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Properties of low-spin states in  $^{114}\text{Cd}$  have been studied with the  $(n, n' \gamma)$  reaction.  $\gamma$ -ray angular distributions and excitation functions have been used to characterize the decays of the excited levels, and level lifetimes have been obtained with the Doppler-shift attenuation method. The one-phonon, mixed-symmetry strength is found to be concentrated in the  $2_6^+$  state, which exhibits a strong  $M1$  transition to the first-excited  $2^+$  state and a weak  $E2$  transition to the ground state. The data agree well with expectations of the neutron-proton interacting boson model.

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### I. INTRODUCTION

In the framework of the interacting boson model [1,2], phonon excitations can be described by boson wave functions, and multiphonon excitations are described in this model as a result of the coupling between these wave functions. In the basic interacting boson model (IBM-1) [3,4], the neutron and proton bosons are not distinguishable; hence their boson wave functions are symmetric with regard to the exchange of protons and neutrons, resulting in fully symmetric states. The neutron-proton version of the interacting boson model (IBM-2) [5–7] treats the states in which neutron and proton bosons are distinguishable. Nonsymmetric or mixed-symmetry (MS) states are those with less than maximum neutron-proton symmetry. In IBM-2, nuclear states are characterized by the  $F$  spin, which is the isospin for proton and neutron bosons. By coupling the collective proton and neutron degrees of freedom in a nucleus with  $N_\pi$  proton pairs and  $N_\nu$  neutron pairs, the  $F$  spin assumes values from  $F_{max} = (N_\pi + N_\nu)/2$  to  $F_{min} = (N_\pi - N_\nu)/2$ . The fully symmetric states have maximum  $F$  spin, i.e.,  $F = F_{max}$ , while MS states are those with  $F < F_{max}$ . The IBM-2 predicts enhanced  $M1$  transitions between the MS states with  $F = F_{max} - 1$  and symmetric states with  $F = F_{max}$  and the same number of phonons, with matrix elements of the order of  $1 \mu_N$ . In addition, the IBM-2 predicts weakly collective  $E2$  transitions between the symmetric and mixed-symmetric states following the phonon selection rule  $\Delta N_{ph} = 1$ .

A well-known example of a mixed-symmetry state is the  $1^+$  scissors mode, which was first experimentally observed by Bohle *et al.* [8], who discovered a relatively large magnetic dipole strength in  $^{156}\text{Gd}$  at about 3 MeV. Since then, this mode has been identified in a wide range of deformed nuclei, primarily in the rare-earth region, and the behavior of the  $1^+$  scissors mode is now well characterized [9–14].

In nearly spherical nuclei, the fundamental one-phonon  $2^+$  MS state, from which the scissors mode arises, is expected to lie somewhat lower in energy [6]. In recent measurements, the  $2^+$  MS states have been identified in the

$N=52$  isotones  $^{92}\text{Zr}$ ,  $^{94}\text{Mo}$ , and  $^{96}\text{Ru}$  [15–21]. Moreover, the  $1^+$ ,  $2^+$ , and  $3^+$  MS two-phonon states resulting from the coupling of the MS phonon and the symmetric quadrupole excitation were clearly identified in  $^{94}\text{Mo}$  [15,16,21]. This extensive new information is a strong motivation for identifying MS states in other mass regions and exploring the systematic behavior of these excitations.

Several years ago, Garrett *et al.* [22] identified  $2^+$  states at 2156 and 2231 keV in  $^{112}\text{Cd}$ , a nucleus well represented in a U(5) description of the IBM-1. These two  $2^+$  levels share the MS strength nearly equally; however, additional examples of MS states in this mass region have not been evident. With the goal of identifying the mixed-symmetry strength in  $^{114}\text{Cd}$ , we have investigated the low-spin states in this nucleus with the  $(n, n' \gamma)$  reaction.

The low-lying states in  $^{114}\text{Cd}$  have been studied previously with a variety of different probes, and the spins and parities of these states are generally well characterized [23–26]. For some time, this nucleus has been regarded as exhibiting a multiphonon U(5) vibrational structure, coexisting with intruder excitations at low excitation energy [26–32]. Giannatiempo *et al.* [33] have analyzed the low-lying collective states of  $^{110,112,114}\text{Cd}$  nuclei in the framework of IBM-2 to identify the  $2^+$  mixed-symmetry states in these nuclei. They suggested the  $2_3^+$  state at 1364 keV in  $^{114}\text{Cd}$  as a pure one-phonon mixed-symmetry state; however, this state seems to be significantly lower in energy than expected in nearly spherical nuclei [6]. Moreover, this state, which has been studied extensively [26], is generally regarded as having an intruder structure [31]. This apparent ambiguity motivated us to search again for the lowest MS state in  $^{114}\text{Cd}$ .

### II. EXPERIMENTAL DETAILS AND RESULTS

Low-lying states of  $^{114}\text{Cd}$  have been studied at the University of Kentucky 7-MV accelerator facility through the inelastic scattering of fast neutrons. A pulsed proton beam (pulse width  $\sim 1$  ns, frequency  $\sim 2$  MHz) with a beam current of about  $2 \mu\text{A}$  was passed through a cylindrical gas cell with a length of 3.0 cm and a diameter of 1.0 cm, filled with tritium gas at nearly 1 atm pressure. A molybdenum foil with a thickness of  $8 \mu\text{m}$  served as a window to the gas cell. Monoenergetic neutrons with an energy spread of about 60

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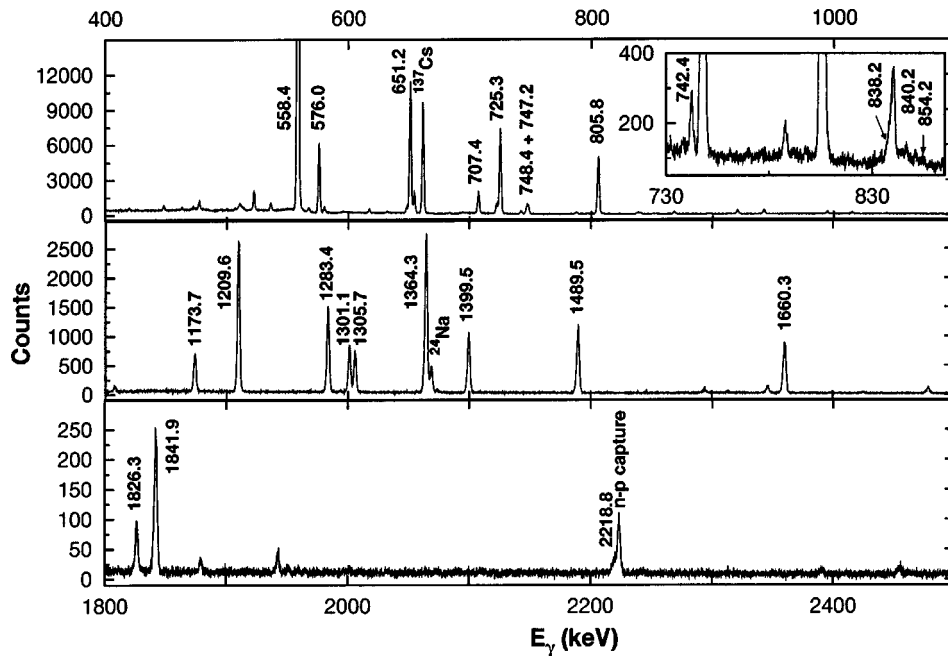


FIG. 1.  $\gamma$ -ray spectrum obtained in the  $^{114}\text{Cd}(n,n'\gamma)$  reaction at a neutron energy of 2.5 MeV and at a detection angle of  $90^\circ$ . Peaks labeled with energies in keV are from  $^{114}\text{Cd}$ .

keV were produced through the  $^3\text{H}(p,n)^3\text{He}$  reaction. The scattering sample, 13 pieces of metallic  $^{114}\text{Cd}$  (isotopic enrichment 98.55%) totaling 47.835 g, was arranged within a cylindrical polyethylene container 1.8 cm in diameter and 3.6 cm in height. This sample was suspended in the neutron flux at a distance of 5 cm from the end of the gas cell.

The  $\gamma$  rays emitted in the  $^{114}\text{Cd}(n,n'\gamma)$  reaction were recorded with a Compton-suppressed HPGe detector with a relative efficiency of 55%, compared to that of a  $7.6 \times 7.6 \text{ cm}^2$  NaI detector. An annular BGO shield was used for Compton suppression. The HPGe and BGO detectors were at a distance of 115 cm from the scattering sample, and were further shielded by boron-loaded polyethylene, copper, and tungsten. Time-of-flight gating was implemented to suppress background radiation and improve the quality of the spectra. The neutron flux was monitored by a  $\text{BF}_3$  proportional counter fixed at  $90^\circ$  relative to the axis of the incident beam and at a distance of 3.78 m from the gas cell. The neutron flux was further monitored by observing the time-of-flight spectra of neutrons in a fast liquid scintillator (NE218) at an angle of  $43^\circ$  relative to the incident beam axis and at a distance of 5.9 m from the gas cell. Energy and efficiency calibrations of the HPGe detector were performed with a  $^{226}\text{Ra}$  radioactive source. More detailed descriptions of the experimental setup may be found elsewhere [34,35].

The  $\gamma$ -ray excitation functions of the levels in  $^{114}\text{Cd}$  were measured over the range of neutron energies from 1.9 to 3.8 MeV in 0.1-MeV steps. To study the angular distributions of  $\gamma$  rays emitted in the  $^{114}\text{Cd}(n,n'\gamma)$  reaction, spectra were recorded at 11 different angles from  $40^\circ$  to  $150^\circ$  with respect to the incident 2.5-MeV neutrons. In these experiments, the energy calibration of the HPGe detector was continuously monitored with the 661.6-, 1368.6-, and 2754.0-keV  $\gamma$  rays

from  $^{137}\text{Cs}$  and  $^{24}\text{Na}$  radioactive sources. Figure 1 shows a typical spectrum of the  $\gamma$  rays obtained at an angle of  $90^\circ$  with 2.5-MeV neutrons. The 1660.3-keV transition from the  $2_6^+$  state at 2218.8 keV to the  $2_1^+$  state at 558.4 keV is clearly visible. We have also observed a new transition from this state to the ground state. This 2218.8-keV transition is weak and, unfortunately, appears as a doublet with the 2223.3-keV background  $\gamma$  ray from the  $n$ - $p$  capture reaction. We have studied the shape of this doublet with changes in energy and angle, and found that this  $\gamma$  ray exhibits the expected energy threshold. Moreover, the peak position of the 2218.8-keV  $\gamma$  ray shifts in energy with angle, whereas that of the 2223.3-keV line does not. We have also observed a weak (compared to the 1660.3-keV transition) 854.2-keV transition from the  $2_6^+$  level to the intruder  $2_3^+$  state at 1364.3 keV. Additional, much weaker decay transitions from this level, which are listed in the data compilation [36], were not observed.

The angular distributions of the  $\gamma$  rays were fit to even-order Legendre polynomial expansions, and compared to theoretical predictions calculated with the code CINDY [37] to determine the multipolarities of the decay transitions. The angular distributions of the 1660.3- and 2218.8-keV  $\gamma$  rays emitted from the 2218.8-keV level are shown in Fig. 2. Comparisons with CINDY calculations support the spin assignment of the level as  $J=2$ . Because of the fast ground-state transition, we can also confirm positive parity for this level. This  $2^+$  assignment is in agreement with the  $(n,\gamma)$  work by Mheemeeed *et al.* [23]. Similarly, the angular distributions of the 838.2- and 1489.5-keV transitions from the 2047.9-keV level support a  $J=2$  assignment, and the fast transition from this level to the  $0_3^+$  state indicates positive parity. The values of the  $E2/M1$  mixing ratios  $\delta$  and the branching ratios of the

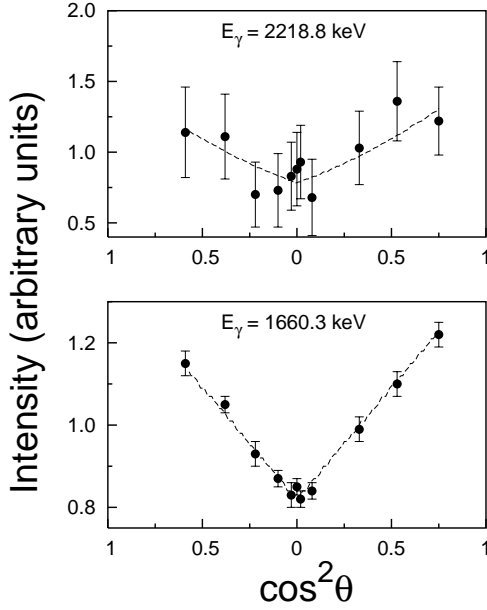


FIG. 2. Angular distributions of the 1660.3- and 2218.8-keV  $\gamma$  rays observed in the  $^{114}\text{Cd}(n,n'\gamma)$  reaction at a neutron energy of 2.5 MeV.

relevant transitions are given in Table I.

Lifetimes of the low-lying excited states have been extracted from the angular distribution data by considering the Doppler shifts of the  $\gamma$  rays with change in the angle. The position of the centroid of the  $\gamma$ -ray peak,  $E_\gamma(\theta)$ , at an emission angle  $\theta$  relative to the incident neutrons can be described [38] as

$$E_\gamma(\theta) = E_0 \left( 1 + F(\tau) \frac{v_{\text{c.m.}}}{c} \cos \theta \right), \quad (1)$$

where  $E_0$  is the unshifted  $\gamma$ -ray energy and  $F(\tau)$  is the Doppler-shift attenuation factor. At 2.5 MeV neutron energy, the velocity of the recoiling nucleus in the center-of-mass frame is  $v_{\text{c.m.}} = (6.37 \times 10^{-4})c$ . The observed energies of the

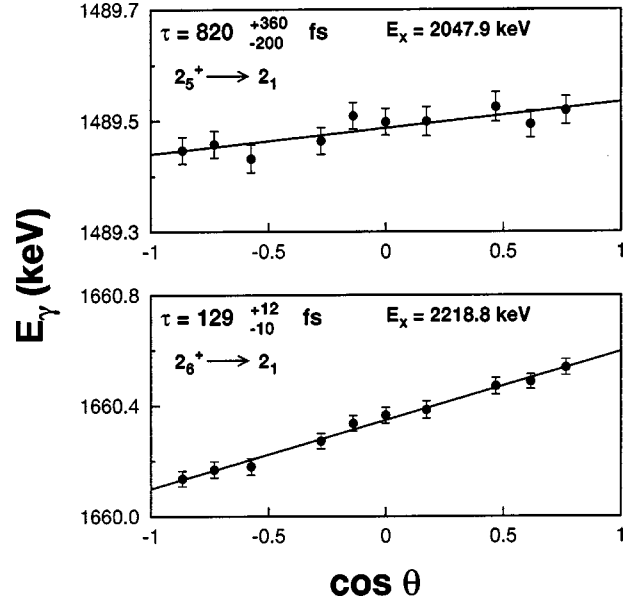


FIG. 3. Shift in  $\gamma$ -ray energies as a function of  $\cos \theta$  for the indicated transitions. The lines are linear fits to the data, from which the  $F(\tau)$  values have been extracted.

1489.5- and 1660.3-keV  $\gamma$  rays as a function of the emission angle are shown in Fig. 3. The straight lines indicate the fits to the experimental data from which the  $F(\tau)$  values have been determined. Lifetimes can be obtained by a comparison of the experimental  $F(\tau)$  values of Fig. 3 with those calculated following the nuclear stopping theory of Winterbon [39,40]. The level lifetimes obtained are summarized in Table II. Casten *et al.* [26] obtained lifetimes for the  $2_5^+$  and  $2_6^+$  levels by the  $\gamma$ -ray induced Doppler-broadening technique. A comparison of our more precise results with their earlier measurements shows good agreement.

### III. DISCUSSION

The lifetimes of all the observed  $2^+$  states up to 2.5 MeV are presented in Table II. As the lowest four  $2^+$  levels are too

TABLE I. Properties of selected transitions in  $^{114}\text{Cd}$ .

$J_i^\pi$	$J_f^\pi$	$E_\gamma$ (keV)	B.R.	$\delta(J_i^\pi \rightarrow J_f^\pi)$	$B(M1)$ $\mu_N^2$	$B(E2)$ (W.u.)
$2_5^+$	$0_3^+$	742.4(1)	$0.075 \pm 0.002$	$E2$		$10.0^{+3.3}_{-3.0}$
	$2_2^+$	838.2(1)	$0.041 \pm 0.003$	$2.4^{+3.3}_{-1.2}$	$\leq 0.003$	$2.6^{+1.6}_{-1.4}$
				$0.00^{+0.29}_{-0.24}$	$0.005^{+0.002}_{-0.002}$	$3.0^{+1.2}_{-3.0}$
	$2_1^+$	1489.5(1)	$0.884 \pm 0.003$	$-0.32^{+0.03}_{-0.02}$ <sup>a</sup>	$0.017^{+0.005}_{-0.005}$	$0.34^{+0.17}_{-0.14}$
$2_6^+$	$2_3^+$	854.2(3)	$0.009 \pm 0.001$	$10.0^{+5.0}_{-0.9}$		$3.6^{+1.2}_{-1.1}$
				$0.64^{+1.05}_{-0.53}$	$0.005^{+0.003}_{-0.003}$	$1.1^{+2.3}_{-1.1}$
	$2_1^+$	1660.3(1)	$0.961 \pm 0.002$	$0.19^{+0.04}_{-0.05}$ <sup>a</sup>	$0.089^{+0.009}_{-0.009}$	$0.50^{+0.26}_{-0.24}$
				$1.50^{+0.11}_{-0.10}$	$0.028^{+0.005}_{-0.005}$	$10.2^{+1.3}_{-1.3}$
$0_1^+$	2218.8(2)	$0.030 \pm 0.002$	$E2$		$0.107^{+0.017}_{-0.017}$	

<sup>a</sup>Accepted values for  $\delta$ .

TABLE II. Lifetimes of the low-lying  $2^+$  states in  $^{114}\text{Cd}$ .

$J_i^\pi$	$E_x$ (keV)	$\tau$ (fs)
$2_1^+$	558.4(1)	14700(900) <sup>a</sup>
$2_2^+$	1209.7(1)	4500(400) <sup>a</sup>
$2_3^+$	1364.3(1)	7500(600) <sup>a</sup>
$2_4^+$	1841.9(1)	940(170) <sup>a</sup>
$2_5^+$	2047.9(1)	$820_{-200}^{+360}$ <sup>b</sup>
$2_6^+$	2218.8(1)	$129_{-10}^{+12}$ <sup>b</sup>

<sup>a</sup>Reference [36].<sup>b</sup>Present measurement.

long lived to be measured by the Doppler-shift attenuation technique, we obtained only lower limits for their lifetimes. Therefore, the values for these levels listed in the table are taken from Ref. [36]. Moreover, these lowest  $2^+$  levels have been well established as either vibrational phonon or intruder states [26]. We have examined two  $2^+$  levels as possible mixed-symmetry states. These states are well within the energy range 1.7–2.7 MeV, expected from IBM-2 calculations for  $2^+$  MS states [6].

Transitions to the  $2_1^+$  state have been observed from the  $2_5^+$  and  $2_6^+$  levels at 2047.9 and 2218.8 keV, respectively. As noted earlier, we have observed the ground-state transition from the  $2_6^+$  level, but we do not observe the  $2_5^+$  ground-state transition reported earlier [36]. The primary decay of the  $2_5^+$  level is the 1489.5-keV transition. In addition, another weak transition of 838.2 keV from the  $2_5^+$  level has been observed in this study. Considering the 1489.5-keV transition as the strongest from the  $2_5^+$  level, and as representing 100% intensity, we have calculated the sensitivity limit of our detection system and have found that we could have observed a transition directly to the ground state with a peak intensity as low as 1.4%. This intensity limit is significantly below the value of 7.6% reported in Ref. [36]. Interestingly, we have observed a 2047.8-keV transition with a threshold around  $3250 \pm 50$  keV in the excitation function measurements. Hence we conclude that the 2047.8-keV transition is a decay from a level above 3 MeV.

Transition strengths of several levels have been calculated from the level lifetimes, the branching ratios, and the  $E2/M1$  multipole mixing ratios  $\delta$  of the  $\gamma$  rays. Table I displays the information obtained in our experiments and used in the calculation of transition strengths. Unfortunately, the angular distribution data for the 1489.5- and 1660.3-keV transitions

exhibit two solutions for  $\delta$ , with more or less equal  $\chi$ -squared fits to the statistical model calculations [37]. We compare our results with those from previous work (see Table III). We should note that our values are generally in excellent agreement with those obtained by Demidov and co-workers [41,42] from  $(n, n' \gamma)$  measurements with reactor fast neutrons. They also experienced a similar ambiguity in selecting unique values of the mixing ratios for the 1660.3-keV transition. In  $\gamma$ - $\gamma$  directional correlation measurements following the  $(n, \gamma)$  reaction, Hungerford and Hamilton [43] have determined the mixing ratios of the 1489.5- and 1660.3-keV transitions. By combining these values with the internal conversion coefficients measured by Mheemed *et al.* [23], Hungerford and Hamilton determined the  $E2$  contributions of these transitions to be between 0.7% and 44% for the 1489.5-keV transition, and  $(24 \pm 21)\%$  for the 1660.3-keV transition. Clearly, these data strongly support our choice of the smaller value of  $\delta$  in each case. Accepting our lower values of  $\delta$ 's, we calculate the  $M1$  transition strengths to be  $B(M1; 2_5^+ \rightarrow 2_1^+) = (0.017 \pm 0.005) \mu_N^2$  and  $B(M1; 2_6^+ \rightarrow 2_1^+) = (0.089 \pm 0.009) \mu_N^2$ , respectively.

Figure 4 displays the partial level scheme relevant to this work; it appears quite similar to that observed in  $^{112}\text{Cd}$  [22]. It is clear that for both the  $2_5^+$  and  $2_6^+$  states, the largest decay branches are predominantly  $M1$  transitions to the  $2_1^+$  state. But both levels also decay to intruder states. The  $B(E2)$  value of  $10.0_{-3.0}^{+3.3}$  W.u. for the transition from the  $2_5^+$  state to the intruder  $0_3^+$  state suggests the presence of a sizable intruder component in the wave function of the  $2_5^+$  state. This value is in reasonable agreement with the accepted value of  $17 \pm 5$  W.u. [36]; however, since the angular distribution was measured at 2.5 MeV incident neutron energy, it was not affected by contributions from the 742.9-keV  $\gamma$  ray, known to arise from a state at 2701 keV [23]. The 838.2-keV  $\gamma$  ray forms a doublet with the strong 840.2-keV transition from the 2204.5-keV level, and the 854.2-keV  $\gamma$ -ray peak is small. Hence, it is difficult to obtain precise values of  $\delta$  in these cases.

According to the IBM-2 for nuclei in the U(5) limit, the  $M1$  transition strength from the one-phonon  $2^+$  MS state ( $2_{1,ms}^+$ ) to the one-phonon fully symmetric ( $2_1^+$ ) state can be calculated [44] as

$$B(M1; 2_{1,ms}^+ \rightarrow 2_1^+) = \frac{3}{4\pi} (g_\nu - g_\pi)^2 6 \frac{N_\nu N_\pi}{N^2} \mu_N^2. \quad (2)$$

TABLE III. Comparison of results for  $E2/M1$  mixing ratio from different experiments.

$E_\gamma$ (keV)	$\delta$ (Present work)	$\delta^a$ ( $n, n' \gamma$ )	$\delta^b$ ( $n, \gamma$ )
1489.5 (1)	$-0.32_{-0.02}^{+0.03}$ , <sup>c</sup> $10.0_{-0.9}^{+5.0}$	$-0.29_{-0.05}^{+0.05}$	$-0.90 \leq \delta \leq -0.09$
1660.3 (1)	$0.19_{-0.05}^{+0.04}$ , <sup>c</sup> $1.50_{-0.10}^{+0.11}$	$0.17_{-0.06}^{+0.06}$ , $1.5_{-0.2}^{+0.2}$	$0.56_{-0.20}^{+0.34}$

<sup>a</sup>References [41,42].<sup>b</sup>Reference [43].<sup>c</sup>Accepted values for  $\delta$ .



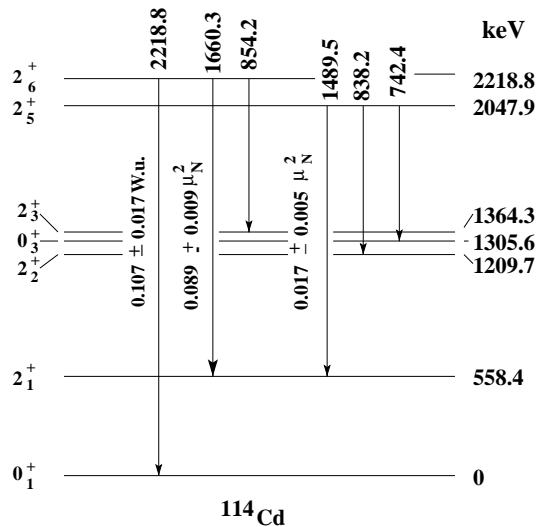


FIG. 4. Partial level scheme of  $^{114}\text{Cd}$  relevant to this work.  $E2$  strength is given in W.u.;  $M1$  strengths are in  $\mu_N^2$ . Transition and level energies are in keV.

Considering  $^{100}\text{Sn}$  as the inert core, the neutron and proton boson numbers are  $N_\nu=8$  and  $N_\pi=1$ . With standard boson  $g$  factors,  $g_\nu=0$  and  $g_\pi=1$ , the calculated value for  $^{114}\text{Cd}$  is  $B(M1; 2_{1,ms}^+ \rightarrow 2_1^+) = 0.14\mu_N^2$ . As noted earlier, the experimentally observed  $B(M1)$  strengths of the transitions from the  $2_5^+$  and  $2_6^+$  levels to the first-excited state are  $(0.017 \pm 0.005)\mu_N^2$  and  $(0.089 \pm 0.009)\mu_N^2$ , respectively. Hence, it can be concluded that the mixed-symmetry strength in  $^{114}\text{Cd}$  is fragmented between the  $2_5^+$  and  $2_6^+$  levels at 2047.9 and 2218.8 keV in  $^{114}\text{Cd}$ . If we sum these transition strengths, the measured  $B(M1)$  from the one-phonon mixed-symmetry state to the first-excited state is  $(0.106 \pm 0.010)\mu_N^2$ . This approaches the value predicted by the IBM-2, and is comparable to that observed in  $^{112}\text{Cd}$ ,  $0.099\mu_N^2$ . However, most of the mixed-symmetry strength in

$^{114}\text{Cd}$  is concentrated in a single state, the 2218.8-keV level. This behavior is in contrast with  $^{112}\text{Cd}$ , where the strength is shared nearly equally between the states at 2156 and 2231 keV.

The ground-state transition of the 2218.8-keV level has a  $B(E2)$  of only  $0.107 \pm 0.017$  W.u. While this value is much smaller than, for example, the  $B(E2)$  values of the ground-state transitions in the  $N=52$  isotones, it is similar to that observed in  $^{112}\text{Cd}$ .

#### IV. SUMMARY AND CONCLUSIONS

Inelastic neutron scattering experiments have been performed on  $^{114}\text{Cd}$  to identify the lowest mixed-symmetry state in this nucleus. The properties of the  $2^+$  states around 2 MeV have been examined through  $\gamma$ -ray angular distribution and excitation function measurements, and the Doppler-shift attenuation method has been employed to determine the lifetimes of these states. The  $2_5^+$  state at 2047.9 keV and the  $2_6^+$  state at 2218.8 keV have been found as the main fragments of the one-phonon mixed-symmetry state, with most of the strength concentrated in the latter. The  $M1$  transitions from these levels to the  $2_1^+$  state indicate that these states are the largest fragments of the one-phonon mixed-symmetry state originating from the isovector quadrupole excitations in the valence shells of  $^{114}\text{Cd}$ . The energies of these states are very similar to those observed for MS states in  $^{112}\text{Cd}$ . Strong  $E2$  transitions from the  $2_5^+$  level to the intruder state are indicative of mixing of intruder components in the wave function of this level.

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