Structure of neutron-rich nuclei around ¹³²Sn

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Recent studies have provided new experimental information on neutron-rich nuclei around doubly magic 132 Sn. We have performed shell-model calculations for the two- and three-proton N=82 isotones 134 Te and 135 I using a realistic effective interaction derived from the Bonn A nucleon-nucleon potential. The results are in remarkably good agreement with the experimental data evidencing the reliability of our realistic effective interaction. [S0556-2813(97)50407-9]

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The N=82 region has long come in focus for shell-model studies of nuclear structure. The ¹³²Sn nucleus shows, in fact, strong shell closures for both protons and neutrons. In addition, a long string of nuclei is built by adding protons to the doubly closed core.

From the experimental point of view, the naturally stable nuclei in this region have been extensively investigated and a large amount of experimental data is available for them. On the other hand, the neutron-rich nuclei, with few valence protons, lie well away from the valley of stability and until now experimental information, especially for ¹³⁴Te and ¹³⁵I, was very scanty. The properties of these nuclei are of special interest for a stringent test of the basic ingredients of a shell-model calculation, as they represent a direct source of knowledge of the effective proton-proton interaction in this region. Recently, use of large multidetector γ -ray arrays with high analyzing power has made accessible the study of these nuclei. In particular two recent studies [1,2] have led to new experimental data for ¹³⁴Te and ¹³⁵I.

In Ref. [1] the level scheme of ¹³⁴Te has been extended up to about 4.6 MeV excitation energy. All the states arising from the $\pi g_{7/2}^2$ and $\pi g_{7/2} d_{5/2}$ configurations, except the 3⁺, have been observed below 3 MeV, while five negative-parity states, belonging to the $\pi g_{7/2} h_{11/2}$ configuration, have been identified between 4.0 and 4.6 MeV. The experiment of Ref. [2] has also revealed seven positive-parity levels lying between 4.56 and 7.56 MeV, which have been interpreted as excitations of the ¹³²Sn core. Regarding ¹³⁵I, five new states, three of them with nega-

Regarding ¹³⁵I, five new states, three of them with negative parity, have been identified [2] below 3.8 MeV. However, no information about transition multipolarities was obtained and spin-parity assignments were based in part on theoretical considerations. As in the case of ¹³⁴Te, the observed levels above 4.2 MeV have been interpreted as neutron particle-hole states.

In this paper, we present the results of a shell-model study of ¹³⁴Te and ¹³⁵I, in which we assume that ¹³²Sn is a closed core and let the valence protons occupy the five single-particle (s.p.) orbits $0g_{7/2}$, $1d_{5/2}$, $1d_{3/2}$, $2s_{1/2}$, and $0h_{11/2}$. As regards the energy spacings between the five s.p. levels, we take three of them from the experimental spectrum of ¹³³Sb [3]. In fact, the $g_{7/2}$, $d_{5/2}$, $d_{3/2}$, and $h_{11/2}$ states can be

associated with the ground state and the 0.962, 2.708, and 2.793 MeV excited levels, respectively. As for the $s_{1/2}$ state, its position has been determined by reproducing the experimental energy of the $\frac{1}{2}$ ⁺ state at 2.150 MeV in ¹³⁷Cs, which is predominantly of s.p. nature, as indicated by the experimental one-proton spectroscopic factor [4]. This yields the value $\epsilon_{s_{1/2}}$ = 2.8 MeV, which comes close to that obtained from the empirical analysis of Ref. [5] (2.99 MeV).

In our study we make use of a realistic effective interaction derived from the Bonn A free nucleon-nucleon potential. Our effective interaction was obtained using a *G*-matrix folded-diagram formalism, including renormalizations from both core polarization and folded diagrams. For the N=82isotones we have chosen the Pauli exclusion operator Q_2 in the *G*-matrix equation,

$$G(\omega) = V + VQ_2 \frac{1}{\omega - Q_2 TQ_2} Q_2 G(\omega), \qquad (1)$$

as specified by $(n_1, n_2, n_3) = (11, 28, 45)$ [6]. Here *V* represents the *NN* potential, *T* denotes the two-nucleon kinetic energy, and ω is the so-called starting energy. We employ a matrix inversion method to calculate the above *G* matrix in an essentially exact way [6]. The effective interaction V_{eff} , which is energy independent, can be schematically written in operator form as

$$V_{\rm eff} = \hat{Q} - \hat{Q}' \int \hat{Q} + \hat{Q}' \int \hat{Q} \int \hat{Q} - \hat{Q}' \int \hat{Q} \int \hat{Q} \int \hat{Q} \cdots,$$
(2)

where \hat{Q} and \hat{Q}' represent the \hat{Q} box, composed of irreducible valence-linked diagrams, and the integral sign represents a generalized folding operation. We take the \hat{Q} box to be composed of *G*-matrix diagrams through second order in *G*; they are just the seven first- and second-order diagrams considered by Shurpin *et al.* [7]. Since the valence-proton and -neutron orbits outside the ¹³²Sn core are different, in the present calculation we use an isospin uncoupled representation, where protons and neutrons are treated separately. The shell-model oscillator parameter used by us is $\hbar \omega = 7.72$ MeV. A detailed description of our derivation including more references can be found in Ref. [8].

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FIG. 1. Experimental and calculated spectrum of ¹³⁴Te.

To our knowledge, these are the first realistic shell-model calculations for N=82 nuclei. To date, the most complete shell-model calculations are those of Ref. [5] which were carried out in the same model space employing a semirealistic interaction (a bare reaction matrix of the Reid soft core potential plus phenomenological corrections). In an earlier work [9], use was made of the modified surface delta interaction in a restricted model space. The new experimental results [1,2] offer a unique opportunity to test directly the matrix elements of our calculated realistic effective interaction.

The experimental [1,10] and theoretical spectra of 134 Te are compared in Fig. 1, where all the calculated and experimental levels up to 3.2 MeV excitation energy are reported. We see that while the theory reproduces all the observed levels, it also predicts the existence of a 3⁺ and a 0⁺ state at 2.51 and 2.65 MeV, respectively. This prediction is strongly supported by the experimental information available for the two heavier even isotones. In fact, in 136 Xe a 0⁺ state has been observed at 2.56 MeV, while in 138 Ba both a 0⁺ and a 3⁺ state have been located at 2.34 and 2.45 MeV, respectively. Above 3.2 MeV excitation energy the comparison between theory and experiment is made only for those ob-

served levels which have received a spin-parity assignment. We do not include the new levels observed in [2] since, as already mentioned, all of them should be interpreted as neutron particle-hole states. This interpretation is confirmed by our calculations. In fact, the only two states, having J^{π} $=8^+$ and 10^+ , which can be constructed in our model space are both predicted to lie at about 7.1 MeV, while the two experimental states with these spin-parity assignments have been located at 4.557 and 5.622 MeV, respectively [2]. We see that the calculated spectrum reproduces very well the experimental one, the discrepancies between theory and experiment being smaller than 100 keV for the excitation energies of several states. A measure of the quality of the results is given by the rms deviation σ [11], whose value is 145 keV. It should be noted that all the calculated states lie below the experimental ones, the only exception being the 2_3^+ state. The experimental level at 2.934 MeV excitation energy was, however, only tentatively identified as a 2⁺ state [12] and is not reported in [1]. It turns out that a downshift of 100 keV of the calculated ground state brings σ down to 100 keV and to only 60 keV if we exclude the 2^+_3 state.

As regards the structure of the states, we find that the three groups of states reported in Fig. 1 (the first one up to 1.7 MeV, the second between 2.2 and 3.2 MeV, and the third above 3.8 MeV) are dominated by the $g_{7/2}^2$, $g_{7/2}d_{5/2}$, and $g_{7/2}h_{11/2}$ configurations, respectively. Of course, this is not true for the 0_2^+ , 2_3^+ , and 5_2^+ states. In fact, the dominant configuration is $d_{5/2}^2$ for the two former states and $g_{7/2}d_{3/2}$ for the latter. Our results substantiate the interpretation given in [2] of the nature of the levels in ¹³⁴Te. It should be mentioned, however, that our wave functions are not really pure, as assumed in [2], the contribution coming from other configurations being particularly significant for the ground state, for which the percentage of configurations other than $g_{7/2}^2$ is 17%.

In Fig. 2 we compare the calculated spectrum of ¹³⁵I with the experimental one [2,13] up to 4.0 MeV excitation energy. As in the case of 134 Te, we exclude the experimental levels above 4.2 MeV, which originate from core excitations. We should note that the spectra of Fig. 2 include all experimental and calculated levels up to 1.5 MeV. The experimental level at 1.184 MeV has been observed in a ¹³⁵Te β^- -decay study [14] and the most likely spin-parity assignment is $\frac{9}{2}^+$. Our results strongly favor this assignment. Above 1.5 MeV several other levels without assigned spin and parity are reported in [13]; we compare our calculated states only with those observed in [2]. From Fig. 2 we see that the excitation energies are remarkably well reproduced for all the reported states, the σ value being 77 keV. We have associated the experimental level at 1.010 MeV with the theoretical $\frac{3}{2}^+$ at 0.931 MeV.

From the structure of our wave functions, it turns out that the states up to 1.5 MeV excitation energy, but the first $\frac{5}{2}^+$ state, can be identified as the members of the $g_{7/2}^3$ multiplet. These states are, however less pure than those of 134 Te. The percentage of other components is about 4% for all the states, except the ground state and the $(\frac{5}{2}^+)_2$ state, for which this value becomes 18% and 11%, respectively. The $(\frac{5}{2}^+)_1$ state is of v = 1 nature and is dominated by the $g_{7/2}^2 d_{5/2}$ conR18



FIG. 2. Experimental and calculated spectrum of ¹³⁵I.

figuration. As regards the $\frac{17}{2}^+$ state, as well as the three negative-parity states, our wave functions are dominated by the two configurations $g_{7/2}^2 d_{5/2}$ and $g_{7/2}^2 h_{11/2}$, respectively.

We have also calculated the ground-state binding energies (relative to ¹³²Sn) for ¹³⁴Te and ¹³⁵I. The mass excess value for ¹³³Sb needed for absolute scaling of the s.p. levels was taken from [15]. As for the Coulomb energy, we have taken that of a homogeneous charged sphere with $r_0 = 1.2$ fm. We find $E_b(^{134}\text{Te})=20.563$ MeV and $E_b(^{135}\text{I})=29.440$ MeV, to be compared with the experimental values 20.357 ± 0.045 MeV [15] and 29.034±0.037 MeV [16], respectively. Keeping in mind how simple is the model used for the evaluation of the Coulomb corrections, the agreement between theory and experiment may be considered quite satisfactory. A more reliable way of estimating the Coulomb energy is provided by the work of Ref. [17]. Making use of Eq. (3) of this paper, one obtains an expression for the binding energy of an N= 82 isotone depending on two parameters, V_c and b. Typical values [17] of these parameters extracted from experimental Coulomb displacement energies for the mass region A = 41-56 are 0.3 and 0.1 MeV, respectively. Since no such analysis is available for the N=82 isotones, we make use of the two above values of V_c and b to calculate the binding energies for ¹³⁴Te and ¹³⁵I. We obtain $E_b(^{134}\text{Te})=20.383$ and $E_b(^{135}I)=29.098$ MeV, in excellent agreement with the experimental values.

At this point we should mention that the authors of Ref. [2] claim to have discovered a serious inconsistency in the accepted masses of N=82 isotones near ¹³²Sn. In this regard, we note that in the calculation of the mass "window"

TABLE I. Calculated and experimental $B(E\lambda)$ values (in W.u.) for ¹³⁴Te. The experimental data are from [1].

$\overline{J_i^{\pi} \rightarrow J_f^{\pi}}$	λ	$B(E\lambda)_{expt}$	$B(E\lambda)_{calc}$
$4_1^+ \rightarrow 2_1^+$	2	4.3 ± 0.3	4.3
$6_1^+ \rightarrow 4_1^+$	2	2.05 ± 0.03	2.0
$9_1^- \rightarrow 6_1^-$	3	3.8 ± 0.2	1.0
$9_1^- \rightarrow 6_2^-$	3	8.0 ± 1.3	8.7

W of [2] two approximations are made which cast doubts on the above conclusion. On the one hand, the value of *W* obtained directly from the relevant N=82 masses (see [2]) does not take into account the Coulomb corrections. On the other hand, the value of *W* from spectroscopy is obtained by making the assumption that the $J^{\pi} = \frac{15}{2}^{+}$ state in ¹³⁵I is a pure $g_{7/2}^3$ configuration. From our calculation it turns out that the percentage of this component is 96%.

In Table I we compare the experimental reduced transition probabilities in ¹³⁴Te with the calculated ones. We have used an effective proton charge $e_p^{\text{eff}} = 1.55e$. This is consistent with the values adopted by other authors [4,18]. The theoretical B(E2) values are in very good agreement with experiment. As regards the E3 transitions, we find that the $B(E3;9_1^- \rightarrow 6_2^+)$ is well reproduced, while the $B(E3;9_1^- \rightarrow 6_1^+)$ is underestimated by a factor of about 4. A possible reason for this discrepancy lies in the fact that only a small amount of configuration mixing is present in the calculated 6^+ states. In fact, the decay to the 6^+_2 state is dominated by the single-proton transition $(h_{11/2}g_{7/2})_9 \rightarrow (g_{7/2}d_{5/2})_6^+$, while that to the 6_1^+ state by the transition $(h_{11/2}g_{7/2})_9 \rightarrow (g_{7/2}^2)_6^+$, which is retarded owing to spin flip. The theoretical $B(E3;9_1^- \rightarrow 6_1^+)$ value could be brought in agreement with experiment by an amount of configuration mixing of about 15%, which would, of course, reduce the $B(E3;9_1^- \rightarrow 6_2^+)$ value. It should be noted, however, that the latter would still be within the error bar.

The magnetic moment of the 6_1^+ state in ¹³⁴Te has been measured to be 5.08 ± 0.15 n.m. [10]. We have calculated it by using the g_s^{free} factor and an effective g_l factor g_l^{eff} = $1.3g_l^{\text{free}}$. We obtain $\mu(6_1^+)=5.01$ n.m. The above values of the gyromagnetic factors have been determined from an analysis of the measured magnetic moments in the three isotones ¹³⁴Te, ¹³⁶Xe, and ¹³⁷Cs and lead to an excellent agreement between theory and experiment also for the two latter nuclei [19].

In summary, we have shown that our effective interaction derived from the Bonn A nucleon-nucleon potential leads to a very good description of the two N=82 nuclei ¹³⁴Te and ¹³⁵I. It should be stressed that no adjustable parameter appears in our calculations.

Based on these findings, we are currently studying the heavier N=82 isotones using the same realistic effective interaction. This should permit to gain further insight into the role of modern realistic interactions in the shell-model approach to the nuclear many-body problem.

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