Configurations of superdeformed bands in 193Pb

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The six superdeformed bands in ^{193}Pb have been studied with the EUROGAM 2 γ -ray spectrometer using the ¹⁶⁸Er(³⁰Si,5*n*)¹⁹³Pb reaction. The results are discussed in terms of cranked-Hartree-Fock-Bogolioubov-Lipkin-Nogami calculations. From the $\mathfrak{F}^{(2)}$ moment of inertia behavior as function of the rotational frequency and the *M*1 and *E*2 decay competition of the superdeformed states, the bands are interpreted as three pairs of signature partners based on quasineutron excitations. Dipole transitions linking two signature partner superdeformed bands have been observed and, for the first time in lead isotopes, the branching ratio $B(M1)/B(E2) = 0.15 \pm 0.04$ μ_N^2/e^2 b² has been extracted. [S0556-2813(96)02406-5]

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I. INTRODUCTION

One of the most interesting ways to study the nucleus under extreme conditions of deformation and angular momentum is the observation of superdeformed (SD) states. The existence of SD nuclei has been predicted in the mass $A \sim 190$ region both by microscopic and macroscopicmicroscopic calculations $[1–5]$. Experimentally more than 40 SD bands have been discovered in 20 nuclei $[6]$. For the lead isotopes, microscopic Hartree-Fock plus BCS calculations [5] have predicted the occurrence of a SD well for ¹⁹²Pb. This nucleus appears as the borderline case of the superdeformation island for the even-even lead isotopes. SD bands have been observed very recently in odd-*A* Pb nuclei, $193,195,197$ Pb [7-9].

For many SD bands in the mass $A \sim 190$ region, the dynamical moments of inertia $\mathfrak{F}^{(2)}$ show a typical rise with increasing rotational frequency $\hbar \omega$. This behavior has been attributed to the alignment of quasiparticle pairs from high-*N* intruder orbitals in the presence of pairing. However some exceptions remain, in particular two SD bands in odd-*A* lead nuclei have been observed with approximately constant $\mathfrak{F}^{(2)}$ $[7-9]$ such as in 192,194 Tl $[10,11]$ and, at low frequencies, in odd-A mercury isotopes [12,13]. These "flat" bands have been interpreted in terms of Pauli blocking of quasiparticle alignments in intruder orbitals for odd-*A* Pb and odd-odd Tl isotopes and, for odd-*A* Hg isotopes, in terms of occupation of the unfavored $N=7$ neutron orbitals.

Another interesting feature connected to the SD nuclei in the mass $A \sim 190$ region is the measurement of the magnetic properties. The branching ratios of *M*1 transitions between signature partner SD bands have been measured in 193 Hg [14] and later in odd proton nuclei 195 Tl [15] and 193 Tl [16]. Crosstalk between SD bands has also been observed in 194 Tl [11] and 193,195,197 Pb [7-9].

In this paper, we report on the new results obtained for the six SD bands observed recently by Hughes et al. $[7]$ in the nucleus 193Pb which is the lightest known odd-*A* Pb isotope containing SD bands. From the $\mathfrak{F}^{(2)}$ moment of inertia behavior as a function of the rotational frequency and the *M*1 and *E*2 decay competition of the SD states, the six bands are interpreted as three pairs of signature partners involving the

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FIG. 1. Background-substracted triple-gated spectra for the six SD bands of $193Pb$. SD band transitions are labeled by \blacksquare , band 1; \Box , band 2; \bullet , band 3; \circ , band 4; ∇ , band 5; \triangle , band 6. Low-lying yrast transitions are denoted by *y*. In these spectra, all indicated transitions are used as gates except 708 keV for band 1; 610, 649, and 690 keV for band 2; 251, 673, and 707 keV for band 3; 273, 676, and 709 keV for band 4; 213, 254, 596, 632, and 667 keV for band 5; and 234, 684, and 717 keV for band 6. Insets give the relative transition intensities, corrected for *E*2 internal conversion, as a percentage of the largest peak intensity in the band.

 $[761]3/2j_{15/2} = 7_2$, $[642]3/2$ and $[624]9/2$ neutron orbitals. We have observed the crosstalk transitions between two of these SD bands and, for the first time in lead isotopes, we were able to measure the *M*1/*E*2 branching ratio.

II. EXPERIMENT

The fusion reaction ${}^{30}Si+{}^{168}Er$ at a beam energy of 159 MeV was used in order to populate high-spin states in $193Pb$ via the 5*n* evaporation channel. The beam was delivered by the Vivitron accelerator at the Centre de Recherches Nucléaires in Strasbourg. The experiment was carried out with two self-supporting thin 600 μ g cm⁻² targets. Gamma rays were detected using the EUROGAM 2 spectrometer [17] which consists of 15 large escape suppressed Ge detectors at backward and forward angles, respectively, and 24 escape suppressed ''clover'' Ge detectors near 90° relative to the beam direction.

Approximately 6×10^8 four- and higher-fold events were recorded on magnetic tapes. After unfolding $\sim 3 \times 10^9$ quadruple coincidences were obtained. 40% of the events correspond to ¹⁹³Pb residues. With this reaction we have also populated high-spin states in ^{192}Pb (20% of the events) and we have confirmed the existence of a SD band in this nucleus [18]. We have to note that charged-particle channels $\alpha 4n$

 (^{190}Hg) and $p4n$ (^{193}Tl) are also open in this reaction with the relative yields of \sim 15% and \sim 12% respectively. The data set has been sorted into different multidimensional spectra (1D spectra, 2D matrices, 4D database). The SD bands have been isolated using directly the triple-gated spectra obtained from four- and higher-fold events and the fourdimensional DATABASE program $[19]$. The intensities of the gamma rays have been extracted from double-gated spectra, the background has been substracted according to the method of Crowell *et al.* [20] modified for an event-by-event reading mode. The algorithm determines, by minimization, the respective weights of single gated and total projection spectra to substract for each pair of a given set of gates.

III. RESULTS AND DISCUSSION

Analysis of the data first revealed the presence of the six SD bands as reported by Hughes *et al.* [7] using the 174 Yb(24 Mg,5*n*) reaction with a beam of 131 MeV and the GAMMASPHERE early implementation array (36 detectors). Figure 1 shows triple-gated spectra for the six SD bands found in our data. The relative intensities of the transitions in the SD bands are shown in the insets of Fig. 1. The intensities relatively to band 1 are estimated at 0.5, 0.5, 0.5, $0.3, 0.3$ for bands $2, 3, 4, 5,$ and 6 , respectively (with the

Band 1 (27/2)	Band 2 (17/2)	Band 3 (21/2)	Band 4 (23/2)	Band 5 (17/2)	Band 6 (19/2)
277.2(3)	190.5(5)	$250.6(5)*$	$273.0(7)*$	212.9(6)	234.1(7)
317.2(3)	232.5(4)	291.5(3)	313.7(6)	254.5(7)	275.8(6)
357.3(3)	275.0(4)	332.0(3)	352.9(3)	295.4(6)	315.9(6)
397.4(3)	317.9(4)	371.8(3)	391.6(5)	335.7(7)	355.7(6)
437.6(3)	360.9(3)	411.2(4)	429.8(4)	375.0(5)	394.4(6)
477.3(4)	403.6(4)	450.4(4)	466.9(4)	413.6(6)	432.9(6)
517.0(5)	445.7(4)	488.8(4)	503.7(5)	451.6(5)	470.4(6)
555.8(4)	488.3(5)	526.5(5)	539.9(6)	488.8(7)	507.5(6)
594.5(6)	527.5(6)	563.1(5)	575.0(5)	526.2(8)	543.6(6)
632.5(6)	$569.8(7)*$	600.1(5)	609.1(5)	$561.5(6)*$	579.4(7)
$671.0(6)*$	$610.2(8)*$	$636.6(6)*$	$643.0(6)*$	$596.5(10)*$	$614.9(8)*$
$708.2(8)*$	$649.5(8)*$	$672.7(6)*$	$676.4(6)*$	$632.0(8)*$	$649.3(9)*$
	$689.8(8)*$	$707.3(6)*$	$709.3(6)*$	$667.0(8)*$	$683.7(9)*$ $717.5(10)*$

TABLE I. γ -ray energies (in keV) of the six SD bands in ¹⁹³Pb. The new γ rays are labeled by *.

same numbers as Hughes *et al.* [7]) with a \sim 20% uncertainty. Bands 1, 2, 3, 4, and 6 are clearly demonstrated by our quadruple data and are in coincidence with yrast normal deformed transitions in ^{193}Pb [21] such as 881 keV $(17/2^+\rightarrow 13/2^+)$, 520 keV $(21/2^+\rightarrow 17/2^+)$, 593 keV $(25/2^+\rightarrow 21/2^+)$ for bands 3, 4, 5, and 6. Band 1 also strongly feeds the $21/2^-$ state (184 keV transition) and band 2 seems to decay directly to the 881 keV level. Band 5 is strongly contaminated by five transitions in the normal deformed level scheme, namely the 213 keV transition (compared to the 213 SD one), 252 keV (254 keV SD), 334 keV (335 keV SD), 413 keV (414 keV SD), and 528 keV (527 keV SD). Therefore the extracted intensities for this band are rather uncertain. Furthermore, to extract this band, we were not able to use as many gates as for the other bands and band 5 seems less intense than band 6 in Fig. 1 whereas their intensities are nearly equal.

Twenty-two new transitions, over and above those observed by Hughes *et al.* [7], have been identified in the six SD bands, 2 at low energies and 20 at high energies as shown in Table I. The spin values of the lowest SD states in the bands have been derived according to the method of Becker *et al.* [22] and Wu *et al.* [23]: 21/2, 23/2, 17/2 and 19/2 for bands 3, 4, 5, and 6, respectively, and for bands 1 and 2 we adopted the same spin values of Hughes *et al.* [7]: 27/2 and 17/2. As shown in Fig. 1, at low frequency the transition energies of band 3 lie at the midpoint of the corresponding transition energies of band 4, bands 5 and 6 present a similar relationship up to the highest observed frequency. As Hughes *et al.* [7], we suggest that bands 1-2, 3-4, and 5-6 are signature partners.

The experimental $\mathfrak{F}^{(2)}$ dynamical moments of inertia for the six SD bands in $193Pb$ are plotted in Fig. 2 as a function of the rotational frequency, $\hbar \omega$, and for comparison, the $\mathfrak{F}^{(2)}$ for the yrast SD band in ^{192}Pb [18] is also shown. It is clear that bands 3-4 and 5-6 present the same behavior as the yrast band of 192 Pb with the typical rise from 95 to $115\hbar^2/\text{MeV}$ with increasing rotational frequency. However for bands 1 and 2, the dynamical moments of inertia are quite constant as a function of frequency. The experimental Routhians for the

six SD bands are plotted in Fig. 3. The \mathcal{I}_0 and \mathcal{I}_1 parameters used for the reference are those extracted from a Harris fit to the yrast SD band in ¹⁹²Pb [18] $(\mathcal{I}_0 = 89.7\hbar^2 \text{ MeV}^{-1}$ and $\mathscr{T}_1 = 104.3\hbar^4$ MeV⁻³). The relative excitation energies for the Routhians are governed by the two following assumptions: (i) the ordering is consistent with the measured relative population of the bands; (ii) at zero frequency the bands 1-2, 3-4, and 5-6 are degenerate since they are signature partners. Bands 1-2 and 5-6 show the same behavior as those given by Hughes *et al.* [7]. Bands 5 and 6 are degenerate along the whole frequency range but, for bands 3 and 4, with the new

FIG. 2. Experimental $\mathfrak{F}^{(2)}$ dynamical moments of inertia as a function of the rotational frequency for the six SD bands in ¹⁹³Pb \mathbb{Z} , band 1; \Box , band 2; \bullet , band 3; \Diamond , band 4; ∇ , band 5; \triangle , band 6) and for the yrast SD band in $192Pb$ (dashed line).

FIG. 3. Experimental Routhians as a function of the rotational frequency for the six SD bands observed in ¹⁹³Pb (\blacksquare , band 1; \Box , band 2; \bullet , band 3; \circlearrowright , band 4; ∇ , band 5; \triangle , band 6).

transitions we added, a splitting clearly appears at $\hbar\omega$ ~300 keV.

In order to interpret our data, we have extended, for ¹⁹²Pb, the microscopic cranked-Hartree-Fock-Bogolioubov calculations with the parametrization SkM* of the Skyrme force using the Lipkin-Nogami prescription for the pairing treatment [24]. These results have been obtained with a seniority force $G_{\tau}=12.6$ MeV. The neutron single-particle and quasiparticle Routhians are plotted in Figs. $4(a)$ and $4(b)$. As shown in Fig. $4(a)$, the valence single particles available above the Fermi level (λ) are the $[642]3/2$, $[512]5/2$, [624] $9/2$ and below the [640] $1/2$, [761] $3/2j_{15/2} = 7₂$ and $[505]$ 11/2. For the theoretical quasineutron Routhians represented in Fig. 4(b), at $\hbar \omega$ =200 keV, the ordering of the levels is the following: the intruder $\alpha = -1/2$ [761] $3/2$ (hole excitation), the two $\left| \frac{642}{3}{\right|}$ (particle excitations), $\alpha=+1/2$ $[761]3/2$ (hole excitation), the two degenerate $[505]11/2$ (hole excitations), the two $[640]1/2$ (hole excitations), the two $\left| \frac{512}{5/2} \right|$ (particle excitations) and the two degenerate $[624]9/2$ (particle excitations). As expected the intruder state $7₂$ presents a large splitting. At $\hbar\omega=0$, all the states between $[642]3/2$ and $[624]9/2$ are located within 400 keV. We can compare these microscopic theoretical results to those of the cranked shell model (CSM) for an axial deformation of $\beta_2=0.478$ and $\beta_4=0.07$ of Hughes *et al.* [7]. In our results, two supplementary low-lying neutron hole excitations, $[640]1/2$ and $[505]11/2$, appear and in both calculations the lowest-energy orbital is the $N=7$, $\alpha=-1/2$.

For bands 1 and 2, we obtain a good agreement for the Routhians between the experimental splitting and the predicted one of the $[761]3/2$ signatures. This splitting starts at a rotational frequency $\hbar \omega$ =50 keV and reaches a value of 330 keV at $\hbar \omega$ =300 keV. This compares well with the predicted value of 400 keV. It is in fact extremely clear that for frequencies higher than 100 keV this quasiparticle state corre-

FIG. 4. (a) CHFBLN single-neutron and (b) CHFBLN quasineutron Routhians as a function of the rotational frequency. (π,α) : solid= $(+,+)$, dashed= $(+,-)$, dash-dotted= $(-,+)$, dotted $= (-,-)$. *h*, hole excitation; *p*, particle excitation.

sponds to the lowest excitation energy in the HFB spectrum. As expected the corresponding dynamical moment of inertia shown in Fig. 2 presents a flat behavior characteristic of the blocking due to the odd neutron. This pairing blocking effect has already been observed in lead isotopes for bands 1-2 in $193,195,197$ Pb $[7-9]$, in thallium isotopes such as bands 3-4 of ¹⁹²Tl [10], bands 3a-3b of ¹⁹⁴Tl [11] and more recently in 191 Hg [13]. So we agree with the interpretation of these two

FIG. 5. Incremental alignments as a function of the rotational frequency for bands 3 \bullet and 4 \circ in ¹⁹³Pb and bands 2 \circ and 3 (\blacklozenge) in ¹⁹¹Hg relative to band 1 in ¹⁹⁴Pb and ¹⁹²Hg, respectively.

bands as due to the $[761]3/2$ intruder $N=7$ neutron state as suggested by Hughes *et al.* [7]. Band 1 is then identified as the favored partner, $\alpha = -1/2$, of the [761] $3/2$ orbital and band 2 the unfavored one, $\alpha=+1/2$. This assignment is in total agreement with the estimated spin values of 27/2 for band 1 and 17/2 for band 2. We have to note that the spin difference between the normal deformed ground state $13/2^+$ and the estimated spin of the lowest SD state in band 2 is only $2\hbar$. The bump observed in the dynamical moment of inertia for band 2 at $\hbar\omega$ =250 keV could be due to the crossing of the $[505]11/2$ orbital. In fact, our CHFBLN calculations show an interaction between the $N=7$ and $N=5$ orbitals, with same parity and same signature, occurring at $\hbar \omega$ $=$ 250 keV. Nevertheless, a band which could be a candidate for the other signature partner $(\alpha=-1/2)$ of the [505]11/2 was looked for and was not found.

Concerning bands 3 and 4, with the new observed transitions at high energy, the experimental Routhians show clearly a splitting with a strength around 50 keV at $\hbar\omega$ =350 keV. Hughes *et al.* [7] assigned these bands to the $[512]5/2$ orbital. In our theoretical scheme, the $[642]3/2$, $[512]5/2$, $[624]9/2$ orbitals are available in particle excitations with increasing excitation energy. The $\frac{624}{9/2}$ orbital presents no splitting all along the frequency range. The $[642]3/2$ and [512]5/2 orbitals display a splitting at $\hbar\omega$ =100 keV and $\hbar\omega$ $=250$ keV, respectively, with a value of 90 and 30 keV, respectively, at $\hbar\omega$ =350 keV. Three points lead us to propose finally for bands 3 and 4 the $[642]3/2$ assignment at variance with Hughes *et al.* [7].

~i! The intensities of these two bands are similar to that of band 2; this is in favor of the orbital the closest in energy to the yrast SD favored band 1 $[761]3/2$, the ordering of the first predicted levels at $\hbar\omega=200$ keV being $\alpha = -1/2$ [761] 3/2, $\alpha = -1/2$ [642] 3/2, $\alpha = +1/2$ [642] 3/2, $\alpha = +1/2$ [761] $\frac{3}{2}$ states.

(ii) The energies of the gamma transitions are identical to the ones of bands 2 and 3 in the isotone $N=111$ ¹⁹¹Hg interpreted by Carpenter *et al.* $[13]$ as $[642]3/2$ in Woods-Saxon calculations. Figure 5 shows the incremental alignments $[25]$ as a function of the rotational frequency for bands 3-4 in 193 Pb and bands 2-3 in 191 Hg relative to band 1 in

FIG. 6. Low-energy part of the background-substracted triplegated spectrum for band 6 shown in Fig. 1. (∇ , band 5; \triangle , band 6; *, interband dipole transitions!.

 $194Pb$ and $192Hg$, respectively. The similar behaviors of these plots reinforce the idea that these bands are due to the same neutron hole added to the two different cores ¹⁹⁴Pb and 192 Hg.

(iii) The last point which is the strongest is that we have observed no *M*1 crosstalk transitions at low energy linking the proposed signature partners while we do observe such dipole transitions, as will be discussed in the next paragraph for the weaker bands 5 and 6. We have extracted an upper limit of $B(M1)/B(E2) = 0.01 \mu_{N:2}/e^2$ b² for bands 3 and 4. We know that for $K=3/2$ bands the calculated $B(M1)$ rates are small $({\sim}0.01\mu_N^2$ for spin 23/2) and such linking transitions do not compete with the *E*2 intraband transitions. On the contrary the $B(M1)$ rates are calculated to be strong for $K = 5/2$ and 9/2 bands (50 times stronger than for $K = 3/2$ bands: from 0.47 to $0.77\mu_N^2$ and have been measured in ¹⁹³Hg [14] $B(M1) = 0.81 \pm 0.20 \mu_{N:2}$ for the $K = 5/2$ bands. The lack of crosstalk transitions is corroborated by the fact that we have no strong x rays (same intensity as for bands 1 and 2) and the intensities of the bands show a plateau before a sharp cutoff.

Of course the experimental splitting occurs at $\hbar\omega=250$ keV instead of 100 keV in our theoretical cranked HFBLN calculations, as was the case for 193 Hg [24]. This discrepancy could be explained by a small renormalization of the pairing constant. For 194Pb, the calculations of Terasaki *et al.* [26], using the CHFBLN method, predict that the splitting of the [642] $3/2$ orbital occurs at higher frequency, $\hbar \omega$ \sim 200 keV, with pairing correlations described by a zerorange density-dependent interaction instead of $\hbar \omega \sim 150 \text{ keV}$ with a seniority force and there is no change for the other orbitals. So we propose the $[642]3/2$ assignment for bands 3 and 4 which present a clear splitting and no crosstalk transitions, band 3 (4) being the $\alpha=+1/2$ $(-1/2,$ respectively) partner.

The experimental Routhians of bands 5 and 6 present no splitting up to the highest observed frequency. In particle excitations, the $[512]5/2$ and $[624]9/2$ predicted orbitals satisfy this condition up to 250 and 400 keV, respectively. Both configurations must induce large *B*(*M*1) crosstalk rates. Figure 6 shows the 213, 252, 295, 336, 375 keV transitions of band 5 on a spectrum gated on band 6 and also, between 100

FIG. 7. Level scheme for the pair of signature partner bands. The energies of the dipole transitions are assigned within 0.5 keV uncertainty.

and 230 keV, 13 crosstalk transitions. The presence of strong x rays twice as intense for these two bands compared to the others indicates the presence of relatively highly converted transitions. Figure 7 displays the level scheme for the observed bands 5 and 6 structure. The energy sum rules are fulfilled with a maximum error of 0.5 keV from the crosstalk transitions 100 to 221 keV, i.e., up to the 433-keV SD *E*2 transition ($\hbar \omega$ =0.2 MeV). Up to this point of the discussion two configurations are possible: $[512]5/2$ and $[624]9/2$. We have extracted the $B(M1)/B(E2)$ ratios directly from the γ -ray photon $M1/E2$ branching ratios and we obtain values around $0.15 \pm 0.04 \mu \frac{2}{N} / e^2$ b². The large error is due to the lack of statistics. The absolute *B*(*M*1) values have been derived taking into account the theoretical quadrupole moment Q_0 values of ¹⁹²Pb. In the strong-coupling limit the *B*(*M*1) value for a $K \neq 1/2$ band can be written

$$
B(M1) = \frac{3}{4\pi} (g_K - g_R)^2 K^2 \langle IK10|I - 1K \rangle^2 \quad (\mu_N^2),
$$

$$
g_K = g_l + (g_s - g_l) \frac{\langle S_z \rangle}{\Omega},
$$

and

$$
B(E2) = \frac{5}{16\pi} \langle IK20|I - 2K\rangle^2 Q_0^2 \quad (e^2 \text{ fm}^4).
$$

Concerning the Q_0 value, the experimental result for ¹⁹⁴Pb is 20 ± 4 *e* b [27] and the corresponding theoretical values in static HF+BCS calculations using the parametrization SkM^* of the Skyrme force $\lceil 5 \rceil$ are 18.2 *e* b for ¹⁹⁴Pb and 18.4 *e* b for 192Pb. However in fully self-consistent GCM calculations performed for the even-even lead isotope series $[28]$, taking into account all the quantal fluctuations associated with the collective variable q_2 related to the axial quadrupole deformation, the existence of a GCM superdeformed state in ¹⁹²Pb is confirmed at lower excitation energy than in the heavier lead isotopes, but with a smaller quadrupole deformation, $Q_0 = 16.7$ *e* b. The GCM calculation result for ¹⁹⁴Pb, Q_0 = 18.7 *e* b, is in perfect agreement with the experi-
mental value. Figure 8 shows the deduced mental value. Figure 8 shows the deduced $(g_K - g_R) K f(I,K)/Q_0$ ($f(I,K) = \langle IK10|I - 1K \rangle / \langle IK20|I$ $-2K$) values for four SD states of band 6 as a function of their evaluated spins. Band 5 was too contaminated to extract the γ -ray photon *M*1/*E*2 branching ratios. The theoretical limits for the configurations $\left[\frac{512}{5/2}\right]$ and $\left[\frac{624}{9/2}\right]$, using $g_s^{\text{eff}}=0.9g_s^{\text{free}}$, are indicated by full lines for the experimental value $Q_0 = 20 \pm 4$ *e* b of ¹⁹⁴Pb, and dotted and dashed lines for the predicted values of ¹⁹²Pb, $Q_0 = 18.4$ *e* b and Q_0 =16.7 *e* b, respectively. The data are in agreement with the assignment of the $[624]9/2$ configuration. This is corroborated by the fact that the γ -ray energies of these two SD bands and the energies of the linking *M*1 transitions are identical to those of bands 2b and 3 in 193 Hg [14] which have also been interpreted as $[624]9/2$. This assignment is also in agreement with the calculations of Terasaki *et al.* [26]. The average $(g_K - g_R)K f(I,K)/Q_0$ value was found to be equal to -0.245 ± 0.070 (*e* b)⁻¹. So, using the conventional $g_R = Z/A$ and $Q_0 = 18.4$ *e* b, we obtain for the experimental value $g_K = -0.39 \pm 0.12$. In Table II are reported the theoretical values: $\langle s_z \rangle$, the intrinsic spin on the *z* axis, and g_K , for the neutron [512]5/2 and [624]9/2 configurations, extracted from Hartree-Fock+BCS calculations using the parametrizations SkM^* [29] and SIII [30] of the Skyrme force, and Woods-Saxon wave functions of Semmes *et al.* [31]. The first remark is that the microscopic (HF) and the macroscopic-microscopic (WS) approaches are in perfect agreement for these two configurations. The theoretical g_K

FIG. 8. The extracted $(g_K - g_R)Kf(I,K)/Q_0(f(I,K))$ $=$ $\langle IK10|I-1K\rangle/\langle IK20|I-2K\rangle$ values for four SD states in band 6 as a function of their evaluated spins. The theoretical limits for the neutron [512]5/2 and [624]9/2 configurations, using g_s^{eff} $=0.9g_s^{\text{free}}$, are indicated by solid lines for the experimental value Q_0 =20 \pm 4*e* b of ¹⁹⁴Pb, and dotted and dashed lines for the predicted values of ¹⁹²Pb $Q_0 = 18.4e$ b and $Q_0 = 16.7e$ b, respectively.

values can be compared to the two experimental values in ¹⁹³Hg [14] and ¹⁹³Pb (this work). The experimental g_K values are in agreement with the predicted ones if one takes $g_s^{\text{eff}} \sim 0.9 g_s^{\text{free}}$. This assignment for bands 5 and 6 puts a question as regards to the non-observation of the two SD bands corresponding to the quasineutron $[512] \frac{5}{2}$ configuration. It could be understood if one of these nonobserved bands is a pair of identical bands of opposite parity as it is the case for bands 2a and 2b in 193 Hg [14]. Our difficulties to isolate band 5, which is strongly contaminated, could explain this nonobservation.

IV. CONCLUSION

The main results of this work are the following: first, the confirmation of the six SD bands discovered by Hughes

TABLE II. Values of the intrinsic spin on the *z* axis, $\langle s_z \rangle$, and g_K for the neutron [512]5/2 and [624]9/2 configurations, extracted from Hartree-Fock+BCS calculations using the parametrizations $[HF (SkM*)] SkM* [29] and [HF (SIII)] SIII [30] of the Skyrme$ force, and Woods-Saxon (WS) wave functions of Semmes *et al.* [31] calculated with $g_s^{\text{eff}}=0.7g_s^{\text{free}}$ and $g_s^{\text{eff}}=0.9g_s^{\text{free}}$ and experimental value of g_K measured in ¹⁹³Hg [14] and ¹⁹³Pb (this work).

		[512]5/2	[624]9/2
	$HF(SkM^*)$	0.4259	0.4614
$\langle S_z \rangle$	HF(SIII)	0.4625	0.4630
	WS	0.45	0.46
	$HF(SkM^*)$	-0.456	-0.275
$g_K(0.7g_s^{\text{free}})$	HF(SII)	-0.495	-0.276
	WS	-0.482	-0.274
	$HF(SkM^*)$	-0.587	-0.353
$g_K(0.9g_s^{\text{free}})$	HF(SIII)	-0.637	-0.354
	WS	-0.620	-0.352
g_K (expt.)		-0.65 ± 0.14	-0.39 ± 0.12

et al. [7] and the assignment of bands 1 and 2 as due to the $[761]3/2$ intruder $N=7$ neutron state. Second, at variance to the previous work, we proposed the $[642]3/2$ assignment for bands 3 and 4 which present a clear splitting in the experimental Routhians and no crosstalk transitions. Finally, we have observed for the first time in lead isotopes the *M*1 connecting transitions between bands 5 and 6 and the measurements of the branching ratios that we have extracted from these data lead us to propose for these bands the assignment of the $[624]9/2$ quasineutron configuration.

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- [1] P. Bonche, S. J. Krieger, P. Quentin, M. S. Weiss, J. Meyer, M. Meyer, N. Redon, H. Flocard, and P.-H. Heenen, Nucl. Phys. A 500, 308 (1989).
- [2] M. Girod, J. P. Delaroche, and J. F. Berger, Phys. Rev. C 38, 1519 (1988); M. Girod, J. P. Delaroche, D. Gogny, and J. F. Berger, Phys. Rev. Lett. **62**, 2452 (1989).
- [3] R. R. Chasman, Phys. Lett. B **219**, 227 (1989).
- [4] W. Satula, S. Cwiok, W. Nazarewicz, R. Wyss, and A. Johnson, Nucl. Phys. A **529**, 289 (1991).
- [5] S. J. Krieger, P. Bonche, M. S. Weiss, J. Meyer, H. Flocard, and P.-H. Heenen, Nucl. Phys. A 542, 43 (1992).
- [6] R. B. Firestone and B. Singh, "Table of superdeformed

nuclear bands,'' LBL Report No. LBL-35916, unpublished, and references therein.

- [7] J. R. Hughes *et al.*, Phys. Rev. C **51**, 447 (1995).
- [8] L. P. Farris *et al.*, Phys. Rev. C 51, R2288 (1995).
- [9] I. M. Hibbert *et al.*, submitted to Phys. Rev. C.
- [10] Y. Liang *et al.*, Phys. Rev. C 46, R2136 (1992).
- [11] J. Duprat et al., in Proceedings of the International Confer*ence on the Future of Nuclear Spectroscopy, Crete, Greece* (Institute of Nuclear Physics, Athens, 1993), p. 199.
- [12] M. J. Joyce et al., Phys. Lett. B 340, 150 (1994).
- [13] M. P. Carpenter *et al.*, Phys. Rev. C **51**, 2400 (1995).
- [14] M. J. Joyce *et al.*, Phys. Rev. Lett. **71**, 2176 (1993).
- $[15]$ J. Duprat *et al.*, Phys. Lett. B 341, 6 (1994).
- [16] S. Bouneau *et al.*, Phys. Rev. C 53, R9 (1996).
- [17] P. J. Nolan, Nucl. Phys. A **520**, 657c (1990); F. A. Beck, in *Proceedings of the First European Biennial Workshop on Nuclear Physics*, Megève, edited by D. Guinet and J. R. Pizzi (World Scientific, Singapore, 1991), p. 365; N. Redon, EURO-GAM Collaboration, in *Proceedings of the XXXIII International Winter Meeting on Nuclear Physics*, Bormio, edited by I. Iori (Ricerca Scientifica ed Educazione Permanente, Milano, 1995), p. 1 and references cited therein.
- $[18]$ L. Ducroux *et al.*, Z. Phys. A 352, 13 (1995).
- [19] S. Flibotte, U. J. Hüttmeier, P. Bednarczyk, G. De France, B. Haas, P. Romain, Ch. Theisen, J. P. Vivien, and J. Zen, Nucl. Instrum. Methods Phys. Res. A 320, 325 (1992).
- [20] B. Crowell, M. P. Carpenter, R. G. Henry, R. V. F. Janssens, T. L. Khoo, T. Lauritsen, and D. Nisius, Nucl. Instrum. Methods Phys. Res. A 355, 575 (1995).
- [21] J. M. Lagrange, M. Pautrat, J. S. Dionisio, Ch. Vieu, and J.

Vanhorenbeeck, Nucl. Phys. A **530**, 437 (1991).

- [22] J. A. Becker *et al.*, Phys. Rev. C 46, 889 (1992).
- [23] C. S. Wu, L. Cheng, C. Z. Lin, and J. Y. Zeng, Phys. Rev. C 45, 2507 (1992).
- [24] B. Gall, P. Bonche, J. Dobaczewski, H. Flocard, and P.-H. Heenen, Z. Phys. A 348, 183 (1994).
- [25] F. S. Stephens *et al.*, Phys. Rev. Lett. **65**, 301 (1990).
- [26] J. Terasaki, P.-H. Heenen, P. Bonche, J. Dobaczewski, and H. Flocard, Nucl. Phys. A **593**, 1 (1995).
- [27] P. Willsau et al., Z. Phys. A 344, 351 (1993).
- [28] J. Meyer, P. Bonche, M. S. Weiss, J. Dobaczewski, H. Flocard, and P.-H. Heenen, Nucl. Phys. A **588**, 597 (1995).
- [29] S. Perries *et al.*, unpublished.
- [30] M. Meyer, N. Redon, P. Quentin, and J. Libert, Phys. Rev. C **45**, 233 (1992).
- [31] P. B. Semmes, I. Ragnarsson, and S. Aberg, Phys. Lett. B 345, 185 (1995).