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β -delayed α decay of ¹⁷N

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The β -delayed α spectrum of ¹⁷N has been measured using a molecular ¹⁷NO⁺ beam from the TRIUMF isotope separator. This surface barrier detector pairs were used to count the α particles in coincidence with ¹³C recoil nuclei. The resulting spectrum has been fitted with a K-matrix parametrization. The β -delayed α decay of states at 7.99 and 8.20 MeV in the ¹⁷O daughter has been observed. A total $\beta\alpha$ -branching ratio of $(2.5 \pm 0.4) \times 10^{-5}$ has been determined for this decay mode of ¹⁷N.

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I. INTRODUCTION

In a recent study in our laboratory, the E1 component of the astrophysical S factor for the ${}^{12}C(\alpha, \gamma){}^{16}O$ reaction was deduced, in part, from a precision measurement of the β -delayed α spectrum of ${}^{16}N$ [1]. In order to identify contaminant contributions to the α spectrum from nitrogen nuclides other than ${}^{16}N$, the β -delayed α spectra of ${}^{17}N$ and ${}^{18}N$ were also measured.

Although both ¹⁶N and ¹⁸N are known β -delayed α emitters, this form of decay has previously not been observed for ¹⁷N. However, with a Q_{β} of 8.680 MeV for ¹⁷N and an α separation energy of 6.359 MeV in ¹⁷O, the β -delayed α emission of ¹⁷N is allowed by 2.321 MeV. Approximately 95% of ¹⁷N β decay is accounted for by β -delayed neutron emission from states at 4.55, 5.38, and 5.94 MeV excitation in the ¹⁷O daughter (see Fig. 1). The remainder of the β decay populates mainly the ground and the first two excited states of ¹⁷O (below the neutron emission threshold) [2]. Using a high-efficiency surface-barrier detector system, designed to measure β delayed charged particle emission [1,3], low-intensity, β delayed α branches have been observed, for the first time, from states at 7.99 and 8.20 MeV in ¹⁷O.

II. EXPERIMENTAL DETAILS

A radioactive ion beam of ¹⁷N was produced using the thick-target on-line isotope separator, TISOL, at the TRIUMF cyclotron facility [4,5]. A 13 g/cm² target of Zeolite X spheres contained in a stainless steel target oven was irradiated with a 500 MeV, 1.5 μA proton beam. The target was heated to about 600 °C and was coupled to the electron cyclotron resonance (ECR) ion source [6]. Using an extraction voltage of 12 kV, ion beams were magnetically mass analyzed and transported to a low-background experimental area where they were implanted into thin (10 μ g/cm²) self-supporting collector carbon foils.

Four 1-cm-diam collector foils were positioned (with 90° relative spacing) about the circumference of a wheel rotating in the plane perpendicular to the ion beam axis. The wheel was mounted such that one foil intercepted the ion beam while the other three were simultaneously positioned between three pairs of silicon surface-barrier detectors. Successive 90° rotations of the wheel allowed collection of the ion beam and simultaneous counting of previously implanted foils at the three detector stations.



FIG. 1. β -decay scheme of ¹⁷N. Level energies are given in MeV above the ground state of ¹⁷O. Branching ratios to states below 7 MeV are from Ref. [2]. The 90° rotation time was measured to be 0.2 s, while a collect/count dwell time of 4 s was used to optimize the collecting and counting efficiency and suppress contaminant activities having different half-lives. With the foils positioned between the detectors (~ 8 mm separation), alpha particles were collected in coincidence with recoil carbon nuclei in the opposite detector.

Thin (10.6–15.8 μ m) transmission-mount Si surfacebarrier detectors, with 50 mm^2 active areas, were used to minimize the deposited energy of the more intense β activity. An 8-mm-diam, liquid-nitrogen-cooled collimator was mounted immediately upstream of the collector foil to ensure centering of the implanted ion beam and to avoid carbon deposition on the foil. Detector signals were processed and written to tape in an event-by-event mode for subsequent off-line analysis. A trigger condition was set such that all analog-to-digital converter (ADC) outputs were recorded whenever at least one detector registered an event corresponding to an α -particle energy greater than about 250 keV. Each event was tagged with its time, relative to the end of each wheel rotation, for determining half-life information. To avoid electronic noise, data acquisition was disabled during wheel rotation and coincidence events from unpaired detectors were discarded.

III. β -DELAYED α SPECTRUM OF ¹⁷N

Initially, α activity attributed to ¹⁷N was observed at the mass A = 17 separator position in conjunction with the shorter-lived activity of ¹⁷Ne. For final data acquisition, the ¹⁷N yield was maximized at A = 33. This mass position contained the least amount of contaminant activity (¹⁶N and ¹⁸N) relative to ¹⁷N, which was presumably separated as the ¹⁷N¹⁶O⁺ molecule. Prior to the run, all six detectors were energy calibrated using the known [7,8] monoenergetic α lines of ¹⁸N [E_{α} = 1.083 ± 0.004 MeV and $E_{\alpha} = 1.409 \pm 0.003$ MeV (lab)] mass separated as ${}^{18}N^{16}O^+$ (A = 34). During the 26 h data acquisition, $^{18}\mathrm{N}~\alpha$ particles were also observed in the first and second detector pair spectra, allowing a check of the energy calibration. In order to obtain a ¹⁷N β -delayed α spectrum free of ¹⁸N, only events occurring after 11 half-lives of ¹⁸N were used. A small amount of $^{16}\mathrm{N}$ contamination above $E_{\alpha}=1.6~\mathrm{MeV}$ did not obscure the ¹⁷N spectrum. The assignment of the remaining α activity to the decay of ¹⁷N was in part based on a leastsquares fit to the total α activity (in the third detector pair) as a function of time. The determined value of 3.92 ± 0.44 s was in good agreement with the accepted 4.173 ± 0.004 s half-life of ¹⁷N [2]. In Fig. 2 both the energy and time distributions of the alpha events recorded at the three detector stations are shown. The summed β -delayed α spectrum of ¹⁷N is displayed in Fig. 3.

IV. DATA ANALYSIS

A. K-matrix analysis

The spectrum was fitted using the K-matrix parametrization of Ref. [9] as extended to β -delayed α



FIG. 2. Delayed α spectra from the three detector stations as functions of energy and time. The first spectrum is predominantly ¹⁸N, while the last is entirely due to ¹⁷N.

decay in Ref. [10]. Ref. [10] dealt specifically with the decay of ¹⁶N; the relevant equations given there have been modified for ¹⁷N decay to take into account the strong neutron decay channel as well as the differing angular momenta. The following equation describes the spectrum of α particles following ¹⁷N decay given the assumptions (i) β decay to allowed states $(J^{\pi} = \frac{1}{2}^{-}$ or $\frac{3}{2}^{-})$ only, and (ii) neutron emission is the dominant decay mode:

$$W_{\alpha}(E) = \sum_{l=0,2} f_{\beta}(E) p_{l\alpha}^{2}(E) \left| \frac{\sum_{i} B_{li} g_{l\alpha i} / (E_{li} - E)}{1 - i p_{1n}^{2}(E) K_{lnn}} \right|^{2},$$
(1)



FIG. 3. β -delayed α spectrum of ¹⁷N, including a two-level K-matrix fit to the data. The dashed lines represent the contributions from individual levels (see Table I).

$$K_{lnn} = \sum_{i} \frac{g_{lni}^{2}}{E_{li} - E},$$
(2)

where the subscript l refers to the orbital angular momentum for alpha decay of the ¹⁷O state $(l = 0 \text{ and } 2 \text{ for} J^{\pi} = \frac{1}{2}^{-} \text{ and } \frac{3}{2}^{-}$, respectively), $f_{\beta}(E)$ is the integrated Fermi distribution, $p_{mc}^{2}(E)$ is the K-matrix penetrability [9] for channel c with orbital momentum m (m = 1 for the neutron channel in both J^{π} cases), E_{li} is the energy of the state i, g_{lci} is the K-matrix partial amplitude of state i for channel c, and B_{li} is the β -feeding factor into state i.

Equation (1) was convoluted with the detector resolution before comparison to the α -particle spectrum. This resolution was treated as a variable parameter in the fits with the measured resolution of 35 ± 10 keV [full width at half maximum (FWHM)] being included as an additional data point. This allowed the uncertainties due to the resolution to be included in the calculation of the errors (defined as the point at which the χ^2 increased by 1.0). Errors in the calibration using the two ¹⁸N lines were incorporated in a similar fashion.

Because of the large statistical error for many data points, an iterative fitting procedure was used in which the errors assigned to the data points were taken to be the square root of the points calculated from the previous fit, rather than the square root of the actual numbers of counts.

The initial fit was performed assuming the existence of only two states, with three parameters being varied for each: E_{li} , g_{lni} , and the product $B_{li}g_{l\alpha i}$. This twolevel fit, with a χ^2 for 57.3 for 77 degrees of freedom, is shown in Fig. 3. The spectrum consists of one broad and one narrow resonance at $E_{c.m.} = 1.629$ and 1.844 MeV, respectively. These energies correspond to excited states in ¹⁷O previously identified in ¹³C(α, n) and ¹⁶O(n, n) studies [11,12]. The state energies and neutron widths (as determined by the K-matrix analysis) are presented in Table I together with the results of the *R*-matrix analysis results of Ref. [12]. Assuming allowed β transitions to both states (see $\log ft$ values in Table II) and given the fact that neither resonance shows an interference pattern, the J^{π} assignments of Ref. [12] are consistent with our fits of $J^{\pi} = \frac{1}{2}^{-}$ or $\frac{3}{2}^{-}$. References [2] and [12] indicate the presence of two

References [2] and [12] indicate the presence of two other levels that may influence the ¹⁷N α spectrum: a broad ($\Gamma_{ln} = 560 \pm 60 \text{ keV}$) $\frac{3}{2}^{-}$ state at $E_x = 7.56 \pm 0.02$ MeV and possibly a state at 8.18 ± 0.02 MeV with $J^{\pi} = \frac{1}{2}^{-}$ ($\Gamma_{ln} = 79 \pm 8 \text{ keV}$). Although these levels have small alpha widths compared with the states al-

TABLE I. Alpha-emitting states populated by ¹⁷N β decay.

	$E_x[^{17}O]$	(MeV)	Γ_x (keV)		
J^{π}	This work ^a	Ref. [12] ^b	This work ^a	Ref. [12] ^b	
$\frac{1}{2}^{-}$	7.985 ± 0.015	7.990 ± 0.050	407±33	390±39	
$\frac{3}{2}$ -	$8.204 {\pm} 0.006$	$8.197{\pm}0.008$	$43{\pm}10$	53 ± 5.3	

^aFrom a K-matrix analysis; width defined as $2p_{ln}^2 g_{ln}^2$.

^bFrom an *R*-matrix analysis; width defined as $2P_n\gamma_{\lambda n}^2$.

ready seen, making the products $B_{li}g_{l\alpha i}$ likely to be negligible, they can affect the fit through interference in Eq. (2). Additional fits were performed incorporating these states.

The broad $\frac{3}{2}^{-}$ state ($E_{\text{c.m.}} = 1.20 \text{ MeV}$) was included with its energy and neutron width fixed at the literature values and $B_{2i}g_{2\alpha i} = 0$. Interference caused the narrow state at 8.20 MeV ($E_{\text{c.m.}} = 1.84 \text{ MeV}$) to be shifted up in resonance energy by 12 keV and to be broadened by 14 keV. The χ^2 increased slightly to 57.8. The broad $\frac{1}{2}^{-}$ state was unaffected.

Incorporating the 8.18 MeV $\frac{1}{2}^{-}$ state proved difficult, as it is located within the energy region of the intense 8.20 MeV $\frac{3}{2}^{-}$ peak, and the interference with the broad $\frac{1}{2}^{-}$ state takes the form of a sharp minimum, narrower than the experimental resolution. The existence of this level is supported only by the neutron work of Ref. [12], where it was introduced to account for large cross sections at $E_x = 8.2$ MeV. A fit with fixed parameters, as was done for the broad state, gave a χ^2 of 62.9. A χ^2 of 58.5 could be obtained by allowing $B_{0\alpha i}g_{0\alpha i}$ to vary, but the best fit appeared to minimize the effect of the state on the observed spectrum. We conclude that the presence of this level in ¹⁷O is not supported by the ¹⁷N $\beta\alpha$ -decay data.

B. Branching ratios

The determination of the absolute β branching to the α -emitting states in ¹⁷O was based on the relative amounts of ¹⁷N and ¹⁸N, and the known decay of ¹⁸N [7]. The production yields of the three nitrogen isotopes present in the A = 33 beam were determined by gamma counting the ion beam intercepted by a movable Faraday cup situated 0.5 m upstream of the final collector station. A Ge(Li) detector was used to determined ¹⁶N, ¹⁷N, and ¹⁸N yields of $(1.9 \pm 0.5) \times 10^3$, $(8.4 \pm 1.2) \times 10^4$, and $(2.9 \pm 0.4) \times 10^3$ nuclei/s, respectively, based on their characteristic gamma rays [13]. The relative intensity ratio of the 871 to 2184 keV gammas of ¹⁷N was deter-

TABLE II. Branching ratios of ¹⁷N β -delayed α decay.

$E_{ m c.m.}$ (MeV)	$egin{array}{c} etalpha B \ (\%) \end{array}$	$\Gamma_{oldsymbol{lpha}}/\Gamma^{f a}$	βB (%)	$\log ft$
1.844 ± 0.006	$(9.8\pm2.0)\times10^{-4}$	0.077 ± 0.008	$(1.3\pm0.3) imes10^{-2}$	4.02 ± 0.11
$1.629 {\pm} 0.016$	$(1.5 \pm 0.3) \times 10^{-3}$	0.059 ± 0.007	$(2.6 \pm 0.6) \times 10^{-2}$	4.34 ± 0.11
~ 1.2	$< 6.9 imes 10^{-5}$	0.0002	$< 3.5 \times 10^{-1}$	≥ 4.0

^aReferences [11,12].

mined to be 11.1 ± 2.2 , in agreement with the 9.6 ± 0.4 value determined by Alburger and Wilkinson [14], but not with the values of Silbert and Hopkins [15] or Poletti and Pronko [16] (6.8 ± 0.9 and 6.36 ± 0.20 , respectively).

The β -delayed α branching of ¹⁷N was determined from the relative α activities of ¹⁷N and ¹⁸N in the first and second detector pairs and the relative total yields of the two isotopes in the ion beam. The total initial ¹⁸N activity (¹⁸A₀) of the deposited ion beam is given by

$${}^{18}A_0 = {}^{18}Y(1 - \exp\{-\lambda_{18}t\}); \tag{3}$$

where ¹⁸Y is the yield of ¹⁸N as determined by gamma counting the ion beam, λ_{18} is the decay constant of ¹⁸N, and t is the collection time; an analogous relation defines the total activity of ¹⁷N. The total initial ¹⁸N α activity (¹⁸ A_{α}) is given by

$${}^{18}A_{\alpha} = {}^{18}A_0({}^{18}B_{\alpha}), \tag{4}$$

where ${}^{18}B_{\alpha}$ is the total β branching to α -emitting states in 18 O. Again, an analogous relation exists for 17 N. Since the α -detection efficiency for both isotopes is the same, the ratio of total α activities of 18 N and 17 N is then given by

$$\frac{{}^{18}A_{\alpha}}{{}^{17}A_{\alpha}} = \frac{{}^{18}A_0({}^{18}B_{\alpha})}{{}^{17}A_0({}^{17}B_{\alpha})}.$$
 (5)

Clearly, the total ¹⁷N β -delayed alpha branching ratio (¹⁷ B_{α}) can be determined from the measured ratios of total activities and alpha activities if the β -delayed α branching of ¹⁸N is known.

The β -delayed α branching of ¹⁸N was taken at 12.2 \pm 0.6%, the sum of the branches of the three dominant alpha peaks in the decay of ¹⁸N reported in Ref. [7]. The total $\beta\alpha$ -decay branching of ¹⁷N was then determined to be $(2.5 \pm 0.4) \times 10^{-5}$ using Eq. (5). The $\beta\alpha$ branches to the individual ¹⁷O states were determined by partitioning the total $\beta\alpha$ branching by the relative intensities of the two alpha peaks as determined by the *K*-matrix analysis. These branching ratios are only lower limits of the β branching to the two ¹⁷O states, until account is taken

of the competing, dominant, β -delayed neutron emission from these states. Absolute β -decay branches were calculated by using the relevant alpha and total widths of the ¹⁷O excited states as determined by Fowler, Johnson, and Feezel [11] and Johnson [12]. The results are presented in Table II with log ft values as determined using the tables of Gove and Martin [17].

Although two states are sufficient to fit the α spectrum with a *K*-matrix parametrization, the possibility of an additional β decay to a broad state at 7.56 MeV in ¹⁷O cannot be entirely discounted. The small alpha width of this state [11,12] does not allow its α decay to be resolved from that of the broad 7.99 MeV state. An upper limit for the branching ratio to this state has been included in Table II based on the estimate that $\leq 3\%$ (100 counts) of the total α spectrum may result from the decay of this state.

V. COMPARISON WITH ¹⁷N MIRROR DECAY

The β -delayed proton decay of ¹⁷Ne was reported in detail by Hardy et al. [18]. More recently, Borge et al. [19] have remeasured the proton spectrum with improved statistics and have, additionally, observed β -delayed α emission. Both studies reported β decay to three states in 17 F with log ft and J^{π} values that are consistent with an assignment as mirror decays of the present work. Table III shows the comparison with the data of Ref. [19], in which the J^{π} assignments of the ¹⁷F states are based on a $\frac{3}{2}^{-}$ assignment for the 8.2 MeV (¹⁷F) level. This assignment is, in turn, based on the assumption that the 8.2 (¹⁷F) MeV state is the mirror level of the 7.56 MeV state in ¹⁷O [20]. Consequently, the 8.2 and 7.99 MeV states of ¹⁷O would be the mirror levels of the 8.08 and 8.43 MeV states, respectively, of ¹⁷F. This assignment is further supported by the fact that no delayed α emission is observed from either the 8.2 MeV state of ¹⁷F [19] or the 7.56 MeV state of ¹⁷O. Also included in Table III are the corresponding comparisons for the lower-lying negative parity states given in Ref. [19].

		1		U		
¹⁷ N decay			¹⁷ Ne decay			
¹⁷ O*		0	${}^{17}F^{*}$		·	Asymmetry
(MeV)	J^{π}	$\log ft$	(MeV)	J^{π}	$\log ft^+$	$\delta = [ft^+/ft^-] - 1$
8.2	$\frac{3}{2}^{-}$	4.02 ± 0.11	8.08	$\frac{3}{2}^{-}$	3.93 ± 0.06	-0.19 ± 0.29
7.99	$\frac{1}{2}$ -	4.34 ± 0.11	8.43	$\frac{1}{2}$ -	4.05 ± 0.11	-0.49 ± 0.16
7.56	$\frac{3}{2}$ -	> 4.0	8.2	$\frac{3}{2}$ -	4.51 ± 0.06	< 2.0
5.94	$\frac{1}{2}$ -	4.35 ± 0.03	6.04	$\frac{1}{2}$ -	4.55 ± 0.01	0.58 ± 0.12
5.38	$\frac{3}{2}$ -	3.86 ± 0.02	5.49	$\frac{3}{2}$ -	3.81 ± 0.01	-0.10 ± 0.04
4.55	$\frac{3}{2}$ -	4.41 ± 0.02	4.65	$\frac{3}{2}$ -	4.58 ± 0.01	0.47 ± 0.08
3.06	$\frac{1}{2}$ -	7.08 ± 0.08	3.10	$\frac{1}{2}$ -	7.11 ± 0.11	0.1 ± 0.3

TABLE III. Comparison of mirror decays of ¹⁷N and ¹⁷Ne.^a

^aThe $\log ft^+$ values for the three highest energy states of ¹⁷F have been calculated using the branching ratios given in Ref. [19]. The $\log ft$ and asymmetry values for the four lower energy states of both isotopes are taken from Table 6 of Ref. [19].

VI. SUMMARY

Two weak branches of β -delayed α decay of ¹⁷N have been observed through excited states at 8.204 and 7.985 MeV in ¹⁷O. These account for $(2.5 \times 10^{-3})\%$ of the total ¹⁷N decay. The deduced ¹⁷O state energies and widths agree well with previous measurements using ¹³C(α, n) and ¹⁶O(n, n) reactions. In comparing the strengths of the allowed mirror decays in mass 17, it is noted that the transition to the third $\frac{1}{2}^{-}$ state is substantially stronger in ¹⁷N than in ¹⁷Ne, whereas the reverse is true of transitions to the second $\frac{1}{2}^{-}$ states.

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