Near yrast states in doubly odd ²¹⁴Fr

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High spin states of doubly odd 214 Fr₁₂₇ have been investigated using in-beam γ -ray and conversion electron spectroscopy techniques through the 206 Pb $(^{11}$ B,3n) and 208 Pb $(^{11}$ B,5n) fusion-evaporation reactions. Completely new spectroscopic information has been obtained. The yrast level structure is established up to spin (19^+) and some information on γ transitions from higher-lying levels is also obtained. Two new isomers $T_{1/2} = 174(20)$ ns and $T_{1/2} = 11(2)$ ns were found. Configuration assignments for the low-lying levels are discussed. Information on residual proton-neutron interactions is extracted.

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I. INTRODUCTION

The region of the nuclear chart between the double closed shell nucleus ²⁰⁸Pb and the well-deformed actinides is rich in structural changes. In particular, in the last decade, this region has become the object of numerous studies related to the discovery of very low-lying negative-parity collective states indicating the presence of an octupole instability and eventually stable octupole deformation. Most of the available experimental information, however, refers to even-even and odd-mass nuclei [1-12]. Comparatively little is known from in-beam studies on doubly-odd isotopes in this region [13-16]. A microscopic understanding of the development of collectivity will probably demand a better knowledge of residual proton-neutron (p-n) interactions which is contained in the evolution of the *p*-*n* $(j_{\pi} \otimes j_{\nu})_{J^{\pi}}$ multiplets. The present study of ²¹⁴Fr is carried out as a contribution in that framework.

Prior to this study no γ transitions were known in ²¹⁴Fr. The only previous information was the existence of two isomeric α -emitting states [17], namely, $I^{\pi} = (1^{-})$ of $T_{1/2} = 5$ ms and $I^{\pi} = (9^-)$ of $T_{1/2} = 3.4$ ms. So far the excited (9^-) state in ²¹⁴Fr was proposed exclusively on the basis of energy differences of α -particle groups stemming from this excited state and decaying into ²¹⁰At (Ref. [18]). Results of a contemporary study of 214 Fr by Byrne et al. [19] indicate an 8^- state, 45 keV below the 9^- , with a half-life of 4.9 ms, and the (1^-) as the two

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lowest-lying α -decaying states along with a rather complete level scheme very similar to the one presented in this paper.

The major difference between the two schemes is the relative ordering of the 143.2-299.2 keV and 312.7 - 118.7 keV transitions. There is a clear support for our placement in the first case, due to the existence of a 607.0 keV line, which is observed in the γ - γ coincidence spectra when gating on the 299.2, 312.7, and 471.8 keV transitions. The order of the 312.7-118.7 keV transitions is strongly supported by the intensity balance in the coincidence data. The E1 character of the 312.7 keV line follows from the conversion electron measurements. A coincidence intensity balance in spectra gated on transitions above the (17^+) state indicates an M1 character for the 118.7 keV line, while the ordering shown in Fig. 2 arises from balance in spectra gated on transitions below the (15^-) state.

Finally, the level scheme presented by Byrne *et al.* [19], reaches higher spin states being more complete above the (17^+) state, possibly due to the different reactions used in the two γ - γ coincidence experiments.

Here we report on the low and medium spin structures of ²¹⁴Fr where two isomers have been observed. Preliminary results of this work were reported earlier [20].

II. MEASUREMENTS AND RESULTS

Our measurements comprise gamma-ray excitation functions (in the 64-80 MeV energy range) and conversion electron spectra using the 208 Pb $(^{11}B,5n)$ fusion-evaporation reaction and were performed at the TANDAR Laboratory in Buenos Aires. γ - γ Compton

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^{*}Deceased.

suppressed (CS) coincidences and γ -beam time distributions were measured through the ²⁰⁶Pb(¹¹B,3n) reaction at 55 MeV using the Nuclear Structure Facility at the State University of New York at Stony Brook.

Two delayed transitions of 11(2) and 174(20) ns were assigned to ²¹⁴Fr by means of excitation functions and γ - γ coincidences. The half-life of these two isomers was obtained via a ¹¹B pulsed-beam measurement. The γ - γ coincidences were performed with the Stony Brook 30% CS HPGe and BGO filter array. Three representative gates are shown in Fig. 1. The conversion electron measurement was made through the ²⁰⁸Pb(¹¹B,5n)²¹⁴Fr at 73 MeV with a permanent magnet BaFe miniorange filter in conjunction with a liquid-N₂-cooled Si(Li) (300 mm² × 2 mm) detector positioned at 135° with respect to the beam direction. The conversion coefficient results are summarized in Table I.

Excited states in ²¹⁴Fr were studied and a level scheme up to an excitation energy of 3.6 MeV (Ref. [20]) was established (see Fig. 2). The excitation energies in ²¹⁴Fr are given relative to the $I^{\pi} = (9^{-})$ state. An intense γ ray of 471.8 keV, which is in delayed coincidence with all the transitions assigned to ²¹⁴Fr and decays with a half-life of 174(20) ns, is hence proposed to establish an isomeric state (see Fig. 2). This transition is the most important line in the conversion electron spectrum (Fig. 3) and has M2 character (Table I). The strong 1023.0 keV E3 transition and the competing 580.5 keV M2 line, both decaying with a half-life of 11(2) ns (see Fig. 2), establish the second isomeric level at 1494.8 keV excitation energy.

The other transitions below the 1495 keV level have all M1 or E2 character. An intensity balance does not allow an unambiguous determination of the sequence of the 143.3 and 299.2 keV transitions. Their relative position in the level scheme was fixed by the parallel 607.0 and 906.5 keV weak transitions, and an indication of the deexcitation of the 1378 keV level through the 53.2 keV line, observed in coincidence spectra. The multipolarities of the 71.5(M1) and 135.1(E2) keV transitions which de-



FIG. 1. Gamma-ray spectra gated on three representative transitions assigned to 214 Fr. The spectra correspond to the 206 Pb $(^{11}B,3n)$ reaction at 55 MeV.



FIG. 2. Experimental level scheme of ²¹⁴Fr from the present study. The excitation energies are given relative to the $I^{\pi} = (9^{-})$ state.



FIG. 3. Conversion electron spectrum from the reaction 208 Pb $(^{11}B,5n)^{214}$ Fr at 73 MeV.

populate the 1566 keV state were assigned by intensity balance in coincidence spectra and similarly for the 118.7 keV line.

The E1 character of the 312.7 keV line follows from the conversion coefficient measurement and the relative position of this and the 118.7 keV transitions follows from coincidence intensity considerations.

The part of the scheme above the 1997.8 keV level is substantiated by the γ - γ coincidence data. The relative weakness of these lines only allows to tentatively assign a spin-parity of (19⁺) to the 2898.8 keV level (from the E2 multipolarity of the 892.0 keV line).

TABLE I. γ -ray energies and intensities, theoretical (Ref. [29]) and experimental conversion coefficients, total transition intensities, and adopted multipolarities. The electron data correspond to the ${}^{208}\text{Pb}({}^{11}\text{B},5n)$ ${}^{214}\text{Fr}$ reaction at 73 MeV.

$\begin{array}{c} E_{\gamma}^{\mathbf{a}} \\ (\mathrm{keV}) \end{array}$	I_{γ}	$egin{array}{c} E1 \ lpha_K^{ m th} \ E2 \ M1 \end{array}$	$lpha_K^{ ext{exp}}$	$egin{array}{cc} E1 \ lpha_L^{ m th} & E2 \ M1 \end{array}$	$lpha_L^{ ext{exp}}$	$egin{array}{cc} E1\ lpha_M^{ m th} & E2\ M1 \end{array}$	$lpha_M^{ ext{exp}}$	I^{Tot}	Adopted Multip.
53.2 64.2 71.5 118.7 135.1 ^{b,c}	$0.7(2) \\ 0.9(2) \\ 8(2) \\ 6.0(4) \\ 3.4(7)$							$1.1(2) \\ 9(2) \\ 75(15) \\ 61(4) \\ 12(2)$	$E1^{ m d}\ M1^{ m d}\ M2^{ m d}$
$ \begin{array}{c c} 143.3 \\ 209.2^{b,c} \\ 228.0 \end{array} $	1.7(3) 11(2) 3.0(5)							16(3)	$M1^{ m d}$
299.2	13(2)	0.028 0.070 0.590	0.45(18)	$\begin{array}{c} 0.005 \\ 0.056 \\ 0.116 \end{array}$	0.16(6)	$0.0011 \\ 0.015 \\ 0.028$	0.048(20)	22(4)	M1
300.05	9(2) 100(5)	$0.024 \\ 0.060 \\ 0.470$	0.032(13)					100(8)	E1
382.4 442.8	12(2) 5.2(6)	$0.012 \\ 0.032 \\ 0.173$	0.22(4)	$0.0015 \\ 0.013 \\ 0.031$	0.042(9)	$0.0004 \\ 0.0036 \\ 0.008$	0.0054(20)	5.4(6)	M1
471.8	63(3)	$0.028(E2) \ 0.182(M1) \ 0.438(M2)$	0.41(8)	$0.0123 \\ 0.031 \\ 0.103$	0.10(2)	$\begin{array}{c} 0.0028 \\ 0.007 \\ 0.025 \end{array}$	0.023(4)	98(5)	M2
509.0 ^b	3.5(7)	0.009		0.0015		0.020		3.5(7)	$E2^{\mathrm{d}}$
516.7	19(3) 3 5(7)	$\begin{array}{c} 0.025\\ 0.148\end{array}$	0.018(5)	$\begin{array}{c} 0.0102\\ 0.023\end{array}$	0.004(2)			19(3)	E1 E2 ^d
580.5	7.4(7)	$0.019(E2) \ 0.115(M1) \ 0.300(M2) \ 0.0054$	0.23(4)	$\begin{array}{c} 0.006 \\ 0.019 \\ 0.068 \end{array}$	0.073(15)	$0.0015 \\ 0.0036 \\ 0.017$	0.037(8)	10(1)	M2
607.0 ^b	2.6(5)	0.0064 0.021 0.101	0.21(5)					3.0(6)	M1
738.3	11(2)	0.0035							
892.0	47(9)	0.0091 0.0366 0.003	0.0070(10)	0.0004				15(3)	E2
906.5	3.0(3)	0.008 0.034	0.039(8)	0.0020	0.0065(12)	0.0000		4.0(4)	M1
1023.0	84(4)	$\begin{array}{c} 0.0231(M1) \\ 0.0524(M2) \\ 0.0147(E3) \end{array}$	0.015(3)	$0.004 \\ 0.0103 \\ 0.0046$	0.0042(8)	0.0009 0.0025 0.0012	0.0008(3)	84(4)	E3

^aErrors in E_{γ} are about 0.2 keV.

^bContaminated lines. Relative intensities were deduced from coincidence spectra.

^cTheoretical values from Ref. [29].

^dThe multipolarities result from an intensity balance in coincidence spectra.

III. DISCUSSION

Figure 4 shows the one-quasiparticle energies for neutrons (a), E_{ν} , and protons (b), E_{π} , vs the number of protons and neutrons, respectively, above the N = 126, Z = 82 double magic gap, relative to the ground state of each nucleus [namely, relative to $E_{\pi h_{9/2}}$ ($E_{\nu g_{9/2}}$) for the odd proton (neutron) nuclei]. From this information it is possible to obtain a zero-order estimate for the excitation energies in $^{213}_{87}$ Fr₁₂₇. The relevant proton energies are obtained from 213 Fr and the neutron energies from 213 Rn. For the $\nu i_{11/2}$ orbit in 213 Rn extrapolated values were used due to lack of experimental information on one-quasiparticle energies. The zero-order energies in ²¹⁴Fr are given in Table II where each entry corresponds to a degenerate $(j_{\pi} \otimes j_{\nu})_{J^{\pi}}$ multiplet.

On the other hand, the matrix element of the effective p-n force, $V_{J^{\pi}=9^{-}}^{\text{eff}}$, between the unpaired $h_{9/2}$ proton and $g_{9/2}$ neutron quasiparticles in the ²¹⁴Fr (or other doubly odd cases) (9⁻) state is given by the difference between the p-n separation energy S_{np} relative to the ²¹²Rn core and the proton and neutron separation energies from the ²¹³Fr and ²¹³Rn ground states, respectively (see Table III):

$$S_{np}(Z+1, N+1, J) - S_{j_{\nu}}(Z, N+1) - S_{j_{\pi}}(Z+1, N)$$

= $-V_{J=9^{-}}^{\text{eff}} = M(Z, N) - M(Z+1, N+1) - [M(Z, N) - M(Z, N+1)] - [M(Z, N) - M(Z+1, N)].$ (1)

 $S_{j_{\nu}}(S_{j_{\pi}})$ are the neutron (proton) separation energies and *M*'s the masses [21] of the different nuclei.

The difference between the excitation energy, E^* , of a state of spin J in the doubly odd nucleus associated predominantly with one configuration $(j_{\pi} \otimes j_{\nu})_{J^{\pi}}$ and the zero-order energy $E_{\pi} + E_{\nu}$, is a measure of the effective residual proton-neutron interaction $V_{J^{\pi}}^{\text{eff}}$, correcting for the proton-neutron force in the (9⁻) state. The equation expressing these relations is:

$$E^* - E_{j_{\pi}} - E_{j_{\nu}} + V_{9^-}^{\text{eff}} = V_{J^{\pi}}^{\text{eff}}.$$
 (2)

The values of $V_{J\pi}^{\text{eff}}$ so obtained are given in Table III for the three isotones ²¹⁰Bi (which is nearest to the bare *p*-*n* force), ²¹²At and ²¹⁴Fr.

The largest amplitude in the wave function of the (9^-) state in ²¹⁴Fr is most likely associated with the stretched coupling $(\pi h_{9/2} \otimes \nu g_{9/2})_{9^-}$. In this configuration it is reasonable to expect that the *p*-*n* effective interaction is



FIG. 4. Single quasiparticle energy evolution for protons (a) and neutrons (b) beyond the doubly closed shells, Z = 82 and N = 126. All energies are relative to the $\nu g_{9/2}$ and $\pi h_{9/2}$ ground states.

small [14], due to the fact that the proton Fermi level is approximately in the middle of the $h_{9/2}$ shell corresponding to occupation amplitudes, $v_{\pi} = u_{\pi} = 1/\sqrt{2}$, while the neutron Fermi level lies at the beginning of the $g_{9/2}$ shell. It is worth recalling that the expression for the effective *p*-*n* interaction becomes (Ref. [22]) $V_{J\pi}^{\text{eff}} = u_{\pi}^2 V_{J\pi} + v_{\pi}^2 V_{J\pi}^{-1}$ where $V_{J\pi} = \langle (j_{\pi} \otimes j_{\nu})_{J\pi} | V_{p-n} | \rangle$ and $V_{J\pi}^{-1} = \langle (j_{\pi}^{-1} \otimes j_{\nu})_{J\pi} | V_{p-n} | \rangle = -V_{J\pi}$. This is borne out in the first row of Table III: $V_{J\pi}^{\text{eff}} = -199$ keV as compared to the bare value -398 keV in ²⁰⁹Bi.

The $I^{\pi} = (11^+)$ assignment for the first excited state follows from the M2 character of the isomeric transition of 472 keV and its most probable configuration is $(\pi i_{13/2} \otimes \nu g_{9/2})_{11^+}$. One expects in this case a strongly attractive p-n interaction due to the particle character of both excitations, which turns out to be -832 keV, relatively close to the ²¹⁰Bi value. With these assignments the M2 character of the 472 keV transition is associated to the proton orbit change $\pi i_{13/2} \longrightarrow \pi h_{9/2}$. The $B(M2) = 12.6(1.4)\mu_N^2$ fm² [the Weisskopf value is $B(M2)_W \simeq 60\mu_N^2$ fm²] obtained from the experimental

TABLE II. Zero-order excitation energies for seniority-2 configurations in 214 Fr. The proton (neutron) single quasiparticle energies are taken from 213 Fr (213 Rn) and are measured relative to their ground states (see text).

E_{ν} (keV)	E_{π} keV)	$h_{9/2}$ 0	f _{7/2} 498	i _{13/2} 1105
<i>g</i> _{9/2} 0		0	498	1105
$rac{i_{11/2}}{570}$		570	1068	1675
$j_{15/2} \\ 896$		896	1394	2001

TABLE III. $V_{p=n}^{eff}$ matrix element evolution for (in keV) some relevant two-quasiparticle configurations in the N=127 isotones ²¹⁰Bi, ²¹²At, and ²¹⁴Fr (see text).

		$V_{J^{\pi}}^{\mathrm{eff}}~(\mathrm{keV})$	
Configuration	²¹⁰ Bi	²¹² At	²¹⁴ Fr
$(\pi h_{9/2} \otimes u g_{9/2})_{9^-}$	-398	-265	-199
$(\pi i_{13/2}\otimes u g_{9/2})_{11^+}$	-961	(-957) ^a	-832
$(\pi h_{9/2} \otimes u j_{15/2})_{12^+}$	-622	-280	-181
$(\pi i_{13/2}\otimes u j_{15/2})_{14^-}$	-966	b	-705
	L.		

^aTentatively assigned in ²¹²At (Ref. [11]).

^bThe 14⁻ state is not known in ²¹²At.

half-life, $T_{1/2} = 174(20)$ ns of the $(11^+, 472 \text{ keV})$ level is in fact comparable to the $B(M2) = 18(12)\mu_N^2$ fm² extracted [17] from the 1.608 MeV transition in ²⁰⁹Bi, which is normally associated with the single particle transition between the $i_{13/2}$ and $h_{9/2}$ proton orbitals. The value in ²¹⁴Fr is very similar to those measured in the odd-odd nuclei ²¹²At (Ref. [13]), ²¹⁶Fr (Ref. [23]) and ²¹⁸Ac (Ref. [14]).

The other isomeric state assigned in the present work is the (14⁻) at 1495 keV with a half-life of $T^{1/2} = 11(2)$ ns. It decays mainly through an enhanced E3 transition of 1023 keV with a $B(E3) \simeq 83(15)10^3 \ e^2 \, {\rm fm}^6$ $(\simeq 30 \text{ Weisskopf units})$, which is very similar to the value for the $\nu j_{15/2} \longrightarrow \nu g_{9/2}$ transition in ²⁰⁹Pb [$B(E3) \simeq$ 70(20)10³ e^2 fm⁶ (Ref. [24])]. The suggested configuration is $(\pi i_{13/2} \otimes \nu j_{15/2})_{14^-}$. It has the maximum possible spin within the available seniority two proton-neutron configuration space defined in Table II. The excitation energy of this state implies, within this simple picture, an attractive p-n interaction of the order of -705 keV, similar to the situation for the (11^+) state to which it decays. The admixture of a collective octupole component $(3^- \otimes \nu g_{9/2})$ into the particle state $\nu j_{15/2}$ (and $3^- \otimes \nu j_{15/2}$ into $\nu g_{9/2}$) is most likely responsible for the observed enhancement of the E3, 1023 keV, transition given the similarity to ²⁰⁹Pb. The 3⁻ in this case corresponds to the particle-hole phonon of ²⁰⁸Pb (Ref. [25]). Obviously a more sophisticated calculation allowing for the phonon admixture may modify the value of the estimated p-n force.

The only seniority-two configurations which can contribute to the (12^+) state at 914 keV are $(\pi h_{9/2} \otimes \nu j_{15/2})$

and $(\pi i_{13/2} \otimes \nu i_{11/2})$, the first one being the more likely candidate due to its lower zero-order energy (though this conclusion has to be taken with caution because of the possible presence of differing contributions from the *pn* force). The isomeric (14^-) decays to this (12^+) state through an *M*2 transition of 580.5 keV with a B(M2)of $5.5(1.0)\mu_N^2$ fm². The comparison of this value with the $B(M2) = 18(12)\mu_N^2$ fm² for the $\pi i_{13/2} \rightarrow \pi h_{9/2}$ in ²⁰⁹Bi (Ref. [17]) and $B(M2) = 33(8)\mu_N^2$ fm² for the $\nu j_{15/2} \rightarrow \nu i_{11/2}$ in ²⁰⁹Pb (Ref. [24]), might suggest a larger $(\pi h_{9/2} \otimes \nu j_{15/2})$ component in the (12^+) state, although a destructive interference of both terms cannot be ruled out (Ref. [26]).

The large attractive values for the proton-neutron effective force in the $(\pi i_{13/2} \otimes \nu g_{9/2})_{11^+}$ and $(\pi i_{13/2} \otimes$ $\nu j_{15/2})_{14^-}$ terms imply that the occupation of the $\pi i_{13/2}$ and $\nu j_{15/2}$ orbits will tend to increase significantly in the light actinide open-shell nuclei beyond the zero p-n force occupation values, thus providing a microscopic basis for the development of valence-shell octupole collectivity connected with a coherent superposition of twoquasiparticle states like $\nu(j_{15/2}g_{9/2})$ and $\pi(i_{13/2}f_{7/2})$. This reasoning resembles the Federman-Pittel (Ref. [27]) mechanism for the quadrupole degree of freedom and is in line with the discussion in Ref. [28] about the onset of collectivity, in particular, in the actinide region. In fact the interaction between $\pi h_{9/2}$ and $\nu g_{9/2}$ is comparatively weak in comparison to the n-n (or p-p) force (Ref. [28]) and significantly smaller than the one between the $\pi i_{13/2}$ and $\nu g_{9/2}$, $\nu j_{15/2}$ orbits. Apparently the appearance of octupole collectivity requires at least 5 protons and 3 neutrons outside closed shells as shown in a study on ²¹⁶Fr (Ref. [15]).

IV. CONCLUSIONS

²¹⁴Fr has been studied using γ -ray and e^- spectroscopy techniques following the ²⁰⁶Pb(¹¹B,3n) and ²⁰⁸Pb(¹¹B,5n) reactions. A completely new near-yrast level scheme has been obtained for ²¹⁴Fr up to an excitation energy of 3.6 MeV. Starting from the spin and parity assignments, and the half-life measurements, dominant configurations for several states are suggested and estimated values for the effective proton-neutron interaction are extracted suggesting a relation between the onset of collectivity and the strong proton-neutron force acting between $\pi i_{13/2}$ and $\nu g_{9/2}$, $\nu j_{15/2}$ single particle states which thus promotes the occupation of the intruder orbits $\pi i_{13/2}$ and $\nu j_{15/2}$.

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