Core polarization effect on the discrete proton hole states of ²⁰⁵Tl

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The distribution of the discrete proton hole states of 205 Tl has been obtained within the hole-core vibrational scheme. The theoretical single-hole distribution pattern of these low-lying spin states has been discussed in the light of the recent experimental results based on the 208 Pb(\vec{p}, α) reaction. Side by side, the shell-model hole states of the 205 Tl have been compared with the hole states of the 207 Tl to prove the rigid collectivity of the 206 Pb nucleus.

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I. INTRODUCTION

In recent years various experimental data have been obtained to understand the shell-model aspect of the discrete low-lying neutron and proton hole states of ²⁰⁸Pb [1-3] and ²⁰⁶Pb [4]. The distributions of the $3s_{1/2}$ proton states of ²⁰⁷Tl [1] and the $2f_{7/2}$ neutron state of ²⁰⁷Pb [3] clearly indicate the nature of the deviation of the shell-model identity of these two discrete low-lying spin states. This invariably exhibits explicitly the strong interaction of the collective vibrational states of ²⁰⁸Pb nuclei with single-particle proton or neutron states. The outcome of this interaction bears relevance to contemporary theoretical calculations on the shell-model aspect of discrete spin states in the vicinity of ²⁰⁸Pb. We will discuss this theoretical aspect in Sec. IV. The present research deals with the effect of the core polarization on low-lying spin states of ²⁰⁵Tl, and side by side, we will compare the results on ²⁰⁵Tl with those of ²⁰⁷Tl to prove the rigid collec-

tivity of the ²⁰⁶Pb core nucleus. Our theoretical work is based on recent experimental results on the fragmentation of the shell-model proton hole states of ²⁰⁵Tl by the ²⁰⁸Pb(\vec{p}, α) reaction [5]. The proton hole states of ²⁰⁵Tl have been mixed with the vibrational configurations of ²⁰⁶Pb [6] to set up the relevant Hamiltonian matrices for the $\frac{1}{2}^+$, $\frac{3}{2}^+$, $\frac{5}{2}^+$, $\frac{7}{2}^+$, $\frac{9}{2}^+$, and $\frac{11}{2}^-$ states, and the matrices have been diagonalized to obtain the eigenvalues and eigenvectors [7]. The zero-order energies of the proton hole states have been obtained through the numerical solution of the second-order Schrödinger wave equation with existing potential parameters [8].

II. SHELL-MODEL ENERGIES OF THE PROTON HOLE STATES OF ²⁰⁵Tl

To salvage the energies of the proton hole states of ²⁰⁶Pb, we have solved the Schrödinger equation with a potential well consisting of the Woods-Saxon, spin-orbit, and Coulomb terms. The form of the potential well is

$$V = -\left[V_0\left\{1 + \exp\left[\frac{r - r_0 A^{1/3}}{a_0}\right]\right\}^{-1} + V_S \frac{1}{r} \frac{d}{dr}\left\{1 + \exp\left[\frac{r - r_S A^{1/3}}{a_S}\right]\right\}^{-1} + \mathbf{L} \cdot \mathbf{S}\right] + V_C(r) , \qquad (1)$$

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where

$$V_{C}(r) = \begin{cases} \frac{1.44Z}{2R} \left[3 - \frac{r^{2}}{R_{C}} \right] & \text{for } r < R_{C} ,\\ \frac{1.44Z}{4} & \text{for } r > R_{C} , \end{cases}$$

and

 $R_C = r_C A^{1/3}$.

III. HOLE-CORE COUPLING MODEL

The total Hamiltonian of the hole-core interaction scheme is [7]

$$H = H_p + H_{\rm vib} + H_{\rm int} \ . \tag{2}$$

Here $\langle H_p \rangle$ and $\langle H_{\rm vib} \rangle$ signify the energies (in MeV) of the shell-model proton states and the collective vibrational states of the ²⁰⁶Pb, respectively. $H_{\rm int}$ is the interaction Hamiltonian. For the distortion of the collective core due to the core polarization effect, the main coupling term for $H_{\rm int}$ is linear in the vibrational amplitude $\alpha_{\lambda\mu}$. In the spherical nucleus, the coupling is the scalar product of the tensors $\alpha_{\lambda\mu}$ and $Y_{\lambda\mu}$ for the shape vibration and so $H_{\rm int}$ is

$$H = (2\lambda + 1)^{1/2} K(r) \left[\sum_{\mu} \alpha_{\lambda\mu} Y_{\lambda}(\theta, \phi) \right]_{0}$$
$$= (2\lambda + 1)^{1/2} K(r) \left[\alpha_{\lambda} Y_{\lambda}(\theta, \phi) \right]_{0}.$$
(3)

The zero-point amplitude for the individual $\lambda\mu$ mode of the collective vibrational state $(\alpha_{\lambda})_0$ is

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TABLE I. Potential parameters and shell-model energies of the proton hole states of ²⁰⁵Tl from the core-polarization effect. $V_0 = 64.366$ MeV, $r_0 = 1.18$ fm, $a_0 = 0.64$ fm, $V_S = 32.38$ MeV, $r_S = 1.134$ fm, $a_S = 0.785$ fm, and $r_C = 1.184$ fm.

Hole states	3s _{1/2}	$2d_{3/2}$	$2d_{5/2}$	1g _{7/2}	$1g_{9/2}$
Energies	0.800	1.020	2.590	4.300	8.470
(MeV)	$2p_{1/2}$	$2p_{3/2}$	$1f_{5/2}$	$1f_{7/2}$	$1h_{11/2}$
	8.930	9.920	11.980	14.840	1.610

$$(\alpha_{\lambda})_{0} \equiv [\langle n_{\lambda} = 0 | \alpha_{\lambda}^{2} | n_{\lambda} = 0 \rangle]^{1/2}$$
$$= \langle n_{\lambda} = 1 | \alpha_{\lambda} | n_{\lambda} = 0 \rangle = \frac{(4\pi G_{\lambda})^{1/2}}{Z(\lambda + 3)} ,$$
$$G_{\lambda} = \frac{B(E\lambda)}{B(E\lambda)_{W,W}} .$$
(4)

1 -1 /2

The radial function K(r) in H_{int} [Eq. (3)] is

1 21

- /

$$K(r) = -r\frac{dV}{dr} . (5)$$

The matrix elements of K(r) are determined by numerical integration utilizing harmonic-oscillator wave functions for the proton shell-model orbitals. The Hamiltonian H has been diagonalized by using the wave function for the $J=j_1$ spin state as

$$\varphi_J = \sum_{\lambda j_2} a_{\lambda j_2} | n_{\lambda}; \lambda j_2, j_1 \rangle .$$
(6)

Here j_2 and λ are the angular momenta for the proton hole state and vibrational state, respectively. Vectorially,

$$\lambda + \mathbf{j}_2 = \mathbf{j}_1 \,. \tag{7}$$

The matrix elements of H_{int} in the $|\lambda j_2\rangle$ basis [Eq. (6)] is

$$\langle n_{\lambda} = 1; \lambda j_{2}, j_{1} | H_{\text{int}} | n_{\lambda} = 0, 0 j_{1}, j_{1} \rangle$$

$$= \langle j_{2} | K(r) | j_{1} \rangle \langle j_{2} \| Y_{\lambda} \| j_{l} \rangle (2 j_{1} + 1)^{-1/2} \langle \alpha_{\lambda} \rangle .$$

$$(8)$$

IV. RESULTS AND DISCUSSION

The proton hole states as exhibited in Table I have been combined with collective vibrational states, shown in Table II, to set up the Hamiltonian matrices of the $\frac{1}{2}^+$, $\frac{3}{2}^+$, $\frac{5}{2}^+$, $\frac{7}{2}^+$, $\frac{9}{2}^+$, and $\frac{11}{2}^-$ spin states of ²⁰⁵Tl (Table III). The results of the diagonalization of the matrices are depicted in Tables IV-IX. First of all, we have calculated the energies of the shell-model hole states (Sec. III) with the potential parameters listed in Table I. The calculated

energies have been optimized using a χ^2 minimization procedure for the diagonalization to reproduce the shell-model states of the $\frac{1}{2}^+$, $\frac{3}{2}^+$, $\frac{5}{2}^+$, and $\frac{11}{2}^-$ states of ²⁰⁵Tl. The main contribution of the collective state for the fragmented spin state is also shown side by side in the same tables. The spreading of the discrete state indicates the strong interaction of the shell-model hole states with the collective excited states of the ²⁰⁶Pb core nucleus. Comparison of the experimental results (Table III) with the theoretical results (Tables IV-IX) indicates that our calculated results support the experimental ones for the $3s_{1/2}$, $2d_{3/2}$, $2d_{5/2}$, and $1h_{11/2}$ hole states of ²⁰⁵Tl. The experimental results listed in Table III show the nature and distribution of the hole states with regard to their shell-model identities. A quantitative comparison of the experimental results with the present theoretical ones is difficult to reproduce because of the uncertainties in the evaluation of the spectroscopic factors from the distorted-wave Born approximation differential cross sections $(d\sigma/dw)_{\rm DW}$. Even the experimental spectroscopic factors differ appreciably if the calculations are carried out by finite-range distorted-wave Born approximations based on the double-folded α -particle potential instead of using the usual wave functions derived from general Woods-Saxon potentials [5]. The theoretical results further indicate that the hole strength might extend beyond the excitation energies quoted in the corresponding experimental results [5]. The physical reason for the spreading is due to the coincidence of the zero-order shell-model energies (Table I) for the above hole states with hole-coupled vibrational configurations. The frag-ments of the $1g_{9/2}$ shell-model hole state of ²⁰⁵Tl must lie in a higher excitation energy region as its unperturbed energy centers around 8.47 MeV (Table I). In any event, the shell-model hole strengths of these two high-spin $1g_{7/2}$ and $1g_{9/2}$ hole states are convincingly damped out, as should have occurred, as both the vibrational states and shell-model hole states of ²⁰⁶Pb span a broad excitation energy which forces the mixing of the $1g_{7/2}$ and

TABLE II. Vibrational states of ²⁰⁶Pb. λ^{π} indicates the vibrational spin states. *E* is the energy in MeV, and $\langle \alpha_{\lambda} \rangle$ is the vibrational amplitude of the λ^{π} vibrational state.

λ^{π}	21+	2^{+}_{2}	23	41	4_{2}^{+}	43	44
Ε	0.803	1.469	4.107	1.686	1.998	2.928	4.333
$\langle \alpha_{\lambda} \rangle$	0.030	0.007	0.021	0.014	0.008	0.010	0.018
λ^{π}	6+	8+	3-	5^{-}_{1}	5^{-}_{2}	5_{3}^{-}	
E	4.357	4.580	2.648	2.782	3.558	3.772	
$\langle \alpha_{\lambda} \rangle$	0.015	0.008	0.041	0.008	0.007	0.013	

Ε

1.208

1.760

2.057

2.280

2.484 3.460

4.558

4.652

4.950

5.136 5.177

5.402

5.528

5.986

6.712

6.292

0.025

0.007

0.013

0.012

0.009

0.003

0.005

0.007

TABLE III. Experimental energies and spectroscopic factors of the fragmented states of 205 Tl. *E* is the energy in MeV, and *S* is the spectroscopic factors.

	E	S
$3s_{1/2}$ state	0.000	0.540
	1.218	0.070
	1.829	0.090
$2d_{3/2}$ state	0.207	1.000
• / •	1.141	0.030
	1.342	0.090
	1.694	0.040
	2.222	0.040
	2.749	0.100
$2d_{5/2}$ state	0.619	1.450
0,2	1.575	0.090
	1.860	0.170
	1.946	0.250
	2.838	0.200
	2.885	
$1g_{7/2}$ state	0.923	1.500
0.,,	2.302	0.170
	2.339	0.100
	2.885	
$1g_{9/2}$ state	1.430	1.400
	2.486	0.090
	2.630	0.300
	2.711	0.520
$1h_{11/2}$ state	1.483	0.540
	2.584	0.170

TABLE VI. $2d_{5/2}$ state of ²⁰⁵Tl. $a_{0j_2}^2$ $a_{\lambda j_2} \ (\lambda, j_2)$ $0.683 \ (2_1^+, 3s_{1/2})$ 0.391 $0.823 \ (2_1^+, 2d_{3/2})$ 0.040 $0.508 \ (2_1^+, 2d_{3/2})$ 0.296 $0.962 \ (2_2^+, 3s_{1/2})$ 0.034 $-0.996 (2^+_2, 2d_{3/2})$ 0.004 $0.960 \ (2_1^+, 2d_{5/2})$ 0.026 $-0.611 \ (4_2^+, 2d_{5/2})$ 0.017 $-0.668 (3^-, 1, h_{11/2})$ 0.075

 $0.909~(2^+_3, 3s_{1/2})$

 $-0.785 (2_3^+, 2d_{3/2})$

 $0.873~(5_2^-,1h_{11/2})$

 $\begin{array}{c} 0.961 & (5_{3}^{-}, 1h_{11/2}) \\ 0.689 & (4_{3}^{+}, 2d_{5/2}) \\ -0.996 & (4_{1}^{+}, 1g_{7/2}) \end{array}$

 $0.989 \ (2_3^+, 2d_{5/2})$

 $0.699 (4_4^+, 2d_{5/2})$

 $1g_{9/2}$ states with several hole-vibrational mixed configurations of ²⁰⁵Tl. Comparisons of theoretical results on the low-lying discrete states of ²⁰⁷Tl with the experimental ones [2,9] as exhibited in Table X show explicit less quenching of the hole strengths from their main shell-model orbitals for the $3s_{1/2}$, $2d_{3/2}$, $2d_{5/2}$, and $1h_{11/2}$ states. For the $1g_{7/2}$ orbital, the proton knockout strength is explicitly far less than its sum-rule limit. This is true from experimental [2] and theoretical findings (Table X). We are not yet aware of the quantitative nature of the spreading of the $1g_{9/2}$ state of ²⁰⁷Tl as regards its hole-strength distribution. In spite of this, strong damping of this $1g_{9/2}$ state for both ²⁰⁵Tl and ²⁰⁷Tl is ex-

TABLE IV. $3s_{1/2}$ state of ²⁰⁵Tl. *E* is the energy of the fragmented states in MeV, $a_{\lambda j_2}(\lambda, j_2)$ is the collective configuration of the states, and $a_{0j_2}^2$ is the shell-model hole strength of the fragments.

E	$a_{\lambda j_2} (\lambda, j_2)$	$a_{0j_2}^2$
0.008		0.826
1.979	$0.949 \ (2^+_1, 2d_{3/2})$	0.068
2.489	$-0.996 \ (2^+_2, 2d_{3/2})$	0.003
3.541	$-0.965 \ (2^+_1, 2d_{5/2})$	0.042
4.403	$-0.994 (5_1^-, 1h_{11/2})$	0.005
5.180	$-0.852 \ (5^{-}_{2}, 1h^{+}_{11/2})$	0.005
5.420	$-0.975 (5_3, 1h_{11/2})$	0.010
6.007	$-0.991 \ (4_1^+, 1g_{7/2})$	0.005
6.741	$0.975 \ (2^+_3, 2d_{5/2})$	0.010
8.658	$-0.997 \ (4_4^+, 1g_{7/2})$	0.004
14.792	$-0.997 (3^{-}, 1f_{5/2})$	0.005
17.563	$0.997(3^-, 1f_{7/2})$	0.005

TABLE V. $2d_{3/2}$ state of ²⁰⁵Tl. $a_{0j_2}^2$ Ε $a_{\lambda j_2}$ (λ, j_2) 0.803 0.523 $-0.841 \ (2_1^+, 3s_{1/2})$ 0.051 1.709 $-0.861 \ (2_2^+, 2d_{3/2})$ 0.078 1.889 $-0.995 \ (2^+_2, 3s_{1/2})$ 0.005 2.268 3.460 $-0.982 \ (2_1^+, 2d_{5/2})$ 0.026 6.919 $0.991 \ (2^+_3, 3s_{1/2})$ 0.004

TABLE VII. $1g_{7/2}$ state of ²⁰⁵Tl.

$\frac{1 \text{ABLE VII. } 1g_{7/2} \text{ state of } 100 \text{ II.}}{100 \text{ II.}}$			
Ε	$a_{\lambda j_2}(\lambda, j_2)$	$a_{0j_2}^2$	
1.705	$-0.969 \ (2^+_1, 2d_{3/2})$	0.050	
2.446	$-0.867 (4_1^+, 3s_{1/2})$	0.020	
2.679	$0.975 \ (4_1^+, 2d_{3/2})$	0.012	
2.782	$-0.986 (4_2^+, 3s_{1/2})$	0.004	
3.002	$-0.991 \ (4_2^+, 2d_{3/2})$	0.007	
3.341	$0.936 (2^+_1, 2d_{5/2})$	0.068	
3.634	$(4^+_3, 3s_{1/2})$	0.203	
3.816	$-0.646 \ (4^+_3, 3s_{1/2})$	0.194	
3.976	$0.878 \ (4_3^+, 2d_{3/2})$	0.070	
4.054	$-0.987 \ (2^+_2, 2d_{5/2})$	0.005	
4.346	$0.613 (3^-, 1h_{11/2})$	0.059	
4.405	$-0.845 \ (5_1^-, 1h_{11/2})$	0.047	
4.488	$0.986 \ (4_2^+, 2d_{5/2})$	0.007	
5.287	$0.669 \ (4_4^+, 2d_{3/2})$	0.033	
5.464	$-0.597 (4_3^+, 2d_{5/2})$	0.064	
5.545	$-0.793 \ (4_3^+, 2d_{5/2})$	0.067	
6.007	$0.977 \ (4_1^+, 1g_{7/2})$	0.019	
5.771	$0.983 \ (2_2^+, 1g_{7/2})$	0.009	
6.397	$0.995 \ (4_2^+, 1g_{7/2})$	0.004	
6.987	$0.910 \ (6^+, 2d_{5/2})$	0.019	
7.229	$-0.995 (4_3^+, 1g_{7/2})$	0.003	
8.422	$0.991 \ (2_3^+, 1g_{7/2})$	0.005	
8.664	$0.871 \ (6^+, 1g_{7/2})$	0.005	
11.615	$-0.995 (3^-, 2p_{1/2})$	0.006	
14.654	$0.996 \ (3^-, 1f_{5/2})$	0.003	

 $a_{0j_2}^2$ Ε $a_{\lambda j_2}$ 3.325 $0.986 \ (2_1^+, 2d_{5/2})$ 0.014 $0.923~(3^-,1h_{11/2})$ 4.138 0.029 5.104 $-0.973 (4_4^+, 3s_{1/2})$ 0.006 $\begin{array}{c} 0.576 & (2_{1}^{+}, 2d_{5/2}) \\ 0.706 & (2_{1}^{+}, 2d_{5/2}) \\ 0.954 & (2_{3}^{+}2d_{5/2}) \end{array}$ 5.325 0.008 6.618 0.037 $0.896 \ (4_4^+, 2d_{5/2})$ 0.014 6.982 8.206 $0.307 (4_4^+, 2d_{5/2})$ 0.487 $-0.945 \ (2_3^+, 1g_{7/2})$ 8.417 0.037 $0.765 \ (6^+, 1g_{7/2})$ 0.070 8.716 $0.950 \ (8^+, 1g_{7/2})$ 8.914 0.042 9.479 $-0.870 (4_1^+, 1g_{7/2})$ 0.159 $0.992 \ (2_2^+, 1g_{9/2})$ 9.939 0.006 $0.983~(4_1^+,1g_{9/2})$ 10.176 0.017 $0.996~(4_2^+,1g_{9/2})$ 10.468 0.004 $0.706 \ (6^+, 2d_{5/2})$ 12.655 0.010 $\begin{array}{c} -0.736 \ (5_3^-, 2p_{1/2}) \\ -0.706 \ (6^+, 1g_{9/2}) \end{array}$ 12.716 0.008 12.859 0.018 $0.994 \ (3^-, 2f_{7/2})$ 17.521 0.005

TABLE VIII. $1g_{9/2}$ state of ²⁰⁵Tl.

pected from our hole-core coupling model calculations. A comparison of the theoretical results on the discrete states of ²⁰⁵Tl with that of ²⁰⁷Tl leads to the conclusion of a strong collective vibrational aspect of the ²⁰⁶Pb core nucleus.

There are various theoretical approaches to realize the distribution of the main hole states of both ²⁰⁷Tl and ²⁰⁵Tl. Within the framework of finite nuclear matter and the repulsive short-range potential among nucleons, the depletion of the shell-model hole strengths can be explained because of the scattering of the fermions from the low-lying states to the comparatively highly energetic shell-model orbitals. The theoretical calculations [10] on the Hartree-Fock occupational probabilities of the single-particle orbitals based on the random-phase approximation method and finite nuclear-matter calculations with the short-range and tensor components of the nucleon-nucleon interaction as well as the random-phase approximation calculation incorporated within the nuclear-matter distribution [11] explain the quenching of the shell-model strengths of only the dominantly excited low-lying spin states of ²⁰⁵Tl. The energies and shellmodel hole-strength distribution of the several low-lying

TABLE IX. $1h_{11/2}$ state of ²⁰⁵ Tl.			
E	$a_{\lambda j_2}$ (λ, j_2)	$a_{0j_2}^2$	
1.076		0.834	
2.550	$0.944 \ (2_1^+, 1h_{11/2})$	0.085	
3.077	$-0.996 \ (2_2^+, 1h_{11/2})$	0.003	
3.310	$0.989 \ (4_1^+, 1h_{11/2})$	0.010	
3.608	$0.975 \ (4_2^+, 1h_{11/2})$	0.004	
4.576	$-0.811 (5_3^-, 3s_{1/2})$	0.003	
5.338	$-0.831 (3^{-}, 2d_{5/2})$	0.016	
5.377	$0.853 (5_1^-, 2d_{5/2})$	0.010	
5.737	$-0.978 \ (2_3^+, 1h_{11/2})$	0.007	
5.983	$0.831 \ (6^+, 1h_{11/2})$	0.008	
11.149	$-0.994 (3^-, 1g_{9/2})$	0.004	

TABLE X. Distribution of the proton hole states of 207 Tl. *E* is the energy in MeV and $a_{0j_2}^2$ is the spectroscopic factors. The value in parentheses indicates experimental estimates. For *E* (expt.), see Refs. [2,9].

State	E	$a_{0j_2}^2$
$3s_{1/2}$	0.000 (0.000)	0.940 (0.900)
$2d_{3/2}$	0.344 (0.350)	0.956 (0.950)
$2d_{5/2}$	1.502 (1.670)	0.860 (0.580)
$1g_{7/2}$	3.135 (3.470)	0.719 (0.450)
$1h_{11/2}$	0.912 (1.330)	0.734 (0.640)

discrete states of ²⁰⁷Tl have been calculated [12] by the coupling of the vibrational states of ²⁰⁸Pb with the hole orbitals. But the calculation is restricted to a very few low-lying states, and a significant distribution pattern has not been obtained. The quasiparticle phonon coupling model [13] and self-consistent mixing of the Hartree-Fock states with the phonon vibrational states arising from the random-phase approximation using the Skyrme III effective force [14] have been developed to explain the spreading of the spectroscopic factors of the hole orbitals of ²⁰⁷Tl. But the broad based distribution of the fragmented states of both the two deep hole $1g_{7/2}$ and $1g_{9/2}$ states cannot be explained by these two theoretical approaches. This has been observed when a comparison of the theoretical results with the recent extensive experimental works on the proton hole orbitals of ²⁰⁷Tl has been performed [2]. Very recently, the energies and single-hole strengths of a few discrete levels of ²⁰⁵Tl have been obtained by the multistep shell-model method [15]. There, the matrices of the hole states have been constructed by the coupling of the proton hole states of ²⁰⁷Tl with the two neutron hole states of ²⁰⁶Pb connected by an effective two-body interaction of the Kuo-Brown type. The results obtained by this approach explain excellently the energies and single-hole components of the low-lying spin states. Though the calculation has been extended up to very-high-spin yrast states, still the spreading of the several hole orbitals, particularly the $1g_{7/2}$ and $1g_{9/2}$ ones, cannot be perceived by this theoretical approach. The other theoretical calculations based on the shellmodel aspect [16,17] and semimicroscopic models [18,19] based on the coupling of the hole states with the phonon vibrational states (within a limited basis) of the core nucleus are mainly concerned with the main low-lying hole orbitals of ²⁰⁵Tl.

Our theoretical approach, where a shell-model hole state can mix with the legion number of the collective vibrational states, is able to explain the broad attenuation of the hole strengths of all the discrete shell-model orbitals of ²⁰⁵Tl. Also, none of the hole strengths of the low-lying states center around a particular excitation energy. In our earlier works on the deep hole states of ²⁰⁷Tl [20], we have explained successfully the nature of the fragmentation by incorporating the high-lying vibrational states from the giant resonances of ²⁰⁸Pb within the framework of the hole-core coupling scheme. But there we did not salvage the shell-model energies more realistically as we have done in the present calculations on both ²⁰⁵Tl and

²⁰⁷Tl. In the case of ²⁰⁵Tl, the vibrational states are strongly collective, as has been seen in the present work, and we have allowed an interaction of the hole states with several vibrational configurations of ²⁰⁶Pb. We are interested in the extraction of the spectroscopic factors and fragmented doorway collective states that strip off a sizable percentage of the shell-model hole strength from the main hole state. The Pauli blocking effect might interfere with the microscopic shell-model calculation of ²⁰⁵Tl

- E. N. M. Quint, J. F. J. van den Brand, J. W. A. den Herder, E. Jans, P. H. M. Keizer, L. Lapikas, G. van der Steenhoven, P. K. A. de Witt Huberts, S. Klein, P. Grabmayer, G. J. Wagner, H. Nann, B. Brois, and D. Gontte, Phys. Rev. Lett. 57, 186 (1986).
- [2] H. Langevin-Joliot, E. Gerlic, J. Guillot, and J. Van de Wiele, J. Phys. G 10, 1435 (1984).
- [3] S. Y. Vandirwerf, M. V. Harakeh, and E. N. M. Quint, Phys. Lett. B 216, 15 (1989).
- [4] M. C. Radhakrishna, N. G. Puttaswamy, H. Nann, J. D. Brown, W. W. Jacobs, W. P. Jones, D. W. Miller, P. P. Singh, and E. J. Stephenson, Phys. Rev. C 37, 66 (1988).
- [5] E. Gadioli, P. Guazzoni, S. Mattioli, L. Zetta, G. Graw, R. Hertenberger, D. Hofer, H. Kader, P. Schiemenz, R. Nen, H. Abele, and G. Staudt, Phys. Rev. C 43, 2572 (1991).
- [6] J. E. Fink, G. M. Crawley, J. A. Nolen, and R. T. Kowzes, Nucl. Phys. A407, 163 (1983).
- [7] R. Majumdar, Phys. Rev. C 42, 631 (1990).
- [8] E. Rost, Phys. Lett. 26B, 184 (1968).
- [9] P. Grabmayr, G. Mairle, V. Schmidt-Rohr, G. P. A. Berg,

where the collective states split into the two shell-model hole states. But the effect does not even dominate much in that case inasmuch as the discrete hole states are well separated as has been realized from the present Table I.

In conclusion, we have attempted to explain the fragmentation of the discrete hole orbitals of 205 Tl by the hole-core coupling scheme [7]. The difficulty in explaining this physical aspect of the shell-model states of 208 Pb was faced by several authors a few years ago [2].

- J. Meissburger, P. Von Rossen, and J. L. Tain, Nucl. Phys. A469, 285 (1987).
- [10] V. R. Pandharipande, C. N. Papanocolas, and J. Wambach, Phys. Rev. Lett. 53, 1133 (1984).
- [11] M. Jaminon, C. Mahaux, and H. Ngo, Nucl. Phys. A440, 228 (1985).
- [12] I. Hamamoto, Phys. Rep. 10, 63 (1974).
- [13] V. G. Soloviev, Ch Stoyanov, and A. I. Vdovin, Nucl. Phys. A399, 141 (1983).
- [14] Pham Van Thieu and N. Van Giai (unpublished).
- [15] L. Rydstrom, J. Blomqvist, R. J. Liotta, and C. Pomar, Nucl. Phys. A512, 217 (1990).
- [16] N. A. F. M. Poppelier and P. W. M. Glaudemans, Z. Phys. A 329, 275 (1988).
- [17] B. Silvestre-Brac and J. P. Brouser, Phys. Rev. C 24, 717 (1981).
- [18] N. Azziz and A. Covello, Nucl. Phys. A123, 681 (1969).
- [19] J. W. Smits and R. H. Siemssen, Nucl. Phys. A261, 385 (1976).
- [20] R. Majumdar, J. Phys. G 12, 641 (1986).