# Shell-model description of the $\beta^-$ decay of the N=21 and 22 isotones <sup>34</sup>Al, <sup>36</sup>Si, and <sup>37</sup>P

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The nuclear structure of the parent and daughter nuclei in the decays  ${}^{34}\text{Al}(\beta^{-}){}^{34}\text{Si}$ ,  ${}^{36}\text{Si}(\beta^{-}){}^{36}\text{P}$ , and  ${}^{37}\text{P}(\beta^{-}){}^{37}\text{S}$  are considered in a spherical shell model comprising the (2s, 1d, 1f, 2p) configuration space. Energy spectra and beta and gamma transition strengths are calculated. These predictions are used to construct decay schemes from recent  $\beta^{-}$ -delayed  $\gamma$ -ray singles spectra for the three decaying nuclei. The predicted half-lives of  ${}^{34}\text{Al}$ ,  ${}^{36}\text{Si}$ , and  ${}^{37}\text{P}$  are 0.037(7), 0.8(4), and 2.0(9) s, where the uncertainties are due to mass uncertainties of the decaying bodies. These predictions are in agreement with recent experimental results of 0.050(25), 0.54(15), and 2.31(13) s, respectively.

#### I. INTRODUCTION

The formation of very neutron-rich light ( $A \leq 40$ ) nuclei and the investigation of their decays is an area of research of considerable current interest and activity. Experimental techniques and apparatus have been greatly improved in recent years, as for example at the GANIL (Grand Accélérateur National d'Ions Lourds, Caën, France) intermediate energy heavy-ion facility.<sup>1,2</sup> The spectroscopy of these exotic nuclei is especially revealing of the underlying nuclear structure.<sup>3</sup>

The shell-model predictions presented here for the  $\beta^-$  decay of <sup>34</sup>Al, <sup>36</sup>Si, and <sup>37</sup>P are a continuation of an investigation into the structure of the neutron-rich nuclei in the  $A \leq 40$  region.<sup>4-6</sup> This study utilizes a spherical shell-model interaction designed to describe nuclear levels in the  $A \sim 40$  region for which the nucleons occupy the seven subshells of the (*sd*) and (*fp*) major shells. The dimensions of the matrices involved increase dramatically with the number of nucleons allowed in the (*fp*) shell and also as N - Z decreases. Thus in our first efforts we have concentrated on the simplest of these nuclei, namely N = 21 and 22 isotones with Z < 20.

We recently presented results for the decays of the N = 21 isotones <sup>35</sup>Si and <sup>36</sup>P (Ref. 5). The experimental results for these nuclei were obtained at the GANIL facility by Dufour *et al.*,<sup>2</sup> who also reported decay information for eleven other A < 40 nuclei. Of these, there is one other N = 21 isotone, <sup>34</sup>Al, and two N = 22 nuclei, <sup>36</sup>Si and <sup>37</sup>P. The spectroscopy of these decays is a logical next step in our overall study. Our calculational procedures are described in the next section and results for these three decays are presented in Sec. III.

#### **II. CALCULATION**

The shell-model interaction, designated as WBMB, has evolved somewhat from that used previously.<sup>4-6</sup> It still utilizes an inert <sup>16</sup>O core, the Wildenthal<sup>7,8</sup> "universal" 2s, 1d (USD) interaction for the (sd) shell, and a modified Millener-Kurath<sup>9</sup> (sd) to (fp) cross-shell interaction. One change is to adopt the McGrory<sup>10</sup> in-

teraction to describe the (fp) shell. This results in a much better description of the A = 42-44 Ca and Sc isotopes. The other modification consists of new procedures for joining these three interactions. Briefly, the two-body matrix elements (2BME's) of the USD interaction have an A dependence of  $A^{-0.3}$  and we adopt the same dependence for the Millener-Kurath and McCrory interactions for the A < 40 nuclei of interest here. One further refinement which was found to give better agreement with experimental binding energies is made. Namely, in calculations within a  $(2s, 1d)^{A-16-n}(fp)^n$  model space, the 2BME of the USD are given an A dependence appropriate to A - n rather than A.

The relative values of the single-particle energies (SPE) of the (2s, 1d) and (1f, 2p) orbits are set at the appropriate values of the USD and McGrory interactions. All that remains to be determined is the energy gap,  $\Delta(df)$ , between the (2s, 1d) and (1f, 2p) shells.

For all three interactions, the (SPE) are taken to be mass independent. For the USD interaction, the constancy of the SPE follows since all A dependence is confined to the 2BME in the least-squares fit to binding energies which yields the interaction. The cross-shell interaction is generated from a potential with some adjustment of crucial  $d_{3/2}$ - $f_{7/2}$  and  $d_{3/2}$ - $p_{3/2}$  2BME in order to fit better the A = 40 1p-1h spectra. The energy gap  $\Delta(df)$  is set for best reproduction of A = 35-41 binding energies for states with one or two nucleons in the fpshell. In doing so we note no significant improvement in the root-mean-square deviation from experiment if  $\Delta(df)$  is allowed to vary linearly with A.

Computation in this and the previous work was carried out with the shell-model  $code^{11}$  OXBASH which is formulated in the *m* scheme. Our calculations will be performed in the model spaces  $(sd)^{A-16-n}(fp)^n$  with n = 0, 1, or 2. We shall refer to states in these spaces as nfpstates. Some of the desired calculations involve dimensions which exceed our computer resources, specifically the available disk space. Dimensions relevant to the present study are collected in Table I. The J dimension D(J) is most critical since a  $D(J) \cdot D(J)$  matrix must be diagonalized. The *m* dimension, D(m), also can be a

	$J^{\pi}, T$	Model space	J dimension	m dimension
<sup>34</sup> Al	3-,4	1 <i>fp</i> (full)	380	922
<sup>34</sup> Si	3-,3	1fp (full)	4431	19 105
<sup>35</sup> Si	7/2-,7/2	1fp (full)	424	1299
<sup>35</sup> P	7/2-,5/2	1 f p (full)	3808	14 674
<sup>36</sup> Si	0+,4	2fp (full)	718	19 3 5 4
<sup>36</sup> P	2-,3	1 f p (full)	353	1655
	1+,3	2fp (full)	18870	227 478
	1+,3	2fp(T-A)	3310	42 606
	1+,3	2fp(T-B)	1841	24 304
<sup>37</sup> <b>P</b>	$1/2^+, 7/2$	2fp (full)	1173	16 539
<sup>37</sup> S	$3/2^{-},5/2$	1fp (full)	210	1149
	3/2+,5/2	2fp (full)	16 197	143 727
	3/2+,5/2	2fp(T-A)	3418	32 327
	3/2+,5/2	2fp(T-B)	1944	17 266

TABLE I. Dimensions of 1fp and 2fp model spaces for A = 34-37 nuclei. The truncations T-A and T-B are explained in the text as is the significance of the dimensions. For each model space the dimensions are given only for the J (of those considered) for which they are maximum.

limiting factor since it enters as  $D(J) \cdot D(m)$  in the projection of basis vectors with good J and T. It is the 2fp calculations for <sup>36</sup>P and <sup>37</sup>S which cannot be performed in the full WBMB space. The calculations for the 2fp states of <sup>36</sup>Si and <sup>37</sup>P and the 1fp states of <sup>36</sup>P and <sup>37</sup>S are well within our capabilities, while the matrices involved in the calculation for the 1fp states of <sup>34</sup>Si are the largest we have successfully diagonalized.

In OXBASH, truncation is accomplished by selection of partitions; a partition being a specific occupancy of the subshells included in the model space. In the present case we designate the partitions as

$$[n(d_{5/2}), n(d_{3/2}), n(s_{1/2});$$
  
For <sup>36</sup>P, the scheme *T-A* is composed of the 87 partitions belonging to the sets:  
$$n(f_{7/2}), n(f_{5/2}), n(p_{3/2}), n(p_{1/2})]$$

$$[8-9, \le 8, \le 4; 2, 0, 0, 0] + [10-11, \le 8, \le 4; \le 2, 0, \le 2, 0] + [12, \le 8, \le 4; \le 2, \le 2, \le 2, \le 2].$$
<sup>(1)</sup>

For <sup>37</sup>S, the  $n(d_{5/2})=8$  partitions were omitted. The scheme *T-B* restricted the  $n(d_{5/2})=10$  partitions to  $n(f_{7/2})=2$ , i.e., the same as for the first term of Eq. (1).

It is instructive to consider the partition composition of the wave functions generated by the calculation in scheme T-A. We list the results for  ${}^{36}P J^{\pi} = 1_1^+$  in Table II: these are representative of the first few  $1^+$  states for  ${}^{36}P$  and the first few  $1/2^+$  and  $3/2^+$  states of  ${}^{37}S$ . Consideration of Table II illustrates why truncation of the fp shell as a function of  $n(d_{5/2})$  is successful. The results suggest that < 1% of the total WBMB wave function is omitted by the truncation T-A in spite of the fact that it has a J dimension  $\sim \frac{1}{6}$  of that for the full WBMB space. Indeed, calculations for higher isospin states (in  ${}^{36}Si, {}^{37}P$ , and  ${}^{38}S$ ) and high-spin states in  ${}^{36}P$  and  ${}^{37}S$ , carried out in both full and truncated basis, support this observation. These comparison calculations also present a means of estimating the effect of the truncation on the predicted binding energies. From a comparison of predicted binding energies for 31 states in A = 36-38 nuclei, we find that the scheme T-A underbinds by  $200\pm100$  keV, where the uncertainty is one standard deviation. This comparison indicates a satisfactorily small state dependence for the binding energy shift. The pre-

where n(j) is the occupancy of the subshell j. In an ex-

amination of the effects of truncation, many different

truncation schemes were tried. We were challenged to

obtain the closest approximation possible to a full (2s, 1d, 1f, 2p) calculation for the specific purpose of cal-

culating allowed Gamow-Teller (GT) beta decay. The

truncation T-A of Table I gives dimensions which are

just within the available computer resources for the  ${}^{37}S$   $1/2^+$ ,  $3/2^+$  levels and the  ${}^{36}P$  1<sup>+</sup> levels, and thus could be used for the calculation of the GT beta decays. In or-

der to handle 3/2 < J < 9/2 in <sup>37</sup>P and 1 < J < 6 in <sup>36</sup>P it

was necessary to truncate further to the scheme T-B.

TABLE II. Composition of the <sup>36</sup>P  $J^{\pi} = 1_1^+$  wave function in truncation scheme T-A.

Partition group	Intensity (%)
$[8, \leq 8, \leq 4; 2, 0, 0, 0]$	0.2
$[9, \leq 8, \leq 4; 2, 0, 0, 0]$	1.5
$[10, \leq 8, \leq 4; 2, 0, 0, 0]$	9.1
$[10, \le 8, \le 4; 0-1, 0, 1-2, 0]$	0.4
$[11, \leq 8, \leq 4; 2, 0, 0, 0]$	17.0
$[11, \leq 8, \leq 4; 0-1, 0, 1-2, 0]$	1.5
$[12, \leq 8, \leq 4; 2, 0, 0, 0]$	61.3
$[12, \leq 8, \leq 4; 0-1, 0, 1-2, 0]$	6.5
$n(d_{5/2}) = 12; n(f_{5/2}) + n(p_{1/2}) > 0$	2.5

dictions of scheme T-A were accordingly shifted by 200 keV. Similar comparison of the results from truncation scheme T-B showed that the binding energy shift associated with its use was also relatively state independent. Thus, a similar shift of 340 keV was made for the results of truncation scheme T-B. Truncation of the full WBMB model space will introduce some spuriousity. In OXBASH, spuriousity is routinely eliminated by the method of Gloeckner and Lawson.<sup>12</sup> This method is approximate so that our results do contain some spuriousity; however, since the truncation eliminates < 1% of the wave functions, it seems reasonable that the spuriousity is limited to some fraction of < 1% and is, therefore, not a serious problem. OXBASH contains standard procedures for testing for the effects of spuriousity which involve repeating the diagonalization under different conditions. Due to computer time restrictions we did this for <sup>36</sup>P only. The tests indicate completely negligible effect on the 10 lowest <sup>36</sup>P 1<sup>+</sup> states of either spuriousity or the method used to eliminate it.

Our procedures for calculating  $\beta$  and  $\gamma$  decay observables follow those described in our report of the decays of <sup>35</sup>Si and <sup>36</sup>P (Ref. 5). In particular, the Gamow-Teller beta-decay transition strength, B(GT), was calculated for all energetically accessible final states. This was found to demand ~200 final states for <sup>34</sup>Al( $\beta^-$ )<sup>34</sup>Si which has  $Q(\beta^-)=16459$  keV and three possible final state spins, but only ~20 final states for <sup>36</sup>Si( $\beta^-$ )<sup>36</sup>P which has a smaller available phase space,  $Q(\beta^-)=7347$  keV, and only one possible final state spin. The phase-space factor f was calculated using the Wilkinson-Macefield<sup>13</sup> parametrization and for each state k the half-life  $t_k$  was calculated from

$$t_k = 6166 / [f \cdot B(GT)]_k$$
 (2)

The total half-life for allowed decays is then obtained from

$$1/t = \sum_{k} 1/t_k \quad . \tag{3}$$

We use the effective Gamow-Teller operator described in Ref. 4; it is based on the "final fit" sd-shell value of Brown and Wildenthal.<sup>14</sup> Resulting B(GT) values are ~60% of B(GT) values obtained using the free nucleon Gamow-Teller operator. That is, half-lives calculated with the free nucleon GT operators would be ~60% of those presented here. Electromagnetic and firstforbidden beta-decay matrix elements are evaluated with harmonic oscillator radial wave functions, utilizing a length parameter  $b = (41.467/\hbar\omega)^{1/2}$  fm  $(\hbar\omega)^{1/2} = 45A^{-1/3} - 25A^{-2/3}$  MeV). The calculations of these observables follow the procedures described in Ref. 6.

The reliability of the calculations. Our experience to date with the WBMB interaction and its predecessor, the SDPF interaction, lead us to expect that level energies will be calculated with ~200-keV root-mean-square deviation from experiment. We expect to predict medium-to-strong M1, E2, and  $E3 \gamma$  transitions and GT  $\beta$  transitions with quite high accuracy (within ~40% in the matrix elements).<sup>15,16</sup> Weak transitions are usually

subject to cancellation between various contributions and thus are not normally capable of being reproduced with accuracy. We are usually satisfied if the calculated values are also weak. E1 transitions are always a problem because of the well-known diminution of strength for low-lying transitions at the expense of the E1 giant resonance, and because what would be the dominant contribution, e.g.,  $d_{3/2} \leftrightarrow f_{7/2}$  in the present case, is forbidden for E1 decays.

For GT transitions, which are our main concern, the scale of transition strengths is established by the sum rule limit

$$\sum_{f} B(GT) = (1.26)^2 3(N_i - Z_i) , \qquad (4)$$

which applies to  $\beta^-$  decays in these neutron rich nuclei. For <sup>36</sup>Si and <sup>37</sup>P decays these sums are 38 and 33, respectively. Our experience is that B(GT) values less than  $\sim 50 \times 10^{-3}$  (i.e.,  $\sim 0.1\%$  of the sum rule) cannot be predicted reliably.

### **III. RESULTS**

#### A. Binding energies and energy spectra

We first compare the experimental and predicted binding energies of the *nfp* model spaces of interest. The mass excesses of  ${}^{34}$ Al,  ${}^{36}$ Si, and  ${}^{37}$ P have recently been measured for the first time.<sup>17</sup> Results (nucleus: mass excess, binding energy)-with the energies in keV and the uncertainty in the last figure in parentheses—are [<sup>34</sup>Al:  $-3500(400), -267756(400)], [^{36}Si: -12900(600),$ -292517(600)], [<sup>37</sup>P: -19310(400), -306220(400)]. There have been three recent measurements of the  ${}^{34}Si$  mass excess.  ${}^{18-20}$  The three, which are not in very good agreement, yield the average results: [<sup>34</sup>Si: -19959(24), -283433(24)]. The mass excess of <sup>36</sup>P has been measured by Mayer et al.<sup>18</sup> and Drumm et al.<sup>21</sup> The results of -20252(15) keV and -20251(27) keV are in excellent agreement, yielding the weighted averages:  $[^{36}P: -20249(13)]$ , -299081(13)]. The mass excess and binding energy of  $^{37}$ S, as reported in the mass table,<sup>22</sup> are  $[^{37}$ S:  $-26\,896.59(26), -313\,019.8(4)$ ].

The predicted binding energies  $E_{Bcorr}$  of the WBMB interaction do not include Coulomb contributions and they are relative to the <sup>16</sup>O core. Comparison to experiment is made by subtracting the Coulomb contribution from the experimental binding energies to yield experimental values for  $E_{Bcorr}$ . There are several possible ways of estimating the Coulomb corrections, all of which entail uncertainties of the order of 100-200 keV. We start from Wildenthal's results<sup>8</sup> for the lighter Z = 14-16 isotopes and assume that the difference between the experimental binding energy and the corrected binding energy,  $E_{\text{Bcorr}}$ , is independent of A for a given Z. We adopt the average of the results obtained by extrapolation from the 3-4 next lighter isotopes. This procedure gives the experimental  $E_{\text{Bcorr}}$  of Table III. Except for <sup>34</sup>Al, the comparison of predicted and empirical  $E_{Bcorr}$  shown in Table III displays quite satisfactory agreement, and indicates

 $E_{Bcorr}$  (keV) State Difference  $J^{\pi}$ Nucleus Expt. Pred. (keV) <sup>34</sup>Al 4-,5--562(400)-161650(400)-161088<sup>34</sup>Si 0+ -182594(24)-182 747 +153(24)<sup>34</sup>Si 4--178 520 <sup>36</sup>Si 0+ -191753(600)-191 948 +185(600)<sup>36</sup>P 4--204074(13)-204410+336(13)<sup>36</sup>P  $1^{+}$ -202771(13) $-203\,206$ +435(13)<sup>37</sup>P

-211474

-224043

-222 444

-211079(400)

-223872(1)

-222 477(1)

TABLE III. Experimental and predicted Coulomb corrected binding energies,  $E_{Bcorr}$ , for the lowest-lying state of each nfp model space of interest. The difference (experiment minus predicted) is also given if known.

that the WBMB interaction has useful predictive powers for binding energies at least for A > 34. For <sup>34</sup>Al we appear to be seeing the onset of deformation which is known to occur for  $N \simeq 20$ ,  $A \sim 30-33$  nuclei.<sup>3</sup> If so, proper account of the binding energy of <sup>34</sup>Al would necessitate inclusion of  $>1\hbar\omega$  terms in the wave functions. The WBMB predictions for the 1fp spectrum of  $^{34}Al$  and the 2fp spectra of  $^{36}Si$  and  $^{37}P$  are listed in Table IV. As discussed, these were calculated within a full WBMB basis. There is no known experimental information on the spectra of any of these three nuclei.

 $1/2^{+}$ 

7/2-

3/2+

<sup>37</sup>S

<sup>37</sup>S

The WBMB predictions for the (0-1)fp spectrum of <sup>34</sup>Si and the (1-2)fp spectra of <sup>36</sup>P and <sup>37</sup>S are listed in Table V. The <sup>34</sup>Si spectrum and the 1 fp spectrum of <sup>36</sup>P and <sup>37</sup>S are for the full WBMB space; the results for the 2fp spectra of <sup>36</sup>P and <sup>37</sup>S are from truncation scheme T-B, with all excitation energies shifted downwards by 340 keV as explained in Sec. II.

<sup>34</sup>Si excited states. Both Mayer et al.<sup>18</sup> and Fifield et al.<sup>19</sup> used two-proton pickup reactions on <sup>36</sup>S to form <sup>34</sup>Si. Mayer *et al.*<sup>18</sup> reported one excited state at 3590(25) keV, which, however, Fifield et al.<sup>19</sup> did not observe. The reactions used in the two investigations are similar enough so that this is a real discrepancy, and therefore the existence of this excited state must be viewed as questionable. Fifield et al.<sup>19</sup> observed an excited state at 5330(50) keV. They present arguments associating this state with the  $2^+_1$  state predicted to lie at 4888 keV (Table V). As noted by Fifield et al.,<sup>19</sup> two proton pickup would not be expected to form the 1fpstates with observable cross sections.

A question of interest is at what excitation energy the  $2\hbar\omega$  2fp states will commence. The  $(2s, 1d)^{16}(fp)^2$  space is too large for us to treat without truncation. Therefore, calculations were performed in several truncation schemes in order to estimate this energy. The results indicate that the 2fp states start with a  $0^+$  state at ~7-MeV excitation with a  $2^+$  state ~1.5 MeV higher. A calculation in the mixed (0+2)fp space was also made using the van der Poel interaction which uses the truncated  $(s_{1/2}, d_{3/2}, f_{7/2}, p_{3/2})$  configurational space.<sup>23</sup> This calculation gave ~4 MeV for the excitation of  $0_2^+$  in <sup>34</sup>Si. In either case, the excitation energy of the first 2fp

 $2^+$  state would be too high to have any influence on the present results, i.e., too high to be formed significantly either directly or indirectly by  $\beta^-$  decay from <sup>34</sup>Si.

+395(400)

+171(1)

-33(1)

<sup>36</sup>P excited states. Prior to the beta-decay results of Dufour et al.,<sup>2</sup> energy levels were reported in  ${}^{36}P$  at 252(10) keV (Ref. 21) and 450(22) keV (Ref. 18) from heavy-ion transfer results. The <sup>36</sup>Si  $\beta^-$  decay results of Ref. 2 suggest levels below 1300-keV excitation at 250.25(40) and 424.90(40) keV in agreement with the transfer results and in satisfactory agreement with our predictions (Table V) for the lowest  $4^-$ ,  $3^-$ , and  $2^-$  levels. We have previously presented evidence from an analysis<sup>5</sup> of the  ${}^{36}P(\beta^{-}){}^{36}S$  results of Dufour *et al.*,<sup>2</sup> which supports an assignment of  $4^-$  to the  ${}^{36}P$  ground state.

<sup>37</sup>S excited states. Prior to the <sup>37</sup>P( $\beta^{-}$ )<sup>37</sup>S results of Dufour et al.,<sup>2</sup> information on the energy spectrum of <sup>37</sup>S has come mainly from the <sup>36</sup>S(d,p)<sup>37</sup>S reaction,<sup>24,25</sup> the <sup>36</sup>S(n, $\gamma$ )<sup>37</sup>S reaction,<sup>26</sup> and the <sup>37</sup>Cl(t,<sup>3</sup>He)<sup>37</sup>S reaction.<sup>27</sup> Only one definite and one probable even-parity state were identified, and we will find, not surprisingly, that new <sup>37</sup>S states are involved in the allowed beta decay of  $J^{\pi} = 1/2^{+37}$ P.

Our main concern at this point is to attempt an identification of the lowest-lying odd-parity intruder states, i.e., those arising from nfp excitations with n > 1and therefore outside our model space. The WBMB predictions for the single-neutron spectroscopic factors of  ${}^{36}S + n \rightarrow {}^{37}S$  are listed in Table VI for the first five J = 1/2 - 7/2 1fp states of <sup>37</sup>S. The predicted stripping strength is concentrated in the first two  $7/2^-$  and  $3/2^$ states and the first  $1/2^-$  state. For  $J^{\pi} = 5/2^-$ , the strength is predicted to be more widely fragmented with the centroid at  $\sim$ 5-MeV excitation. These results are consistent with the previous predictions of Woods,<sup>28</sup> <sup>37</sup>S performed calculations for in a who  $(1d_{5/2}, 1d_{3/2}, 2s_{1/2}, 1f_{7/2}, 2p_{3/2})$  model space and thus presented  $S_n^+$  factors for  $7/2^-$  and  $3/2^-$  states (but not for  $1/2^-$  or  $5/2^-$  states). The predictions are compared to experiment in Table VII and Fig. 1 with the purpose of identifying intruder states: That there are low-lying intruder states is evident from the comparison of Fig. 1. There are seven experimental levels below 4-MeV excita-

TABLE IV. The predicted $1fp$ spectra of ${}^{34}A1$ and $2fp$ spectra of ${}^{36}Si$ and ${}^{37}P$ . No. orders the
states of a given $J^{\pi}$ by energy. All states are listed up to the first No. equal to 8, after that only yras
(i.e., No equal to 1) states are listed.

	<sup>34</sup> Al			<sup>36</sup> Si			<sup>37</sup> P	
$E_x$			$E_x$			$E_{x}$		
(keV)	$J^{\pi}$	No.	(keV)	$J^{\pi}$	No.	(keV)	J *	No.
0000	5-	1	0000	0+	1	0000	1/2+	1
0002	4-	1	1898	2+	1	1480	3/2+	1
0476	3-	1	3074	4+	1	1753	5/2+	1
0515	6-	1	4022	2+	2	2506	3/2+	2
0757	2-	1	4022	6+	1	2817	9/2+	1
1502	3-	2	4936	4+	2	2914	7/2+	1
1769	4-	2	5034	3+	1	3416	5/2+	2
1848	2-	2	5055	0+	2	3672	3/2+	3
2544	1-	1	5085	2+	3	3770	13/2+	1
3124	2-	3	5428	5+	1	3876	11/2+	1
3151	3-	3	5761	3+	2	4031	5/2+	3
3295	4-	-3	6055	2+	4	4112	7/2+	2
3371	3-	4	6275	4+	3	4292	9/2+	2
3509	2-	4	6372	3+	3	4321	5/2+	4
3908	5-	2	6450	0+	3	4328	1/2+	2
3909	1-	2	6500	4+	4	4581	1/2+	3
4129	1-	3	6611	3+	4	4633	7/2+	3
4216	0-	1	6846	4+	5	4686	11/2+	2
4498	3-	5	7096	1+	1	4830	7/2+	4
4521	2-	5	7289	2+	5	4923	3/2+	4
4524	4-	4	7395	6+	2	4929	5/2+	5
4801	7-	1	7402	5+	2	5000	5/2+	6
4843	2-	6	7481	2+	6	5204	9/2+	3
4849	6-	2	7562	2+	7	5455	9/2+	4
4884	5-	3	7574	5+	3	5535	11/2+	3
4896	6-	3	7787	6+	3	5546	5/2+	7
4954	1-	4	7884	3+	5	5606	3/2+	5
4991	3-	6	7909	1+	2	5619	7/2+	5
5139	4-	5	8005	2+	8	5674	9/2+	5
5359	0-	2	8371	7+	1	5798	7/2+	6
5416	4-	6	8905	8+	1	5868	9/2+	6
5494	2-	7	9921	9+	1	5895	15/2+	1
5498	5-	4	11 467	10+	1	6025	7/2+	7
5509	1-	5	15 895	11+	1	6092	9/2+	7
5604	5-	5	16814	12+	1	6216	5/2+	8
5642	6-	4	24 117	13+	1	8139	17/2+	1
5647	3-	7				10 480	19/2+	1
5720	2-	8				11 199	$21/2^+$	1
6239	8-	1				15 009	23/2+	1
7720	9-	1				18 982	25/2+	1
12 899	10-	1						2

tion with  $l_n = 1$  assignments, but the WBMB interaction predicts only three  $1/2^-$  or  $3/2^-$  states below 4.5 MeV. We have made two estimates of the excitation energies of intruder states. The first, described in Ref. 25, uses the Bansel-French weak coupling model<sup>29</sup> and is labeled BF in Fig. 1. The second is a shell-model calculation with the WDF interaction<sup>30</sup> in a  $(d_{3/2}f_{7/2})^5$  model space. The results are labeled WDF in Fig. 1. Both predict that odd-parity intruder states will start at  $E_x = -2$ MeV, but the order of the levels is not at all certain. Based on a scrutiny of the spectroscopic factors of Tables VI and VII and Fig. 1, we would identify the 1992-, 2023-, and 2517-keV levels as intruders. Certainly, this identification results in a much better overall agreement of predictions and experiment of the  $(2J+1)S_n^+$  than would be the case for no assumed intruders. Based on the  ${}^{36}\text{S}(n,\gamma){}^{37}\text{S}$  results (Ref. 26) and  ${}^{36}\text{S}(d,p){}^{37}\text{S}$  results, as reviewed in Ref. 25, these states would most likely have  $J^{\pi}=3/2^-$ ,  $5/2^-$ , and  $7/2^-$ , respectively. This bandlike sequence is similar to systematics of intruder states in heavier odd-A *nfp* nuclei (see Table V of Ref. 6). Note, however, that comparison of the predicted and experimental  $S_n^+$  values suggests some mixing of the 1*fp* and intruder states.

	<sup>34</sup> Si			<sup>36</sup> P		······	<sup>37</sup> S	
$E_x$			$E_x$	-		$E_{x}$	2	
(keV)	$J^{\pi}$	No.	(keV)	$J^{\pi}$	No.	(keV)	$J^{\pi}$	No.
0000	0+	1	0000	4-	1	0000	7/2-	1
4227	4-	1	0169	3-	1	0691	3/2-	1
4465	3-	1	0765	2-	1	1599	3/2+	1
4558	5-	1	1204	1+	1	2660	5/2-	1
4888	2+	1	1486	2+	1	2720	1/2+	1
5142	3-	2	1540	1-	1	3042	7/2+	1
5296	2-	1	2112	2-	2	3114	5/2+	1
5648	3-	3	2212	0+	1	3349	7/2-	2
5999	3+	1	2305	5-	1	3575	1/2+	2
6117	2-	2	2403	0-	1	3615	3/2+	2
6143	4-	2	2425	1+	2	3635	9/2-	1
6238	1-	1	2464	2+	2	3821	5/2-	2
6426	1-	2	2593	4+	1	3889	3/2+	3
6623	0-	1	2649	1-	2	3945	5/2+	2
7135	1-	3	2658	3+	1	4109	9/2+	1
7526	2-	3	2713	3-	2	4126	7/2-	3
7600	0+	2	3001	3+	2	4127	11/2+	1
7686	2-	4	3140	1+	3	4228	9/2-	2
7932	4+	1	3190	4-	2	4273	7/2+	2
8058	5-	2	3451	2+	3	4419	7/2+	3
8128	6-	1	3482	1+	4	4475	5/2+	3
8333	2-	5	3545	2+	4	4501	3/2+	4
8370	4-	3	3567	0+	2	4583	5/2+	4
8467	2+	2	3650	3+	3	4583	3/2+	3
8536	0-	2	3838	1+	5	4671	13/2+	1
8555	1-	4	3845	4+	2	4694	3/2+	5
8590	3-	4	4028	2+	5	4701	7/2-	4
8590	5-	3	4034	0-	2	4717	1/2-	2
8732	3-	5	4043	5-	2	4785	5/2-	3
8804	3+	2	4045	5+	1	4820	3/2+	6
8822	3-	6	4074	6+	1	5171	15/2+	1
10041	8-	1	4120	4-	3	7062	17/2+	1
10 142	1+	1	4124	2+	6	7338	13/2-	1
11 676	9-	1	4443	6-	1	7534	15/2-	1
12 659	5+	1	4754	7+	1	7909	19/2+	1
13 835	6+	1	5212	8+	1	11 368	21/2+	1
16044	10-	1	7093	7-	1	11 368	17/2-	1
17 539	11-	1	7220	9+	1	11 900	23/2+	1
21 603	7+	1	7689	8-	1	15 035	19/2-	1
24 426	12-	1	8752	10+	1	15 200	25/2+	1
32 029	13-	1	11 059	11+	1	18 860	$\frac{27}{2^+}$	1
			11 496	9-	1	26 823	29/2+	1
			11 896	12+	1			-
			15 615	10-	1			
			15 879	13+	1			
			19316	14+	1			
			27 201	15+	1			

TABLE V. The predicted (0-1)fp spectrum of <sup>34</sup>Si and (1-2)fp spectra of <sup>36</sup>P and <sup>37</sup>S. No. orders the states of a given  $J^{\pi}$  by energy. All states are listed up to the first No. equal to 6, after that only yrast (i.e., No equal to 1) states are listed.

#### B. Beta decay

Decay of <sup>34</sup>Al to <sup>34</sup>Si was calculated using the experimental  $Q(\beta^-)$  of 16459(400) keV and the <sup>34</sup>Si energy spectrum of Table V. The prediction (Table IV) for the ground-state spin of <sup>34</sup>Al is ambiguous; it could as well be J = 4 or 5. Thus, the beta decay was calculated for both alternatives. Results for allowed transitions are given in Tables VIII and IX. First-forbidden transitions were found to be strongly inhibited due both to the high excitation energies of the 0fp states with  $J \ge 2$  in <sup>34</sup>Si and to unusually small matrix elements. For instance, the <sup>34</sup>Al(4<sup>-</sup>) $\rightarrow$ <sup>34</sup>Si(2<sup>+</sup>) unique first-forbidden transition

TABLE VI. Predicted  $(2J+1)S^+$  spectroscopic factors for the reaction  ${}^{36}S(d,p) {}^{37}S$  leading to 1fp states of  ${}^{37}S$ . The first five states, ordered by energy, are listed for each  $J^{\pi}$ . Numbers in parentheses are powers of 10.

		(2 <b>J</b> + 1	$S_n^+$	
No.	1/2-	3/2-	5/2-	7/2-
1	1.94	3.43	0.05	7.28
2	1.3(-3)	0.48	0.06	0.32
3	2.5(-3)	2.0(-3)	0.92	1.1(-6)
4	2.2(-4)	3.0(-4)	3.19	1.8(-2)
5	2.0(-5)	1.2(-2)	0.19	4.2(-2)

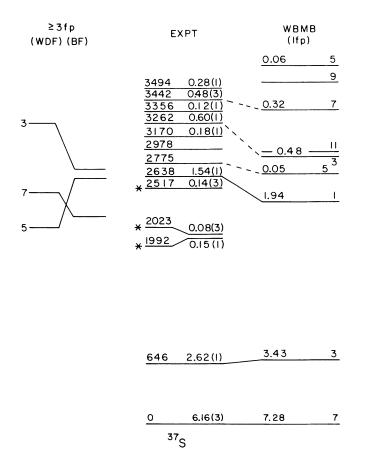


FIG. 1. Comparison of calculated and experimental properties for odd-parity (and possible odd-parity) levels of <sup>37</sup>S for  $E_x < 4.0$  (expt.) and < 4.5 MeV (WBMB). The experimental spectrum is from Refs. 24 and 25, as reviewed in Ref. 25. For each level the excitation energy (in keV) is given on the left and the  ${}^{36}S + n$  spectroscopic factor  $(2J + 1)S_n^+$  is given on the right with the associated  $l_n$  value in parentheses. For clarity, the experimental scheme between 2.9 and 3.5 MeV is not quite to scale. For the WBMB predictions, the  $(2J+1)S_n^+$  are given on the left and 2J is on the right. Associations between experiment and the WBMB predictions are connected by solid lines if considered definite and dashed lines otherwise. The three experimental levels labeled with an asterisk are our choices for the three lowest-lying intruder (>3fp) states. The two estimates of the 3fp spectra, labeled by 2J, are for the WDF interaction and the Bansel-French weak coupling model (see text).

strength was calculated to be of order  $10^{-3}$  relative to a  $f_{7/2} \rightarrow d_{3/2}$  single-particle transition resulting in a  $\beta^-$  branching ratio of  $\sim 1.3 \times 10^{-4} \%$ .

The experimental results given by Dufour *et al.*<sup>2</sup> for <sup>34</sup>Al decay are very simple. One  $\beta^-$ -delayed  $\gamma$  ray of 123.8(4) keV was observed, with a half-life of 0.050(25) s. The predicted half-lives for the two choices of <sup>34</sup>Al spins are coincidentally equal and are in agreement with experiment. We can understand the observation of only one low-energy  $\gamma$  ray if we make the reasonable assumption that the efficiency for observing high-energy  $\gamma$  rays was low enough so that ground-state decays from the predicted 1 f p levels were overlooked. We note that our interaction tends to underbind the lowest  $3^-$  state in  $N \leq 20$  nuclei because it does not adequately incorporate the octupole collectivity of this state. (This is not true for N = 21 isotones since the particle-hole interaction involved in the 1fp states of these nuclei is solely T = 1with no contribution from the T = 0 component responsible for the aforementioned deficiency.) Then, referring to Tables VIII and IX, the observed 124-keV  $\gamma$  ray could correspond to a  $3_1^- \rightarrow 4_1^-$  or  $4_1^- \rightarrow 3_1^-$  transition (depending on the order of the  $3_1^-$  and  $4_1^-$  states) if  $J^{\pi}({}^{34}\text{Al}) = 4^-$  and either a  $5^-_1 \rightarrow 4^-_1$  or a  $4^-_1 \rightarrow 3^-_1$  transition if  $J^{\pi}({}^{34}\text{Al}) = 5^-$ . As noted above, we expect most likely that the  $3_1^-$  level of <sup>34</sup>Si is actually the lowest 1fpstate so that the 124-keV  $\gamma$  ray corresponds to a  $4_1^- \rightarrow 3_1^-$  transition. It would then seem most likely that  $J^{\pi}({}^{34}\text{Al}) = 4^{-}$ , since for a 5<sup>-</sup> assignment two observable transitions are expected; i.e., the two members of the  $5_1^- \rightarrow 4_1^- \rightarrow 3_1^-$  cascade. These speculations are intended to suggest the type of experimental information needed before the ambiguity in the spin of <sup>34</sup>Al can be resolved. Two immediate studies come to mind: First, the ground-state transitions should be sought, and, second, the results of a simple timing measurement would differentiate between an E3  $3_1^- \rightarrow 0^+$  decay and an M4  $4_1^- \rightarrow 0^+$  decay. We present in Table X the predicted transition strengths connecting the lowest  $0^+$ ,  $3^-$ ,  $4^-$ , and  $5^-$  states of <sup>34</sup>Si. These transition strengths can be used to interpret future results on  ${}^{34}Al(\beta^{-}){}^{34}Si$ .

#### 2. ${}^{36}Si(\beta^-){}^{36}P$

Initial results for the allowed beta decay of  $J^{\pi}=0^{+36}$ Si to 1<sup>+</sup> states of <sup>36</sup>P were calculated using the

Experimental state			$(2J+1)S_{n}^{+}$			Model state <sup>a</sup>		
			Expe	riment	Shell	model		
J <sup><i>π</i></sup>	$E_x$ (keV)	l <sub>n</sub>	Ref. 25	Ref. 24	Present	Ref. 28	$J_k^{\pi}$	$E_x$ (keV)
1/2-	2638	1	1.54	1.66	1.94		$1/2_{1}^{-}$	2360
3/2-	646	1	2.62	2.80	3.43	2.98	$3/2^{-1}$	691
$(3/2)^{-}$	1993	1	0.15	0.30	0.48	0.90	$3/2^{-}_{2}$	2839
3/2-	3261	1	0.60	0.57	0.48	0.90	$3/2^{-}_{2}$	2839
3/2-	3261		0.60	0.57	2.0(-3)		$3/2\frac{1}{3}$	4583
(5/2-,7/2-)	2024	(3)	0.14		0.05		$5/2^{-}_{1}$	2660
(5/2,7/2)-	5499	3	1.20		3.19		5/24	5101
7/2-	0	3	6.16	7.33	7.28	7.08	$7/2^{-}_{1}$	0
$(5/2^{-},7/2^{-})$	2517	(3)	0.08	0.27	0.32	0.37	$7/2^{-}_{2}$	3349
	3443	3	0.34	0.48	0.32	0.37	$7/2^{-}_{2}$	3349

TABLE VII. Comparison of experimental and theoretical spectroscopic strengths for the <sup>36</sup>S(d,p)<sup>37</sup>S reaction.

<sup>a</sup>The subscript k orders the states of a given  $J^{\pi}$  by excitation energy.

experimental  $Q(\beta^{-})$  of 7347(600) keV and the <sup>36</sup>P energy spectrum of Table V. On the basis of these results, and from calculations of  $\gamma$ -ray transition strengths, the six  $\beta^{-}$ -delayed  $\gamma$  rays observed by Dufour *et al.*<sup>2</sup> were placed in the scheme of Fig. 2. Then the  $\beta^{-}$  decay log*ft* values and branching ratios were recalculated using the proposed two lowest energy levels of Fig. 2 together with the predicted excitation energies of the higher-lying 1<sup>+</sup> states. Results are given in Table XI. The two firstforbidden decays which were calculated to be the strongest are also included. These are negligible compared to the allowed decays, so that the observed  $\beta^{-}$ -delayed  $\gamma$ ray flux can be attributed to decays to 1<sup>+</sup> states only (the 0<sup>+</sup>, T = 4 analog of the <sup>36</sup>Si ground state is, of course, not energetically accessible).

Gamma-ray transitions. We now consider the WBMB predictions for  $\gamma$ -transition branching ratios since they are needed for the best interpretation of the observed  $\beta^-$  delayed  $\gamma$  rays. We first consider transitions between the 1fp states.

As discussed in Sec. II A, the 250- and 425-keV levels were observed previously and, assuming they have odd parity, we have the very strong prediction that the flux into the 425-keV level is from  $\gamma$  decay of 1<sup>+</sup> states pop-

TABLE VIII. Predictions of  ${}^{34}\text{Al}(\beta^-){}^{34}\text{Si}$  for a  ${}^{34}\text{Al} J^{\pi} = 4^-$  ground state. The predicted half-life is 0.037(7) s where the uncertainty is due to that in the mass of  ${}^{34}\text{Al}$ . Only  ${}^{34}\text{Si}$  states for which the branching is > 1% are listed.

$J_k^{\pi}$	$E_x$ (keV)	$\frac{B(\text{GT})}{(\times 10^3)}$	log ft	Branching (%)
<b>4</b> <sup>-</sup> <sub>1</sub>	4227	143.5	4.63	37.5
$3^{-}_{1}$	4465	154.1	4.60	36.7
$3\frac{1}{1}$ $5\frac{1}{1}$	4558	19.9	5.49	4.6
$3^{-}_{2}$	5142	29.4	5.32	5.3
$3\frac{1}{2}$ $3\frac{1}{3}$	5648	7.9	5.89	1.2
4-	8370	52.8	5.07	2.0
44	8865	38.8	5.20	1.1
$3^{-}_{7}$	9191	51.4	5.08	1.2
$4_{3}^{-} \\ 4_{4}^{-} \\ 3_{7}^{-} \\ 3_{8}^{-}$	9325	59.8	5.01	1.3

ulated in allowed decay. This gives us a model-dependent choice of  $J^{\pi}=2^{-}$  for the 425-keV level from the  $J^{\pi}=2^{-}$ ,  $3^{-}$ , and  $4^{-}$  alternatives offered by the calculation and, thus, the order of the three lowest states as shown by the dashed lines connecting the WBMB predictions to the experimental level scheme. With these proposed  $J^{\pi}$  assignments the  $\gamma$ -ray branching ratio of the 425-keV level seems surprising; it demands that the  $2_1^- \rightarrow 4_1^-$  E2 transition strength be ~800 times the M1  $2_1^- \rightarrow 3_1^- M1$  strength [both expressed in Weisskopf units (W.u.)]. In actual fact these branchings are quite consistent with the WBMB predictions which are for a 11 W.u.  $2_1^- \rightarrow 4_1^-$  E2 decay (corresponding to a partial meanlife of 0.74 ns) and an essentially vanishing  $2_1^- \rightarrow 3_1^-$ M1 transition strength ( $\sim 5 \times 10^{-5}$  W.u.). Since matrix elements which are very small due to cancellation effects cannot be calculated with any accuracy, the small predicted M1 strength is consistent with the  $\sim 10^{-3}$  W.u. needed to explain the observed branching ratio. Our predictions for the  $3_1^- \rightarrow 4_1^-$  transition are for a 0.16 W.u. M1 decay with a meanlife of 13 ps.

As shown in Fig. 2 we have placed the observed 922keV  $\gamma$  ray as feeding the 425-keV level so as to help explain the surplus flux out of the 425-keV state. Then the only candidates we have to associate with the resulting 1347-keV level are the  $1_1^-$  or  $2_1^+$  model states. For the  $1_1^-$  level possibility we predict a 0.81 W.u. *M*1 decay to  $2_1^-$  and a 50 W.u. *E*2 decay to  $3_1^-$ . In spite of the ex-

TABLE IX. Predictions of  ${}^{34}\text{Al}(\beta^{-}){}^{34}\text{Si}$  for a  ${}^{34}\text{Al} J^{\pi} = 5^{-}$  ground state. The predicted half-life is 0.037(7) s where the uncertainty is due to that in the mass of  ${}^{34}\text{Al}$ . Only  ${}^{34}\text{Si}$  states for which the branching is > 1% are listed.

$J_k^{\pi}$	$E_x$ (keV)	$\frac{B(\text{GT})}{(\times 10^3)}$	log <i>ft</i>	Branching (%)
<b>4</b> <sup>-</sup>	4227	248.5	4.40	64.0
$4_1^-$ $5_1^-$	4558	90.2	4.84	20.4
$4^{-}_{2}$	6143	23.0	5.43	2.7
43	8370	45.1	5.14	1.7
$4_{3}^{-}$ $4_{5}^{-}$	8903	55.0	5.05	1.5

TABLE X. <sup>34</sup>Si electromagnetic transition strengths connecting the lowest-lying 0<sup>+</sup>, 3<sup>-</sup>, 4<sup>-</sup>, and 5<sup>-</sup> states. The units of  $B(\lambda)$  are  $\mu_N^2$  fm<sup>2L-2</sup> and  $e^2$ fm<sup>2L</sup> for *ML* and *EL* transitions, respectively. The corresponding single-particle (Weisskopf) units for M1, E2, E3, and M4 transitions in <sup>34</sup>Si are 1.791  $\mu_N^2$ , 6.54 e<sup>2</sup>fm<sup>4</sup>, 68.7 e<sup>2</sup>fm<sup>6</sup>, and 2018  $\mu_N^2$ fm<sup>6</sup>, respectively.

Transition	Multipole $(\lambda)$	$\boldsymbol{B}(\lambda)^{\mathrm{a}}$
4-→3-	<b>M</b> 1	0.44
5-→4-	<b>M</b> 1	0.26
	E2	29.8
$5^- \rightarrow 3^-$	E2	0.002
3-→0+	E3	51.7(31.4)
$4^- \rightarrow 0^+$	M4	4368(2660)

<sup>a</sup>M1 and E2  $B(\lambda)$  were calculated using the effective (sd) shell operators (see text). B(E3) corresponds to  $e_p = 1.5e$ ,  $e_n = 0.5e$ , and B(M4) to the free nucleon g operators. For the E3 and M4 cases, the numbers in parentheses use the effective (sd) operators for E2 and M1 transitions, respectively.

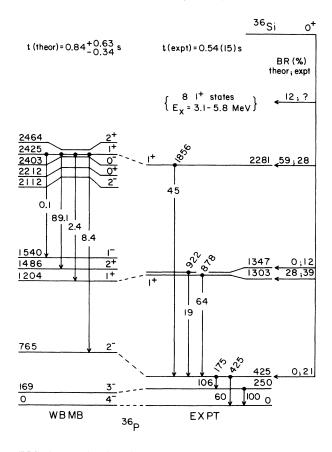


FIG. 2. On the right is shown the proposed decay scheme of  ${}^{36}$ Si as deduced from the  $\beta^-$ -delayed  $\gamma$ -ray spectrum of Dufour *et al.* (Ref. 2). These published results consist of the six  $\gamma$  transitions with their energies given in keV above the transitions and their relative intensities given within the transitions. The  $\beta^-$  branching ratios (BR) we infer from the intensities are given to the far right where they are compared to the WBMB predictions (Table XI). On the left is shown the WBMB energy spectrum for  $E_x < 2.5$  MeV (one 5<sup>-</sup> level is omitted). Also shown are the predicted  $\gamma$ -branching ratios (in percent) of the  $1_2^+$  state. The uncertainty assigned to the theoretical half-life is due to that in the mass of  ${}^{36}$ Si.

tremely large strength of the E2 decay, the kinematics favor the M1 branch which is predicted to be 97%. The  $2_1^+$  state is predicted to have branching ratios to the  $2_1^$ and  $3_1^-$  states of 40% and 60%, respectively. Thus, a  $1_1^-$  assignment to the 1347-keV level would give better agreement of the predictions with experiment than would a  $2_1^+$  assignment.

For either a  $1_1^-$  or  $2_1^+$  assignment to the 1347-keV level, the observed intensity (12%) of the 922-keV  $\gamma$  transition needs to be explained by  $\gamma$  transitions from higherlying levels. This is also true for the extra flux (21%) out of the 425-keV level. Thus, even the 12%  $\beta^-$  intensity we predict for levels in the 3.1-5.8 MeV range of excitation is not adequate to explain the extra 33%  $\beta^$ flux out the 425- and 1347-keV levels. We are led to propose the possibility of an overlooked 934-keV 2281 $\rightarrow$ 1347  $\gamma$  branch. The  $\gamma$ -ray transition strengths necessary to check whether the WBMB predictions for the decay of  $1_2^+$  are consistent with this proposal are collected in Table XII and the resulting branching ratios (in

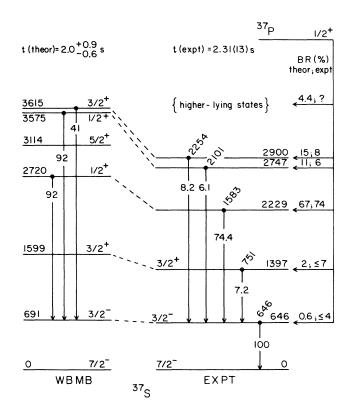


FIG. 3. On the right is shown the proposed decay scheme of <sup>37</sup>P as deduced from the  $\beta^-$ -delayed  $\gamma$ -ray spectrum of Dufour *et al.* (Ref. 2). These published results consist of the five  $\gamma$  transitions with their energies given in keV above the transitions and their relative intensities given within the transitions. The  $\beta^-$  branching ratios (BR) we infer from these intensities are given to the far right where they are compared to the WBMB predictions (Table XIII). Only states pertinent to the  $\beta^-$  decay are shown. On the left is shown the partial WBMB energy spectrum (only  $J^{\pi} \leq 5/2^+$  levels are shown for  $E_x > 2.5$  MeV). The uncertainty assigned to the theoretical half-life is due to that in the mass of <sup>37</sup>P.

TABLE XI. WBMB description of  ${}^{36}\text{Si}(\beta^{-}){}^{36}\text{P}$ . The predicted half-life is  $0.84^{+0.63}_{-0.34}$  s where the uncertainty is due to that in the mass of  ${}^{36}\text{Si}$ . Only  $1^{+}$   ${}^{36}\text{P}$  states for which the branching is > 1% are listed.

	$E_x$ (WBMB)		<b>B</b> ( <b>GT</b> )		Branching
$J_k^{\pi}$	(keV)	$E_x (expt)^a$	(×10 <sup>3</sup> )	logft	(%)
$2_{1}^{-}$	765	425		f = 10	9×10 <sup>-2</sup>
$1_{1}^{+}$	1204	1303	127	4.69	28.3
$1^{-}_{1}$	1540	(1347) <sup>b</sup>		f = 0.4	$7 \times 10^{-3}$
$1_{2}^{+}$	2425	2281	599	4.01	59.1
$1_{3}^{+}$	3140		224	4.44	8.7
$1_{4}^{+}$	3482		97	4.80	2.4
$1_{5}^{+}$	3838		73	4.92	1.3
Total					99.9

<sup>a</sup>When listed, the  $E_x$  (expt) were used in the calculation of f. For the remaining levels f was calculated using  $E_x$  (WBMB).

<sup>b</sup>Uncertain assignment.

TABLE XII. Predicted electromagnetic decays of <sup>36</sup>P 1<sup>+</sup> states. The transition strength  $B(\lambda)$  is in units of  $\mu_N^2$  for M1 transitions and  $e^2 \text{fm}^{2L}$  for EL transitions. Numbers in parentheses are powers of 10.

$\boldsymbol{E}_i$	$J_{j}$	π k				Γγ	BR <sup>b</sup>
(keV)	Initial	Final	λ	$B(\lambda)^{a}$	$E_{\gamma}$ (keV)	(meV)	(%)
1303	$1_{1}^{+}$	$2_{1}^{-}$	E1	3.82(-6)	878	8.87(-3)	100
2281	$1_{2}^{+}$	$2_{1}^{-}$	E1	5.84(-6)	1856	3.91(-2)	8.4
	$1_{2}^{+}$	$1_{1}^{+}$	M1 E2	2.38(-4) 1.21(+1)	978 978	2.58(-3) 8.72(-3)	2.4
	$1_{2}^{+}$	(21)	M1 E2	4.24(-2) 2.65(+1)	934° 934°	4.01(-1) 1.52(-2)	89.1
	12+	(11)	<b>E</b> 1	4.36(-7)	934°	3.72(-4)	0.1

<sup>a</sup>For <sup>36</sup>P, single particle (Weisskopf unit) values for the  $B(\lambda)$  are 0.703, 7.061, and 1.791 for E1, E2, and M1 transitions, respectively.

<sup>b</sup> $\gamma$ -ray branching ratio.

<sup>c</sup>Assuming the final state is at 1347 keV.

TABLE XIII. WBMB description of  ${}^{37}P(\beta^-){}^{37}S$ . The predicted half-life is  $2.0^{+0.9}_{-0.6}$  s where the uncertainty is due to that in the mass of  ${}^{37}P$ . Only even-parity  ${}^{37}S$  states for which the branching is > 1% are listed.

$J_k^{\pi}$	$E_x$ (WBMB) (keV)	$E_x(expt)^a$ (keV)	<i>B</i> (GT) (×10 <sup>3</sup> )	logft	Branching (%)
$3/2_{1}^{-}$	691	646		f = 3.3	0.12
$3/2^+_1$	1599	1397	3	6.28	2.0
$1/2^{-}_{1}$	2360	2638		f = 2.2	$8.2 \times 10^{-2}$
$1/2_{1}^{+}$	2720	2229	214	4.46	67.3
$1/2^+_2$	3575	2747	55	5.05	10.8
$3/2^+_2$	3615	2900	90	4.84	15.3
3/2+	4820		33	5.27	1.2
Total					96.8

<sup>a</sup>When listed the  $E_x(expt)$  were used in the calculation of f. For the remaining levels f was calculated using  $E_x(WBMB)$ .

TABLE XIV. Predicted electromagnetic decays of <sup>37</sup>S  $1/2^+$  and  $3/2^+$  states. The transition strength  $B(\lambda)$  is in units of  $\mu_N^2$  for M1 transitions and  $e^2 \text{fm}^{2L}$  for EL transitions. Numbers in parentheses are powers of 10.

$E_i$ (keV)	$J_{i}$	π c			$E_{\gamma}$	$\Gamma_{\gamma}$	BR⁵
	Initial	Final	λ	$B(\lambda)^{a}$	(keV)	(meV)	(%)
1397	$3/2_{1}^{+}$	$3/2_{1}^{-}$	<b>E</b> 1	4.89(-7)	751	3.03(-4)	100
2229	$1/2_{1}^{+}$	$3/2_{1}^{-}$	<b>E</b> 1	2.13(-4)	1583	8.85(-1)	92
	1/21+	3/21+	M1 E2	9.75(-3) 4.36(+1)	832	6.49(-2) 1.40(-2)	8
2747	$1/2_{2}^{+}$	3/2-	<b>E</b> 1	8.37(-4)	2101	1.18(+1)	92
2747	1/22+	3/21+	M1 E2	3.74(-2) 2.50(+0)	1350	1.06(+0) 9.03(-3)	8
2900	$3/2_{2}^{+}$	3/21	<b>E</b> 1	1.52(-5)	2254	1.82(-1)	41
2900	3/22+	3/21+	M1 E2	5.11(-3) 9.33(+0)	1503	2.00(-1) 5.75(-2)	58
2900	3/22+	1/21+	M1 E2	3.11(-4) 1.64(+1)	671	1.09(-3) 1.80(-3)	1

<sup>a</sup>For <sup>37</sup>S, single particle (Weisskopf unit) values for the  $B(\lambda)$  are 0.717, 7.324, and 1.791 for E1, E2 and M1 transitions, respectively.

 ${}^{b}\gamma$ -ray branching ratios.

percent) are shown in the WBMB predictions of Fig. 2. Clearly the predictions are in disagreement with experiment. For instance, we predict a  $1_2^+ \rightarrow 2_1^+$  branch ~10 times stronger than the  $1_2^+ \rightarrow 2_1^-$  branch we associate with the 1856-keV  $\gamma$  rays. We note, however, that as discussed in Sec. II, the predicted E1 transition strengths are subject to larger uncertainties than, say M1 strengths. Nevertheless, the predictions for  $\gamma$ -ray decays discussed here suggest the possibility of ambiguities in the singles  $\beta^-$ -delayed  $\gamma$ -ray spectrum; i.e., the predicted  $\gamma$ -ray transition energies are such as to suggest an unusually high probability for  $\gamma$ -ray energy doublets in the 900-950 keV range as well as the usual probability of overlooking weak transitions.

In conclusion, we predict the <sup>36</sup>Si  $\beta^-$  decay is mainly to the first two 1<sup>+</sup> states. When these states are placed as shown in Fig. 2, we obtain a  $\beta^-$  half-life in agreement with experiment. We view our predictions for E1 decays as unreliable, and the experimental  $\gamma$ -ray results as only partially understood, i.e., there are obvious disagreements of the predictions with experiment.

## 3. ${}^{37}P(\beta^-){}^{37}S$

<sup>37</sup>P decay was calculated initially with the experimental  $Q(\beta^-)$  value, 7587(400) keV, and the <sup>37</sup>S spectrum of Table V. With that result as orientation, the level scheme of Fig. 3 was constructed from the five  $\beta^-$ delayed  $\gamma$  rays reported by Dufour *et al.*<sup>2</sup> In doing so we relied on the predicted  $\gamma$ -ray transition strengths and the fact that first-forbidden decay is, once again, of no real importance at the present level of experimental sensitivity. In Table XIII we give the  $\beta^-$  decay results recalculated using the proposed decay scheme of Fig. 3. Predicted  $\gamma$ -ray transition strengths pertinent to the proposed decay scheme are listed in Table XIV. The predicted  $\gamma$  branchings of the  $1/2_1^+$ ,  $1/2_2^+$ , and  $3/2_2^+$  states are of particular interest. For the  $1/2^+$  states the dominant branch (92% in each case) is predicted to be to  $3/2_1^-$  and thus agrees with the proposed decay scheme on the right of Fig. 3. For the  $\gamma$  decay of  $3/2^+_2$  we have a mild disagreement in that the branch to  $3/2_1^-$  is predicted to be 41% with a 58% 1503-keV branch to  $3/2_1^+$ at 1397 keV. This latter transition was not observed. We have shown the experimental branching ratios into the 646- and 1397-keV levels as limits because the excess  $\gamma$ -ray flux out of these levels could very well be due to  $\gamma$ -ray cascades from higher-lying levels such as the  $2900 \rightarrow 1397$  transition just discussed. Given this interpretation, the WBMB predictions are in very good quantitative agreement with the proposed scheme.

#### **IV. DISCUSSION**

The present results join previous  $\operatorname{ones}^{4,5}$  in which a good account is given of allowed transitions between  $(2s, 1d)^n (fp)$  states<sup>1,2</sup> in neutron-rich  $A \leq 40$  nuclei. We believe that use of the extremely successful USD (2s, 1d) interaction is the principal reason for this success. We have concentrated on the  $\beta^-$  decay of N = 21 and 22 isotones. The daughters have Z < 20 and the smaller Z is the more that the 1fp or 2fp states in the daughter nu-

cleus are dominated by neutron, as opposed to proton, excitations to the (fp) shell. Thus, the allowed  $\beta^-$  decays, being  $\nu \rightarrow \pi$ , are dominated by  $(s,d) \rightarrow (s,d)$  transitions with the (fp) or  $(fp)^2$  neutrons as spectators. In the present cases, for instance, the contributions from  $\nu(fp) \rightarrow \pi(fp)$  transitions are all but negligible. Thus, the success of our calculations of Gamow-Teller transition rates in the present three cases and for <sup>37</sup>S, <sup>38</sup>Cl (Ref. 4) and <sup>35</sup>Si, <sup>36</sup>P (Ref. 5) serve to illustrate the validity of the USD interaction outside the range in which it was heretofore tested. As a corollary of these arguments, we note that the dominance of  $(s,d) \rightarrow (s,d)$  transitions justifies our use of the effective Gamow-Teller operator extracted from consideration of Gamow-Teller transitions between (*sd*) shell nuclei (Ref. 13).

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