

$\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  reaction in the one-gluon-exchange and the  $^3P_0$  models

M. Burkardt and M. Dillig

*Institute for Theoretical Physics, Universität Erlangen-Nürnberg, Erlangen, West Germany*

(Received 2 April 1987)

As an alternative to conventional meson-exchange models, we study exclusive  $\bar{p}p \rightarrow \bar{Y}Y$  production in the nonrelativistic one-gluon-exchange and the  $^3P_0$  model. Adjusting the overall coupling strengths at  $P_{lab} = 2.0$  GeV/c, the main uncertainty originates from the oscillator constant. Though both models yield qualitative agreement with experiment, a more detailed comparison favors the one-gluon-exchange model.

With the recent advent of the low-energy antiproton ring (LEAR), a systematic study of the production mechanism for strange baryon-antibaryon pairs in  $\bar{p}p$  annihilation becomes feasible. In fact, particularly for exclusive  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  production the rather scarce data<sup>1</sup> have been improved substantially around and slightly above the threshold.<sup>2</sup> Besides the threshold behavior of the total  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  cross section, angular distributions and asymmetries have been measured at four different energies. Information on other  $\bar{Y}Y$  channels, particularly on the  $\bar{\Lambda}\Sigma^0 + \bar{\Sigma}^0\Lambda$  and the  $\bar{\Sigma}^+\Sigma^+$  final state, will be available in the near future.

Exclusive  $\bar{Y}Y$  production is highly interesting from the theoretical point of view. Besides the novelty of the reaction, such a process involves a large momentum mismatch of typically  $> 600$  MeV/c, even at threshold. Consequently, this reaction is ideally suited for probing exotic degrees of freedom at very short distances  $< 0.4$  fm. By testing the “quark core” of the baryon-antibaryon interaction we expect information on dynamical aspects, not only in the framework of the “old-fashioned” meson-exchange model, but rather on the level of quark and gluon degrees of freedom.<sup>3,4</sup>

In this spirit we present, the following estimates for the  $\bar{p}p \rightarrow \bar{Y}Y$  cross sections, particularly for  $\bar{\Lambda}\Lambda$  production in terms of the one-gluon-exchange [OGE, Fig. 1(a)]<sup>5</sup> and the vacuum pair creation (VPC)  $^3P_0$  model [Fig. 1(b)].<sup>6</sup>

Though both models parametrize quark-gluon dynamics in a similar framework, the philosophy behind them is rather different: While the OGE model relies on the perturbative gluon exchange in lowest order, the  $^3P_0$  model

parametrizes  $\bar{q}q$  annihilation in the strong coupling limit. This characterizes the range where the two models should be applicable. For hard processes, like  $\bar{c}c$  and  $\bar{b}b$  creation, where  $\alpha_s(q^2)$  is small, perturbation theory should be justified,<sup>7</sup> whereas “soft”  $\bar{u}u$  and  $\bar{d}d$  production should be more adequately described in the  $^3P_0$  model.<sup>8</sup> For  $\bar{s}s$  production around  $q^2 = (1 \text{ GeV})^2$ , where neither a perturbative evaluation to first order in  $\alpha_s$ , nor in  $1/\alpha_s$ , seems to be justified.<sup>9</sup> Possibly, both parametrizations overlap.

The main obstacle for a formulation of  $\bar{p}p \rightarrow \bar{Y}Y$  on the level of quarks are “conventional” initial and final state interactions due to the coupling of the  $\bar{B}B$  system to the elastic and to inelastic channels. The introduction of purely phenomenological optical potentials—as done conventionally—raises immediately a serious double-counting problem. To avoid that, we proceed here rather pragmatically. Working in the plane wave Born approximation (PWBA) we sum up distortion effects in an effective, energy-independent coupling constant, which we normalize to the total cross section at 600 MeV/c above the  $\bar{\Lambda}\Lambda$  threshold. The smooth energy dependence of the distortion effect in the  $\bar{p}p$  channel, and presumably also in the  $\bar{Y}Y$  channel supports such a simple prescription.

Final state interactions in the  $\bar{Y}Y$  channel are not known experimentally. However, simple theoretical estimates indicate that at a scattering energy  $p_{lab} \approx 2$  GeV/c for the incoming  $\bar{p}$  the  $\bar{Y}Y$  interaction should be significantly weaker than the  $\bar{p}p$  interaction. Hence, except for  $\bar{Y}Y$  production very close to the corresponding  $\bar{Y}Y$  threshold we expect distortion effects to be dominated by the very strong  $\bar{p}p$  initial state interaction.<sup>10-12</sup>

With these preliminaries the differential cross section is given (in an obvious notation) by

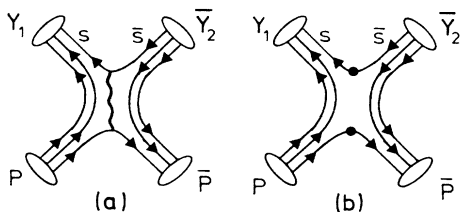


FIG. 1. Schematical representation of  $\bar{p}p \rightarrow \bar{Y}Y$  in the (a) one-gluon exchange and (b) the vacuum pair creation model.

$$\frac{d\sigma}{d\Omega} = \frac{P_f}{P_i} \frac{m_N m_\Lambda}{4\pi^2} |V(q)|^2. \tag{1}$$

Following standard arguments (details are given in a forthcoming paper) the corresponding transition operator is given in the OGE model by<sup>12,13</sup>

$$\hat{T} = \frac{\alpha_s}{(2m_q)^2} \frac{(\lambda_q - \lambda_{\bar{q}}^*)^2}{24} \frac{(\sigma_q + \sigma_{\bar{q}})^2}{4} \delta(\mathbf{r}), \tag{2}$$

where  $\lambda$  denotes  $SU_3$  Gell-Mann matrices for the color sector. Correspondingly, the  ${}^3P_0$  operator reads<sup>14</sup>

$$\hat{T} = g_{{}^3P_0} \Theta^\dagger \Theta, \quad (3)$$

with

$$\Theta = (\chi_{\bar{q}q}^{S-1}, \nabla)^{J=0} \delta(\mathbf{r}).$$

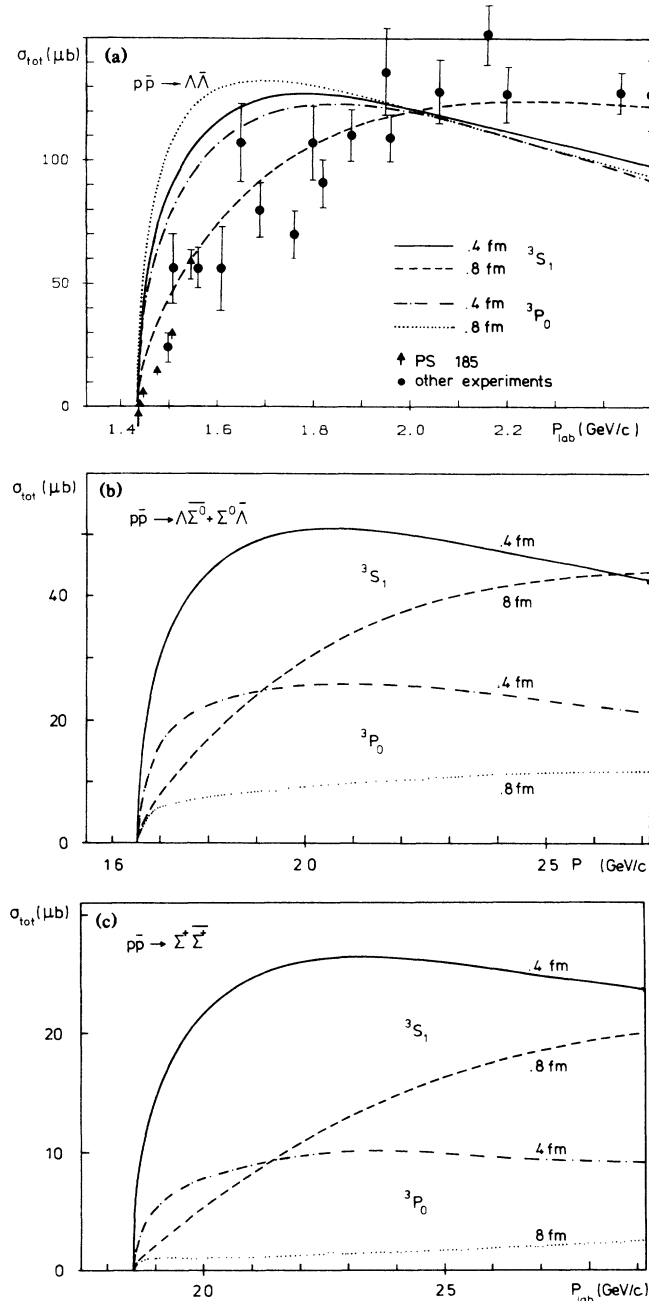


FIG. 2. Energy dependence of the total  $\bar{p}p \rightarrow \bar{Y}Y$  cross section into (a) the  $\bar{\Lambda}\Lambda$ , (b) the  $\bar{\Lambda}\Sigma^0 + \Sigma^0\bar{\Lambda}$ , and (c) the  $\bar{\Sigma}^+\Sigma^+$  antihyperon-hyperon channels. Compared are the OGE model [Fig. 1(a); full and dashed line] and the VPC model [Fig. 1(b); dashed-dotted and dotted line] for two oscillator radii  $R=0.4$  fm and 0.8 fm. The data for the  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  channel (for the other channels the existing experimental data are very poor) are taken from Refs. 1 and 2.

Note that  $g_{\text{OGE}}$  and  $g_{{}^3P_0}$ , which are originally given as

$$g_{\text{OGE}} = a_s / (2m_q)^2, \quad (4)$$

$$g_{{}^3P_0} = \gamma^2 / (2m_{\text{eff}}),$$

are treated in the following as effective coupling constants.

For Gaussian wave functions<sup>15</sup>

$$\psi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3, \mathbf{r}) = (\sqrt{3}\pi R^2)^{-3/2} \exp\left[-\sum_i (\mathbf{r}_i - \mathbf{r})^2 / (2R^2)\right] \times \delta\left(\frac{1}{3}(\mathbf{r}_1 + \mathbf{r}_2 + \mathbf{r}_3) - \mathbf{r}\right), \quad (5)$$

together with the completely antisymmetric color term

$$\chi_c = e_{ijk} \langle q_i, q_j, q_k \rangle, \quad (6)$$

the transition matrix element yields

$$V({}^3S_1; \mathbf{q}) = \frac{4}{9} g_{\text{OGE}} M_{\text{SF}} \exp(-q^2 R^2 / 3), \quad (7)$$

and

$$V({}^3P_0; \mathbf{q}) = \sum_{m, m'} g_{{}^3P_0} K(m, m') [\mathbf{e}_m \mathbf{e}_m^* - \frac{2}{3} R^2 (\mathbf{e}_m \mathbf{q})(\mathbf{e}_m^* \mathbf{q})] \times \exp(-q^2 R^2 / 3), \quad (8)$$

respectively [above  $M_{\text{SF}}$  and  $K(m, m')$  denote appropriate spin-flavor factors]. The polarization vectors  $\mathbf{e}_m$  and  $\mathbf{e}_m^*$  reflect the annihilation of the  $\bar{q}q$  ( $q=u, d$ ) and the creation of the  $\bar{s}s$  pair in the spin-triplet ( $1, -m$ ) and ( $1, -m'$ ) states, respectively.

With  $g_{\text{OGE}}$  and  $g_{{}^3P_0}$  fixed from the data, the oscillator parameter  $R$  remains the only free parameter in the two models. [As an effective radius,  $R$  should not be confused with the conventional baryon radius, in our static model for the  $\bar{q}q \rightarrow \bar{s}s$  transition operator,  $R$  summarizes, in addition, nonstatic corrections in  $(p/m)$ , or, equivalently, nonlocalities of the order of the  $\bar{s}s$  Compton-wave length.]

Characteristic results are presented in the following figures. In Fig. 2 the total cross section for  $\bar{p}p$  annihilation into  $\bar{\Lambda}\Lambda$  and— to illustrate the differences— into other  $\bar{Y}Y$  channels are compared. The differential cross section for  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  at a lab momentum of 1508 MeV/c is shown in Fig. 3. The basic trends of the results are easily understood: They dominantly reflect the interplay of the large momentum transfer, the size of the interacting objects, and phase-space constraints. Comparison with recent experimental data from LEAR for the channel<sup>6</sup> indicates that a consistent fit of the energy dependence of both the total and the differential cross section with a given  $R$  is difficult in the  ${}^3P_0$  model. The data seem to favor the OGE model: a qualitative consistency is obtained with the effective oscillator constant  $R=0.8$  fm. Comparing other  $\bar{Y}Y$  channels with  $\bar{\Lambda}\Lambda$  production our results predict a stronger sensitivity on  $R$  due to an increase in the momentum transfer and from the different  $SU_6$  wave functions.

Summarizing, we have presented simplistic calculations for the  $\bar{p}p \rightarrow \bar{Y}Y$  reaction in the “QCD-inspired” OGE and  ${}^3P_0$  model. As a preliminary conclusion, existing data seem to favor an effective one-gluon exchange mechanism.

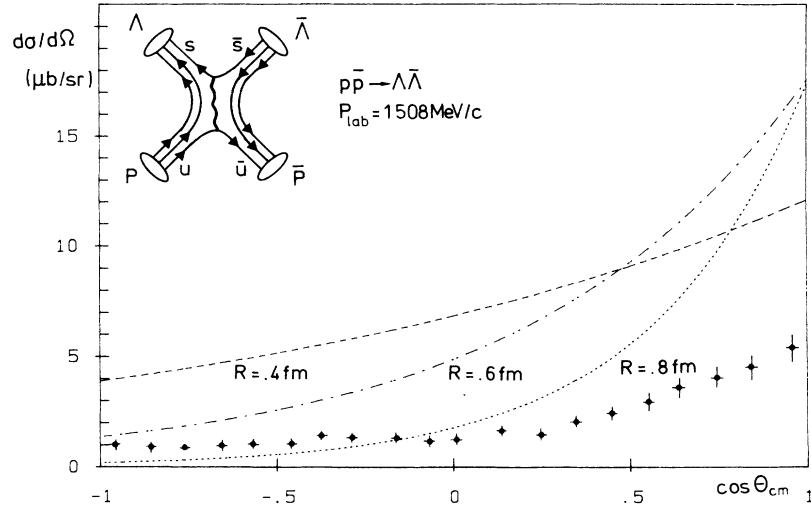


FIG. 3. Differential  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  cross section at a lab momentum of 1508 MeV/c for the OGE and the VPC model. The predictions for three different oscillator constants are compared with recent data from LEAR (Ref. 2).

For a more quantitative insight, however, a systematic comparison with different observables for the  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  reaction (cross section, analyzing power, and spin correlations) and an extension of the experimental information on other  $\bar{Y}Y$  channels are obviously necessary.

This work was supported in part by Bundesministerium für Forschung und Technologie, Bonn, West Germany.

<sup>1</sup>R. Armenteros and B. French, in *High Energy Physics*, edited by E. H. S. Burhop (Academic, New York, 1969), Vol. IV.

<sup>2</sup>K. Kilian, in *Workshop on Spin Phenomena in Hadronic Interactions*, Wuppertal, 1986; P. D. Barnes *et al.*, in *Proceedings of the Conference on Antinucleon and Nucleon-Nucleus Interactions, Telluride, Colorado, 1986*, edited by G. E. Walker, C. D. Goodman, and C. Olmer (Plenum, New York, 1985).

<sup>3</sup>R. H. Dalitz *et al.*, in *Proceedings of the International Conference on Hypernuclear and Kaon Physics*, Heidelberg, 1982, edited by B. Povh (unpublished).

<sup>4</sup>H. Genz and S. Tatur, *Phys. Rev. D* **30**, 63 (1984).

<sup>5</sup>A. Faessler, G. Lübeck, and K. Shimizu, *Phys. Rev. D* **26**, 3280 (1982).

<sup>6</sup>A. Le Yaouanc *et al.*, *Phys. Rev. D* **8**, 2223 (1973); **9**, 1415 (1974); **11**, 1272 (1975); and A. M. Green, J. A. Niskanen, and S. Wycech, *Phys. Lett.* **139B**, 15 (1984).

<sup>7</sup>H. R., Rubinstein and H. Snellman, *Phys. Lett.* **165B**, 187 (1985).

<sup>8</sup>H. G. Dosch and D. Gromes, *Phys. Rev. D* **33**, 1378 (1986); N. Isgur and J. Paton, *ibid.* **31**, 2910 (1985).

<sup>9</sup>A. M. Green, in *International Symposium on Hypernuclear and Kaon Physics*, Tokyo, 1986 (unpublished).

<sup>10</sup>F. Tabakin and R. A. Eisenstein, *Phys. Rev. C* **31**, 1857 (1985).

<sup>11</sup>M. Dillig and R. v. Frankenberg, in *Proceedings of the Conference on Antinucleon and Nucleon-Nucleus Interactions, Telluride, Colorado, 1985*, edited by G. E. Walker, C. D. Goodman, and C. Olmer (Plenum, New York, 1985).

<sup>12</sup>M. Kohno and W. Weise, *Phys. Lett. B* **179**, 15 (1986).

<sup>13</sup>S. Furui and A. Faessler, *Nucl. Phys. A* **468**, 669 (1987).

<sup>14</sup>A. M. Green and J. A. Niskanen, Report No. HU-TFT-86-40 (unpublished); and A. M. Green, in *Proceedings of the 1986 INS International Symposium on Hypernuclear Physics, Tokyo, 1986*, edited by H. Bando, O. Hasimoto, and K. Ogawa (Institute for Nuclear Study, University of Tokyo, Tokyo, 1986).

<sup>15</sup>M. Oka and K. Yazaki, *Phys. Lett.* **90B**, 41 (1980).