High spin states in ¹²⁸Ce

J. L. S. Carvalho,^{*} F. M. Bernthal,[†] and R. M. Ronningen Department of Chemistry and Cyclotron Laboratory, Michigan State University, East Lansing, Michigan 48824

N. R. Johnson, J. S. Hattula,[‡] I. Y. Lee, and M. P. Fewell[§] Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831

L. L. Riedinger

University of Tennessee, Knoxville, Tennessee 37916 and Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831

J. C. Wells

Tennessee Technological University, Cookeville, Tennessee 38505 and Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831 (Received 30 November 1984)

Properties of high spin states in ¹²⁸Ce have been measured following the reaction ¹¹²Cd(²⁰Ne, 4n) ¹²⁸Ce induced by 103-MeV ²⁰Ne ions. High efficiency γ - γ coincidence measurements and angular distribution measurements showed a series of stretched *E*2 transitions that form the yrast sequence up to $I = 24^+$, six stretched *E*2 transitions which form one sideband, and four transitions of undetermined multipolarity forming a second sideband.

An inspection of both the energy level spacings and the lifetimes of excited states in the light cerium nuclei reveals a region of pronounced collective behavior. An examination of the data in Refs. 1–4 shows that this collective pattern evolves rapidly in moving from ¹³⁴Ce to ¹³²Ce to ¹³⁰Ce. Ward *et al.*⁵ carried out measurements on the yrast sequence in ¹²⁸Ce up through the 16⁺ state and found a level sequence indicative of enhanced collective behavior. To further clarify the collective behavior in this light cerium region we have carried out detailed γ - γ coincidence measurements on ¹²⁸Ce. Preliminary accounts of this work are contained in Refs. 6 and 7 while a more detailed treatment can be found in Ref. 8.

For the present studies the reaction ¹¹²Cd(²⁰Ne,4n) ¹²⁸Ce was utilized by employing a beam of 103-MeV ²⁰Ne ions from the Oak Ridge Isochronous Cyclotron (ORIC). Selfsupporting target foils of ¹¹²Cd used in these experiments were 1.0 mg/cm² thick and were 98.5% enriched. The beam energy, selected after carrying out excitation function measurements, brought about 45th of maximum angular momentum into the compound system according to calculations that assume sharp nuclear surfaces. The experimental apparatus consisted of seven large volume germanium detectors in the horizontal plane and two 25 cm×25 cm NaI detectors located above and below the reaction chamber. The NaI detectors served as a total γ -ray energy spectrometer and, thus, provided a means for selective gating in the total energy spectrum with a resulting enhancement of the desired 4n reaction channel. However, since ¹²⁸Ce lies somewhat close to the proton drip line, it was necessary to contend with several charged particle reaction channels (e.g., $\alpha 3n$, p3n, and 2p2n) which are not well separated from the 4n channel with a total energy selection device. Nevertheless, because much of the cross section went into the 4n channel, the coincidence spectra were of good qualitv.

The coincidence event count rate was approximately 2 kHz, while the average count rate for the NaI detectors was around 80 kHz and for the Ge detectors it was about 8 kHz. About 240 million pairs of $\gamma - \gamma$ coincidence events were stored in list mode on magnetic tape. Regions of the total energy spectrum were selected that gave enhancement of the dominant reaction channels and with these restrictions. the tapes were scanned for prompt $\gamma - \gamma$ coincidence events which were constructed into 4096×4096 channel coincidence matrices. From these matrices, one-dimensional spectra for any γ -ray energy gating interval of interest could be extracted. To illustrate these data, the coincidence spectrum from summed gates in the yrast band is shown in Fig. 1. From the coincidence data it was possible to develop the yrast sequence up to $I = 24^+$ and to assign with less certainty two partially developed side bands. The level scheme shown in Fig. 2 summarizes these results. An additional 429.9-keV transition identified with sideband 2 is not shown in Fig. 2, but it probably depopulates the 2418.7-keV level. Angular distribution data showed that the yrast sequence in this scheme consisted of stretched E2 transitions, as does sideband 1. However, since we were unable to determine the multipolarities of the interband transitions between sideband 1 and the ground band, it was not possible to assign spins to these sideband states. Also, the data were not of sufficient statistical quality for a determination of the multipolarities in sideband 2.

At spin 10⁺ in this nucleus, a backbend similar to the ones seen in ^{130,132,134}Ce is observed. Assuming K = 0 in both the ground and s bands, we plot in Fig. 3 the angular momentum along the rotation axis, I_x , $(I_x = I + \frac{1}{2})$ as a function of the rotational frequency $(\hbar \omega)$ for all four of these nuclei. Inspection of these curves shows that in moving to the lighter cerium isotopes the backbending sets in at a lower rotational frequency. However, ^{128,130,132,134}Ce show very similar crossing frequencies of ~ 0.3 MeV and have



FIG. 1. Coincidence spectrum from summed gates on transitions in the yrast sequence of 128 Ce.

very similar alignment gain (ΔI_x) values of 8, 9, 10, and 9.3, respectively, in the backbending process. It appears that the alignments all come from a strongly decoupled high-*j* orbit. In principle, this could be either the $h_{11/2}$ protons or the $h_{11/2}$ neutrons since both orbitals are near the Fermi surface in these nuclei. However, blocking measurements in 127 La and 129 La by Ward *et al.*, ⁵ in 129 Ce by Aryaeinejad et al.,⁹ and in ¹³¹Ce by Nolan et al.² have shown rather conclusively that the $h_{11/2}$ protons are responsible for the backbending in this region. Additional verification on this point is provided by cranked shell model calculations. We have carried out such calculations for ¹²⁸Ce, as did Nolan et al.² for ¹³⁰Ce, and in both cases the alignment gains and crossing frequencies are consistent with alignment by $h_{11/2}$ protons. (In these calculations the nucleus was assumed to be prolate, i.e., $\gamma = 0^{\circ}$.) It should be pointed out, however, that in these light cerium nuclei, one must retain some reservation about the particles active in the alignment process. This is because it appears quite probable that neutrons play a role in ¹³⁴Ce backbending, based on the measured g-factor value of -0.30 for the 10^+ state by Zemel et al.¹⁰ Todd et al.⁴ interpreted the reduced frequency of the highest state they observed in ¹³⁰Ce (26⁺) as an effect



FIG. 2. Level scheme of 128 Ce deduced from the present coincidence measurements.

of the $h_{11/2}$ neutron alignment process, as predicted by cranked shell model calculations. Such a crossing has apparently not begun yet at I = 24 in ¹²⁸Ce, judging from the I_x vs $\hbar \omega$ curve shown in Fig. 3. It is possible that such a crossing will occur in ¹²⁸Ce at slightly higher frequencies.



FIG. 3. Plots of aligned momentum along the rotation axis (I_x) vs rotational frequency $(\hbar \omega)$ for ^{128,130,132,134}Ce.

The present study has provided increased understanding of the high spin states in ¹²⁸Ce and verified the presence of an increased moment of inertia which is indicative of increasing collectivity in this nucleus. In a separate recent study, we¹¹ measured lifetimes of yrast states in ¹²⁸Ce by the Doppler-shift recoil-distance method and showed clear evidence for enhanced collective behavior in the ground band. The B(E2) values deduced for the 2⁺ through 14⁺ states indicated that in the ground band ¹²⁸Ce conforms much more closely to rigid-rotor behavior than do the heavier cerium isotopes. It is interesting that in the *s* bands, the moments of inertia of ^{128,130,132}Ce are very similar as evidenced by the I_{χ} vs $\hbar \omega$ curves (Fig. 3) which practically coincide. This is in contrast to the markedly varying moments in the ground bands. Although it appears that the

- *Permanent address: Instituto de Radioprotecao e Dosimetria, Comitato Nazionale per l'Energia Nucleare, Rio de Janeiro, Brazil.
- [†]Present address: United States Nuclear Regulatory Commission.
- *Permanent address: University of Jyväskylä, Finland.
- Permanent address: Australian National University, Canberra, Australia.
- ¹D. Husar, S. J. Mills, H. Gräf, U. Neumann, D. Pelte, G. Seiler-Clark, Nucl. Phys. A292, 267 (1977).
- ²P. J. Nolan, D. M. Todd, P. J. Smith, D. J. G. Love, P. J. Twin, O. Andersen, J. D. Garrett, G. B. Hagemann, and B. Herskind, Phys. Lett. **108B**, 269 (1982).
- ³P. J. Nolan, R. Aryaeinejad, D. J. G. Love, A. H. Nelson, P. J. Smith, D. M. Todd, P. J. Twin, J. D. Garrett, G. B. Hagemann, and B. Herskind, in *Proceedings of the Conference on High Angular Momentum Properties of Nuclei*, Oak Ridge, Tennessee, edited by N. R. Johnson (Harwood Academic, New York, 1983), p. 57.
- ⁴D. M. Todd, R. Aryaeinijad, D. J. G. Love, A. H. Nelson, P. J. Nolan, P. J. Smith, and P. J. Twin, J. Phys. G **10**, 1407 (1984).

alignment of the $h_{1/2}$ protons affects these moments of inertia greatly, producing nearly identical values in the *s* bands of ¹²⁸⁻¹³²Ce, it must be stressed that there seems to be no general consensus on the underlying causes for this behavior.

One of us (J.L.S.C.) wishes to thank the Physics Division of the Oak Ridge National Laboratory for its hospitality during his one and one-half year stay there. This research was supported by the U.S. Department of Energy under Contract No. DOE-AC05-840R21400 with Martin Marietta Energy Systems, Inc. Research at the University of Tennessee is supported by the U.S. Department of Energy under Contract No. DE-AS05-76ER0-4936.

- ⁵D. Ward, H. Hertschat, P. A. Butler, P. Colombani, R. M. Diamond, and F. S. Stephens, Phys. Lett. 56B, 139 (1975).
- ⁶J. Carvalho, F. Bernthal, R. Ronningen, M. Fewell, J. Hattula, N. Johnson, I. Y. Lee, H. Ower, L. Riedinger, and J. Wells, Bull. Am. Phys. Soc. 24, 518 (1982).
- ⁷J. L. S. Carvalho, N. R. Johnson, R. M. Ronningen, J. S. Hattula, I. Y. Lee, M. P. Fewell, F. M. Bernthal, J. C. Wells, L. L. Riedinger, and H. Ower, Oak Ridge National Laboratory Physics Division Progress Report No. ORNL-6004, 1983, p. 88.
- ⁸J. L. S. Carvalho, Ph.D. thesis, Michigan State University, 1982.
- ⁹R. Aryaeinejad, D. J. G. Love, A. H. Nelson, P. J. Nolan, P. J. Smith, D. M. Todd, and P. J. Twin, J. Phys. **10**, 955 (1984).
- ¹⁰A. Zemel, C. Broude, E. Dafni, A. Geldberg, M. B. Goldberg, J. Gerber, G. J. Kumbartzki, and K. H. Speidel, Nucl. Phys. A383, 165 (1982).
- ¹¹J. C. Wells, N. R. Johnson, J. Hattula, M. P. Fewell, D. R. Haenni, I. Y. Lee, F. K. McGowan, J. W. Johnson, and L. L. Riedinger, Phys. Rev. C **30**, 1532 (1984).