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PHYSICAL REVIEW C

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40 K $(n, \gamma){}^{41}$ K Reaction and the Level Structure of 41 K[†]

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The low-lying level structure of ⁴¹K has been studied using the thermal-neutron capture reaction ${}^{40}K(n, \gamma){}^{41}K$ on an isotopically separated target of ${}^{40}K$. The γ -ray spectrum from this reaction has been studied in the energy range from 0.1 to 10.1 MeV using a Li-drifted Ge spectrometer system. γ - γ coincidence measurements using Ge(Li) detectors have also been made. Spin and parity assignments for the excited states below 2450 keV are proposed, primarily on the basis of γ -ray branching to levels with established spin and parity values. The proposed level energy $[\text{keV}(I^{\pi})]$ values are $0(\frac{3}{2}^+)$, 980.4 $(\frac{1}{2}^+)$, 1293.4 $(\frac{7}{2}^-)$, 1559.9 $(\frac{1}{2}^+)$, $1582.0(\frac{5}{2}^+), \ 1677.5(\frac{5}{2}^+, \frac{7}{2}^+), \ 1698.1(\frac{5}{2}^\pm, \frac{7}{2}^+), \ 2144.1(\frac{5}{2}^+), \ 2166.0(\frac{1}{2}^+, \frac{3}{2}^\pm), \ 2316.5(\frac{5}{2}^\pm, \frac{7}{2}^+), \ 2316.5(\frac{5}{2}^\pm,$ 2447.9 $(\frac{1}{2}^{\pm}, \frac{3}{2}^{\pm})$. Additional levels have been observed at 2494.7, 2507.9, 2527.9, 2599.8, 2681.5, 2712.2, 2756.5, 2760.7, 3042.1, 3142.1, 3164.5, 3213.4, 3235.6, and 3281.1 keV. These low-lying excited states of ⁴¹K are discussed in terms of two-particle, one-hole configurations of the form $p (d_{3/2})^{-1} n (f_{7/2})^2$.

I. INTRODUCTION

This work describes an investigation of the ⁴¹K energy levels below ≈ 3.3 MeV that are populated in the ${}^{40}K(n, \gamma){}^{41}K$ reaction. The low-lying excited levels of ⁴¹K have been studied previously by observation of the radioactive decay of ⁴¹Ar and ⁴¹Ca and by a variety of charged-particle reactions.¹⁻⁴ The principal sources of information have been studies of the ${}^{41}K(p,p'){}^{41}K$ reaction² and the ${}^{40}Ar$ - $(p, \gamma)^{41}$ K reaction,³ which have identified a rather large number of levels. In addition, spin and parity values have been proposed for the ground state and the five lowest excited levels.⁴⁻⁷

No direct study of the ${}^{40}K(n,\gamma){}^{41}K$ reaction has been reported previously, and the only data available on this reaction are from an early pair-spectrometer study in which a natural potassium target was used.⁸ Three weak transitions observed in that study were assigned to ⁴¹K because they had energies in excess of the binding energy of the other naturally occurring potassium isotopes.

II. EXPERIMENTAL PROCEDURE

A. Capture γ -Ray Spectrum

The thermal-column through-port capture γ -ray facility at the Los Alamos Omega West Reactor was used to record the ${}^{40}K(n, \gamma)$ spectrum. This facility has been described in detail elsewhere.⁹ The spectrum was studied throughout the energy range of 0.1-10.1 MeV. The thermal-neutron flux at the target was $\approx 3 \times 10^{11} n/cm^2$ sec.

The ⁴⁰K target was obtained from Oak Ridge Na-

tional Laboratory and consisted of 55.7 mg of K_2CO_3 powder enriched to 30.3% in ${}^{40}K$. To identify those lines in the spectrum arising from contaminating isotopes, a natural potassium target was also studied.

The target material, enclosed in a high-purity graphite sample container, was inserted into an evacuated Bi channel in the thermal column of the Omega West Reactor. A Ge(Li) detector, located ≈ 6 m from the target, viewed the sample through a series of collimators.

The spectrometer system used consisted of an ≈ 6 -cm³ Ge(Li) detector, surrounded by a large bifurcated NaI(Tl) annulus (20 cm diam by 30 cm long, with a 6.5-cm bore along its axis). The

TABLE I. High-energy γ rays from the ${}^{40}K(u, \gamma){}^{41}K$ reaction.

	γ-ray	Partial cross	Excitation
Line	energy	section	energy
No.	(keV)	(mb)	(keV)
1	8802.5 ± 0.4	351 ± 73	1293.5
2	8579.2 ± 0.5	22 ± 5	1516.8
3	8513.7 ± 0.4	55 ± 12	1582.3
4	8417.7 ± 0.4	34 ± 8	1678.2
5	8397.6 ± 0.4	55 ± 13	1698.3
6	7951.2 ± 0.4	816 ± 180	2144.8
7	7791.5 ± 1.1	56 ± 19	2304.5
8	7779.1 ± 0.4	2613 ± 570	2316.9
9	7601.5 ± 0.5	93 ± 21	2494.5
10	7588.3 ± 0.4	189 ± 42	2507.6
11	7416.6 ± 0.7	84 ± 23	2679.3
12	7384.5 ± 0.4	679 ± 150	2711.5
13	7340.2 ± 0.4	626 ± 140	2755.8
14	6979.7 ± 0.7	38 ± 11	3116.2
15	6953.6 ± 0.4	596 ± 140	3142.4
16	6882.2 ± 0.4	489 ± 110	3213.8
17	6860.7 ± 1.0	75 ± 26	3235.3
18	6663.9 ± 0.4	254 ± 57	3432.1
19	6646.0 ± 0.5	93 ± 23	3450.0
20	6629.3 ± 0.7	38 ± 10	3466.7
21	6620.6 ± 0.5	65 ± 15	3475.4
22	6607.2 ± 0.6	27 ± 7	3488.8
23	6574.7 ± 0.5	56 ± 15	3521.3
24	6561.2 ± 1.0	192 ± 43	3534.8
25	6535.5 ± 1.0	27 ± 6	3560.5
26	6500.8 ± 1.5	11 ± 4	3595.2
27	6483.5 ± 1.0	38 ± 9	3612.5
28	6452.8 ± 1.2	13 ± 4	3643.2
29	6445.1 ± 1.0	124 ± 28	3650.9
30	6395.5 ± 1.1	23 ± 6	3700.5
31	6333.6 ± 0.2	498 ± 100	3762.4
32	6320.4 ± 0.3	251 ± 55	3775.5
33	6289.4 ± 0.5	69 ± 16	3806.6
34	6268.0 ± 0.2	267 ± 56	3827.9
35	6225.5 ± 0.3	48 ± 11	3870.5
36	6111.5 ± 0.5	177 ± 51	3984.5
37	6098.7 ± 0.2	1715 ± 350	3997.3
38	6068.6 ± 0.2	46 ± 10	4027.3

Ge(Li) detector has an energy resolution width of $\approx 4 \text{ keV}$ at 1.0 MeV and a resolution of $\approx 6 \text{ keV}$ at 8 MeV. In the energy range below 2 MeV the system was operated as a total-energy spectrometer (anti-coincidence mode). For energies >2 MeV the system was operated as a two-quantum escape-pair spectrometer (pair-production mode). The spectra obtained with both modes are substantially free of underlying Compton distributions.

The capture γ -ray spectra were recorded with a 1600-channel pulse-height analyzer in four separate runs covering the energy ranges 0.1–2.1, 1.6–4.6, 4.0–6.8, and 6.1–10.1 MeV.

Correction for the nonlinearity of the electronic system was made using a precision pulser to provide reference points at \approx 70 channel intervals. Digital gain stabilization was applied to the analyzer analog-to-digital converter to obviate electronic drifts. The stabilizer was locked on artificially generated peaks which were produced by a highly stable pulser.¹⁰ This pulser produces two independent pulse amplitudes so that both the gain and the zero intercept of the analyzer can be simultaneously stabilized. During runs lasting as long as 23 h, no line broadening was observed.

For energies <2 MeV both the relative detection efficiency of the spectrometer and the energy calibration were determined from measurements on a series of calibrated radioactive sources. Above 2 MeV the spectrometer calibration was performed using as standards the energies¹¹ and cross sections¹² of the ¹⁴N(n, γ)¹⁵N lines emitted from a melamine target.

The spectral data were analyzed with the aid of a variable-metric minimization computer program which least-squares fitted a Gaussian function to the observed peaks. This technique permits the energies of the more intense γ -ray transitions to be determined with an accuracy of ≈ 0.5 keV.

B. γ - γ Coincidence Studies

Coincidences of low-energy γ transitions with other low-energy γ transitions (low-low coincidences) were studied with the coincidence capture γ -ray facility at the Los Alamos Omega West Reactor. The general features of this facility have been described in a previous paper.¹³ A neutron beam, $\frac{3}{8}$ in. in diameter, with an intensity of about $3 \times 10^6 n/\text{sec}$ impinges on the target, which is placed outside the biological shield of the reactor. The two Ge(Li) detectors used in the present measurements had active volumes of 35 and 45 cm³. The detectors were placed close to the neutron beam, 180° apart, and in a line perpendicular to the beam. A thin ceramic disk containing ⁶LiF was placed between each detector and the target to

209

	γ -ray	Partial cross				γ-ray	Partial cross		
Line	energy	section	Level		Line	energy	section	Level	
No.	(keV)	(mb)	assignment	Confidence	No.	(keV)	(mb)	assignment	Confidence
1	198 8 + 0 5	146 ± 50			56	1920 0 + 0 8	643 ± 170	3213→1293	0
2	246.8 ± 0.4	274 ± 85		9	57	1920.0 ± 0.0	539 ± 200	3210 + 1293	C
3	380.8 ± 1.4	48 ± 41		a	58	1946.4 ± 1.2	322 ± 170	0200 1200	C
4	384.2 ± 1.2	69 ± 48	$1678 \rightarrow 1293$	Ъ	59	1910.1 = 1.2 1950.3 ± 1.2	224 ± 140		
5	396.2 ± 0.4	235 ± 74	$2712 \rightarrow 2317$	ĉ	60	1973.9 ± 0.9	270 ± 79		
6	445.8 ± 0.4	114 ± 38	$2144 \rightarrow 1698$	c	61	2047.7 ± 1.1	138 ± 54		
7	510.9 ± 0.4		Annihilation		62	2062.0 ± 1.3	106 ± 45	$3042 \rightarrow 980$	b
•	01010 011		radiation		63	2114.4 ± 0.9	325 ± 83		
8	516.6 ± 0.7	281 ± 100	$2682 \rightarrow 2166$	b	64	2138.7 ± 0.9	506 ± 140		
9	579.3 ± 0.4	443 ± 140	$1560 \rightarrow 980$	e	65	2144.1 ± 0.8	1655 ± 370	$2144 \rightarrow 0$	b
10	584.1 ± 0.4	599 ± 200	$2144 \rightarrow 1560$	c.d	66	2156.6 ± 0.9	469 ± 130		
11	584.2 ± 0.4	147 ± 82	$2166 \rightarrow 1582$	c.d	67	2167.0 ± 1.3	152 ± 85	$2166 \rightarrow 0$	b
12	601.2 ± 0.4	460 ± 140	$1582 \rightarrow 980$	c c	68	2171.4 ± 1.3	156 ± 82		
13	613.1 ± 0.4	328 ± 100	$2757 \rightarrow 2144$	e	69	2194.5 ± 1.2	128 ± 62		
14	622.4 ± 1.2	60 ± 26		-	70	2202.2 ± 1.3	122 ± 62		
15	634.1 ± 0.5	345 ± 110	$3142 \rightarrow 2508$	c	71	2214.6 ± 1.1	266 ± 79		
16	640.2 ± 1.3	68 ± 37	$2317 \rightarrow 1678$	b	72	2223.3 ± 0.8	200 10	$H(n, \gamma)$	
17	655.9 ± 0.5	282 ± 91	$3165 \rightarrow 2508$	ê	73	2240.9 ± 1.0	257 ± 77		
18	670.5 ± 0.4	219 ± 70	$3165 \rightarrow 2495$	e	74	2248.4 ± 1.3	116 ± 61		
19	694.0 ± 0.5	98 ± 36	$3142 \rightarrow 2448$	h	75	2298.3 ± 0.9	135 ± 44		
20	719.2 ± 0.7	98 ± 49	$3213 \rightarrow 2495$	b	76	2316.1 ± 0.9	261 ± 77	$2317 \rightarrow 0$	h
21	733.8 ± 0.5	331 ± 120	$2317 \rightarrow 1582$	ĉ	77	2319.6 ± 0.9	362 ± 95		Ň
22	788.4 ± 0.8	222 ± 130	$3236 \rightarrow 2448$	b	78	24151+11	184 ± 70		
23	796.9 ± 0.4	407 ± 130	$2495 \rightarrow 1698$	c	79	2431.6 ± 1.3	101 ± 10 115 ± 52		
24	817.5 ± 0.4	1305 ± 420	$2495 \rightarrow 1678$	c	80	2437.3 ± 1.0	335 ± 98		
25	830.5 ± 0.4	1342 ± 430	$2508 \rightarrow 1678$	c	81	2441.6 ± 1.1	202 ± 76		
26	850.4 ± 0.4	1536 ± 480	$2528 \rightarrow 1678$	2	82	2448.0 ± 1.1	120 ± 53	$2448 \rightarrow 0$	а
27	896.0 ± 0.5	158 ± 59	$3213 \rightarrow 2317$	b	83	2460.3 ± 1.0	43 ± 18		
28	918.9 ± 0.4	335 ± 110	$3236 \rightarrow 2317$	c	84	2467.7 ± 0.8	162 ± 37		
29	947.6 ± 0.5	178 ± 63	$2508 \rightarrow 1560$	е	85	2481.5 ± 0.8	230 ± 50		
30	980.4 ± 0.4	1504 ± 470	$980 \rightarrow 0$	с	86	2487.7 ± 0.8	460 ± 95		
31	1006.7 ± 1.3	343 ± 160			87	2502.6 ± 0.8	352 ± 75		
32	1012.7 ± 1.8	321 ± 200	$2712 \rightarrow 1698$	с	88	2508.4 ± 0.8	959 ± 200	2508 - 0	Ъ
33	1017.0 ± 1.4	$474\pm\!220$			89	2532.7 ± 0.8	141 ± 35		
34	1022.9 ± 0.4	4970 ± 1530	$2317 \rightarrow 1293$	с	90	2541.8 ± 1.1	77 ± 26		
35	1039.8 ± 0.4	347 ± 110	2600 - 1560	b	91	2562.4 ± 0.8	198 ± 46		
36	1110.1 ± 0.6	243 ± 90			92	2600.1 ± 1.3	74 ± 35	$2600 \rightarrow 0$	ъ
37	1122.2 ± 0.5	${\bf 154}\pm {\bf 61}$	$2682 \rightarrow 1560$	b	93	2605.2 ± 0.9	126 ± 49		
38	$\textbf{1130.6} \pm \textbf{0.5}$	492 ± 160	$2712 \rightarrow 1582$	с	94	2669.1 ± 0.9	366 ± 89		
39	1164.1 ± 0.5	505 ± 160	$2144 \rightarrow 980$	с	95	$\textbf{2677.0} \pm \textbf{1.1}$	116 ± 46		
40	$\textbf{1185.8} \pm \textbf{0.4}$	225 ± 76	$2166 \rightarrow 980$	с	96	$\textbf{2681.9} \pm \textbf{1.3}$	61 ± 36	$2682 \rightarrow 0$	b
41	1201.4 ± 0.4	1723 ± 530	2495 ightarrow 1293	с	97	$\textbf{2688.9} \pm \textbf{1.0}$	141 ± 47		
42	1214.1 ± 0.6	190 ± 87	$2508 \rightarrow 1293$	с	98	2702.8 ± 1.0	126 ± 48		
43	1261.7 ± 0.4		$^{12}C(n, \gamma)$		99	$\textbf{2734.7} \pm \textbf{0.8}$	185 ± 40		
44	$\textbf{1293.6} \pm \textbf{0.4}$	18719 ± 5850	$1293 \rightarrow 0$	с	100	2757.0 ± 0.8	$931\pm\!200$	$2757 \rightarrow 0$	b
45	$\textbf{1418.9} \pm \textbf{0.4}$	1525 ± 470	$2712 \rightarrow 1293$	с	101	$\textbf{2764.0} \pm \textbf{0.9}$	145 ± 40		
46	1467.3 ± 0.4	1717 ± 530	$2761 \rightarrow 1293$	с	102	2852.2 ± 0.8	253 ± 59		
47	1560.0 ± 0.4	1743 ± 530	$1560 \rightarrow 0$	с	103	2865.0 ± 0.8	183 ± 49		
48	$\textbf{1582.0}\pm\textbf{0.4}$	1428 ± 440	$1582 \rightarrow 0$	с	104	2899.9 ± 0.8	${\bf 165 \pm 38}$		
49	1677.3 ± 0.4	8031 ± 2460	$1678 \rightarrow 0$	с	105	2928.0 ± 1.0	185 ± 57		
50	1697.9 ± 0.4	2957 ± 900	$1698 \rightarrow 0$	с	106	2935.6 ± 0.9	292 ± 75		
51	1734.8 ± 0.6	224 ± 97			107	2950.5 ± 0.8	486 ± 110		
52	1737.9 ± 0.9	174 ± 83	97		108	2967.6 ± 2.1	73 ± 36		
53	1778.5 ± 0.8		4 Al (n, γ)		109	2981.3 ± 0.8	697 ± 160		
54	1849.0 ± 0.8	1307 ± 300	$3142 \rightarrow 1293$	с	110	3024.3 ± 1.0	140 ± 38		
55	1992.3 ± 0.9	354 ± 120			111	3041.5 ± 1.0	219 ± 58	$3042 \rightarrow 0$	b

TABLE II. Low-energy γ rays from the 40 K $(n, \gamma){}^{41}$ K reaction.

211

Line No.	γ-ray I energy (keV)	Partial cross section (mb)	Level assignment	Confidence	Line No.	γ-ray energy (keV)	Partial cross section (mb)	Level assignment	Confidence
112	3047.9±1.6	137 ± 65			120	3163.4 ± 0.8	203 ± 48		
113	3052.4 ± 1.8	153 ± 53			121	3179.9 ± 0.8	215 ± 49		
114	3067.0 ± 1.1	136 ± 41			122	3229.1 ± 0.9	181 ± 45		
115	3073.9 ± 0.8	373 ± 84			123	3244.1 ± 0.9	123 ± 30		
116	3089.6 ± 0.9	62 ± 19			124	3251.9 ± 0.9	174 ± 40		
117	3099.4 ± 0.8	147 ± 37			125	3259.6 ± 0.8	375 ± 82		
118	3145.9 ± 0.9	121 ± 31			126	3281.1 ± 1.1	58 ± 18	$3281 \rightarrow 0$	b
119	3152.6 ± 0.9	91 ± 24							

TABLE II (Continued)

^aSee discussion in Sec. IV B.

^bEnergetically possible.

^cDefinite - coincidence evidence.

prevent scattered neutrons from reaching the detectors. In the 180° geometry coincidences can result from the backscatter of a single γ ray from one detector into the other. Several such backscatter peaks appear in the coincidence data and have been appropriately identified.

A 1600×1600-channel two-parameter magnetic-

^dThis doublet is unresolved in the singles spectrum. Intensities are apportioned from the coincidence data. ^eProbable - not certain.

tape storage analysis system was used to record the coincidence spectra. The average true-tochance coincidence ratio was ≈ 11 . The coincidence studies required approximately three weeks, during which time electronic drifts were obviated by digital stabilization. In total, about 1.6×10^7 coincidence events were recorded. The primary mode



FIG. 1. High-energy portion of the γ -ray spectrum from the 40 K $(n, \gamma)^{41}$ K reaction, obtained with a Ge(Li) detector. Only double-escape peaks are present in this spectrum (Sec. II A) and the abscissa is the γ -ray energy to be associated with the double-escape peaks. The numbered peaks correspond to entries in Table I.



FIG. 2. Low-energy portion of the γ -ray spectrum from the 40 K $(n,\gamma){}^{41}$ K reaction, obtained with a Ge(Li) detector. The detector was operated inside a large anticoincidence NaI annulus (Sec. II A). The numbered peaks correspond to the γ rays listed in Table II.

of data processing was to scan the data tape to obtain the spectrum in coincidence with particular transitions.

III. EXPERIMENTAL RESULTS

Analysis of the ${}^{40}K(n, \gamma){}^{41}K \gamma$ -ray spectra yields the results summarized in Tables I and II. Excluded from each table are some γ rays which were observed but which have been identified as arising from contaminants. The major source of such contamination is the ${}^{39}K(n, \gamma){}^{40}K$ reaction. No γ rays were observed which could be attributed to either the ${}^{40}K(n, \rho_{\gamma}){}^{40}Ar$ or the ${}^{40}K(n, \alpha_{\gamma}){}^{37}C1$ reactions.

Figures 1 and 2 show portions of the 40 K capture γ -ray spectra. In these figures the lines are numbered to correspond to the tables, and the more intense peaks due to contaminants are identified.

The radiative capture cross section σ_c for ${}^{40}\text{K}$ can be determined from the relationship

$$\sigma_{c} = \frac{1}{B_{n}} \sum_{\gamma} E_{\gamma} \sigma_{\gamma} ,$$

where B_n is the neutron binding energy of ⁴¹K, σ_{γ} is the partial cross section of the γ ray with energy E_{γ} , and the sum is taken over all transitions. From this equation the cross section was calculated to be $\sigma_c = 30 \pm 8$ b, which is considerably below the value of 70 ± 20 b reported in the work of Hughes and Schwartz.¹⁴

The results of the low-low $\gamma - \gamma$ coincidence mea-



FIG. 3. 40 K($n, \gamma \gamma'$). Spectra of low-energy γ rays in coincidence with the 980.4- and 1201.4-keV transitions.

γ-ray energy (keV)	817	830	850	980	1022	1201	1293	1467	1560	1582	1677	1697	1849
(Kev)	011			000	1022	1201	1200	1401	1000	1002	1011		1040
246			0.11								0.18		
396					0.05		0.07						
445												0.36	
579				1.00									
584				0.39					1.00	0.44			
601				0.75									
613				0.28									
634		0.14									0.14		
655		0.08											
670							0.04						
733										0.17			
796												1.00	
817											0.89		
830											1.00		
850											1.00		
918					0.08		0.09						
947									0.10				
1012												0.32	
1022							1.00						
1130										1.00			
1164				0.32									
1185				0.21									
1201							0.27						
1214							0.10						
1293					1.00	1.00		1.00					1.00
1418							0.52						
1467							0.49						
1677	1.00	1.00	1.00										
1697													
1849							0.28						
1920							0.14						
1942							0.26						

TABLE III. Relative intensities of low-energy transitions from the reaction ${}^{40}\text{K}(n,\gamma){}^{41}\text{K}$ as observed in coincidence with other low-energy transitions. Intensities are normalized to unity for the strongest line in each coincidence spectrum. Blanks indicate that no coincidence was observed. Errors in the listed intensities vary from about $\pm 10\%$ for the more intense lines to about $\pm 30\%$ for the weaker lines.

surements for the 40 K $(n, \gamma)^{41}$ K reaction are presented in Table III, and some sample spectra are shown in Figs. 3 and 4.

IV. INTERPRETATION

A. General Considerations

A level scheme which summarizes the experimental results is shown in Fig. 5. The primary γ -ray transition energies together with the ⁴¹K-(p, p') data² were used to locate low-lying levels. The coincidence data were then used to define the positions of the low-energy transitions in the level scheme. Some transitions whose locations were not definitely established by the coincidence data were assigned on the basis of energy and intensity considerations. There remain a few low-energy transitions for which no unique assignment could be determined from the existing data. Presumably, most of these unassigned transitions involve states of high excitation energy.

A computer routine was used to search for alternate placements of the transitions among the known levels as well as to attempt to define new levels on the basis of energy loops involving the known transitions. Table II indicates the level of origin for each assigned transition and the degree of confidence ascribed to that assignment. These confidence specifications are based, in part, on the results of the computer analysis described above.

B. Level Energies

A weighted least-squares analysis was used to obtain the level energies shown in Fig. 5. In this analysis "best values" for the level energies were deduced from the energies of the known γ -ray transitions. In Table IV these level energies are listed and compared with level excitation energies derived from the ⁴¹K(p, p') data.²



FIG. 4. 40 K($n, \gamma \gamma'$). Spectra of low-energy γ rays in coincidence with the 1293.6- and 1677.3-keV transitions.

A value of $B_n = 10\,096.0 \pm 0.8$ keV was deduced for the neutron binding energy of ⁴¹K on the basis of the least-squares level-energy analysis. This value is slightly higher than the value of 10 090.5 ± 3.7 keV listed in current *Q*-value tables.^{15, 16}

Not shown in Fig. 5 are possible levels at 1516.8, 2304.5, and 3116.2 keV. Evidence for the existence of each of these levels consists of the observation of a low-intensity high-energy γ transition, which is assumed to directly populate the level. No transitions depopulating these levels were observed, which is perhaps not unexpected in view of the low intensity of the primary transitions.

On the basis of the coincidence studies two additional levels are suggested. In particular, a moderately intense transition with an energy of 1467.3 keV is seen in coincidence with only a single line, namely, the strong transition which depopulates the 1293.4-keV level. This result is most reasonably interpreted as evidence of a 1467.3-1293.4keV cascade which depopulates a previously unobserved level at 2760.7 keV. Similarly, a level at 2527.9 keV is suggested by the coincidence of the 850.4-keV transition with the previously assigned 1677.3-keV transition. This latter proposal is



FIG. 5. Level structure of 41 K. All energies are in keV. γ -ray intensities are proportional to the widths of the lines representing them. Flags on the left indicate direct population by primary transitions.

Level No.	Level energy from 40 K (n, γ) 41 K (keV)	Level energy from 41 K $(p,p'){}^{41}$ K a (keV)
1	980.4 ± 0.4	978 ± 6
2	1293.4 ± 0.4	1291 ± 6
3	1516.8 ± 0.6	•••
4	$\textbf{1559.9} \pm \textbf{0.4}$	1559 ± 6
5	$\textbf{1582.0} \pm \textbf{0.4}$	1580 ± 6
6	1677.5 ± 0.6	$\bf 1675 \pm 6$
7	1698.1 ± 0.7	1696 ± 6
8	2144.1 ± 0.5	2143 ± 6
9	2166.0 ± 0.9	2165 ± 6
10	2304.5 ± 1.1	• • •
11	2316.5 ± 0.7	2315 ± 6
12	2447.9 ± 0.7	2438 ± 6
13	2494.7 ± 0.5	2493 ± 6
14	2507.9 ± 0.5	$2507\pm\!6$
15	2527.9 ± 0.7	•••
16	2599.8 ± 0.7	2588 ± 6
17	2681.5 ± 1.5	2673 ± 6
18	2712.2 ± 0.9	2709 ± 6
19	2756.5 ± 0.8	2755 ± 6
20	2760.7 ± 0.7	• • •
21	3042.1 ± 0.8	3045 ± 6
22	3116.2 ± 0.7	• • •
23	3142.1 ± 0.5	3139 ± 6
24	$\textbf{3164.5} \pm \textbf{1.0}$	3173 ± 6
25	3213.4 ± 0.6	3212 ± 6
26	3235.6 ± 0.6	3230 ± 6
27	$\textbf{3281.1} \pm \textbf{1.1}$	3279 ± 6

TABLE IV. Comparison of the ⁴¹K level excitation energies deduced from the ⁴⁰K $(n, \gamma)^{41}$ K reaction and the ⁴¹K $(b, b')^{41}$ K reaction.

^aExcitation energies are from Kelley, Moore, and Enge (Ref. 2).

more tentative, since both the 850.4- and 1677.3keV transitions are seen in coincidence with an unassigned 246.8-keV γ ray.

In an earlier paper⁸ it was proposed that a highenergy (9390±60-keV) transition may populate directly a level at \approx 710 keV. In the present work no evidence was found for either a γ ray with E_{γ} \approx 9390 keV or a level at 710 keV.

C. Spin and Parity Assignments

Since ⁴⁰K has a ground-state spin and parity of 4⁻,¹⁷ the compound state formed through capture of a thermal neutron must have a spin and parity of $\frac{7}{2}$ or $\frac{9}{2}$. It is assumed that dipole transitions from the capturing state predominate in the high-energy capture spectrum, so that ⁴¹K levels with $I^{\pi} = (\frac{5}{2}, \frac{7}{2}, \frac{9}{2}, \frac{11}{2})^{\pm}$ should be populated strongly by direct transitions. Levels with spins outside this range can be excited, of course, by secondary γ -ray transitions.

Ground State

The ⁴¹K ground-state spin has been measured to be $\frac{3}{2}$ by means of molecular-beam techniques.¹⁸ ⁴¹K falls near the Schmidt limit for which I=j $= l - \frac{1}{2}$, implying l = 2 and hence positive parity. As would be expected, no transition was observed to proceed directly from the capture state to the $\frac{3}{2}^+$ ground state in the ⁴⁰K(n, γ)⁴¹K reaction.

980.4-keV Level

The assignment of $I^{\pi} = \frac{1}{2}^{+}$ for the 980.4-keV level is discussed by Sharp *et al.*⁷ and is supported by the inelastic neutron scattering study of Nichols and McEllistrem,⁵ and the ⁴²Ca(*d*, ³He)⁴¹K study of Yntema.⁴ The present work also supports this assignment, since no direct transition to this level from the capture state is observed.

1293.4-keV Level

The isomeric level at 1293.4 keV has been assigned^{19,20} $I^{\pi} = \frac{7}{2}^{-}$ on the basis of the multipolarity (M2) of the transition to the ground state. This multipolarity was deduced from a half-life measurement of $\approx 6.7 \times 10^{-9}$ sec for the 1293.4-keV level. The inelastic neutron scattering study⁵ and the ⁴²Ca(d, ³He) study⁴ support this assignment. This level is the lowest-lying level found to be populated directly in the ⁴⁰K(n, γ)⁴¹K reaction. The direct (n, γ) population is consistent with the $\frac{7}{2}^{-}$ assignment.

1559.9-keV Level

The level at 1559.9 keV is not observed to be populated directly in the 40 K $(n, \gamma)^{41}$ K reaction, so it probably has a spin outside the range $\frac{5}{2} \le I \le \frac{11}{2}$. Inelastic neutron scattering studies⁵ are in agreement with this limitation and suggest a spin range of $I \le \frac{5}{2}$ for this level. Since the 1559.5-keV level decays to the $\frac{3}{2}$ ⁺ ground state and to the $\frac{1}{2}$ ⁺ level at 980.4 keV, but not to the $\frac{7}{2}$ ⁻ level at 1293.4 keV, the most probable spin assignment for this level is $I = \frac{1}{2}$ or $\frac{3}{2}$. The 1559.9-keV level may be identical with one excited at 1590 ± 40 keV in the 42 Ca- $(d, {}^{3}$ He) 41 K reaction. On the basis of the 42 Ca- $(d, {}^{3}$ He) 41 K study, Yntema²¹ has suggested $I^{\pi} = \frac{1}{2}^{+}$ for the \approx 1590-keV level.

1582.0-keV Level

The 1582.0-keV level is populated directly from the capture state and therefore presumably has $\frac{5}{2} \le I \le \frac{11}{2}$. The 1582.0-keV level decays to the $\frac{3}{2}^+$ ground state by a 1582.0-keV transition and to the $\frac{1}{2}^+$ level at 980.4 keV by a 601.2-keV transition, as listed in Table II. Thus, the most probable

spin assignment for this level is $\frac{5}{2}$. If one assumes $I=\frac{5}{2}$, a negative-parity assignment for the 1582.0-keV level would require that the 1582.0keV ground-state transition have E1 character and that the 601.2-keV transition have M2 character. If the parity is assumed to be positive, however, the 1582.0-keV transition would be M1 and the 601.2-keV transition would be E2. The relative intensities of the two transitions involved favors the latter choice. It should be noted that the $\frac{5}{2}$ + assignment suggested in this paper is outside the range $I^{\pi} = (\frac{9}{2}, \frac{11}{2})^{\pm}$ which was previously suggested for this level on the basis of $(n, n'\gamma)$ angular-distribution studies.⁵ However, the angular-distribution work employed a NaI(T1) detector, and the spectrum was not well resolved in the region including this level.

1677.5-keV Level

Direct population of the 1677.5-keV level from the capture state implies $\frac{5}{2} \le I \le \frac{11}{2}$. Since the strongest decay transition proceeds to the ground state, it is probable that $I^{\pi} = (\frac{5}{2}, \frac{7}{2})^{\pm}$. The decay mode of this level yields no further restrictions on the assignment. However, studies of the β decay of ⁴¹Ar suggest positive parity.⁶ The $(n, n'\gamma)$ angular distribution studies⁵ suggest $I \le \frac{5}{2}$, but, as mentioned previously, this region of the spectrum was not well resolved in that work.

1698.1-keV Level

The 1698.1-keV level is populated directly from the capture state, implying $\frac{5}{2} \leq I \leq \frac{11}{2}$. Since no level other than the ground state is observably populated by the decay of the 1698.1-keV level, spin and parity values of $\frac{5}{2}^{\pm}$ or $\frac{7}{2}^{+}$ are suggested.

2144.1-keV Level

Direct population of the 2144.1-keV level from the capture state implies $\frac{5}{2} \le I \le \frac{11}{2}$. This level decays to the $\frac{3}{2}$ ⁺ ground state, the $\frac{1}{2}$ ⁺ level at 980.4 keV, the $\frac{3}{2}$ ⁺ level at 1559.9 keV, and the $\frac{5}{2}$ [±] level at 1698.1 keV. Decay to the low-spin levels eliminates spin values of $I \ge \frac{7}{2}$, leaving $I = \frac{5}{2}$ as the preferred assignment. A negative-parity assignment would require that the 1164.1-keV transition to the 980.4-keV level have M2 character and that the ground-state transition have E1 character. A positive-parity assignment would require the 1164.1-keV transition to be E2 and the groundstate transition to be M1. The relative transition intensities favor the latter case.

2166.0-keV Level

Since no transition has been observed that directly connects the capture state with the 2166.0-keV level, and since this level decays to levels with spin values in the range $\frac{1}{2} \leq I \leq \frac{5}{2}$, the 2166.0-keV state presumably has $I^{\pi} = \frac{1}{2}^{\pm}$ or $I^{\pi} = \frac{3}{2}^{\pm}$.

2316.5-keV Level

The 2316.5-keV level is populated directly from the capture state by the 7779.1-keV transition, which is assumed to have *E*1 character, since it is the most intense transition in the high-energy (n, γ) spectrum. Direct population by an *E*1 transition implies a spin range of $\frac{5}{2} \le I \le \frac{11}{2}$ and positive parity for this level. The 2316.5-keV level deexcites to levels with spin and parity assignments of $\frac{3}{2}^+$, $\frac{5}{2}^+$, and $\frac{7}{2}^-$, which suggests a probable assignment of $I^{\pi} = \frac{5}{2}^+$ or $\frac{7}{2}^+$.

2447.9-keV Level

A level at 2447.9 keV is proposed on the basis of three otherwise unassigned transitions which can connect a state at this energy with other low-lying states. Since no direct population of this level from the capture state was detected and since the proposed level is observed to decay only to the ground state, the spin is assumed to be $I=\frac{1}{2}$ or $\frac{3}{2}$. The 2447.9-keV level may be identical to a level reported at 2438 ± 6 keV in a ${}^{41}\text{K}(p,p')$ study.²

Higher Energy Levels

Many levels have been identified at excitation energies \geq 2400 keV. In general, there is insufficient experimental information available to define the spin of these levels beyond the usual restrictions implied by direct population from the capture state.

D. Theoretical Interpretation

Since ⁴¹K has two neutrons in excess of the 20neutron closed shell and one proton missing from the 20-proton closed shell, it is expected that the ⁴¹K level structure should include many positiveparity two-particle, one-hole (2p-1h) states arising from various couplings of the $p(d_{3/2})^{-1}n(f_{7/2})^2$ configuration. A calculation of the low-lying ⁴¹K 2p-1h states has been published by Pellegrini.²² In his calculation, it is assumed that these states arise from a pure $p(d_{3/2})^{-1}n(f_{7/2})^2$ configuration, so that the interaction matrix elements are given by

$$\langle p(d_{3/2})^{-1} n(f_{7/2})^{2}{}_{I'} | V_{nn} + \sum_{\text{pairs}} V_{pn} | p(d_{3/2})^{-1} n(f_{7/2})^{2}{}_{I} \rangle_{J}$$

$$= \langle n(f_{7/2})^{2} | V_{nn} | n(f_{7/2})^{2} \rangle_{I} , \delta_{II} ,$$

$$+ 2 \sum_{J'} U(\frac{7}{2} \frac{7}{2} J \frac{3}{2} | I' J') U(\frac{7}{2} \frac{7}{2} J \frac{3}{2} | IJ')$$

$$\times \langle p(d_{3/2})^{-1} n(f_{7/2})^{1} | V_{nn} | p(d_{2/2})^{-1} n(f_{7/2})^{1} \rangle_{J'} ,$$

where V_{nn} is the neutron-neutron interaction and V_{pn} is the proton-neutron interaction. In the present paper we have repeated the calculation of Pellegrini using the most recent experimental information to define the nucleon-nucleon interactions.

If the low-lying levels of ⁴²Ca result from pure $n(f_{7/2})^2$ configuration, these level energies then give the interaction energies between two neutrons in the $f_{7/2}$ shell. These energies are $E(0^+)=0.0$ MeV, $E(2^+)=1.524$ MeV, $E(4^+)=2.751$ MeV, and $E(6^+)=3.190$ MeV.¹

The assumption was made by Pellegrini that ⁴¹K 2p-1h states arise from a pure $p(d_{3/2})^{-1}n(f_{7/2})^2$ configuration. It is probable that the low-lying states of ⁴¹K also include some admixture of other shell-model configurations. In particular the ground state of ⁴¹K is known^{23, 24} to contain a significant $p(s_{1/2})^{-1}n(f_{7/2})^2$ component. The effect of such mixing should be included. Presumably, the interaction between an $f_{7/2}$ neutron and an $s_{1/2}$ proton hole would result in a multiplet of high-energy states in the level structure of certain nuclei, such as ³²P, but the present experimental data are insufficient to locate such a multiplet. The low-lying 1p-1h states of ⁴⁰K presumably arise primarily



FIG. 6. (a) Experimental levels of 41 K with the known negative-parity states omitted. (b) Calculated eigenvalues of the $p(d_{3/2})^{-1}n(f_{7/2})^2$ configuration in 41 K.

Energy (MeV)	Ι	$(d_{3/2})^{-1}(f_{7/2})^2_0$	$(d_{3/2})^{-1}(f_{7/2})^2_2$	$(d_{3/2})^{-1}(f_{7/2})^2_4$	$(d_{3/2})^{-1}(f_{7/2})^{2}_{6}$
0	$\frac{3^{+}}{2}$	0.9184	-0.3957		
1.018	$\frac{1}{2}^{+}$		1.0000		
1.570	$\frac{7}{2}$ +		0.9297	-0.3683	
1.890	$\frac{5}{2}^{+}$		0.8362	-0.5484	
2.140	$\frac{3}{2}^{+}$	0.3957	0.9184		
2.816	$\frac{11}{2}^+$			-0.5713	0.8207
2.885	$\frac{9+}{2}$			0.8759	-0.4825
3.065	$\frac{5}{2}^{+}$		0.5484	0.8362	
3.137	$\frac{13}{2}^+$				1.000
3.254	$\frac{7}{2}^{+}$		0.3683	0.9297	
3.523	$\frac{11}{2}^+$			0.8207	0.5713
3.845	$\frac{9}{2}^{+}$			0.4825	0.8759
4.163	<u>15</u> + 2				1.000

TABLE V. Calculated eigenvalues and eigenvectors of the $p(d_{3/2})^{-1}n(f_{1/2})^2$ configuration in ⁴¹K.

from the $p(d_{3/2})^{-1}n(f_{7/2})^1$ configuration, with some admixture of the $p(s_{1/2})^{-1}n(f_{7/2})^1$ configuration. If it is assumed that the proton configuration of $^{\rm 40}{\rm K}$ is not significantly altered by the addition of a neutron, then the ⁴¹K and ⁴⁰K proton configurations should be similar. Therefore, it has been assumed that configuration mixing in ⁴¹K can be implicitly included by using the experimentally derived interaction energies obtained from the level structure of ⁴⁰K. These proton-neutron interaction energies are $E(4^{-}) = 0.0 \text{ MeV}, E(3^{-}) = 0.030$ MeV, $E(2^{-}) = 0.800$ MeV, and $E(5^{-}) = 0.890$ MeV.¹

Calculation of the appropriate matrix elements and diagonalization of the resulting matrices were performed using the interaction energies listed above. The results of this calculation are sum-

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marized in Table V. In Fig. 6 the calculated eigenvalues are compared with the experimental ⁴¹K levels (the known negative-parity levels have been deleted for clarity). For the lowest few states there is seen to be a satisfactory correspondence between the calculated and observed energies. It is not surprising that at higher energies many more levels exist than can be accounted for on the basis of a simple 2p-1h description.

In addition to the 2p-1h states, levels should be observed which result from excitation of the unpaired proton into the $f_{7/2}$ shell, giving a proton configuration of $(d_{3/2})^{-2} (f_{7/2})^1$ with perhaps some $(s_{1/2})^{-2}(f_{7/2})^1$ mixing. Such a proton excitation is assumed to be the origin of the negative-parity level at 1293.4 keV.

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