# Beta-decay energies and masses of  $103 - 105$ In

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Decay energies of  $103-105$ In have been determined by  $\beta-\gamma$  coincidence spectroscopy on sources obtained from an on-line mass separator. Comparisons of the measured decay energies and deduced masses are made with the predictions of several different theoretical models. The <sup>103</sup>In mass is found to be more bound by 1 MeV than predicted by mos models, which reproduce adequately the masses of the heavier indium isotopes. Systematic trends of the masses and neutron separation energies of the indium isotopes between the closed  $N=50$  and 82 shells are presented.

RADIOACTIVITY  $^{103-105}$ In [from Mo( $^{14}$ N,xn), Mo( $^{16}$ O,pxn)]; measured  $E_{\beta+}$ ,  $\beta\gamma$  coin; deduced  $Q_{\text{EC}}$ , mass excesses. On-line mass separation; enriched and natural targets; Ge(Li), scintillator telescope detectors; response function correction  $E$  scintillator.

#### I. INTRODUCTION

An extension of the experimentally known nuclidic mass surface to nuclei far from the region of  $\beta$ stability is of fundamental interest in providing a better determination of the input parameters for the various nuclear mass formulae, allowing a more accurate prediction of the limits of nuclear stability. In addition, a study of the shape of the mass surface in the vicinity of the doubly-closed nuclide  $100$ Sn provides information on the strength of the shell closure to be expected when  $Z = N = 50$ . Recently, masses of highly neutron-deficient nuclei in this region, especially Sn and Te isotopes such as <sup>105</sup>Sn and Te, were deduced by Plochocki et al.<sup>1</sup> from measurements of  $\beta^+$ /(EC+ $\beta^+$ ) decay probability ratios and mass difference data from particle spectroscopy studies.

As a further step in the extension of the mass surface we have determined the decay energies for  $103 - 105$  In by  $\beta$ -end-point measurements with mass separated samples from the mass separator  $RAMA<sub>1</sub><sup>2-4</sup> located on-line at the Lawrence Berkeley.$ ley Laboratory 88-Inch Cyclotron. The experimentally determined decay energies and derived masses for  $103 - 105$  In are compared with the predictions of different mass models to identify which models are more successful in this region. Further, the inclusion of the available data on the neutron-rich indium nuclei in these comparisons permits a systematic study of the ground state mass behavior of these isotopes as a function of the neutron number between the shell closures at  $N = 50$  and 82. An examination of single- and two-neutron separation energies in the vicinity of  $103 - 105$  In is also performed to investigate possible systematic variations in the mass surface in a model-independent way.

#### II. EXPERIMENT

Heavy-ion beams of <sup>12</sup>C, <sup>14</sup>N, and <sup>16</sup>O were direct ed onto various targets to produce the isotopes of interest via  $(HI, xn)$  and  $(HI, pxn)$  reactions. More specifically,  $^{103}$ In was produced via the  $\text{Mo}(^{14}\text{N}, 3n)$  and  $^{92}\text{Mo}(^{16}\text{O}, p 4n)$  reactions with beam energies of 80 and 115 MeV, respectively; <sup>104</sup>In was produced via the  $^{92}$ Mo( $^{16}$ O,p3n) reaction at 95 MeV; and  $^{105}$ In was produced via the  $^{nat}$ Mo( $^{14}$ N, xn) and  $^{92}$ Mo( $^{16}$ O,p2n) reactions with beam energies of 100 and 75 MeV, respectively. All targets were  $\sim$  2  $mg/cm<sup>2</sup>$  thick; the average beam intensity varied between 2 and 4  $e\mu$ A. To improve the yield at a given beam energy, two identical targets were used simultaneously in conjunction with a multiple capillary system. The nuclear reaction recoils were thermalized behind each target in 1.5 atm of helium, collected by the multiple capillary system, and transported via a helium jet to the hollow-cathode ion source of the mass separator  $RAMA.<sup>2-4</sup>$  The mass-analyze 18 keV ion beam was implanted onto Mylar tape

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FIG. 1. Schematic view of the  $\beta$ - $\gamma$  detector station.

during a suitable collection interval, and rapidly transported  $\left( < 250 \right)$  msec) to a detector station configured for  $\beta$  singles and  $\beta$ - $\gamma$  coincidence spectroscopy. (See Fig. 1.)

The detector station consisted of a scintillator telescope, positioned facing the source side of the tape, for  $\beta$  counting and a 15% Ge(Li) detector, located on the opposite side of the tape, for  $\gamma$  counting. The  $\beta$  telescope comprised a 10 mm diam and 1 mm thick NE102 plastic scintillator as a  $\Delta E$ counter (for  $\gamma$ -ray rejection) and a large cylindrical NE102 plastic scintillator, 11.4 cm in both diam and length, as an E detector. Standard fast-slow coincidence networks were appropriately set up using the three detectors so that both  $\beta$ -singles spectra as well as  $\beta-\gamma$  coincidence spectra could be obtained. The final coincidence timing of 5 nsec (FWHM) between the two scintillators and 20 nsec (FWHM) between the  $\beta$ -E scintillator and the Ge(Li) counter greatly reduced chance coincidences between detectors at the modest maximum singles counting rate  $\zeta$  < 2000 counts/sec) in each detector. Multiparameter events were stored sequentially on magnetic tape using the cHAOS (Ref. 5) (now called MNUs3) acquisition and analysis FORTRAN code running on a ModComp IV computer.

Positron spectra, coincident with known transitions in the daughter nuclei, were subsequently obtained by software gating the coincidence event data with the appropriate  $\gamma$  rays and subtracting background  $\beta$  spectra obtained from "off peak"  $\gamma$ -ray gates. Energy end-point determinations were then calculated from appropriately weighted linear leastsquares fits to Fermi-Kurie plots of the data after correcting for the finite energy resolution of the  $E$  scintillator. This correction is calculated by assuming a theoretical shape,  $T(E)$ , for the  $\beta$  spectrum with end-point energy  $E_0$  and distorting it using a semiempirically derived response function,  $R(E, E'),$ for the  $E$  detector. This procedure, initially suggested by Rogers and Gordon, $<sup>6</sup>$  yields an energy-</sup> dependent correction factor,  $K(E)$ , by which the measured  $\beta$  spectrum is multiplied. Following Beck<sup>7</sup> and Otto et al.,  $8$  a Gaussian response function was employed with a  $\sqrt{E}$  dependence for the FWHM. This FWHM was determined to be 200 keV at 976 keV by using the conversion electrons from <sup>207</sup>Bi. The overall correction factor,  $K(E)$ , can thus be written as

$$
K(E) = T(E) / \left[ \int^{E_0} T(E') R(E, E') dE' \right]
$$
 (1)

with the response function given by

$$
R(E, E') = \frac{1}{\sigma_1 \sqrt{2\pi E'}} e^{-(E - E')^2 / 2\sigma_1^2 E'},
$$
 (2)

where  $\sigma_1$  is a proportionality constant. For decays proceeding via several major branches, appropriate single branch, theoretical beta spectra  $T(E)$ ; were summed together using the branching ratios derived from the literature.

A two-step procedure was used for calculating the error in the individual end points. A statistical error was determined using the formalism of Rehfield<sup>9</sup> which weights the Fermi-Kurie plot by the factor

$$
\omega_i \equiv 1/\sigma_i^2 = 4p_i F_i E_i \tag{3}
$$

and determines the error in the end point to be

$$
\sigma_{E_0}^2 = \frac{1}{A^2 \Delta} \sum (E_0 - E_i)^2 / \sigma_1^2 , \qquad (4)
$$

with

$$
\Delta = \sum \frac{1}{\sigma_i^2} \sum \frac{E_i^2}{\sigma_i^2} - \left[ \sum \frac{E_i}{\sigma_i^2} \right]^2.
$$
 (5)

In these expressions  $F_i$  is the Fermi function,  $p_i$  the momentum, and  $E_i$  the energy corresponding to channel  $i$ . The slope and end point of the Fermi-Kurie plot are indicated by  $A$  and  $E_0$ , respectively. The range of the summations is determined by the limits of the least-squares fit. This statistical error was adjusted by accounting for the variation in the end point with shifts in the energy limits over which the least-squares fit was performed. The statistical error was then added quadratically to the error due to the energy calibration of the  $\beta$  telescope to obtain the final error in the end point:

$$
\sigma_{E_{\text{calib.}}}^2 = \sum_i^N \left\{ \sigma_{\text{lit}_i}^2 \left[ \chi_0 \frac{\partial f_A}{\partial E_i} + \frac{\partial f_B}{\partial E_i} \right]^2 + \sigma_{\text{FK}_i}^2 \left[ \chi_0 \frac{\partial f_A}{\partial \chi_i} + \frac{\partial f_B}{\partial \chi_i} \right]^2 \right\}, \quad f_A = f_A(E_i, \chi_i), \quad f_B = f_B(E_i, \chi_i) \tag{6}
$$



FIG. 2. (a) Fermi-Kurie plot of the  $38$ K positron spectrum in coincidence with the 2168 keV  $\gamma$  transition in the daughter. (b) The energy calibration from the beta telescope using the calibration activities listed in Table II.

In Eq. (6) the slope  $f_A$  and the intercept  $f_B$  of the calibration function depend on the literature values for the end points of the calibration nuclei  $E_i$  with uncertainties  $\sigma_{\text{lit}_i}$  and the corresponding measure channel numbers  $\chi_i$  with errors  $\sigma_{FK_i}$ . The channel number corresponding to the calculated end-point

energy  $E_0$  is indicated by  $\chi_0$ , and N is the number of calibration nuclei.

Figure 2(a) presents the Fermi-Kurie plot from the decay of  $38K$ , one of the calibration nuclei, with the appropriate error bars as an example of the weighted linear least-squares fits obtained. The slight high energy tailing observed in this spectrum is the result of positron annihilation radiation pileup which necessitated that the least squares analysis be limited to an energy range ending  $\sim$  200 keV below the highest energy events observed in each spectrum. The energy calibration as determined using the calibration activities $^{10,11}$  listed in Table I was found to give a good linear fit [see Fig. 2(b)]. Table I also presents for each calibration activity the  $\gamma$ -gate employed to obtain the  $\beta$  spectrum and the reaction used for the production of the activity.

### III. RESULTS

The final results of our experiments are presented in Table II, which lists the  $\gamma$  rays and their relative intensities as observed following the  $\beta$  decay of In, and in Table III, which lists the calculate  $Q_{\text{EC}}$  values of  $^{103-105}$  In. Close examination of the  $\gamma$ spectrum of  $^{103}$ In in coincidence with  $\beta$ 's revealed two  $\gamma$  rays at 720 and 740 keV, decaying with the proper half-life of 60.5 sec, in addition to the 188 and 202 keV  $\gamma$  rays observed previously by Lhersonneau et al.<sup>12</sup> The observation of these  $\gamma$  rays is in agreement with the recent results of Béraud et al.,<sup>1</sup> although the relative intensities of  $32\%$  and  $19\%$ which are quoted for the 720 and 740 keV  $\gamma$  rays, respectively, are slightly higher than our results indicate. Based on the reaction work of Meye et al.,<sup>14</sup> the 720 keV  $\gamma$  ray corresponds to the first member of a decoupled band based on the 188.1 keV<br> $\frac{7}{2}$  state.

The Fermi-Kurie analysis of the positron spectrum from  $^{103}$ In in coincidence with the 188 keV  $\gamma$ transition in the  $103$ Cd daughter is shown in Fig.  $3(a)$ . A partial decay scheme for  $103$ In is also given in this figure with the beta branching ratios determined from the measured relative  $\gamma$  intensities. Figure 3(a) shows that the linearity of the Fermi-Kurie





TABLE II. Relative intensities of the  $\gamma$  rays in the decay of  $^{103}$ In.



plot is not affected seriously by the small  $\beta$  feeding of the  $\frac{11}{2}^+$  level.

The decay scheme of  $104$ In has been studied inten sively by Huang et  $al$ <sup>15</sup> According to these authors about 22% of the beta decay feeds the second excited state  $(4^+)$  at 1492 keV, while the first excited state  $(2^+)$  at 658 keV is not fed directly. All the higher-lying levels deexcite via the  $4^+$  level by  $\gamma$ -ray emission. Since approximately 50% of the  $\beta$ -decay strength feeds three close-lying states at 2370.2, 2435.4, and 2492.3 keV, the energy range for the least-squares fit in the Fermi-Kurie plot is restricted to the highest <sup>1</sup> MeV of the data. Figure 3(b) presents the Fermi-Kurie analysis for the  $^{104}$ In positron singles spectrum together with a partial decay scheme for  $104$ In. Positron spectra in coincidence with the 658 and 834 keV  $\gamma$  rays yield, within errors, the same  $\beta$  end-point energy, but have lower statistics.

According to Wischnewski et al.,<sup>16</sup> about 27% of the  $\beta$  decay of <sup>105</sup>In feeds the first excited level at 131 keV in  $^{105}$ Cd, while the next strongly fed levels, decaying to the 131 keV state, lie at 770 and 799 keV with  $\beta$  branches of 8% and 9%, respectively. The resulting partial decay scheme and Fermi-Kurie analysis of the positron spectrum in coincidence with the 131 keV  $\gamma$  ray are shown in Fig. 3(c).

The results of the Fermi-Kurie analysis for In are summarized in Table III. The measured  $\beta$  end-point energies,  $E_{\text{max}}$ , along with the  $\gamma$ rays used for gating and the deduced  $Q_{EC}$  values, are given. In addition, the decay energies previously reported in the literature are included in the table for comparison. The decay energies obtained for  $103 - 104$  In agree well with the literature values; for <sup>103</sup>In the uncertainty in the  $Q_{\text{EC}}$  value is substantially reduced. A  $Q_{\text{EC}}$  value for <sup>105</sup>In was not previous ly available.

#### IV. DISCUSSION

The decay energy measurements for  $103-105$ In, reported in this work, can be analyzed in different ways to investigate the mass surface in this region of nuclei. A comparison of the measured decay energies with the predictions of the currently available mass theories can evaluate the reliability of these models in predicting the curvature of the mass surface. Conversion of the  $Q_{\text{EC}}$  values to mass excesses using the known masses of the cadmium isotopes also provides a direct comparison of the absolute mass excesses with the model mass predictions. Direct model-independent information on variations in the mass surface for these indium isotopes can be obtained from an examination of the neutron binding energy systematics in the vicinity of the measured nuclei.

The differences between the measured decay energies and the predictions derived from selected mass models for the neutron-deficient indium isotopes are depicted graphically in Fig. 4. To observe more easily the systematic trends, this comparison is exeasily the systematic trends, this comparison is ex-<br>tended to  $^{110}$ In. (The decay energies for  $^{106-110}$ In are adopted from Wapstra and Bos.)<sup>17</sup> Each arrow in the figure is labeled by a number corresponding to the prediction of a given model. In addition to the different mass formulae presented in Ref. 18, the droplet calculations of Möller and  $Nix^{19}$  are also included.

Figure 4 shows that the results of the shell model calculations of Liran-Zeldes<sup>18d</sup> and the mass formulae, based on the Garvey-Kelson type of relationship, of Jänecke,<sup>18e</sup> Comay-Kelson,<sup>18f</sup> and Jänecke Eynon, <sup>18g</sup> reproduce very well the measured decay energies for  $^{105-110}$ In. In this region the droplet model predictions of Myers, <sup>18a</sup> Groote *et al.*, <sup>18b</sup> Seeger and Howard, <sup>18c</sup> and Möller and Nix<sup>19</sup> are systematically too poorly bound. Beginning with <sup>104</sup>In and continuing to  $^{103}$ In, both types of mass theorie exhibit a sudden downward shift of <sup>1</sup> MeV so that

TABLE III. Summary of the  $Q_{FC}$  determinations.

	---							
Nuclide	Gate(s) (keV)		$Q_{\text{EC}}$ (MeV)					
		$E_{\rm max}$ (MeV)	This work	Literature				
$^{103}$ In	188	$4.17+0.20$	$5.38 \pm 0.20$	$5.8 \pm 0.5$ (Ref. 12)				
$^{104}$ In	658,834 no gate	$4.75 + 0.25$	$7.26 \pm 0.25$	$7.1 \pm 0.2$ (Ref. 15)				
$^{105}$ In	131	$3.99 \pm 0.20$	$5.14 \pm 0.20$					

 $(a)$ 

25

 $20$ 

 $15$ 

 $\overline{10}$ 

5

 $\circ$ 

 $20$ 

 $(b)$ 

 $\overline{c}$ 

 $9/2$ <sup>\*</sup>

 $103<sub>1n</sub>$ 

 $~100$ 

3

 $5^*$  $\overline{104}_{In}$   $\beta$ ; EC

90۶

188

2492 135  $370$ 

 $\overline{\circ}$  $103<sub>Cd</sub>$ 





FIG. 3. The Fermi-Kurie plots and partial decay schemes for (a)  $^{103}$ In, (b)  $^{104}$ In, and (c)  $^{105}$ In.



FIG. 4. Comparison of the experimental  $Q_{EC}$  values with the predictions of several model mass formulae for  $103 - 110$ In. See the text for details.

the Liran-Zeldes and Garvey-Kelson type of relationship now predict a  $Q_{EC}$  which is 1 MeV too large, while those of the droplet model are at this point more accurate.

The mass excesses of  $103 - 105$  In, deduced from the measured  $Q_{EC}$  values using the accurately known<br>cadmium masses,<sup>1,15,20</sup> are listed in Table IV. A direct comparison of the experimental masses with the different model mass predictions is also included in the table. From Table IV it is apparent that none of these mass formulae adequately predict the experimentally-observed mass behavior for  $^{103-105}$ In. Mass theories which reproduce the experimental mass of <sup>105</sup>In (i.e., Groote et al., Liran-Zeldes, Comay-Kelson, and Jänecke-Eynon) place the <sup>103</sup>In mass 1 MeV less bound than is experimentally observed.

Given the sudden deviation in the  $^{103}$ In experimental mass compared to these predictions, and given its proximity to the double shell closure at 100Sn, a comparison of the systematics of the ground

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Nuclide	Mass excess				$M_{\rm exp}-M_{\rm calc}$ (MeV)				
	(MeV)	а				e			
$^{103}$ In	$-75.24 + 0.20$	0.67	$-1.02$	0.76	$-0.73$	$-1.20$	$-0.81$	$-0.81$	$-1.13$
$104$ In	$-76.46 + 0.25$	0.85	$-0.65$	1.14	$-0.26$	$-0.73$	0.03	$-0.22$	$-0.34$
$^{105}$ In	$-79.20 + 0.20$	1.23	$-0.08$	1.90	0.46	0.26	0.57	0.38	0.26

TABLE IV. Summary of experimental mass excesses and comparison with different model mass predictions.

 $Mvers$  (Ref. 18a).

 $b$ Groote et al. (Ref. 18b).

'Seeger-Howard (Ref. 18c).

<sup>d</sup>Möller-Nix (Ref. 19).

state mass behavior for the very neutron-rich indium isotopes near the shell closure at  $N=82$  is of related interest. Aleklett et  $al.^{21}$  have studied the masses of  $120 - 129$  In. For the mass excess of the closed neutron shell nucleus  $^{131}$ In, a value of  $-68.55\pm0.24$  MeV can be calculated from the recently reported decay energies of  $^{131}$ In (Ref. 22) and  $^{131}$ Sn (Ref. 23) and the measured mass of  $^{131}Sb$  (Ref. 24). (The masse of the indium isotopes not explicitly mentioned here were adopted from Ref. 17.)

In Fig. 5 the experimental indium masses for isotopes between the shell closures at  $N=50$  and 82 are compared to the predictions of selected, representative mass theories. The lower part of this figure compares shell and independent particle mass formulae; the upper part compares different liquid drop model predictions. The central part of the mass data between  $N=57$  and 76 is reproduced by the shell model of Liran-Zeldes<sup>18d</sup> and the mass formulae based on the Garvey-Kelson relations<sup>18e-g</sup>; the root-mean-square (rms) deviation of theory from experiment in this region is less than 200 keV for each of these mass models. Approaching the closed  $N = 82$  shell, the different mass predictions diverge slowly. The model of Comay-Kelson<sup>18f</sup> exhibits the best predictive qualities taking into account all of the indium data; the rms deviation from all the measured masses is only 240 keV. For the models of Liran-Zeldes,  $^{18d}$  Jänecke,  $^{18e}$  and Jänecke-Eynon,<sup>1</sup> the corresponding values are 320, 320, and 630 keV, respectively.

From Fig. 5 it is also clear that the different droplet models considered in this work do not predict the masses of the indium isotopes in the region near  $\beta$ stability with the same accuracy as the Liran-Zeldes mass formula and the models based on the Garvey-Kelson type of mass relations. One should remember, however, that the number of input parameters used for the droplet models is far fewer than for the other mass formulae. Near the  $N = 50$ and 82 closed shells the differences between the experimental and calculated mass values for the droplet and Garvey-Kelson type of mass formulae are of

<sup>e</sup>Liran-Zeldes (Ref. 18d). fJänecke (Ref. 18e).

<sup>g</sup>Comay-Kelson (Ref. 18f).

<sup>h</sup>Jänecke-Eynon (Ref. 18g).

the same order. Among the droplet models, the best fit to the experimental data over the known mass range is obtained with the model of Möller and Nix; the rms deviation is 630 keV. In the case of the mass formulae of Myers, Groote et al., and Seeger and Howard this deviation is 1060, 820, and 780 keV, respectively. Finally, the differences between the experimental masses and the various droplet model predictions also show the sharp, systematic drop at mass 103.

As already mentioned, an examination of singleand two-nucleon separation energies can highlight systematic variations of the mass surface in a model-independent way. Figure 6(a) shows the behavior of the single-neutron separation energy,  $S_n$ , as a function of the neutron number for the indium isotopes. In addition to the normal odd-even oscillations, the  $S_n$  plot exhibits an irregular drop for  $N = 55$  and 56. Both  $S_n$  values are about 0.5 MeV lower than those estimated from the systematics of



FIG. 5. Comparison of the experimental masses of all the known indium isotopes with the predictions of several representative model mass formulae.



FIG. 6. (a) Plot of single-neutron separation energies versus neutron number. Upper line is for even  $N$  isotopes while lower is for odd N ones. Dashed lines are  $S_n$  values expected from Wapstra and Bos (Ref. 17) systematics. (b) Plot of experimental and droplet model predicted  $\Delta_n$ values versus neutron number.

Wapstra and Bos,<sup>17</sup> which are indicated in the figure by dashed lines. Since the mass of <sup>105</sup>In is in agreement with the estimate of Wapstra and Bos, the observed deviations reflect the fact that the masses of  $^{104}$ In and  $^{103}$ In are, respectively, 0.5 and 1.0 MeV lower than expected from systematics. From Fig.  $6(a)$  it is apparent that a similar effect is not present for the neutron-rich indium isotopes near the closed  $N = 82$  shell.

Since the neutron pairing energy is closely related to a quantity  $\Delta_n$ , which can be derived from single neutron separation energies using the relationship<sup>22</sup>

$$
\Delta_n = \frac{(-1)^N}{4} [2S_n(N,Z) - S_n(N-1,Z)] ,
$$

a comparison of the experimental behavior of  $\Delta_n$ with the values of the different liquid drop models is informative. The variation of  $\Delta_n$  for the measured indium isotopes is presented in Fig. 6(b) by the dots with error bars. Excluding the values for  $N = 56$ and 57, where  $S_n$  shows an irregular behavior,  $\Delta_n$  is found to fluctuate between 0.95 and 1.15 MeV, resulting in a mean value  $\Delta_n$  of 1.04 ± 0.06 MeV. Comparison with the  $\Delta_n$  values of the models of<br>Myers<sup>18a</sup> and Groote *et al.*<sup>18b</sup> indicates that the pairing terms in these models, which both basically employ the phenomenological  $A^{-1/2}$  mass dependence, are slightly too low. These mass formulae predict mean values  $\Delta_n$  of 0.94 and 0.92 MeV, respectively. On the other hand, the models of Seeger and Howard<sup>18c</sup> and Möller and Nix,<sup>19</sup> which use the BCS formalism to calculate the pairing correction, seem to yield pairing terms which are too high. Mean values  $\Delta_n$  of 1.26 and 1.28 MeV, respectively, are obtained using these macroscopic-microscopic approaches.

The two-neutron separation energies  $S_{2n}$  are plotted in Fig. 7 versus neutron number in the region of the indium isotopes near the closed  $N = 50$  shell. In the  $S_{2n}$  plots, the odd-even oscillations are filtered out. The recently published masses of <sup>97</sup>Pd (Ref. 26), <sup>98</sup>Pd (Ref. 27), <sup>100</sup>Ag (Ref. 28), <sup>103</sup>Cd (Ref. 20), <sup>104</sup>Cd (Ref. 1), and <sup>106, 108</sup>Sn (Ref. 1) were also used to calculate  $S_{2n}$  values. The dashed line in the fig-<br>ure indicates the  $S_{2n}$  behavior according to the sys-



FIG. 7. Plot of the experimental two-neutron separation energies  $S_{2n}$  versus neutron number for elements with  $Z = 40$  to 50 near the closed neutron shell at  $N = 50$ . See the text for details.

tematics of Wapstra and Bos.<sup>17</sup> Except for the well-known discontinuity corresponding to the  $N=50$  closed shell, Fig. 7 only shows a strong deviation from the systematics for the neutron-deficient indium isotopes.

In view of the proximity of the doubly closed shell at  $100$ Sn and the reported systematics of the  $2^+$ and  $4^+$  levels for the light even cadmium isotopes.<sup>13</sup> it is difficult to attribute the observed irregular mass behavior of  $^{103}$ In and  $^{104}$ In to a sudden change in nuclear deformation, as is present in the rare earth region. $29$  A further extension of the experimentally known nuclidic mass surface towards <sup>100</sup>Sn will show whether the extra binding energy of  $103$ In and  $104$ In can be explained by an increase of the proton binding energy when approaching the closed  $N = 50$ shell. Such mutual enforcement of proton and neutron magicity is present in the lead region,  $30$  for example, but is not observed for the very neutron rich indium isotopes near the doubly closed shell nucleus  $132$ Sn.

## V. CONCLUSION

A direct comparison of the masses of  $^{103-105}$ In with the predictions of different available mass models shows that  $^{103}$ In is about 1 MeV more bound than was expected. This conclusion is especially valid for the model of Liran-Zeldes<sup>18d</sup> and several based on Garvey-Kelson type of relations,  $18e-g$ which predict reasonably well the masses of the heavier indium isotopes. In addition, the irregular behavior of the single- and two-neutron separation energies for the very neutron-deficient indium isotopes reveals, in a model-independent fashion, that the  $^{103}$ In and  $^{104}$ In masses are lower than expected from the mass systematics of the heavier indium isotopes. Additional systematic study of the mass surface in the vicinity of  $100$ Sn is necessary to investigate whether the observed deviations are related to the nearby  $Z = N = 50$  shell closures.

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