Neutron multiplicity measurements of Cf and Fm isotopes

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Prompt neutrons in coincidence with the fission fragments from the spontaneous fission of ^{250,252,254}Cf and ²⁵⁷Fm were measured inside a 75-cm-diameter, Gd-loaded liquid scintillation counter having a neutrondetection efficiency of about 78%. Measurements for ²⁵⁶Fm were done just outside the counter with an efficiency of 31%. The kinetic energies of both fission fragments and the number of neutrons for each fission event were recorded. From these data, the fragment kinetic energies and masses and the neutron multiplicity distributions were determined for ^{250,252,254}Cf and ²⁵⁷Fm. Variances of neutron multiplicity distributions as a function of total fragment kinetic energy and the ratio of fragment masses have been calculated and are presented for all the nuclides studied.

RADIOACTIVITY, FISSION ^{250,252,254}Cf, ²⁵⁷Fm; measured neutron multiplicity distributions as a function of total kinetic energy and mass ratio. ²⁵⁶Fm; measured average and variance of neutron multiplicity distributions as a function of total kinetic energy and mass ratio.

INTRODUCTION

We first became interested in measuring the number of prompt neutrons emitted in spontaneous fission (SF) as a result of our early studies¹ of the mass distributions from SF of ²⁵⁷Fm. A knowledge of prompt neutron emission $\overline{\nu}$ as a function of fragment mass and kinetic energy is necessary to obtain pre-neutron-emission mass-yield distributions from radiochemical or kinetic energy measurements of the fission products. The marked differences in the yields obtained for symmetric mass division of ²⁵⁷Fm for different assumptions

TABLE I. Data for neutrons emitted in SF of Cf and Fm isotopes.

Nuclide	ν_T	$\sigma_{\nu_T}^{2}$	Γ2
²⁴⁶ Cf	3.14 ± 0.09^{a}	1.66 ± 0.31^{a}	0.850 ± 0.031^{a}
^{250}Cf	3.50 ± 0.09^{b}		0.839 ± 0.002^{a}
	3.49 ± 0.04^{c}	1.49 ± 0.03 ^c	$0.838 \pm 0.001^{\circ}$
^{252}Cf	3.735 ± 0.014 ^d	1.57 ± 0.01^{a}	0.845 ± 0.001^{a}
		1.55 ± 0.02 ^c	0.843 ± 0.001 ^c
^{254}Cf	3.89 ± 0.05^{b}		
	$3.77 \pm 0.05^{\circ}$	1.56 ± 0.01 ^c	0.846 ± 0.006 ^c
²⁵⁴ Fm	3.96 ± 0.14^{a}	1.50 ± 0.02 ^a	0.843 ± 0.012 ^a
²⁵⁶ Fm	3.73 ± 0.18^{a}	2.30 ± 0.65 ^a	0.897 ± 0.047 ^a
		1.82 ± 0.08 ^c	0.863 ± 0.006 ^c
²⁵⁷ Fm	3.77 ± 0.02^{e}	$\textbf{2.49} \pm \textbf{0.06}^{\text{e}}$	0.910 ± 0.002 ^a
	$3.85 \pm 0.05^{\circ}$	2.51 ± 0.02 ^c	$0.911 \pm 0.001^{\circ}$

^aReference 6.

about the mass dependence of $\overline{\nu}$ were discussed in Ref. 1.

Information concerning the excitation or deformation energies of the fragments can also be deduced from studies of prompt neutron emission. In the case of the Fm isotopes, these quantities have turned out to be of particular interest because of the trend with increasing mass of the Fm isotopes toward symmetric mass division. This symmetric mass division is accompanied¹ by very high total kinetic energy (TKE) and by reduced neutron emission.² The average total neutron emission per fission event $\overline{\nu}_r$ for the low energy



FIG. 1. The "unfolded" frequency distribution $P_t(v)$ for neutron emission from ²⁵⁰Cf (SF). The standard deviation based on the number of events is shown for each point.

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^b Data from Ref. 7 normalized to $\overline{\nu}_T = 3.735$ for ²⁵²Cf.

^c This work.

^dReference 5.

^eReference 2.



FIG. 2. Same as Fig. 1 for 252 Cf (SF).

fission of the heavier actinides generally increases³ with Z and A. However, $\overline{\nu}_{T}$ does not increase with A for Fm isotopes, probably because the increased yield of symmetric mass division results in fragments which are closer to the doubly magic ¹³²Sn configuration. Thus the fragments may be more nearly spherical, resulting in a larger kinetic energy due to Coulomb repulsion, a lower fragment excitation energy, and lower neutron and/or photon emission from the fragments. Since our first measurements² of the prompt neutron emission in SF of ²⁵⁷Fm, we have measured neutrons emitted from fission fragments of other spontaneously fissioning nuclides to look for changes in $\overline{\nu}$ as a function of TKE, mass split, and Z and A of the fissioning nucleus. The neutron



FIG. 3. Same as Fig. 1 for ²⁵⁴Cf (SF).



FIG. 4. Same as Fig. 1 for ²⁵⁷Fm (SF).

multiplicity distributions $\overline{\nu}$ and variances for SF of ²⁵⁰Cf, ²⁵²Cf, ²⁵⁴Cf, and ²⁵⁷Fm, and $\overline{\nu}$ and variance for ²⁵⁶Fm as a function of fragment kinetic energies and mass ratios are presented here.

EXPERIMENTAL

A 75-cm-diam spherical tank containing Nuclear Enterprise NE-323 liquid scintillator loaded with 0.5 wt% gadolinium was used in the current studies. The tank has a 15-cm-diam cylindrical hole through the center, in which was placed an evacuated chamber containing a pair of 200-mm² silicon surface-barrier detectors 1.5 cm apart facing each other. The appropriate SF source on a 40-



FIG. 5. $P_{f}(v)$ for ²⁵⁰Cf as a function of TKE and fragment masses. Total number of fission events observed and \bar{v} are shown for each group.



FIG. 6. Same as Fig. 5 for ²⁵²Cf.

 $\mu g/cm^2$ carbon or VYNS film was held equidistant between the detectors, giving a 20% detection efficiency for coincident fission fragments. In this arrangement, the neutrons emitted as a function of the kinetic energy of the fragments from the SF of ²⁵⁰Cf, ²⁵²Cf, ²⁵⁴Cf, and ²⁵⁷Fm were detected with an efficiency of about 78%. For ²⁵⁶Fm, the evacuated chamber was placed so that the source was at the edge of the tank with one detector inside and the other just outside the tank; the resulting neutron-detection efficiency was 31%. The detection of coincident fission fragments triggered a 40- μ s gate for the tank after a 1- μ s delay to exclude prompt gamma rays from fission and recoil protons from thermalization of neutrons. The background was measured at regular intervals throughout these experiments by using a clock to start the gate at a rate typically several times the average fission rate. Details of the construction and operation of the tank have been given elsewhere.4

The ²⁵⁰Cf, ²⁵²Cf, and ²⁵⁷Fm were produced by successive neutron capture in targets irradiated



FIG. 7. Same as Fig. 5 for ²⁵⁴Cf.



FIG. 8. Same as Fig. 5 for ²⁵⁷Fm.

in the High Flux Isotope Reactor (HFIR), processed at the Oak Ridge National Laboratory, and made available to us under the Transplutonium Production Program of the Division of Research of the U. S. Department of Energy. The ²⁵⁷Fm was further purified from rare earths and other actinides by elution from cation-exchange resin columns with ethanol-HCl and hot alpha-hydroxyisobutyrate solutions. Only relatively small samples of ²⁵⁷Fm are available and the measurements were performed on sources of a few SF's per minute. The ²⁵⁰Cf was prepared by neutron irradiation of ²⁴⁹Bk in the HFIR to make ²⁵⁰Bk which beta decayed to ²⁵⁰Cf and was chemically separated from the target material. At the time of measurement the atom fraction of ²⁵⁰Cf was 0.999. Of the total SF activity



FIG. 9. $P_f(v)$ distributions for ²⁵⁰Cf, ²⁵²Cf, ²⁵⁴Cf, and ²⁵⁷Fm for all fragment masses as a function of TKE.



FIG. 10. $P_t(v)$ distributions for ²⁵⁰Cf, ²⁵²Cf, ²⁵⁴Cf, and ²⁵⁷Fm for all TKE's as a function of fragment masses.

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of $\approx 100 \text{ SF/min}$, 83% was due to 250 Cf and the remainder to ²⁵²Cf. The observed $\overline{\nu}_{\tau}$ and variance were corrected for this contribution from ²⁵²Cf. The 254 Cf ($T_{1/2} = 60$ d) and 256 Fm ($T_{1/2} = 2.6$ h) were prepared by collection on carbon foils of products recoiling from triton irradiations of ²⁵⁴Cf and ²⁵⁴Es. The ²⁵⁴Cf (≈60 SF/min) was self-transferred during irradiation of a ²⁵⁴Cf target and the ²⁵⁶Fm ($\approx 6000 \text{ SF/min}$) was the result of beta decay of an ²⁵⁶Es recoil source produced by the (t, p) reaction on ²⁵⁴Es. These two sources were therefore essentially weightless. Standard sources of ²⁵²Cf of several different strengths were prepared to approximate the samples being measured and were used to determine the neutron-detection efficiency.

RESULTS

In general, the object of these measurements was to obtain $\overline{\nu}$, σ_{ν}^{2} , and neutron multiplicity distribu-

FABLE II.	Means and	variances of	of neutron	multiplicity	distributions	of 250	⁰ Cf (71)	280 fission	events)
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	Mass numbers derived from mass ratios							
	125 - 135	135-145	145 - 155	155-165	165 - 175	All mass		
	125-115	115-105	105-95	95-85	85-75	numbers		
210-230 MeV								
SF ^a	549	407				962		
$\overline{ u}$	1.96	1.36				1.69 ± 0.04		
σ_{ν}^{2}	0.33	0.50				0.50 ± 0.07		
Γ_2	0.577	0.535				$\textbf{0.584} \pm \textbf{0.030}$		
190-210 MeV								
SF ^a	5 0 3 0	13 558	3 236	85		21 909		
$\overline{\nu}$	3.09	2.75	1.99	1.49		2.71 ± 0.01		
σ_{ν}^2	0.67	0.77	0.63	0.28		0.84 ± 0.02		
Γ_2	0.747	0.738	0.657	0.453		0.745 ± 0.003		
170-190 MeV								
SF ^a	3989	17822	12073	1704	22	35 610		
$\overline{\nu}$	4.19	3.99	3.39	3.00	2.26	3.77 ± 0.01		
σ_{ν}^2	1.16	0.98	0.84	0.73	0.29	1.06 ± 0.02		
Γ_2	0.827	0.811	0.778	0.748	0.615	$\textbf{0.809} \pm \textbf{0.001}$		
150-170 MeV								
SF ^a	1 137	3 0 0 5	3 990	1999	222	10353		
$\overline{\nu}$	4.18	4.87	4.59	4.12	3.21	4.51 ± 0.02		
σ_{ν}^2	1.98	1.80	1.17	1.22	1.02	1.57 ± 0.04		
Γ_2	0.874	0.871	0.838	0.829	0.787	$\textbf{0.855} \pm \textbf{0.002}$		
All energies								
SF ^a	10705	34792	19305	3788	244			
$\overline{ u}$	3.56	3.55	3.41	3.56	3.13			
σ_{ν}^{2}	1.40	1.52	1.51	1.38	1.03			
Γ_2	0.829	0.839	0.836	0.828	0.785			

^aNumber of fission events in the specified energy and mass ranges.

	Mass numbers derived from mass ratios						
	126.0-136.1	136.1-146.2	146.2-156.2	156.2-166.3	166.3-176.4	All mass	
	125.0-115.9	115.9-105.8	105.8-95.8	95.8-85.7	85.7-75.6	numbers	
210-230 MeV					<u> </u>		
SFª	623	327				952	
$\overline{\nu}$	2.12	1.45				1.89	
σ_{ν}^{2}	0.35	0.68				0.57	
Γ_2	0.606	0.633				0.630	
190-210 MeV							
SF ^a	5137	12 525	2 900	44		20 606	
$\overline{\nu}$	3.43	2.94	2.07 ± 0.02	1.71		2.93	
σ_{ν}^{2}	0.73	0.79	0.68 ± 0.05	0.11		0.93	
Γ ₂	0.770	0.751	0.676 ± 0.012	0.454		0.767	
170-190 MeV							
SF ^a	2994	15 576	10 303	1141	24	30 038	
$\overline{\nu}$	4.79	4.29 ± 0.01	3.63	3.24	2.81	4.07	
σ_{ν}^{2}	0.91	0.90 ± 0.03	0.75	0.62	0.93	1.01	
Γ_2	0.831	0.816 ± 0.002	0.782	0.751	0.762	0.815	
150-170 MeV							
SF ^a	243	1 485	2 400	987	74	5 189	
$\overline{\nu}$	5.93 ± 1.15	5.69	5.13	4.78	3.81	5.24	
σ_{ν}^2	1.44 ± 0.29	1.05	0.83	0.74	0.96	1.06	
Γ2	0.872 ± 0.009	0.857	0.837	0.823	0.804	0.848	
All energies							
SF ^a	8997	29 913	15 605	2172	98		
$\overline{\nu}$	3.86	3.76	3.57	3.91	3.56		
σ_{ν}^{2}	1.50	1.53	1.55	1.33	1.14		
Γ2	0.842	0.843	0.842	0.831	0.809		

TABLE III. Means and variances of neutron multiplicity distributions of ²⁵²Cf (56 932 fission events).

tions and variances as a function of TKE and fragment mass ratio, rather than to redetermine $\overline{\nu}_{T}$ for these nuclides. This necessitated making energy and neutron measurements of coincident fission fragments from sources on thin films over periods of several weeks in order to obtain statistically significant data from the low intensity sources. Concurrent measurements of ²⁵²Cf sources could not be made in this physical arrangement although measurements of ²⁵²Cf were made before and after each run to monitor the neutrondetection efficiency. (The resulting efficiency was $78.5 \pm 1.0\%$ based on $\overline{\nu}_{T} = 3.735$ for ²⁵²Cf, Ref. 5.) Our values for $\overline{\nu}_{T}$ and $\sigma_{\nu_{T}}^{2}$ for ²⁵⁰Cf, ²⁵⁴Cf, and ²⁵⁷Fm from our current experiments are given in Table I together with averages for these and other Cf and Fm isotopes calculated by Lazarev.⁶ Our currently determined variances of 1.49 ± 0.03 for ${}^{250}Cf$ and 2.51 ± 0.02 for ${}^{257}Fm$ are in agreement

with our earlier^{2,6} reported measurements. Our value of 1.55 ± 0.02 for ^{252}Cf is in good agreement with the reported average⁶ of previous values of 1.57 ± 0.01 . No previous determination has been reported for 254 Cf, but our value of 1.56 ± 0.01 is essentially the same as that for ²⁵²Cf. Our value of $\overline{\nu}_{\tau}$ of 3.49 ± 0.04 for ²⁵⁰Cf was obtained after correction for the SF contribution from the ²⁵²Cf in the sample. This correction decreased the measured value by only 1.2%. The quoted error of 0.04 arises principally from the standard deviation computed for several determinations of the neutron-detection efficiency measured with ²⁵²Cf sources. (The statistical error of the ²⁵⁰Cf measurement was only 0.006.) The value of $\overline{\nu}_{\tau} = 3.49$ ± 0.04 is in excellent agreement with that of Orth⁷ of 3.50 ± 0.09 , obtained by renormalizing his reported value of $\overline{\nu} = 3.53 \pm 0.09$ to $\overline{\nu} = 3.735$ for ²⁵²Cf. Our $\overline{\nu}_{\tau}$ values of 3.77 ± 0.05 and 3.85 ± 0.05 for

	Mass numbers derived from mass ratios						
	127.0-137.2	137.2-147.3	147.3-157.5	157.5-167.6	167.6-177.8	All mass	
	127.0-116.8	116.8-106.7	106.7-96.5	96.5-86.4	86.4-76.2	numbers	
210-230 MeV							
SF ^a	4358	1842	39			6 239	
$\overline{\nu}$	2.35	1.73	0.62			2.15	
σ_{ν}^{2}	0.49	0.58	0.37			0.61	
Γ_2	0.663	0.617	0.356			0.668	
190-210 MeV							
SF ^a	20 429	39 01 1	10 085	207		69732	
$\overline{\nu}$	3.68	3.16	2.27	1.65		3.18	
σ_{ν}^{2}	0.71	0.77	0.57	0.43		0.92	
Γ_2	0.780	0.761	0.670	0.553		0.776	
170-190 MeV							
SF ^a	9 999	44 293	32 677	4092	159	91 220	
$\overline{ u}$	5.00	4.50	3.81	3.43	2.84	4.25	
σ_{ν}^2	0.89	0.88	0.73	0.68	0.45	1.01	
Γ2	0.836	0.821	0.787	0.766	0.704	0.821	
150-170 MeV							
SF ^a	931	4755	8 248	3661	327	17922	
$\overline{\nu}$	6.01	5.83	5.29	4.97	4.27	5.38	
σ_{ν}^2	1.84	1.03	0.76	0.81	0.49	1.03	
Γ2	0.885	0.859	0.838	0.832	0.793	0.850	
All energies							
SF ^a	35757	89 902	51 049	7960	486		
$\overline{\mathcal{V}}$	3.94	3.93	3.74	4.09	3.80		
σ_{ν}^{2}	1.55	1.53	1.52	1.47	0.93		
Γ2	0.846	0.845	0.841	0.843	0.801		

TABLE IV. Means and variances of the neutron multiplicity distributions of ²⁵⁴Cf (185 687 fission events).

²⁵⁴Cf and ²⁵⁷Fm, respectively, are in reasonable agreement with the earlier determinations given in Table I. Again, the quoted error arises primarily from the uncertainty in the efficiency. Due to the relatively long measurement times and the absence of simultaneous efficiency monitoring, we have chosen to normalize our present data to the earlier values⁷,² of 3.89 ± 0.05 and 3.77 ± 0.02 for ²⁵⁴Cf and ²⁵⁷Fm, respectively.

The neutron multiplicity distributions associated with the SF of 250 Cf, 252 Cf, 254 Cf, and 257 Fm are shown in Figs. 1-4. These "unfolded" distributions were obtained from the observed frequency distributions by solving the equations,²

$$p_{d}(n) = \sum_{k=0}^{n} \sum_{\nu=n-k}^{\nu \max} {\nu \choose n-k} e^{n-k} (1-\epsilon)^{\nu-n-k} \\ \times p_{b}(k) p_{t}(\nu), \quad n = 1, \dots, \nu_{\max}$$
(1)

where $p_d(n)$ is the probability of observing *n* events

per fission, ϵ is the neutron-detection efficiency, $p_t(\nu)$ is the probability that ν neutrons are emitted per fission, and $p_b(k)$ is the probability of k background events in 40 μ s. The maximum number of neutrons considered, ν_{max} , was 9. The background was found to follow the Poisson distribution $p_b(k) = e^{-a} d^k/k!$, where a is the average number of background events. The average background was 0.02 to 0.04 counts per 40- μ s gate for most runs, but was 0.20 counts per gate for the ²⁵⁰Cf measurement and 0.14 counts per gate for the ²⁵⁶Fm measurement. The deadtime of 0.1 μ s per pulse was neglected.

The quantity Γ_2 , which is independent of the neutron-detection efficiency,⁸ was calculated from the relationship,

$$\Gamma_2 = (\sigma_d^2 - \sigma_b^2 - \overline{\nu}_d + \overline{\nu}_b)(\overline{\nu}_d - \overline{\nu}_b)^{-2} + 1, \qquad (2)$$

where the subscripts d and b refer to the observed

	Mass numbers derived from mass ratios					
	128.5 -1 38.8 128.5 -1 18.2	138.8 -149.1 118.2 -107.9	149.1–159.3 107.9–97.7	159.3-169.6 97.7-87.4	169.6-179.9 87.4-77.1	All mass numbers
240-260 MeV						
SF ^a	3 294	102				3 3 9 6
$\overline{\nu}$	1.08	0.80				1.07
σ_{ν}^{2}	0.65	1.02				0.66
Γ_2	0.631	1.342				0.644
220-240 MeV						
SF ^a	8 312	2778	71			11 163
$\overline{\nu}$	2.35	2.10	1.31			2.28
σ_{ν}^{2}	1.26	1.08	0.65			1.22
Γ_2	0.800	0.769	0.613			0.796
200-220 MeV						
SF ^a	11922	11 835	2 382	61		26 201
$\overline{\nu}$	3.60	3.44	2.83	2.25		3.46
σ_{ν}^{2}	1.66	1.33	0.98	1.00		1.50
Γ_2	0.851	0.821	0.769	0.753		0.836
180-200 MeV						
SF ^a	8989	11890	6897	1162	50	28 9 88
$\overline{\nu}$	4.34	4.35	3.94	3.38	2.68	4.21
σ_{ν}^{2}	1.82	1.61	1.31	1.18	0.79	1.65
Γ_2	0.866	0.855	0.831	0.807	0.737	0.855
160 – 180 MeV						
SF ^a	4126	4 8 49	4365	2087	421	15848
$\overline{ u}$	4.86	4.89	4.81	4.37	3.72	4.76
σ_{ν}^{2}	1.96	1.86	1.63	1.39	1.35	1.80
Γ_2	0.877	0.873	0.862	0.844	0.829	0.870
All energies						
SF ^a	36643	31 454	13715	3312	472	
\overline{v}	3.41	3.88	4.01	3.99	3.61	
σ_{ν}^{2}	2.75	2.12	1.84	1.59	1.39	
Γ_2	0.944	0.883	0.865	0.849	0.830	

TABLE V. Means and variances of neutron multiplicity distributions of ²⁵⁷Fm (90337 fission events).

and background values, respectively. The calculated values for the overall distributions are given in Table I and are in good agreement with those from previous determinations.

In the case of ²⁵⁶Fm, which was measured with a neutron-detection efficiency of only 31%, $\bar{\nu}_T$ was normalized to the reported value⁶ of $\bar{\nu}_T$ = 3.73±0.18. The distribution was not unfolded because of the low detection efficiency, but the variance $\sigma_{\nu_T}^2$ was calculated from the relationship:

$$\sigma_{\nu_{\tau}}^{2} = \epsilon^{-2} (\sigma_{d}^{2} - \sigma_{b}^{2}) + \epsilon^{-1} (1 - \epsilon^{-1}) (\overline{\nu}_{d} - \overline{\nu}_{b}).$$
(3)

Our value of 1.82 ± 0.08 is smaller than the reported value⁶ of 2.30 ± 0.65 , but is within the quoted

uncertainties. Our value of Γ_2 of 0.863 is also somewhat smaller than the reported value.

Figures 5-8 show the unfolded distributions $P_t(\nu)$ as a function of mass fraction and TKE for ²⁵⁰Cf, ²⁵²Cf, ²⁵⁴Cf, and ²⁵⁷Fm. Figure 9 shows $P_t(\nu)$ for all fragment masses as a function of TKE and Fig. 10 shows $P_t(\nu)$ for all TKE's as a function of fragment masses. The values of $\overline{\nu}$, σ_{ν}^2 , and Γ_2 are given in Tables II through V. Although the unfolded $P_t(\nu)$ distributions could not be derived for ²⁵⁶Fm because of the low efficiency of the measurement, values of $\overline{\nu}$, σ_{ν}^2 , and Γ_2 could still be calculated as a function of mass and TKE and are given in Table VI. (For purposes of display in Figs. 5-10, categories containing ≤ 50

	Mass numbers derived from mass ratios					
	128.0-138.2	138.2-148.5	148.5-158.7	158.7-169.0	All mass	
	128.0-117.8	117.8-107.5	107.5-97.3	97.3-87.0	numbers	
220-240 MeV						
SF ^a	2260	451			2712	
$\overline{\nu}$	1.98	1.51			1.90	
σ_{ν}^{2}	1.15	0.96			1.15	
Γ_2	0.788	0.759			0.792	
200-220 MeV						
SF ^a	8 047	7 088	629		15766	
$\overline{ u}$	3.29	2.80	2.01		3.02	
σ_{ν}^2	1.67	0.56	0.51		1.22	
Γ_2	0.850	0.714	0.629		0.803	
180-200 MeV						
SF ^a	5 214	11 944	4617	337	22119	
$\overline{ u}$	4.53	4.05	3.43	2.95	4.01	
σ_{ν}^{2}	2.18	0.49	0.88	0.69	1.12	
Γ2	0.885	0.783	0.783	0.704	0.820	
160-180 MeV						
SF ^a	760	2414	2424	626	6 263	
$\overline{\nu}$	5.69	5.30	4.69	4.45	5.01	
σ_{ν}^2	0.92	1.26	0.20	2.59	1.19	
Γ2	0.853	0.856	0.796	0.906	0.849	
All energies						
SF ^a	16362	21899	7671	965	46943	
$\overline{ u}$	3.60	3.73	3.71	3.92	3.73 ± 0.18 ^b	
σ_{ν}^{2}	2.65	1.31	1.31	2.40	1.82 ± 0.08	
Γ_2	0.927	0.826	0.827	0.901	0.861	

TABLE VI. Means and variances of the neutron multiplicity distributions of 256 Fm (47366 fission events).

^bReference 6.

events are not shown.) Calculated standard deviations for $\overline{\nu}$, σ_{ν}^2 , and Γ_2 for several cases with different numbers of observed SF events are shown in Tables II and III. (The standard deviations for Γ_2 were calculated using the appropriate correlation coefficients derived from the unfolding procedure.) These given an idea of the statistical errors involved for the other cases presented here.

From our measurements of the kinetic energies of coincident fragments and the emitted neutrons, the TKE, mass fraction (M_H/A) for the fragments, and the average total number of neutrons per fission event can be derived. However, we cannot tell how many of these neutrons were emitted from the light and how many from the heavy fragment. Therefore, in Figs. 5–10 and in Tables II-IV, we give the mass range of both fragments for each group of events.

The $\overline{\nu}$ values for all five nuclides decrease mono-

tonically with increasing TKE for a given mass split. This might be expected since the total energy is approximately constant for a given mass split and is manifested primarily either in the kinetic or excitation energy of the fragments. Thus, as the TKE increases, the excitation energy of the fragments, and hence the energy available for emission of neutrons (and photons), must necessarily decrease. In the case of 257 Fm, $\overline{\nu}$ drops to 1.08 and 0.80, respectively, for symmetric and near-symmetric mass splits for the highest TKE groups, while for the other nuclides $\overline{\nu}$ drops only to 1.96 and 1.36. This difference may be a result of the fact that the TKE for symmetric and near-symmetric mass splits for ²⁵⁷Fm reaches values some 50 to 30 MeV higher (see Fig. 11) than for the other nuclides shown, even though the estimated Q value^{9,10} for 257 Fm is nearly the same as for 256 Fm and only about 15 MeV higher than

for the Cf isotopes. The contour plots of TKE as a function of mass fraction for ²⁵⁴Cf, ²⁵⁶Fm, and ²⁵⁷Fm shown in Fig. 11 illustrate the difference in TKE release and its variance for different mass fractions for these nuclides. ²⁵⁷Fm exhibits much larger spreads in TKE for symmetric mass division than the other nuclides. These differences in TKE in the region of symmetric mass division



FIG. 11. Contour diagrams showing pre-neutronemission TKE distributions as a function of mass fraction for ²⁵⁴Cf, ²⁵⁶Fm, and ²⁵⁷Fm (data for ²⁵⁷Fm from Ref. 1.) The contours are lines of relative numbers of events, based on data groupings 5 MeV \times 0.01 units of mass fraction.

 $(M_H/A = 0.50 \text{ to } 0.54)$ may be due to the approach of the symmetric fragments from SF of ²⁵⁷Fm to the spherical, doubly magic ¹³²Sn configuration for which the Coulomb repulsion, and hence the TKE, should reach a maximum value. (²⁵⁶Fm shows this effect to a lesser degree.) The highest TKE group summed over all mass splits, as shown in Tables II-VI and Fig. 9, shows the lowest neutron emission for all these nuclides, 1.07 to 2.15. The lowest TKE group shows the highest values, $\overline{\nu}$ = 4.51 to 5.38. Thus, $\overline{\nu}$ changes from 1.07 to 5.38 as a function of TKE, but changes only from 3.13 to 4.09 for the various mass groups summed over all TKE's (Tables II-VI and Fig. 10.)

For the lowest TKE groups, $\overline{\nu}$ is typically 1 or 2 neutrons less for asymmetric fissions than for symmetric fissions (see Tables II-VI and Figs. 5-8). Although the Q values decrease by about 35 to 40 MeV as the mass fraction increases from 0.52 to 0.66, the decrease in Q is apparently not completely accounted for by the observed decrease in neutron emission. Since constraining the TKE to low values at symmetry selects the more highly distorted fragments, perhaps more of the energy is dissipated by photon emission for the lowenergy, near-symmetric mass splits.

The mass yield for ²⁵⁷Fm SF events with TKE >235 MeV, where $\bar{\nu}$ is only about 1, is shown in Fig. 12. This mass distribution resembles those measured^{11,12} for SF of ²⁵⁸Fm and ²⁵⁹Fm where the most probable TKE's are 238 and 242 MeV, respectively, and suggests that neutron emission may also be low for ²⁵⁸Fm and ²⁵⁹Fm. This is further supported by the fact that their TKE's are approaching the Q values of 250 to 255 MeV estimated for symmetric fission from mass



FIG. 12. Mass-yield distribution for 257 Fm for fission events with TKE > 235 MeV.

tables.9.10

The large variances observed for neutron emission from 256 Fm and 257 Fm (Table I, Fig. 4) suggest a broad distribution in fragment excitation energies. This may perhaps be attributed to the fact that these nuclides are in a "transition" region, i.e., although symmetric fragments can have the magic proton number of 50, they are still 3 to 4 neutrons from the 82-neutron closedshell configuration. The fragments may then be rather "soft" to deformation, and the observation of symmetric fragments with both very high and very low TKE indicates a rather large difference in their shapes, ranging from elongated to nearly

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spherical.

The number of neutrons emitted per fission and the variance should decrease very sharply for ²⁵⁸Fm and ²⁵⁹Fm and higher mass fermium isotopes as symmetric mass division results in fragments which more closely approach the rigid doubly magic configuration. If this hypothesis is correct, then neutron emission and its variance might be expected to increase again for fissioning systems with Z greater than 100.

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