Total β -decay energies and masses of strongly neutron-rich indium isotopes ranging from 120 In to 129 In

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Experimental total β -decay energies of strongly neutron-rich indium isotopes are presented. The samples were produced as mass-separated fission products by using the on-line isotope separator technique. By means of a Si(Li)-detector system, β spectra were recorded in coincidence with different γ gates, and Q_{β} values for isomers of $^{120-129}$ In were deduced. The atomic mass excess is derived for these nuclei, and comparisons are made with mass formula predictions. The mean uncertainty of the experimental mass excesses is 0.11 MeV. The precision of the mass formulas chosen for the comparison varies widely with rms deviations ranging from 0.21 to 1.36 MeV. For the isotopes $^{124-129}$ In the possibility of delayed-neutron emission is discussed.

RADIOACTIVITY ¹²⁰⁻¹²⁹ In: Measured β - γ coincidences for isomers: deduced total β -decay energies, atomic mass excesses, delayed-neutron windows; comparison with mass formulas. Mass-separated fission products, Si(Li)-detectors, Ge(Li)-detector, NaI(Tl)-detectors.

I. INTRODUCTION

A fundamental property of the atomic nucleus is its mass. The ISOL technique¹ has made an increasing number of nuclides far from the region of β stability available for mass determinations. The most accurate measurements of stable nuclides have been performed with mass spectrometers, and recently such determinations of radioactive neutron-deficient rubidium isotopes were reported² with the spectrometer connected to ISOLDE at CERN. The uncertainties of the latter measurements are reported to be 25-80 keV. So far, direct mass determinations are limited to a few elements by the restriction that no other isobars or isomers are allowed to be present in the samples. This means that accurate direct mass determinations will be extremely difficult to perform for the neutron-rich indium isotopes of interest in this work because of the presence of isomerism. The indirect method of determining the mass differences from nuclear decay energies $(Q_{\beta} \text{ values})$, adopted in the present study, is therefore the only realistic alternative.

Beside the general importance of masses and Q_{β} values, mass data of neutron-rich nuclides are of special interest as these data are essential for the construction of mass formulas used in the theories of nucleosynthesis³ and for predictions about superheavy elements.

The isotope-separator facility OSIRIS⁴ connected to the R2-0 reactor at Studsvik is an excellent tool for producing neutron-rich fission products. With this equipment it has been possible to study indium isotopes ranging from ¹¹⁷In to ¹³²In. In this article Q_{β} values and mass excesses covering the mass range 120–129 are presented. The technique used in these experiments is described in Sec. II, and in Sec. III the results of the Q_{β} measurements are reported. Finally, the experimental Q_{β} values and corresponding mass excesses are compared with predictions from different mass formulas in Sec. IV. In the same section the application of experimentally measured Q_{β} values to the identification of delayed-neutron precursors is described.

II. EXPERIMENTAL TECHNIQUES

A. On-line mass separation and sample production

At the OSIRIS facility, indium isotopes are produced by thermal-neutron induced fission of 235 U. A cylinder consisting of several layers of graphite cloth is impregnated with about 3 g of the target material and enclosed in the ion source of the isotope separator.⁵ The recoiling fission fragments are caught in the graphite, diffuse to the surface, evaporate, and finally, get ionized and separated in a 55° fringing-field type of magnet.⁶ There is very slight element selection in the system, and the samples contain generally two or more isobars which have to be separated by a proper timing of the experiment and also by choosing selective coincidence conditions.

The activities were collected on tape, either in the collector chamber of the separator or at a tape position at the end of a beam line. The collector chamber tape system needed a trans-

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portation time of 3 s,⁷ while the other tape system transports the sample to the detector system within 0.3 s.

In the present work the uranium target was irradiated in a neutron flux of about $10^{10} n_{\rm th} {\rm cm}^{-2} {\rm s}^{-1}$ (the available neutron flux is $4 \times 10^{11} n_{\rm th} {\rm cm}^{-2} {\rm s}^{-1}$).

B. Detector arrangements

The basic principle for the determination of total β decay energies is to measure β branches to known excited states of the daughter nucleus. For this purpose a $\beta\gamma$ -coincidence spectrometer $(Q_{\beta}$ spectrometer) has been constructed. It consists of a system of Si(Li) detectors for β detection and two NaI(T1) detectors, or a Ge(Li) detector, for γ detection.

Three different detector configurations have been used in the present experiment.



FIG. 1. Block diagram of the electronics used for counting β - γ coincidences with method II. The Ge(Li) detector used in method III is also indicated. (PA = preamplifier; SA=sum amplifier; A=amplifier; DA = delay amplifier; COP=crossover pickoff; TSCA = timing single channel analyzer; SCA=single channel analyzer; TPHC=time-to-pulse-height converter; X and Y = analog-to-digital converters.) A star indicates the position of the sample. Method I: a main Si(Li) detector surrounded by three anticoincidence Si(Li) detectors for β measurement and two NaI(Tl) detectors for γ measurement; transport time 3 s.

Method II: a main Si (Li) detector surrounded by two anticoincidence Si(Li) detectors for β measurement and two NaI(Tl) detectors for γ measurement; transport time 0.3 s. Method III: a main Si(Li) detector surrounded by two anticoincidence Si(Li) detectors for β mea-

surement and a Ge(Li) detector for γ measurement; transport time 0.3 s.

In all experiments the same main Si(Li) detector was used: a 25 mm diam \times 5 mm thick transmission detector from which a segment has been cut from the detector itself in such a way that the β particles from a sample will see a sensitive depth up to 23 mm. This corresponds to the range of electrons of energy about 10 MeV. Method I is described in detail in Ref. 7 and will not be further discussed here. In Fig. 1 a block diagram of method II is shown, and the Ge(Li) detector used in method III is also indicated. The response function and the efficiency of the Si(Li) system are discussed in Sec. II E. Method III is described in Ref. 8.

C. Experimental procedures

As no chemical separation was used, the massseparated samples contained in addition to indium, isobaric components consisting of isotopes of cadmium and/or tin. The situation is favorable for the indium isotopes, however, which could in most cases be enhanced by a proper timing of the experiment. For those indium isotopes measured by method III no problem with contamination arises as the γ gates are chosen in a well resolved spectrum measured by a Ge(Li) detector.

Experimentally, it has been found that a counting rate of up to 4000 cps in the main β detector gives a β spectrum free from pileup. This sample strength also gives a suitable counting rate in the γ detectors. The reactor power was adjusted to give this sample intensity. Usually, $(5-10) \times 10^7 \beta$ events were collected in the main detector in order to make possible an accurate Fermi-Kurie (FK) analysis of the coincident β spectra.

The treatment of the 0.9 s activity of ¹²⁹In will now be discussed as an example of method II. The daughter ¹²⁹Sn has such a long half-life, 134 s, compared to ¹²⁹In, that negligible influence is expected with a collection time of 2 s. About 15000 samples were collected and measured during the experiment. The γ spectrum obtained for a few hundred samples is shown in Fig. 2. A γ line corresponding to a ground state transition of 2119



FIG. 2. The γ spectrum of the mass chain 129 recorded with NaI(T1) detectors. The γ gate chosen for the coincident β spectrum is shaded.

keV was chosen as a gate for the β spectrum (see Fig. 4) and the coincident β events were stored directly in the analyzer memory. The time resolution was about 80 ns. The accidental coincidence spectrum obtained by displacing the time window in the coincidence circuit was subtracted, and the true β -pulse spectrum was then transformed to an electron distribution (see Sec. II E). In this case the background effect was negligible.

In method III the narrow time window, 19 ns, makes the accidental coincidence rate negligible at the counting rates used. In this case also the pulses in an energy interval close to each γ gate of width corresponding to that of the gate itself were recorded. The spectra thus obtained were subsequently subtracted from the β spectra coincident with the γ gates to give a background correction.

D. Calibration of the β detector

The linearity of the β detector has been investigated using conversion electrons from ²⁰⁷Bi and from the daughters of ²²⁸Th.⁷ These cover the energy interval from 0.5 to 2.6 MeV. Within this interval the main Si(Li) detector was linear. The electronic system was controlled with a pulse generator and found to be linear at least up to 10 MeV. The maximum deviation from a line defined by the ²⁰⁷Bi conversion electron peaks was 4 keV in the range 1.68–10 MeV.

During the experiments only ²⁰⁷Bi was used as a calibration source, and a linear fit to the three conversion electron lines was used as a calibration line in the analysis.

The adopted Q_{β} values, 3.889 ± 0.005 of 87 Kr and

3.541 ± 0.009 MeV of ¹⁰⁶Rh,⁹ were used as check points of the calibration. Our results were for ⁸⁷Kr Q_{β} = 3.87 ± 0.09 MeV and for ¹⁰⁶Rh Q_{β} = 3.55 ± 0.07 MeV.⁸

E. Data analysis

The pulse distributions coincident with different γ gates were analyzed by means of a computer program in order to determine the end points of the energy spectra from a Fermi-Kurie plot. In a first step the pulse distribution was transformed to an electron distribution, and in a second step the FK parameter $(N/pWF)^{1/2}$ was calculated where N is the transformed electron intensity, p and W are the relativistic electron momentum and energy, respectively, and F is the Fermi function. A weighted least squares fit to these points gave the E_{β}^{max} and, by adding the level energy, the total β -decay energy was deduced.

For the transformation one needs to know the response and the efficiency functions for the β detector. The response function was determined using the ²⁰⁷Bi conversion electron spectrum, and a good approximation was found to be a Gaussian full energy peak (full width at half maximum = 12 keV) with a constant tail down to zero energy.⁸ Within the energy range covered, 0.48-1.68 MeV, the peak-to-total ratio was found to be 0.30 and independent of electron energy.⁸ Berger et al.¹⁰ have made an extensive study of the response function for various types of Si(Li) detectors. They concluded that the peak-to-total ratio was almost constant for energies from 1 to 5 MeV. They also found that the tail down to zero energy was constant even for 5 MeV electrons. In the transformation from pulse distribution to electron distribution a channel width of at least 35-40 keV was chosen. The Gaussian peak then appears in a single channel, which makes the error analysis of the transformation very simple.⁸

The efficiency function of the β -detector system depends mainly on the anticoincidence condition, but also to a certain extent on the response function used. In the energy range 0.48 to 1.68 MeV the conversion electron spectrum of ²⁰⁷Bi can be used for an efficiency check. The ratio of the peak intensities for the lines 1681 and 481 keV recorded with our system was 0.012 ± 0.001, in agreement with 0.012 ± 0.001 from Ref. 11. Thus, in this energy range the efficiency was constant.

The odd-mass indium isotopes provide an excellent possibility to determine the efficiency above 1.68 MeV. One can find several coincident β spectra consisting of only one component. The end points of these branches are between 3.2 and 5.4 MeV. The experimental β spectra were trans-



FIG. 3. The efficiency function of the Si(Li) system. The experimentally determined points are represented by $\diamond (^{207}\text{Bi})$, $\bullet (^{123}\text{In})$, $\Delta (^{125}\text{In})$, $\nabla (^{127}\text{In})$, and $\bigcirc (^{129}\text{In})$. The uncertainties of the experimental points around 1.5 MeV are between 0.05 and 0.07, while an uncertainty between 0.10 and 0.15 is valid for the high energy parts. The solid line represents a fifth degree polynomial fitted to the experimental points.

formed with the response function described above and a constant efficiency yielding a first order approximation of E_{β}^{max} . Using this value a theoretical β spectrum was calculated, and the ratio between the transformed and the calculated electron distributions gives a new set of efficiency values to be used for a second-order approximation of E_{β}^{max} . The procedure was then repeated until no further changes occurred. The resulting efficiency function is shown in Fig. 3. For more details see Ref. 8.

When more than one determination of the Q_{β} value of a nuclide were made, the mean value was calculated with its uncertainty given as

$$\sigma = \left[\overline{\sigma}^2 + \sigma^2 (E_{\text{cal}})\right]^{1/2},\tag{1}$$

where

$$\overline{\sigma} = \left(\sum_{i} \sigma_{i}^{-2}\right)^{-1/2}, \qquad (2)$$

and $\sigma(E_{cal})$ equals the largest calibration uncertainty for the determinations.

The expression (2) was chosen because in all cases it gave values larger than the error deduced from the external consistency of the points. The nonlinearity of the system⁸ was found to introduce negligible error (maximum error 4 keV).

III. EXPERIMENTAL RESULTS

The level structure of tin isotopes has been studied in the mass interval 119-132, $^{12-17}$ and the half-lives of the isotopes of indium have been determined by means of β , γ , and delayed-neutron counting.^{18,19}

A. Odd-mass indium isotopes

1. Nuclides ¹²¹ In, ¹²³ In, and ¹²⁵ In

The decay properties of odd-mass indium isotopes in the mass range 119-125 have been thoroughly investigated by Fogelberg et al.¹² A characteristic feature of these nuclides is the presence of two isomers about 300 keV apart.¹³ The spin and parity assignment is $\frac{9^+}{2}$ for the ground states and $\frac{1}{2}$ for the isomeric states. Partial level schemes of odd-mass tin isotopes from Refs. 12, 14 are shown in Fig. 4. For determinations of total β decay energies of the ground states, the γ transitions 926 keV in ¹²¹Sn, 1020 and 1131 keV in $^{123}\mathrm{Sn},\,$ and 1032 and 1335 keV in $^{125}\mathrm{Sn}$ were chosen as gates for the β spectra. These γ transitions depopulate the $\frac{7}{2}^+$ states which are strongly favored (95-100%) in the β decay. Therefore the coincident β spectra consist of only one component, which makes a linear fit possible over a wide energy range in the FK analysis.

The isomeric states mainly decay to low-lying states in the daughter nuclei. In ¹²¹Sn the $\frac{1}{2}$ ⁺ state is situated at 60 keV which is below our limit for γ gates. The transitions between the $\frac{1}{2}$ ⁺ and the $\frac{3}{2}$ ⁺ states in ¹²³Sn and ¹²⁵Sn of energy 126 and 188 keV, respectively, were chosen as γ gates for the first forbidden β spectra from the isomeric states in ¹²³In and ¹²⁵In. Lacking proper shape factors the spectra were treated as allowed ones in the analysis.

Method I (cf. Sec. II B) was used for 121 In and method III for 123 In and 125 In.

The experimental results are collected in Table I. The Q_{β} value has been deduced for each β



FIG. 4. Partial level schemes for odd-mass tin isotopes.



FIG. 5. Fermi-Kurie plots of the β spectra corresponding to the 1335 and 188 keV gates which depopulate the levels at 1363 and 215 keV in ¹²⁵Sn. These levels are fed by β particles from the ground state and the isomeric state of ¹²⁵In, respectively.

		TABLE I. Resul	lts of FK analyses f	or the odd-mass indium	isotopes ¹²¹ In, ¹²³ In,	, ¹²⁷ In, and ¹²⁹ In		
Nuclide M	Half-lj lethod (s)	Gate ife energy (keV)	y Level (keV)	Range of fit (MeV)	E ^{m ax} (MeV)	Q_{eta} value (MeV)	$\begin{array}{l} \operatorname{Mean} Q_{\beta} \\ \operatorname{value} \\ (\operatorname{MeV}) \end{array}$	Other experimental determinations (MeV)
¹²¹ Ing	I 23.1	a 926	926 ^b	1.2-2.4	2.48 ± 0.05	3.41 ± 0.05		3.38 ± 0.04°
121 Inn	233ª					3.72 ± 0.05 ^d		
123 Irg	III 5.9	8 ^a 1020 1131	1044 ^b 1155	1.2-3.2 1.0-3.2	3.36 ± 0.10 3.30 ± 0.07	$\begin{array}{c} 4.40 \pm 0.10 \\ 4.46 \pm 0.07 \end{array}$	4.44 ± 0.06	4.38 ± 0.05 [€]
123 In ^m	III 47.8 ⁱ	a 126	150 ^b	1.0-4.4	4.54 ± 0.21	4.69 ± 0.21		
125 Ing	III 2.3	3 ^a 1032 1335	1059 ^b 1363	1.5-4.2 1.5-4.0	4.34 ± 0.28 4.13 ± 0.08	5.40 ± 0.28 5.49 ± 0.08	5.48 ± 0.08	8
125 In ^m	III 12.2 ⁶	a 188	214 ^b	1.2-5.2	5.45 ± 0.12	5.66 ± 0.12		
127 In 8	II 1.3 ^c	a 1597 1597	1602 ^f 1602	1.2-4.8 1.2-4.8	4.86 ± 0.08 4.99 ± 0.16	6.46 ± 0.08 6.59 ± 0.16	6.49 ± 0.07	
127 _{In} m	П 3.7'	a 252 252	257 ^f 257 ^f	4.5-6.1 4.5-6.1	6.37 ± 0.28 6.41 ± 0.24	$\begin{array}{c} 6.63 \pm 0.28 \\ 6.67 \pm 0.24 \end{array}$	6.65 ± 0.18	
129 Ing	10.0 ¹	f 2119	2119 ^f	1.5-5.3	5.48 ± 0.12	7.60 ± 0.12		
129 In ^m	II 1.2 ⁴	f 315	315 ^f	5.0-7.5	7.5 ± 0.6	7.8 ± 0.6		
^a Reference 18.	. ^b Reference 12.	^c Reference 9.	^d Obtained by ad	ding the isomeric transit	ion energy to the Q_8	value for ¹²¹ In ^g .	^e Reference 20.	fReference 14.

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FIG. 6. Fermi-Kurie plots of the β spectra corresponding to the 1597 keV (a) and 2119 keV (b) gates. These γ transitions depopulate the levels at 1602 and 2119 keV in ¹²⁷Sn and ¹²⁹Sn, respectively.

branch, and for cases where more than one determination is made the average value has been calculated. The main results are ¹²¹In^s, $Q_{\beta} = 3.41 \pm 0.05$ MeV, ¹²³In^s, $Q_{\beta} = 4.44 \pm 0.06$ MeV, ¹²³In^m, $Q_{\beta} = 4.69 \pm 0.21$ MeV, ¹²⁵In^s, $Q_{\beta} = 5.48 \pm 0.08$ MeV, and ¹²⁵In^m, $Q_{\beta} = 5.66 \pm 0.12$ MeV.

The Q_{β} values for ¹²¹In^s and ¹²³In^s are in excellent agreement with earlier determinations.^{9,20} For ¹²³In and ¹²⁵In the differences between the Q_{β} values for the isomeric states and the ground states are 0.25 ± 0.22 and 0.18 ± 0.14 MeV, respectively, in agreement with the expected value of about 300 keV.¹³

The FK plots of β spectra corresponding to the gates 1335 and 188 keV for the isomers of ¹²⁵In are shown in Fig. 5.

2. Nuclides ¹²⁷ In and ¹²⁹ In

The decay properties of ¹²⁷In and ¹²⁹In, investigated by de Geer and Holm,¹⁴ are similar to those found for ^{121,123,125}In. The main β transition from the ground state of ¹²⁷In feeds the level at 1602 keV in ¹²⁷Sn, while the isomeric state feeds a level at 257 keV. For the 129 In case the analogous levels in 129 Sn are 2119 and 315 keV (see Fig. 4).

Method II was used for this experiment since the activity was too low to permit $\beta\gamma$ coincidences with Si(Li) and Ge(Li) detectors. The γ gates and the measured β end-point energies are given in Table I. The resulting Q_{β} values are ¹²⁷In^s, $Q_{\beta} = 6.49 \pm 0.07$ MeV, ¹²⁷In^m, $Q_{\beta} = 6.65 \pm 0.18$ MeV, ¹²⁹In^s, $Q_{\beta} = 7.60 \pm 0.12$ MeV, and ¹²⁹In^m, $Q_{\beta} = 7.8 \pm 0.6$ MeV.

Fermi-Kurie plots of the β spectra in coincidence with the gates at 1597 and 2119 keV in ¹²⁷Sn and ¹²⁹Sn are shown in Fig. 6.

B. Even-mass indium isotopes

Investigations of the decay properties of evenmass indium isotopes are in progress.^{15,21} Some pieces of information from these studies and from Refs. 22 and 23 needed for the dicussion below are collected in Fig. 7.

Three isomers are found in each of the nuclides ¹²⁰In and ¹²²In, and two isomers in ¹²⁴In, ¹²⁶In, and ¹²⁸In.²¹ The 7⁻ states in ¹²⁰⁻¹²⁸Sn are presumably isomeric with a delay of importance for the coincidence experiments.¹⁵



FIG. 7. Partial level schemes for even-mass tin isotopes. The superscripts l and h stand for "low spin" and "high spin," respectively.

Nuclide	Method	Half-life (s)	Gate energy (keV)	Level (keV)	Range of fit (MeV)	E ^{max} (MeV)	Q ₈ value (MeV)	Mean Q _g value (MeV)	Other experimental determinations (MeV)
120 In'		3.2 ^a	1171 1171 1186 1251	1171 ^b 1171 ^b 2358 ^b 2423 ^b	3.2-4.2 1.4-3.5 1.0-2.4 0.6-2.6	$\begin{array}{c} 4.26 \pm 0.29 \\ 4.06 \pm 0.25 \\ 2.76 \pm 0.72 \\ 2.97 \pm 0.75 \end{array}$	5.43 ± 0.20 5.23 ± 0.25 5.12 ± 0.72 5.39 ± 0.25	5.30 ± 0.17	5.6±0.6°
$120 \mathrm{Im}^{h}$	III	45 ^a	2195 965	2195 ^b 3440 ^b	1.5-3.0	3.10 ± 0.20 2.08 ± 0.40	$5.30 \pm 0.20 \\ 5.52 \pm 0.40 \\ \end{cases}$	5.34 ± 0.17	5.3 ± 0.2°
122 In/		1.5 ^d	2065 2759 1141	3206 ^b 3899 ^b 1141 ^b	0.7 <i>-2.7</i> 0.8 <i>-2.</i> 1 3.0 <i>-</i> 4.6	3.57 ± 0.60 2.55 ± 0.40 5.34 ± 0.36^{f}	$\left\{\begin{array}{c} 6.77 \pm 0.60\\ 6.45 \pm 0.40\\ 6.48 \pm 0.33\end{array}\right\}$	6.51 ± 0.23	6.5 ± 0.2 ^e
$^{122}\ln^{h}$	Ш	10ª	878 1122	3530 ^b - 3530 ^b -	0.8-2.8 1.2-2.8	3.40 ± 0.40 2.98 ± 0.20	$6.93 \pm 0.40 \\ 6.51 \pm 0.20 \\ \end{cases}$	6.59 ± 0.18	6.6 ± 0.2 [€]
$124 \mathrm{In}^{l}$	I, III	3.2 ^g						7.18 ± 0.05 ^h	
$^{124}\mathrm{In}^{h}$	III	2.48						7.37 ± 0.21^{h}	
$^{126}\mathrm{In}^{l}$	II	2.1 ⁱ	3345 3345 3888	3345 ⁱ 3345 ⁱ 388 ⁱ	2.0-4.7 2.0-4.7 2.1-4.2	4.84 ± 0.19 4.98 ± 0.12 4.23 ± 0.11	$\begin{array}{c} 8.19 \pm 0.19 \\ 8.33 \pm 0.12 \\ 8.12 \pm 0.11 \end{array}$	8.21 ± 0.08	a
126 In ^h	Ш	1.55 ⁱ	1637	3856 ⁱ	1.6-4.0	4.20 ± 0.17	8.06 ± 0.17		
$128 \ln l$	Ш	0.91	4300 4300	4300 ⁱ 4300 ⁱ	1.2-4.8 2.0-4.8	4.98 ± 0.18 5.10 ± 0.34	9.28 ± 0.18 9.40 ± 0.34	9.31 ± 0.16	
$^{128}\mathrm{In}^{h}$	Î	0.91	1867	3963 ⁱ	1.9-5.4	5.43 ± 0.22	9.39 ± 0.22		•
a Reference 21 f The β spectru g Reference 24	^b R im correspon	eference 22. ding to the gate at 11 se Table III.	^c Reference 141 keV also coi ⁱ Reference	e 25. ntains a compon 15.	^d Reference 18. ent of energy 3.0 MeV	• Refe belonging to the dec	srence 23. ay of the 10 s isomer.		

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TABLE II. Results of FK analyses for even-mass indium isotopes ¹²⁰ In, ¹²² In, ¹²⁴ In, ¹²⁶ In, and ¹²⁸ In.

1. Nuclide ¹²⁰ In

The half-lives of the β -decaying isomers of ¹²⁰In have been determined to be 3.2 s for the 1⁺ state and 45 s for the (4⁺, 5⁺) and the (8⁻) states.²¹ The 3.2 s isomer decays mainly to the ground state of ¹²⁰Sn, the feeding to the 1170 keV level being about 13%.²² The lowest level fed by the (4⁺, 5⁺) isomer is that at 2195 keV. The energy difference between the two 45 s isomers is smaller than the limits of error in the present investigation.

Using method I two γ gates were chosen at 1171 and 2195 keV (the latter is a sum peak). These gates correspond to levels in ¹²⁰Sn populated in the decay of the 1⁺ isomer and the (4⁺, 5⁺) isomer, respectively. The Q_{β} values thus obtained are 5.43 ± 0.20 MeV for ¹²⁰In¹ and 5.30 ± 0.20 MeV for ¹²⁰In^h, where "l" stands for "low spin" and "h" for "high spin".

With a Ge(Li) detector in the coincidence system (method III), gates were chosen at 1171, 1186, and 1251 keV corresponding to levels at 1171, 2423, and 2358 keV, respectively. All these transitions appear in the decay of the 3.2 s isomer. The resulting Q_{β} value was found to be 5.23 ±0.22 MeV. In the decay of the high-spin isomers in ¹²⁰In only the γ gate at 965 keV, depopulating a level at 3440 keV, has been used for the determination of the total decay energy. The resulting Q_{β} value is 5.52 ± 0.40 MeV.

The average of the Q_{β} values obtained by the two different methods are ¹²⁰In^{*i*}: $Q_{\beta} = 5.30 \pm 0.17$ MeV, and ¹²⁰In^{*i*}: $Q_{\beta} = 5.34 \pm 0.17$ MeV. (See Table II.)

2. Nuclide ¹²² In

The half-lives of the three isomers in 122 In have been determined to be 1.5 s for the 1⁺ isomer and 10 s for the (4⁺, 5⁺) and (8⁻) isomers.²¹

Using method III the Q_{β} value of the low-spin isomer was determined from the β end-point energies of the spectra corresponding to γ gates at 2065, 2759, and 1114 keV, depopulating levels at 3206, 3899, and 1141 keV, respectively (cf. Table II). In the decay of the high-spin isomers γ transitions of energies 878 and 1122 keV were chosen as gates. These transitions depopulate the level at 3530 keV. The resulting Q_{β} values are ¹²²In¹: Q_{β} = 6.51 ± 0.23 MeV, and ¹²²In¹: Q_{β} = 6.59 ± 0.18 MeV, in good agreement with earlier result 6.5 ± 0.2 and 6.6 ± 0.2 MeV for the low-spin and high-spin isomers of ¹²²In, respectively.²³ The difference between the two high-spin isomers is too small to be determined with this technique.

3. Nuclide 124 In

The nuclide 124 In belongs to the following isobaric chain^{15,24}:

The half-lives have been determined by means of γ counting.²⁴

The low-spin isomer is known to decay with feeding to the levels at 2130, 3215, and 3920 keV in 124 Sn. The levels at 2571 and 3688 keV are fed in the decay of 124 In^h.

The γ transition from the 3215 keV state to the ground state gives rise to a rather strong peak in the γ spectrum in an energy region where the background is low. It is therefore well suited as a gate using method I. With the same method a γ gate was also chosen around 1132 keV, but the situation is here more complicated since double escape peaks from three lines around 2150 keV are also present.

A second experiment with method III was performed, and the results of the β end-point energies and the γ gates are collected in Table III together with results obtained with method I. The Q_{β} value of the high-spin isomer was obtained by measuring the β spectrum coincident with γ transitions from the 3688 keV level. The β spectra coincident with transitions from the level at 2571 keV had the same β end-point energies as those depopulating the 3688 keV level, indicating that the β particles mainly feed the latter level. The results are given in Table III.

The mean values of the Q_{β} determinations are ${}^{124}\text{In}^{1}Q_{\beta} = 7.18 \pm 0.05 \text{ MeV}$, and ${}^{124}\text{In}^{1}Q_{\beta} = 7.37 \pm 0.21 \text{ MeV}$.



FIG. 8. Fermi-Kurie plot of the β spectrum corresponding to the gate at 4300 keV in the decay of ¹²⁸In^I

Isomer	Method	Gate energy (keV)	Level (keV)	Range of fit (MeV)	$\frac{E_{\beta}^{\max}}{(\text{MeV})}$	Q_{β} value (MeV)
3.2 s	III	997	2130	2.4-5.0	5.10 ± 0.15	7.23 ± 0.15
	III	1315	3920	1.0-3.0	3.39 ± 0.26	7.31 ± 0.26
	III	1471	2604	1.4-3.1	3.46 ± 0.24	
	III	1572	2705	1.6-3.1	3.82 ± 0.66	
	III	2083	3215	0.6-3.6	4.01 ± 0.31	7.23 ± 0.31
	III	3215	3215	1.3-3.7	3.97 ± 0.16	7.19 ± 0.16
	I	3215	3215	1.6-3.6	3.92 ± 0.12	7.14 ± 0.12
	III	2703ª	3215	0.6-3.6	3.94 ± 0.25	7.16 ± 0.25
	Ι	2703ª	3215	2.5-3.6	3.94 ± 0.12	7.16 ± 0.12
	Ι	2192 ^b	3215	2.5-3.6	3.92 ± 0.09	7.14 ± 0.09
Mean value	:	ï				7.18 ± 0.05
2.4 s	III	244	2571	1.0-3.1	3.50 ± 0.32	
	III	364	2571	1.5-3.2	3.74 ± 0.24	
	III	1118	3688	1.2-3.2	3.66 ± 0.32	7.35 ± 0.32
	III	1361	3688	1.6-3.3	3.70 ± 0.29	7.39 ± 0.29
Mean value	:	ι.				7.37 ± 0.21

TABLE III. Summary of Q_{θ} determination for ¹²⁴ In¹ ($T_{1/2} = 3.2$ s) and ¹²⁴ In^h ($T_{1/2} = 2.4$ s).

^aSingle escape. ^bDouble escape.

4. Nuclides ¹²⁶ In and ¹²⁸ In

The half-lives of the different isomers of the nuclides ¹²⁶In and ¹²⁸In are given in Table II. The high-spin isomers were studied by setting γ gates around the 1637 keV transition depopulating the 3856 keV level in ¹²⁶In (directly or as a cascade) and around the 1867 keV transition depopulating the 3963 keV level in ¹²⁸In.²¹

In order to increase the coincidence rate for these very short-lived activities the experiments were performed with the method II. The results from the FK plots of the various β spectra are collected in Table II, and a FK plot of the β spectrum corresponding to the gate at 4300 keV in the decy of ¹²⁸In^{*i*} is shown in Fig. 8. The results for the different isomers are ¹²⁶In^{*i*}Q_β = 8.21 ± 0.08 MeV, ¹²⁶In^{*h*}Q_β = 8.06 ± 0.17 MeV, ¹²⁸In^{*i*}Q_β = 9.31 ± 0.16 MeV, and ¹²⁸In^{*h*}Q_β = 9.39 ± 0.22 MeV.

IV. DISCUSSION

A. Q_{β} values

In the following, the Q_{β} values for the ground states of the odd-mass indium isotopes will be discussed. The results for the even-mass isotopes are not accurate enough to establish the relative position of the isomers. The low-spin isomers of even-mass isotopes are fed in the decay of evenmass cadmium isotopes and, consequently, their mass excesses should be used when determining the mass excesses for cadmium isotopes by the indirect $Q_{\rm B}$ method.

As predicted Q_{β} values are often used in calculations of log ft values, β strength functions, delayed neutrons, the r process of nucleosynthesis, etc., it is interesting to compare the experimental results with predicted values. In the comparison with predictions from mass formulas, three different types of formulas are chosen, namely, the droplet models of Myers,^{26(a)} Groote, Hilf, and Takahashi,^{26(b)} and Seeger and Howard,^{26(c)} the semiempirical shell model of Liran and Zeldes,^{26(d)} and the empirical mass relations of Comay and Kelson,^{26(e)} Jänecke *et al.*,^{26(f)} and Garvey et al.²⁷ The experimental values and the corresponding deviation in the predictions are compiled in Table IV. The mean experimental error for the complete series ¹²⁰⁻¹²⁹In is 0.11 MeV, and the root-mean-square deviations for the mass formulas used in the comparison vary between 0.18 and 0.77 MeV (see Table IV). The droplet model predictions are less accurate then the others for these nuclides. It should be remembered, however, that they use fewer coefficients than the other formulas.

B. Masses

The mass excesses of $^{120-126}$ Sn and $^{127-129}$ Sn are known from Refs. 9 and 28, respectively. By adding the Q_{β} values from Table IV to these mass ex-

2	0 value	•		MeV)				
Nuclide	(MeV)	а	b	с	d	e	f	g
¹²⁰ In ^{<i>i</i>}	5.30 ± 0.17	0.61	0.95	0.47	-0.04	0.06	-0.07	-0.11
¹²¹ In ^g	3.41 ± 0.05	0.24	0.36	0.58	-0.21	0.15	0.02	-0.13
122 In^{l}	6.51 ± 0.23	0.84	1.13	0.60	0.36	0.31	0.16	-0.04
¹²³ In ^g	4.44 ± 0.06	0.33	0.38	0.41	-0.16	0.20	0.07	0.06
124 In ^{<i>l</i>}	7.18 ± 0.05	0.61	0.83	0.29	-0.04	0.12	-0.01	-0.17
¹²⁵ In ^g	5.48 ± 0.08	0.44	0.43	0.35	-0.01	0.24	0.20	0.01
¹²⁶ In ¹	8.21 ± 0.08	0.75	0.90	0.24	0.30	0.25	0.25	0.05
¹²⁷ In ^g	6.49 ± 0.07	0.56	0.48	0.24	0.20	0.27	0.32	0.12
128 In ^{<i>l</i>}	9.31 ± 0.16	0.98	1.06	0.44	0.60	0.58	0.59	0.39
¹²⁹ In ^g	7.60 ± 0.12	0.80	0.65	0.40	0.62	0.64	0.60	0.29
Root-mean-	square deviation	0.65	0.77	0.42	0.33	0.33	0.31	0.18
^a Reference	e 26(a). ^b Re	eference 26	ó(b).	cRefere	ence 26(c).	d F	Reference 2	6(d).

TABLE IV. Summary of Q_{β} values obtained in the present work and comparison with different mass formulas preductions.

^eReference 26(e). ^fReference 26(f).

^gReference 27.

cesses, the mass of $^{120-129}$ In were deduced. The resulting masses are compared to mass predic $tions^{26(a)-26(f),27}$ in Table V.

The mean experimental error for the indium isotopes studied are 0.11 MeV, and the predictions deviate, on average, by 0.21 to 1.36 MeV.

The formulas of Liran and Zeldes, Comay and Kelson, and Garvey et al. give, in general, predictions with acceptable precision. Among the droplet model formulas, the Seeger-Howard one reproduces the experimental masses well. Before drawing any conclusions about which droplet

TABLE V. Summary of experimental mass excesses obtained for ¹²⁰⁻¹²⁹In and comparisons with different mass formulas predictions.

	Mass avcass			M _e	$x_{p} - M_{pred}$ (MeV)					
Nuclide	(MeV)	а	b	с	d	e	f	g			
¹²⁰ In	-85.80 ± 0.17	1.36	1.35	-0.50	- 0.01	0.18	-0.08	-0.10			
¹²¹ In	-85.79 ± 0.05	. 1.36	1.30	0.60	0.04	0.28	-0.01	-0.17			
¹²² In	-83.44 ± 0.23	1.20	1.10	1.04	0.22	0.03	0.15	-0.55			
¹²³ In	-83.38 ± 0.06	1.44 .	1.26	0.22	0.04	0.41	0.09	-0.02			
¹²⁴ In	-81.06 ± 0.05	1.45	1.20	0.04	-0.02	0.25	-0.04	-0.15			
¹²⁵ In	-80.42 ± 0.08	1.46	1.08	0.08	0.12	0.38	0.21	0.05			
¹²⁶ In	-77.81 ± 0.09	1.18	0.69	-0.61	-0.15	-0.04	0.31	-0.21			
¹²⁷ In	-77.02 ± 0.07	1.34	0.69	-0.32	0.19	0.11	0.37	0.14			
¹²⁸ In	-74.00 ± 0.17	1.49	0.70	-0.30	0.42	0.24	0.66	0.33			
¹²⁹ In	-73.03 ± 0.17	1.25	0.26	-0.53	0.37	0.05	0.64	0.16			
Root-mean	-square deviation	1.36	1.02	0.39	0.21	0.24	0.34	0.24			
^a Reference	26(a). ^b Referen	ce 26(b).	^c Refer	ence 26(c)		^d Refer	ence 26(d).	•			

^eReference 26(e). ^fReference 26(f). ^gReference 27.

Precursor	Q_{β} (MeV)	Emitter	Mass excess (MeV)	B _n (MeV)	Neutron window $Q_{\beta} - B_n$ (MeV)
		¹²³ Sn	-87.82 ± 0.004^{a}		
¹²⁴ In	7.18 ± 0.05	¹²⁴ Sn	-88.24 ± 0.01^{a}	8.49 ± 0.01	-1.31 ± 0.05
¹²⁵ In	5.48 ± 0.08	¹²⁵ Sn	-85.90 ± 0.01^{a}	5.73 ± 0.01	-0.25 ± 0.08
¹²⁶ In	8.21 ± 0.08	¹²⁶ Sn	-86.02 ± 0.01^{a}	8.19 ± 0.01	0.02 ± 0.08
¹²⁷ In	6.49 ± 0.07	¹²⁷ Sn	-83.50 ± 0.03^{b}	5.55 ± 0.03	0.94 ± 0.07
¹²⁸ In	9.31 ± 0.16	¹²⁸ Sn	-83.31 ± 0.06^{b}	7.87 ± 0.06	1.44 ± 0.13
¹²⁹ In	7.60 ± 0.12	¹²⁹ Sn	-80.63 ± 0.12 ^b	5.39 ± 0.13	2.21 ± 0.17

TABLE VI. Values of the "neutron window" deduced from experimental mass data.

^aReference 9. ^bReference 28.

formula is to be used far away from stability, we recapitulate the results²⁸ from mass determinations of neutron-rich tin, antimony, and tellurium isotopes. For these isotopes Myers gives the best predictions (mean deviation 0.32 MeV) while Seeger and Howard and Groote et al., on the average, predict the masses to be 1.0 and 0.87 MeV. less bound than found experimentally. Apparently, the estimates using the formula of Groote et al. are less precise both for isotopes with Z < 50 and $Z \ge 50$. Myers' predictions are very good for the region $Z \ge 50$, but the failure in the predictions for $^{120-129}$ In is grave. This leads us to conclude that, as for neutron-rich zinc, gallium, germanium, and arsenic isotopes,²⁹ the best droplet mass formula for extrapolations far away from stability in the region studied seems to be the one of Seeger and Howard.

C. Predictions about delayed-neutron precursors

In general, predictions concerning the occurrence of delayed-neutron emission are based on mass formula estimates because experimental neutron binding energies are scarce in regions far from stability, and experimental $Q_{\rm B}$ values

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are often lacking. The present investigation makes the situation favorable for predictions about delayed-neutron precursors among the indium isotopes based on experimental mass data.

These data have been used to calculate the neutron window $|Q_{\beta} - B_n|$ for $^{124-129}$ In. The results are collected in Table VI. From this table it is seen that 124 In and 125 In cannot be delayed-neutron precursors, and that 126 In is a doubtful case. In an investigation at this laboratory no delayed neutrons were found at these mass numbers.¹⁹ On the other hand, 127 In, 128 In and 129 In were shown to be neutron precursors in agreement with the positive neutron windows found for those cases.

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