Spectroscopy of ¹⁴⁰Ce and ¹³⁸Ce via the ¹⁴⁰Ce(p, p'), ¹⁴²Ce(p, t), and ¹⁴⁰Ce(p, t) reactions at $E_p = 30$ MeV*

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The nuclei ^{138,140}Ce have been studied by means of the ¹⁴⁰Ce(p, t), ¹⁴²Ce(p, t), and ¹⁴⁰Ce(p, p') reactions at 30 MeV. Angular distributions have been measured from $\theta_{lab} = 16^{\circ}$ to 64° . The inelastic scattering data were analyzed with distorted-wave Born approximation to confirm multipolarities and extract deformation parameters for the strongly excited levels. The (p, t) data were also analyzed with distorted-wave Born approximation to obtain limits on the two-nucleon orbital angular momentum (L) transfer. This analysis, plus the empirical angular distribution shapes of levels with known J^{π} , permits us to suggest (or at least limit) J^{π} values for many new levels. The (p, t) differential cross sections have been further analyzed in terms of simple two-neutron configurations through the enhancement factor concept. The two-neutron transfer results are discussed in terms of the pair vibration model.

NUCLEAR REACTIONS ^{142,140}Ce(p, t), ¹⁴⁰Ce(p, p'), $E_p = 30$ MeV; measured level energies and $\sigma(\theta)$; DWBA analysis, deformation parameters, enhancement factors.

I. INTRODUCTION

Previous investigations¹⁻³ of the (p, t) reaction on the Ce isotopes have been directed mainly toward investigating the usefulness of a pairing vibrational model interpretation⁴ at the N = 82 closed shell. Consequently, a detailed analysis of the spectroscopic information available from the (p, t)reaction on ¹⁴²Ce and ¹⁴⁰Ce targets has not been given up to now. The combination of high beam energy, good energy resolution, and reasonably characteristic angular distributions which hold for the present (p, t) experiments makes such an analysis possible. The ¹⁴⁰Ce(p, p') experiment, done simultaneously with the ¹⁴⁰Ce(p, t) reaction, is also reported here. This reaction is of interest to compare with the isoscalar⁵ excitation of collective levels in ¹⁴⁰Ce as well as comparing with other inelastic proton scattering measurements on N= 82 nuclei.^{6,7} A report on part of the data discussed here is given in Ref. 2.

II. EXPERIMENT

A. Targets

Self-supporting 1.9 cm diam targets of 142 Ce (0.40 mg/cm², 90% enriched) and 140 Ce (0.79 mg/cm², 99.5% enriched) were used in these experiments. All handling of the Ce targets was done in an Ar atmosphere and the targets were kept in vacuum for long term storage. Details of the target preparation may be found in Ref. 8.

B. Experimental procedure

The experiments were carried out with a 30.3 MeV proton beam obtained from the Lawrence Berkeley Laboratory 88-inch cyclotron high resolution beam line.⁹ The data were measured in a 91 cm diam scattering chamber by means of a pair of two-counter telescopes. For the $^{142}Ce + p$ experiment, 250 μ m ΔE Si(P) and 3 mm E Si(Li) detectors were used, while for $^{140}Ce + p$ experiments, 5 mm Si(Li) counters were used. Cooling of the detectors to -25° C was accomplished by means of thermoelectric coolers. The $\Delta E - E$ signals fed a Goulding-Landis¹⁰ particle identifier which produced good separation of the charge one reaction products. A split Faraday cup, mounted approximately 1.5 m from the target position, monitored the directional stability of the beam as well as providing charge integration. Target thickness monitoring was accomplished by a fixedangle detector mounted in the scattering chamber.

Figures 1 and 2 show triton spectra from the $^{142}Ce(p, t)$ and $^{140}Ce(p, t)$ reactions, respectively. The energy resolution in the ^{142}Ce experiment was 30 keV (full width at half maximum) while in the ^{140}Ce experiment it was about 55 keV. Triton and proton angular distributions (Figs. 3–6) were measured between 16° and 64° (lab).

C. Data calibration

1. $^{140}Ce(p,p')$

The ¹⁴⁰Ce(p, p') spectra were calibrated on the basis of known ¹⁴⁰Ce excitation energies^{11,12} as

15

903



FIG. 1. Representative ${}^{142}Ce(p,t){}^{140}Ce$ triton spectrum. The ${}^{17}F$ peaks were used as calibration points.

well as several proton groups arising from light target impurities. The results are given in Table I, where they are compared with the $^{140}Ce(\alpha, \alpha')$ experiment.⁵ The proton energy resolution limited analysis to the strongly excited states in ^{140}Ce .

2. $^{142}Ce(p,t)$

These spectra were calibrated using γ -decay results^{11,12} as well as two impurity peaks from the ¹⁹F(p, t)¹⁷F reaction (see Fig. 1). The calibration covered the full range of excitations observed in the ¹⁴²Ce(p, t)¹⁴⁰Ce reaction, and extrapolations

were not necessary. The ${}^{142}Ce(p, t)$ spectra yielded a total of 45 levels in ${}^{140}Ce$. These are listed in Table II, where they are compared with previous results for the ${}^{140}Ce$ level structure.

3. $^{140}Ce(p,t)$

The energy calibration of the ¹³⁸Ce data relied on accurate excitation energies derived from γ decay studies.¹³ The average excitation energies of the 21 observed levels are listed in Table III, along with results from earlier work. The 10% ¹⁴⁰Ce impurity in the ¹⁴²Ce target allowed the





FIG. 3. Angular distributions from the ${}^{140}Ce(p,p')$ reaction. The solid curves are DWBA calculations, while the dashed curves are empirical (p,p') angular distribution shapes taken from the literature.

 140 Ce(p, t) Q value to be measured relative to that for the 142 Ce(p, t) reaction. The result we obtained was -8.167 ± 0.020 MeV, in good agreement with previous values.^{3,14}

D. Normalization

Absolute cross sections from the ¹⁴⁰Ce target were obtained by two methods. The first method involved a direct weighing of the target along with accurate measurement of the detector solid angles. The second method involved normalizing the measured elastic scattering angular distribution to optical model predictions. The optical parameters chosen



FIG. 4. Angular distributions from the ${}^{142}Ce(\phi, t){}^{140}Ce$ experiment for levels below 4.183 MeV. The solid and dashed curves are DWBA predictions, unless otherwise noted. Except for the L=0 transitions, the angular distributions could usually be reasonably fitted by more than one L transfer. See text for discussion.

were obtained from a global analysis¹⁵ of proton elastic scattering and are given as Set P1 in Table IV. These two methods agreed to 5%. Since no elastic proton data were taken on the ¹⁴²Ce target, this normalization was obtained only from the target weight.



FIG. 5. Angular distributions from the ${}^{142}Ce(p,t){}^{140}Ce$ experiment for levels above 4.242 MeV. See caption to Fig. 4.

Dead time corrections were made with pulser signals triggered by the monitor detector; the monitor was also used to normalize the data from angle to angle. The absolute cross sections displayed in Figs. 3-6 are estimated to have an uncertainty of $\pm 10\%$.



FIG. 6. Angular distributions extracted from the $^{140}{\rm Ce}(p,t)^{138}{\rm Ce}$ experiment. See caption to Fig. 4.

III. ANALYSIS AND DISCUSSION

A. ${}^{140}Ce(p,p')$

The proton inelastic scattering results are given in Table I and Fig. 3. Good agreement with excitation energies and J^{π} assignments was found with the ¹⁴⁰Ce(α, α') work.⁵ We did not observe the 2.35 and 3.04 MeV levels reported there; it is likely that the better resolution (35 keV) of the (α, α') experiment allowed identification of these

		¹⁴⁰ Ce(<i>p</i> , <i>f</i>	oʻ)	¹⁴⁰ Ce(α, α') ^a				
E_x^{b} (MeV)	J^{π}	δ_L^{c} (fm)	G _{IS} u (single-particle units)	E_x (MeV)	J [#]	δ _L (fm)	G _{IS} " (single-particle units)	
1.589	2 *	0.41	5.8	1.597	2*	0.46	7.4	
2.094	4*	0.43	6.9	2.09	4 *	0.42	6.8	
				2.35	(2 *)	0.08	0.22	
2.469	3-	0.79	22.1	2.464	3-	0.67	15.8	
2.902	2 +	0.15	0.76	2.90	2*	0.13	0.55	
				3.04	3-	0.15	0.80	
3.130	2*	0.26	2.3	3.12	2 *	0.22	1.7	
3.264	5-	0.12	0.58	3.25	5-	0.30	3.6	
				3.34	4 *	0.24	2.2	
				3.54	(4)*	0.21	1.7	
				3.98	3-	0.21	1.56	

TABLE I. Comparison of ¹⁴⁰Ce collective levels seen in (p, p') and (α, α') .

^aSee Ref. 5.

 b All excitation energies ±0.01 MeV.

 $^{c}\delta_{L} = \beta_{L}R_{R}, R_{R} = 1.17A^{1/3}.$

^dIsoscalar transition rate in single-particle units assuming a sharp edge mass distribution.

weakly excited levels.

In previous studies^{6,7} of inelastic scattering of 30 MeV protons from ¹³⁸Ba and ¹⁴⁴Sm (also N=82), it was found that the angular distribution shapes are characteristic of the orbital angular momentum transfer (*L*). Since these are $J^{\pi} = 0^{+}$ targets, spin-parity values could then be obtained through use of the natural-parity selection rules, $J_f = L$ and $\pi_f = (-1)^L$, where J_f and π_f are the spin and parity of the excited state. These empirical angular distribution shapes are shown as dashed lines in Fig. 3 for levels with $J^{\pi} = 2^{+}$, 3⁻, and 4⁺. Good agreement between the shapes determined in Refs. 6 and 7 and our ¹⁴⁰Ce(p, p') data is found for the L=2 and L=3 transitions, while the L=4 shape is qualitatively similar.

The ¹⁴⁰Ce(p, p') angular distributions were analyzed using a collective model form factor¹⁶ in a distorted-wave Born approximation (DWBA) calculation. In this theory, the optical model analysis of the proton elastic scattering determines all parameters except the deformation parameter β_L which normalizes the distorted-wave predictions $[\sigma_{DW}(\theta)]$ to the experimental differential cross sections $[\sigma_{exp}(\theta)]$ by the relation

$$\sigma_{\rm exp}(\theta) = \beta_L^2 \sigma_{\rm DW}(\theta) \,. \tag{1}$$

The $\sigma_{DW}(\theta)$ were calculated using the code DWUCK74.¹⁷ Detailed formulas for evaluation of $\sigma_{DW}(\theta)$ have been given in the literature.^{5, 16-18}

The solid curves shown in Fig. 3 are DWBA predictions using proton optical model parameters taken from the literature¹⁵ (and listed as Set P1 in Table IV). The form factor included a Coulomb excitation contribution¹⁶ as well as real and imaginary nuclear terms. This last term has improved theoretical comparisons with experiments involving inelastic scattering of protons (Ref. 19), ³He, (Ref. 20) and ⁴He (Ref. 21) particles. Inclusion of the imaginary term also affected the β_L values extracted from the data¹⁹⁻²¹; in particular, the β_3 for the 2.469 MeV level and the β_2 for the 2.902 MeV state were decreased by about 30% compared with the values obtained from the analysis using only a real form factor. Excluding the Coulomb excitation term caused the first maximum of the L = 2 angular distribution to shift (by 3°) to smaller angles without significantly changing the magnitude, while the L = 3 prediction was hardly influenced.

The DWBA normalizations to experiment are given in Table I in terms of the deformation lengths²² $\delta_L = \beta_L R_R$, where $R_R = 1.17 A^{1/3}$. The isoscalar transition rates in single particle units were calculated from

$$G_{\rm IS}(L, 0 - L) = \frac{Z^2}{4\pi} \frac{(L+3)^2}{(2L+1)} \left(\frac{\beta_L R_R}{R_u}\right)^2, \qquad (2)$$

where $R_u = 1.2 A^{1/3}$ is the uniform mass radius.²³ These isoscalar transition rates are compared with the ¹⁴⁰Ce(α, α') results in Table I. Good agreement between the two experiments is found for the 2⁺ and 4⁺ states. The odd parity levels (2.469 MeV 3⁻ and 3.264 MeV 5⁻) are not in such good agreement, although the δ_3 values extracted for the 2.469 MeV level from the two experiments are consistent within errors. The 3⁻ isoscalar transition strength derived from (p, p') is 40%

			$^{142}Ce(p)$ $E_{p}=21.5$ Ref. 3	, <i>t</i>) MeV 3	Decay data ^a				
Level No.	E_x^b (MeV)	L	Suggested J^{π}	¢°	E_x (MeV)	L	E_x (MeV)	J "	
1	0.0	0	0*	19.3 [3.4]	0.0	0	0.0	0*	
2	1.595	2	2*	2.3 [0.50]	1.600	2	1.5966	2*	
3	1.905	0	0*	2.1	1.906	0	1.9035	0*	
4	2.080	4	4*	0.28			2.0836	4*	
	2.107						2.1082	(6)*	
							2.3484	2*	
							2.3502	(5)-	
-	0 454				0.400		2.4124	3.	
5	2.471				2.468		2.4644	3 (4)+	
6	2 510	9.4	9- 1+	21022			2.4813	(4) (4+ 9+ 9=)	
0	2.019	3,4	0,4	2.1, 0.22			2.5101	(4,3,3)	
							2.5210	(1 2)+	
7	2 912	2	2*	0.46			2.0470	(1, 2) $(1, 2)^{+}$	
8	3 026	0	0 +	1.1	3 020		2.0001	(1,2)	
0	0.010	Ū	v	111	0:020		3,1183	(1, 2)*	
9	3.134	2, 3, 4					011100	(1,2)	
10	3.233	0	0*	13.8	3.223	0			
11	3.334						3.3197	$(1, 2)^{+}$	
12	3.426								
13	3.558	2,3	2*, 3 ⁻	1.7,10.3	3.540				
14	3.664	2,3	2*, 3-	1.3, 8.7	3.654	2			
					3.709				
15	3.731	2,3	2 *, 3 -	13.3,68.8	$3.731 \\ 3.744$	2			
16	3.801	2,3	2*, 3-	1.6, 10.6					
17	3.911	4,5	4*, 5*	0.41, 0.82					
18	3.985	2,3	2*, 3 -	1.7,10.1	3.965	2			
19	4.017								
20	4.125	2,3	2*, 3-	1.1,7.8	4.123	2			
21	4.183	2, (3, 4)	2*, (3 ⁻ , 4*)	1.3	4.188	2			
22	4.242	1,2	1-,2+	4.6, 1.8	4.242				
23	4.296	3,4	3-,4+	12.4, 1.2	4.301				
24	4.360								
25	4.431	2,3	2,3-	1.1,7.8	4.429				
26	4.534	2,3	2', 3-	1.2, 8.7					
21	4.700	0 0	0+ 0=	10 6 69 9	4 994	9			
28	4.027	2,0	2,3 2+ 2-	16 29 4	4.031	2			
30	5.101	$L \ge 5$	2,0	1.0, 20.1					
31	5.157	1 - 0							
32	5,229	2, 3, 4	2 ⁺ , 3 ⁻ , 4 ⁺						
33	5.295	5,6	5-,6+	5.0, 2.1					
34	5.377	4,5	4*, 5-	2.3, 5.5					
35	5.449								
36	$5.574 \pm 15 \text{ keV}$	(0)	(0*)	(2.3)					
37	5.650	2,3	2 * , 3 -	1.7,11.0					
38	5.703	1,2	1-,2*	6.0, 2.1					
39	5.789	2, 3, 4							
40	5.896	1,2	1-,2*	6.9, 2.3					
41	5.989	(3,4)	(3 ⁻ , 4 ⁺)	(15.1, 1.5)					
42	6.078	2,3	2',3-	3.0,21.1					
43	0.107 6.268	2,3 3 / F	2,3	2.1,13.8					
44	6 364	3,4,0 3 1	9 - /+	18 3 9 1					
40	0.004	J, ±	J , T	10.0, 2.1					

TABLE II. Summary of the ${}^{142}Ce(p,t)$ results.

^aSee Refs. 11, 12, and 42. ^bRelative excitation energies ± 10 keV below level 36, ± 15 keV above level 36. ^c Values in square brackets were obtained using the $(2d_{3/2})^2$ form factor, all others assumed a $(1h_{11/2})^2$ configuration. See text.

greater than that from (α, α') and is nearly the same as the electromagnetic transition rate.²⁴

B. 142,140 Ce $(p,t)^{140,138}$ Ce

1. DWBA analysis

Triton angular distributions from (p, t) reactions are known to reflect the total orbital angular momentum (L) of the two picked-up neutrons.²⁵ The zero-range single step DWBA treatment²⁶⁻²⁸ of two-nucleon transfer reactions is generally successful at providing a reasonable description of angular distribution shapes for vibrational muclei,²⁹ although for permanently deformed nuclei calculations including inelastic processes are different in shape from DWBA predictions.³⁰ Further, finite-range DWBA^{31,32} does not seem to differ from the zero-range DWBA as regards angular distribution shape. Thus, by using zerorange DWBA angular distribution predictions as a guide to assigning *L* transfers, along with the natural-parity selection rules for a $J^{\pi} = 0^{+}$ target, J^{π} values or at least J^{π} limits can be assigned to many of the levels observed in the ¹⁴²Ce(p, t) and ¹⁴⁰Ce(p, t) reactions. Wherever possible, empirical angular distributions are also used as a supplemental aid in assigning multipolarities to states with unknown J^{π} .

A comprehensive discussion of parameters that are required for a zero-range DWBA calculation of the |(p, t) reaction has been given.²⁵ In that work the DWBA predictions were not very sensitive to the choice of optical model and form factor parameters, although significant changes in

		¹⁴⁰ Ce(<i>p</i> , <i>t</i>	138 Ce $E_p = 30$ M	/IeV		
Level	E., ^b	r	This work Suggested		Decay e	data ^a
No.	(MeV)	L	J^{π}	€ ^c	(MeV)	J "
1	0.0	0	0+	19 3 [3 7]	0.0	0*
$\frac{1}{2}$	0.788	2	0 2*	18.3 [4.6]	0.7888	2*
					1.4770	0*
3	1.501	2	2*	3.0	1.5109	(2*)
4	1.822	4	4*	5.7	1.8264	4 *
5	2.130	7	7-	4.6	2.1291	7-
6	2.219	5,6	5 - , 6+	20.6,6.4	2.2173	5,6
					2.2368	
7	2.336	0	0*	2.7	2.3403	
8	2.389	(2,3)	(2*, 3-)	(1.3, 8.7)		
9	2.440	4,5	4 * , 5 *	1.3, 3.7		
10	2.640	2,3	2 *, 3 -	3.9,32.1		
11	2.719	4,5	4 * , 5 -	0.92, 2.6		
					2.765	
12	2.885	2,3	2 *, 3 -	3.9, 27.5		
13	2.942	4,5	4 * , 5 -	4.1,11.5		
14	3.005	4,5	4 * , 5 -	3.1, 9.2		
15	3,082	4,5	4 * , 5 -	0.78,2.1		
16	3.220	2,3	2*, 3 -	3.4, 28.9		
17	3.277	(3)	(3~)	21.6		
18	3.356	2,3	2*, 3 -	3.7,27.5		
19	3.429	4,5	4 * , 5 *	1.2,3.9		
20	3.531	(-)	()			
21	3.646	(7)	(7~)	1.8		

^aSee Refs. 13, 45, and 46.

 $^{b}Relative$ excitation energies $\pm 10~\rm keV$ below level 7, $\pm 16~\rm keV$ above level 7.

^cValues in square brackets were obtained using the $(2d_{3/2})^2$ form factor, all others assumed a $(1h_{11/2})^2$ configuration. See text.

	V_R^a (MeV)	<i>r</i> _R (fm)	<i>a_R</i> (fm)	W_V^{a} (MeV)	$W_{\rm SF}{}^{a}$ (MeV)	<i>r_I</i> (fm)	<i>aI</i> (fm)	V _{so} (MeV)	$r_{ m so}$ (fm)	$a_{ m so}$ (fm)	<i>r_c</i> (fm)	Spin orbit unit
P1 ^b	$\begin{pmatrix} 54.0 - 0.32E_{p} \\ +0.4Z/A^{1/3} \\ +24.0(N-Z)/A \end{pmatrix}$	1.17	0.75	$0.22E_{p} - 2.7$	$ \begin{cases} 11.8 - 0.25E_{p} \\ +12.0(N-Z)/A \end{cases} $	1.32	0.63	6.2	1.01	0.75	1.21	
T1 ^c	166.7	1.16	0.752	16.4	• • •	1.498	0.817				1.21	
T2 ^d	$138.8 - 0.157E_t$	1.10	0.853	•••	$ \left\{ \begin{matrix} 37.4 - 0.52E_t \\ +0.0037(E_t)^2 \end{matrix} \right\} $	1.308	0.751				1.25	
T3°.	$ \left\{ \begin{array}{c} 165.0 - 0.17E_t \\ -6.4(N-Z)/A \end{array} \right\} $	1.20	0.72	$ \begin{cases} 46.0 - 0.33E_t \\ -110(N-Z)/A \end{cases} $	•	1.40	0.84				1.30	
Bound state	l f	1.27	0.67									32.0

TABLE IV. Optical model potentials and bound state parameters used in the DWBA calculations. The form of the potentials and notation is that of Ref. 15.

^aThe energy dependent potentials are evaluated at the appropriate laboratory energy.

^dSee Ref. 25.

^eSee Ref. 40.

^f The single-particle bound state potential depth is determined by binding each neutron at half the two-neutron separation energy.

the angular distribution shapes were noted when configuration-mixed wave functions caused destructive interference at the nuclear surface. Since our conclusions concerning parameter sensitivity were not appreciably different from those of Ref. 25, we will not discuss this point in detail here.

Straightforward assumptions about the required parameters resulted in favorable comparisons between the calculations and experimental results for levels in ¹⁴⁰Ce and ¹³⁸Ce for which final J^{π} values are known. The proton¹⁵ (P1) and triton³³ (T1) optical model parameters of Table IV were used. Form factors were constructed for 0⁺ and 2⁺ levels ultilizing the $(1h_{11/2})^2$ and $(2d_{3/2})^2$ single particle wave functions according to Ref. 27. The bound state geometry is included in Table IV.

The results for the two form factors are shown for the ¹⁴⁰Ce ground (0⁺) and 1.595 MeV (2⁺) levels in Fig. 4. The solid curve used the $(1h_{11/2})^2$ form factor, and the dashed curve corresponds to the $(2d_{3/2})^2$ form factor. Similar calculations are shown for the ¹⁴⁰Ce(p, t) reaction leading to the ¹³⁸Ce ground (0⁺) and 0.788 MeV (2⁺) levels in Fig. 6. Both form factors give good agreement for the angular distribution shape in each case. Discussion of the DWBA normalizations for each of these two form factors is given in the next section.

The effect of varying Q values has sizable influence on the shape of the DWBA predictions. Figure 7 illustrates this Q-value effect for the L=2, 3, and 4 transitions; a shift of the first

maximum to larger angles as the Q value becomes more negative is seen. Such a shift for the L = 4case is experimentally observed in the (p, t) transitions to the 140 Ce (2.080 MeV) and 138 Ce (1.822 MeV) states, whose Q values are -6.2 and -10.0MeV, respectively. However, detailed empirical comparisons of experimental angular distributions directed towards examining Q effects are difficult, and the DWBA must be relied upon to describe this effect for the L = 3 and L = 4 transitions. Higher L transfers, such as the 7⁻ level at 2.130 MeV in ¹³⁸Ce, are not accurately described by DWBA calculations at forward angles. It is thus difficult to make restrictive assignments for levels whose angular distributions are characteristic of $L \ge 6$. Figure 7 also shows that, for a given Q value, adjacent L values are similar at c.m. angles beyond about 16°.

2. Enhancement factors

A method of obtaining spectroscopic information from absolute two-nucleon transfer cross sections by analyzing with zero-range DWBA is possible by using the empirical normalization (N) of Flynn and Hansen³⁴ with the enhancement factor³⁵ (ϵ) defined by

$$\sigma_{\rm exp}(\theta) = N \epsilon \sigma_{\rm DW}(\theta) \,. \tag{3}$$

We used the value N = 218 obtained from Ref. 34; this is consistent with the (p, t) work on the titanium,²⁵ and zirconium³⁶ isotopes. However, several (t, p) works^{34, 37} have shown that the nor-

^bSee Ref. 15.

^cSee Ref. 33.



FIG. 7. DWBA calculations for the ${}^{142}\text{Ce}(p,t){}^{140}\text{Ce}$ reaction as a function of Q value for L=2, 3, and 4 transitions. This figure emphasizes the usefulness of forward angle data ($\theta < 16^{\circ}$) in assigning L values by comparing experimental results with DWBA predictions.

malization N depends strongly on the choice of parameters used in the DWBA calculation, so our choice of N = 218 requires that our parameters be chosen in a manner consistent with the prescription given in Ref. 34.

Since the magnitude of $\sigma_{\rm DW}(\theta)$ is sensitive to the two-neutron wave function,²⁶ one may expect ϵ to vary substantially with the choice of configuration. This is illustrated by comparing the values of ϵ extracted from the ground and first excited states in ¹³⁸Ce and ¹⁴⁰Ce assuming a $(1h_{11/2})^2$ or a $(2d_{3/2})^2$ configuration. For N = 218, the results are listed in Tables II and III with the $\epsilon[(1h_{11/2})^2]$ given first, followed by the $\epsilon[(2d_{3/2})^2]$ given in square brackets. For both ¹⁴⁰Ce and ¹³⁸Ce, the $\epsilon[(1h_{11/2})^2]$ values are considerably larger than those found with the $(2d_{3/2})^2$ configuration.

3. Energy dependence

The ¹⁴²Ce(p, t)¹⁴⁰Ce ground state (L = 0) and 3.73 MeV (L = 2) angular distributions have now been

studied at 21.5 MeV (Ref. 3), 30.3 MeV, and 52.1 MeV (Ref. 1). These data therefore offer an opportunity to check the adequacy of zero-range DWBA in describing the energy dependence of two-nucleon transfer reactions. Other investiga-tions of this topic have been made previously.^{25, 38, 39}

The L = 0 and L = 2(p, t) angular distributions from the present work and those from Refs. 1 and 3 were analyzed by forming the ratio R = $= \sigma_{exp}(\theta) / \sigma_{DW}(\theta)$. The calculations used the $(1h_{11/2})^2$ bound state form factor described previously. Three sets of triton optical model potentials, listed in Table IV, were tested in conjunction with proton set P1. The results of the calculations are given in Table V. A change of approximately 16:4:1 occurs for the 142 Ce(p, t)¹⁴⁰Ce(0.0) L = 0 transition as the beam energy is changed from 21.5 to 52.1 MeV. The R values for the L = 2 transition at 3.73 MeV over the same energy range change from 6:2.5:1. These ratios, with the exception of set P1-T2 for the 52.1 MeV data, are reasonably independent of the optical model parameters.

This energy dependence may be related to momentum mismatch in the (p, t) reaction³⁹ which may not be properly described by the zero-range DWBA. At 21.5, 30.3, and 52.1 MeV the proton and triton grazing partial waves (where $\eta_i = 0.5$) for the L = 2 transition differ by 2, 5, and 9, respectively. These values are one unit greater for the transition to the ¹⁴⁰Ce ground state. Thus, good angular momentum matching is not obtained in either case for this range of incident proton energies.

4. Spectroscopic results from $^{142}Ce(p,t)^{140}Ce$

The triton differential cross sections from the 142 Ce(p, t) reaction have been systematically analyzed with the zero-range DWBA theory in order to derive L transfers, suggest J^{π} assignments,

TABLE V. Energy dependence of DWBA calculations.

Optical potential set ^a	$R_{21.5}^{b}$ ¹⁴⁰ Ce (0.0 M	$R_{30.3}^{b}$ (IeV); $L = 0$	R _{52.1} ^b						
P1-T1	13	4.1	0.96						
P1 - T2	19	2.6	0.22						
P1 - T3	16	4.5	0.70						
¹⁴⁰ Ce (3.73 MeV); $L = 2$									
P1-T1	5.5	2.8	1.2						
P1-T2	9.0	2.4	0.3						
P1-T3	6.8	2.8	1.0						

^aSee Table IV.

 ${}^{b}R_{E_{p}} = \sigma_{exp} / \sigma_{DW}$. All entries have been multiplied by 10⁻³. See text.

and extract enhancement factors. Form factors for positive and negative parity transitions were constructed assuming the $(1h_{11/2})^2$ and $(1h_{11/2}1g_{7/2})$ configurations, respectively, with the exception of the L = 1 transfers, for which the $(1h_{9/2}1g_{7/2})$ configuration was assumed. The $1h_{11/2}$ and $1g_{7/2}$ neutron hole states have been observed with large spectroscopic factors in the $^{140}Ce(p,d)$ reaction.⁴¹

While it is sometimes impossible to make unambiguous L assignments to experimental data based on DWBA angular distribution shapes, L = 0transitions are virtually always identifiable. Figure 7 shows that forward angle data (not obtained here) would be most valuable for L assignments. Wherever ambiguities arise, DWBA predictions for both of the possible L transfers are shown in Figs. 4 and 5 with the derived enhancement factors given in Table II. The DWBA calculations used the P1 and T1 optical model potentials and bound state parameters of Table IV and the zero-range normalization N = 218.

The ¹⁴⁰Ce results naturally separate into low excitation (\leq 3.5 MeV) and high excitation (\geq 3.5 MeV) regions. In the former region considerable information exists from decay data,^{11,12,42} inelastic scattering,⁵ and proton transfer work.⁴³ Above 3.5 MeV excitation, most energy level information is derived from two-neutron transfer results and those from the 139 La(³He. d) reaction.⁴³ While the 142 Ce(p, t) data at 21.5 MeV did not populate states above 4.8 MeV excitation, the current data yield level structure up to 6.4 MeV. The 142 Ce(p, t)-¹⁴⁰Ce data are characterized by a strong L = 0ground state transition with weak excitation of levels up to the 3.23 MeV 0⁺ state. Above this excitation, strong transitions are observed in both (p, t) and (t, p) experiments.^{1,3} In general our results (Table II) agree with previous information, with the exceptions noted below.

In the 2.0 to 2.5 MeV region several closely spaced levels exist which could not be resolved in this experiment. The 2.08 MeV level is most consistent with an L = 4 DWBA shape, indicating that the contribution from the 2.108 MeV state $[J^{\pi} = (6)^{+}]$ is small. There is no evidence for the population of the unnatural-parity (3*) state at 2.412 MeV, although it would have been resolved from the nearby 2.47 MeV level. A cross section of $\leq 0.5 \ \mu b/sr$ is an upper limit for exciting this state. The 2.471 MeV angular distribution was not well fitted by any single L transfer, and is probably a doublet made up of the 2.464 and 2.481 MeV states. The 2.912 MeV level has an L = 2shape and thus we suggest that this level be assigned $J^{\pi} = 2^{*}$. We associate this state with the 2.8997 MeV level assigned $(1, 2)^*$ in the decay data. The 3.026 MeV level has the characteristic L = 0angular distribution shape implying $J^{\pi} = 0^*$. This state is probably the same as the 3.04 MeV level which was excited in the (α, α') experiment.⁵ The 3.334 MeV angular distribution is not characteristic of any natural-parity transition. This weak level $[1-3 \ \mu b/sr]$ might be associated with the 3.3197 (1, 2*) level observed in the decay data, and is the most likely candidate in our data for the excitation of an unnatural-parity state.

Sixteen possible L = 2 transitions are found in this work, ranging from 3.558 to 6.187 MeV excitation, that were not reported earlier (see Figs. 4 and 5 and Table II). Quite possibly, at least some of these transitions have L = 3. This ¹⁴²Ce-(p, t) analysis has also revealed possible L = 1transfers to states at 4.242, 5.703, and 5.896 MeV in ¹⁴⁰Ce. These angular distributions are fitted fairly well with L = 1 DWBA calculations, implying $J^{\pi} = 1^{-}$ assignments, although L = 2 assignments cannot be excluded. A $J^{\pi} = 1^{-}$ state might arise from the $(1h_{9/2}1g_{7/2})_{1-}$ configuration, since the $(1h_{9/2})^2$ configuration is probably mixed weakly into the ¹⁴²Ce (ground-state) wave function.⁴⁴ No such L = 1 shapes are observed in the ¹³⁸Ce spectrum (see below) nor are they expected, since the 140 Ce nucleus closes a major neutron shell below the $(1h_{\alpha/2})$ orbital.

Above 3.23 MeV we find evidence for nine possible L = 4 or L = 5 transitions. We also tentatively assign L = 0 to a state at 5.574 MeV. The rapid forward angle rise of the 5.574 MeV angular distribution is characteristic of an L = 0 transition, although at large angles the data do not agree very well with an L = 0 shape. A coupled pair vibration model analysis² predicts L = 0 strength in this region.

Higher L transfers $(L \ge 6)$ are characterized by comparatively flat, featureless angular distributions. In Fig. 5 for example, the empirical L=7shape taken from the ¹⁴⁰Ce(p, t) reaction is compared with the 5.101 MeV state, and L=5 and L=6 DWBA predictions are shown for the 5.295 MeV level. These angular distributions are much flatter (especially at forward angles) than those of the (L=3, 4) 4.296 or 6.364 MeV levels.

Summarizing, we find that over the angular range studied here it is probably impossible, with the exception of L = 0 transitions, to make unique Lassignments based on shapes derived from DWBA calculations. However, limits of two possible Lvalues can usually be made, and valuable conclusions regarding restricted J^{π} values can then be made for many states.

5. Spectroscopic results from $^{140}Ce(p,t)^{138}Ce$

Table III summarizes states observed in the 140 Ce(p, t) reaction, as well as the DWBA analy-

sis of their angular distributions. The DWBA prescriptions used are the same as those given in the previous section. The decay data,^{13, 45, 46} included in Table III, give J^{π} information for the low-lying states. The ${}^{140}Ce(p, t)$ analysis is consistent with every assignment; the only exception is that the (p, t) data show no evidence for the 1.477 MeV 0⁺ state.^{13,46} This level would not have been resolved from the 1.501 MeV transition, and apparently is weakly excited in (p, t) since the 1.501 MeV state shows a pure L = 2 transition (see Fig. 6). Possible L = 2 or L = 3 strength lies at 2.640, 2.885, 3.220, and 3.356 MeV (see Table III), although, as for the ${}^{142}Ce(p, t){}^{140}Ce$ case, the DWBA calculations do not give conclusive L assignments. The 2.389 and 3.277 MeV levels were poorly resolved from neighboring excited states. While these angular distributions do not agree particularly well with any DWBA curve, comparisons to the most plausible L values are shown in Fig. 6. These are listed in Table III in parentheses, indicating uncertain assignments. Transitions characterized by L = 4 or L = 5 occur at 2.440, 2.719, 2.942, 3.005, 3.082, and 3.429 MeV. The fits to the 3.005 and 3.429 MeV levels, while not conclusive, are clearly better described by L = 4than L = 5.

The decay data assign the 2.130 MeV state J^{π} = 7⁻ and the 2.219 MeV state as J = 5, 6. The L = 7DWBA curve predicts very well the maximum in the 2.130 MeV angular distribution at 45° (although it fails at more forward angles), while the 2.219 MeV angular distribution is consistent with L > 4. Comparison with the empirical 2.130 MeV angular distribution shows that the 3.646 MeV level is also consistent with an L = 7 assignment. The 3.531 MeV state is not characteristic of any natural-parity level and is probably due to a group of unresolved states. No likely candidates for L = 1 strength were found in this study of ¹⁴⁰Ce-(p, t).

C. Pairing vibration scheme

Analysis of the ¹⁴²Ce(p, t) and ¹⁴⁰Ce(p, t) reactions within the pairing vibration model⁴ has been given in earlier work.¹⁻³ The lowest-order harmonic model predicts that a $J^{\pi} = 0^{+}$ state in ¹⁴⁰Ce should be excited in the (p, t) reaction with the same Qvalue and strength as the ¹³⁸Ce (ground state). The 0⁺ strength is known to be fragmented,^{2,3} and this division of 0⁺ strength was previously discussed² for ¹⁴⁰Ce using a coupling model.⁴⁷ The monopole pairing model can be extended to include quadrupole pairing phonons, the latter being represented by the 0.788 MeV L = 2 transition from the ¹⁴⁰Ce(p, t) reaction. A more complete discussion

-	E_x (MeV)	L	$\sigma(heta)^{a}$ ($\mu { m b/sr}$)	E	∑ ^b	
-	0.0	0	135	19.3		
	1.905	0	13.5	2.1		
	3.026	0	7.2	1.1 (
	3.233	0	105	13.8 🤇	17.0	
	5.574	(0)	13	(2.3)	(19.3)	
	3.558	2	32	1.7		
	3.664	2	32	1.3		
	3.731	2	290	13.3		
	3.985	2	35	1.7		
	4.125	2	23	1.1		
	4.183	2	21	1.3	20.4	

TABLE VI. Distribution of L = 0 and L = 2 strength in ¹⁴⁰Ce found in the ¹⁴²Ce(p, t) reaction.

^aThe L = 0 cross sections are measured at $\theta_{1ab} = 35^{\circ}$, the L = 2 values are at $\theta_{1ab} = 16^{\circ}$.

^bSum of excited-state enhancement factors.

of these ideas applied to the Ce nuclei is found in Refs. 1-3.

Table VI summarizes the L = 0 and L = 2 strength found in the present ¹⁴²Ce(p, t) work. The L = 2strength listed in Table VI corresponds to the L = 2assignments given in Ref. 3, with the addition of the 3.558 MeV level. The enhancement factors derived from the DWBA calculations using the $(1h_{11/2})^2$ form factor are also given here, along with their sum for the excited states given in the final column. The 3.233 and 3.731 MeV states are candidates¹⁻³ for the expected pairing monopole and quadrupole excitations, but their enhancement factors are considerably less than the ϵ values of 19.3 and 18.3 found for the ¹³⁸Ce (ground state) and ¹³⁸Ce (0.788 MeV) transitions, respectively. However if the enhancement factors for the weaker 0⁺ and 2⁺ transitions are added, much better agreement is found. Two values of the summed L=0 enhancement factors [corresponding to retaining the 5.574 MeV (0^+) transition in the sum and deleting it] are given. Inclusion of the 5.574 MeV strength gives a very good agreement with the ¹³⁸Ce (ground state) transition. Summing the L = 2 fragments listed in Table VI gives similar improvement for the comparison with the ¹³⁸Ce (0.788 MeV) strength.

IV. SUMMARY

The ¹⁴⁰Ce(p, p') and ¹⁴²Ce(p, t) reactions have been used to study the ¹⁴⁰Ce nucleus. The (p, p') work gives results similar to the isoscalar excitation⁵ of the ¹⁴⁰Ce even-parity collective levels, with differences noted for the odd-parity transitions. The ¹⁴²Ce(p, t) reaction has resulted in finding many new levels at excitations \geq 3.5 MeV in ¹⁴⁰Ce, as well as placing limits on their J^{π} values. The zero-range DWBA has been examined using the ¹⁴²Ce(p, t)¹⁴⁰Ce reaction at three incident proton energies, and we find it does not describe the variation of cross section with energy for L = 0 and L = 2 transitions. Three different optical model choices were used in this analysis.

The ¹⁴⁰Ce(p, t) reaction was also studied and yielded new information regarding the energy levels and possible J^{π} assignments for $E_x \ge 2.3$ MeV. The combined ^{142,140}Ce(p, t) results are consistent with pairing vibration model predictions for (p, t)

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transition strengths only if the weak L=0 and L=2 fragments observed in the ¹⁴²Ce(p, t) reactions are summed with the principle L=0 and L=2 excitations.

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