Levels in ¹²³I and ¹²⁵I from $({}^{3}\text{He}, d)$ reactions

A. Szanto de Toledo,^{*} M. N. Rao, N. Ueta, and O. Sala Instituto de Física, Universidade de São Paulo, São Paulo, Brasil (Received 11 February 1976; revised manuscript received 8 September 1976)

Proton states in ¹²³I and ¹²⁵I have been observed by means of the ^{123,124}Te(3 He, d)^{123,125}I reactions at a bombarding energy of 19.5 MeV. Results regarding spin assignments and spectroscopic factors are presented.

 $\begin{bmatrix} \text{NUCLEAR REACTIONS} & ^{122, 124} \text{Te}(^3\text{He}, d), E = 19.5 \text{ MeV}; \text{ measured } \sigma(E_d, \theta), \theta \\ = 10^\circ - 90^\circ, \Delta\theta = 5^\circ, \text{ enriched targets}, \Delta E - E \text{ telescopes}, \text{ resolution } 35 \text{ keV}. \\ & 1^{23, 125}\text{I} \text{ deduced levels } l, J, \pi, S; \text{ DWBA analysis.} \end{bmatrix}$

I. INTRODUCTION

Nuclear structure information on the excited levels of the odd isotopes of iodine has been obtained mainly from radioactive decay measurements. The levels of ^{127,129,131} I have also been studied by the $({}^{3}\text{He}, d)$ reactions by Auble, Ball, and Fulmer.¹ Theoretical interpretations of the properties of the odd-mass iodine nuclei have been performed (i) within the framework of the quasiparticle-plus-phonon model,^{2,3} (ii) by coupling a proton to even core tellurium nuclei (intermediate coupling model),⁴ and (iii) in terms of a three proton cluster coupled to a harmonic quadrupole vibrator field.⁵⁻⁷ All three approaches take into account both the shell model and the collective degrees of freedom. However, only the last one includes explicitly the Pauli principle in the valence shell and the anharmonicities induced in the even tellurium core by the interaction of the two protons with the tin core.

The adopted level schemes of the lighter iodine isotopes^{8,9} are based on the decay studies by Gföller, Schönenberg, and Flammersfeld¹⁰ and Stippler, Lode, and Schrader¹¹ for ¹²³I and by Geiger¹² and Ludziejewski *et al.*¹³ for ¹²⁵I. No information exists on direct proton transfer reactions to the levels of ^{123,125}I.

The present work is a report on the results of $({}^{3}\text{He}, d)$ reactions on ${}^{122}\text{Te}$ and ${}^{124}\text{Te}$ nuclei. An interpretation of the present experimental results in terms of the three proton cluster-phonon coupling scheme mentioned above will be given in a forthcoming article.¹⁴

II. EXPERIMENTAL PROCEDURE

The experiments were performed with the 19.52-MeV ³He beam from the Pelletron 8UD accelerator of the University of São Paulo.¹⁵ Targets of $100-150-\mu g/cm^2$ thickness were obtained by evaporation of enriched (>96%) metallic tellurium isotope onto $20-\mu g/cm^2$ carbon foils. Spectra of the outgoing deuterons were measured from 10° to 90° in steps of 5°, utilizing two $\Delta E - E$ solid state detector telescopes and analog particle identifiers.¹⁶ An overall energy resolution of about 35 keV [full width at half maximum (FWHM)] was obtained by applying a +3-kV bias to the target support, thus preventing secondary electrons produced by the bombardment of the target from reaching the detectors.

A least-squares peak fitting program was employed to obtain the areas under the peaks corresponding to the deuteron groups leading to the various excited levels of the residual nuclei. The statistical errors in the data points in the angular distributions, including the errors due to background subtraction, varied from 7% for the strong well-resolved peaks to 13% in the case of weakly populated levels. Typical results of the peak fitting program are presented in Fig. 1, which shows the deuteron spectra leading to the levels of ¹²³I and ¹²⁵I.

Angular distributions of elastically scattered ³He particles from ¹²²Te and ¹²⁴Te were also measured in order to obtain the optical-model parameters for the entrance channel (Te + ³He). At the incident energy of 19.52 MeV, the ratio of elastic to Rutherford scattering remains essentially unity up to about 45°, permitting absolute cross sections to be obtained assuming pure Coulomb scattering for the forward angle cross sections.

III. ANALYSIS OF DATA

The elastic scattering angular distributions were analyzed using an optical-model search code MODOPT.¹⁷ The initial set of parameters were those used in the description of the 29.5-MeV ³He elastic scattering from ¹¹⁶Sn.¹⁸ No spin-orbit

15

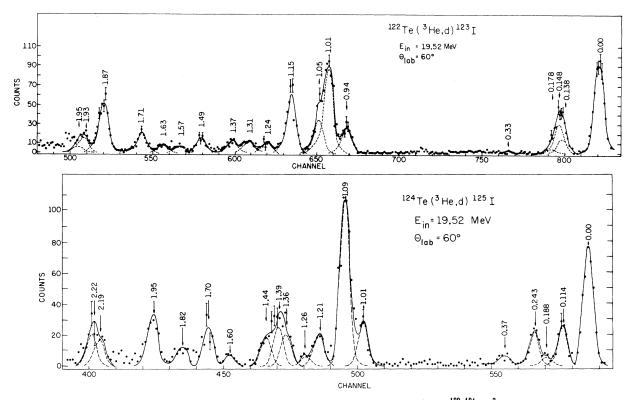


FIG. 1. Typical results of the peak-fitting program showing the spectra from 122,124 Te(3 He, d) reactions.

coupling was included in the entrance channel. The deuteron optical-model parameters were taken from Perey and Perey.¹⁹ A spin-orbit strength of $V_{so} = 6$ MeV was included in the deuteron channel parameters. The transferred proton was described as moving in a Saxon well with a Thomas spin-orbit factor of $\lambda_{so} = 25$. The optical-model parameters as well as the bound state parameters used in the present analyses are given in Table I, and the best fits to the elastic scattering angular distributions are shown in Fig. 2.

The experimental deuteron angular distributions were compared with the distorted-wave Bornapproximation (DWBA) predictions in order to obtain the orbital angular momentum transferred (l_p) and the spectroscopic factors (S_j) for most of the observed levels. The DWBA calculations were performed with the code DWUCK²⁰ in the

TABLE I. Optical-model parameters used in the 122,124 Te $({}^{3}$ He, $d)^{123,125}$ I analyses. The optical potential used was of the form

$$U(r) = -V(1+e^{x})^{-1} - i(W - W'\frac{d}{dx'})(1+e^{x'})^{-1} + (\frac{\hbar}{m_{\pi}c})^{2}V_{so}\frac{l}{r}\frac{d}{dr}(1+e^{x})^{-1}\dot{l}\cdot\sigma,$$

with $x = (r - r_0 A^{1/3})a$, $x' = (r - r_0 A^{1/3})/a'$, $r_c = r_{oc} A^{1/3}$, and $\bar{\sigma} = 2\bar{S}/\hbar$ for spin $\frac{1}{2}$ and $\bar{\sigma} = \bar{S}/\hbar$ for spin 1.

Channel	V (MeV)	r ₀ (fm)	<i>a</i> (fm)	W (MeV)	<i>W</i> ' (MeV)	r' ₀ (fm)	a' (fm)	r _{oc} (fm)	λ_{so}
¹²² Te + ³ He	163.29	1.24	0.667	23.07	0	1.46	0.781	1.25	
¹²⁴ Te + ³ He	163.58	1.24	0.657	22.178	0	1.46	0.776	1.25	
123 • 125 I + d^{a}	101.0	1.15	0.81	0	66.5	1.34	0.68	1.30	5.37
Þ	b	1.20	0.65					1.25	25

^a Obtained from Perey and Perey (Ref. 19).

^b The well depth for the transferred proton is adjusted to give a binding energy equal to the experimental separation energy.

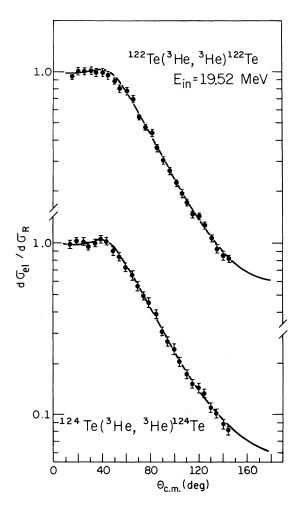


FIG. 2. Angular distributions of 19.52-MeV elastically scattered 3 He from 122 Te and 124 Te.

zero-range approximation. Nonlocality corrections were not made. The cross section for the $({}^{3}\text{He}, d)$ stripping reaction on an even-even target may be written

$$\frac{d\sigma(\theta)}{d\Omega} = N \frac{2J_f + 1}{2J_i + 1} C^2 S_j \frac{\sigma_{\rm DW}^j(\theta)}{(2j+1)} ,$$

where the reduced cross section is the singleparticle cross section obtained from DWBA calculations, *C* is the isospin Clebsch-Gordan coupling coefficient, and J_i , J_f , and j are the total angular momenta of the target nucleus, residual nucleus, and the transferred proton, respectively. A zero-range renormalization factor²¹ of N = 4.42was used in obtaining the spectroscopic factors.

The experimental angular distributions are compared with the DWBA predictions in Figs. 3 and 4.

Unambiguous assignments of the transferred orbital angular momenta were obtained for many of the observed transitions. The observed energy levels in 123 I and 125 I together with l_{p} values and the spectroscopic factors are presented in Tables II and III. Errors from the peak fitting procedure, uncertainties in the measurement of target thickness, and possible nonuniformities in the target contribute to an estimated experimental uncertainty of about 15% in the spectroscopic factors. Uncertainties in the zero-range DWBA have not been included in this present estimate. In the case of the unresolved triplet (0.138, 0.148, and 0.178 MeV) in 123 I, and the unresolved doublet (1.09 MeV) in 125 I, the separation of the corresponding peaks by the peak fitting program, introduces additional uncertainties in the experimental cross sections of the order of 30%.

IV. RESULTS

Levels in ¹²³I

The spin of the ground state of ¹²³I $(J = \frac{5}{2})$ has been measured by atomic beam methods,²² and a positive parity has been assigned⁸ to this state on account of the allowed β decay to the 0.159-MeV $\frac{3}{2}$ ⁺ level in ¹²³Te.

Based on the systematics of low-lying levels in the heavier iodine isotopes, probable multipolarity assignments obtained from the measured conversion coefficients and log ft values from the decay of the ground state of ¹³³Xe (probable spin and parity $\frac{1}{2}^+$), spins and parities of $\frac{7}{2}^+$, $\frac{1}{2}^+$, and $\frac{3}{2}^+$ have been tentatively assigned⁸ to the first three excited states of ¹²³I, respectively. The results obtained in the present work confirm these assignments.

A level at 0.33 MeV is populated extremely weakly in the present ¹²²Te(³He, *d*) measurement. Stippler *et al.*¹¹ have assigned $J^{\pi} = \frac{3}{2}^+$ to this level on the basis of the measured conversion coefficient of the 0.3302-MeV γ ray. No conclusion about the spin and parity of this level could be drawn from the present measurement.

No spins and parities are known from previous measurements for any of the higher excited states in $^{123}\mathrm{I}.$

In the present measurement a level at 0.94-MeV excitation energy has been observed with a transferred orbital angular momentum of $l_p = 5$. On the basis of the single-particle shell model and from the systematics of low-lying levels of the odd-mass antimony and iodine isotopes, this level is likely to have $J^{\pi} = \frac{11}{2}^{-}$.

The $({}^{3}\text{He}, d)$ transitions leading to the levels

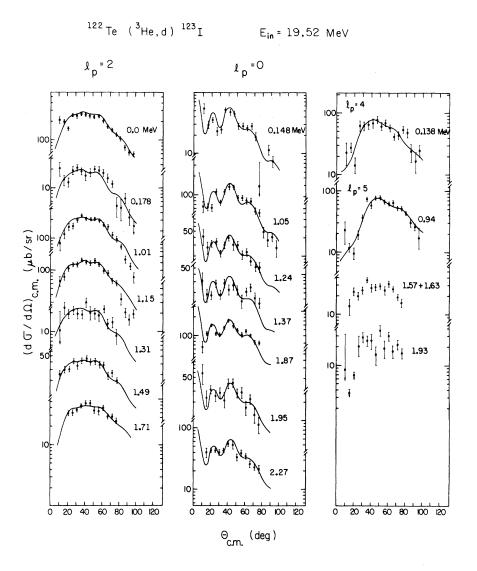


FIG. 3. Experimental and calculated angular distributions for the ${}^{122}\text{Te}({}^{3}\text{He},d){}^{123}\text{I}$ reactions.

with excitation energies of 1.01, 1.15, 1.49, and 1.71 MeV have been assigned $l_p = 2$ in the present work. A weak transition to a level at 1.31 MeV has also been tentatively assigned $l_p = 2$. Between the excitation energies of 1.0 to 2.3 MeV, six $l_p = 0$ transitions have been observed, of which five are considered unambiguous, based on the predicted DWBA shapes. Most of the $l_p = 0$ and 2 transitions seen in this work could be identified with the levels known from decay studies. The energy levels of ¹²³I observed in the present work, together with the transferred angular momenta and the absolute spectroscopic factors are presented in Table II, which also shows the previously known levels in ¹²³I taken from the Nuclear Data Sheets.⁸

Levels in 125 I

The ground and the first three excited states of $\frac{125}{2}$ have been assigned⁹ spins and parities of $\frac{5}{2}^+$, $\frac{7}{2}^+$, $\frac{3}{2}^+$, and $\frac{1}{2}^+$, respectively. The present work confirms these assignments.

Two weak transitions have been observed in the (³He, d) reaction to levels with excitation energies of 0.37 and 0.45 MeV, the first of which has been tentatively assigned an $l_p = 2$.

For the higher excited states in ¹²⁵I no spins

241

¹²⁴Te (³He,d)¹²⁵I

ℓp = 2 lp=2 l_= 4 100 100 0.114 0.0 100 lp=2+lp=5 2.19 1.09 10 ˈdƯ/dΩ)_{cm.} (μb/sr) 100 100 0.243 10 10 0 20 40 60 80 100 120 100 10 50

100

10

ō 20 40

100 120

FIG. 4. Experimental and calculated angular distributions for the ${}^{124}\text{Te}({}^{3}\text{He}, d)$ ${}^{125}\text{I}$ reactions.

 $\Theta_{c.m.}$ (deg)

60 80 100 120

and parities are known from other work.

100

10

ō 20 1 1 1 1

40 60 80

Attempts were made to fit the angular distribution for the transition to the unresolved doublet at 1.09 MeV with combinations of $(l_p = 2 + l_p = 5)$ and $(l_{p}=2+l_{p}=4)$, the former resulting in a better fit. By the arguments utilized in the case of the 0.94-MeV level in ¹²³I, the $l_p = 5$ transition to the unresolved level at 1.09 MeV in ¹²⁵I has been tentatively assigned $J^{\pi} = \frac{11}{2}^{-}$. Between 1.0- and 1.5-MeV excitation energies

in ¹²⁵I, one $l_p = 0$ and five $l_p = 2$ transitions have been observed. The attribution of $l_p = 2$ to the 1.26-MeV transition is tentative. Six new levels have been populated in the present (${}^{3}\text{He}$, d) reaction above an excitation energy of 1.5 MeV.

A summary of these results is presented in Table III, along with the previously known⁹ energy levels in ¹²⁵I from decay studies.

Mass excess of 123 I

As part of the present work, the ground state Q value for the 122 Te(3 He, d) 123 I reaction was measured to within an uncertainty of ± 8 keV. A Q value of 712.0 ± 3.9 keV for the ¹²⁶Te(³He, d)¹²⁷I(g.s.) reaction²³ was used as a reference for the present measurement.

Targets of ¹²²Te and ¹²⁶Te of $\simeq 90-\mu g/cm^2$ thick-

E_{in}= 19.52 MeV

243

Energy ^a (MeV)	Energy ^b (MeV)	$\theta_{c.m.}$ (deg)	<i>dσ/dΩ</i> (μb/sr)	l _p	j °	S _{exp}	S _{Theory}
0.0	0.0	25.5	253	2	$\frac{5}{2}$	0.37	0.29
0.138*	0.138	45.8	81	4	$\frac{7}{2}$	0.75	0.32
0.148*	0.148	35.7	49	0	$\frac{1}{2}$	0.08	0.23
0.178*	0.178	35.7	46	2	$\frac{3}{2}$	0.05	0.10
0.33	0.330	35.7	6				
0.94		51.0	78	5	$\frac{11}{2}$	0.35	0.33
1.01	1.011	35.7	233	2	$\frac{5}{2}, \frac{3}{2}$	0.22,0.43	
1.05	1.049	46.0	135	0	$\frac{1}{2}$	0.17	
1.15	1.113	35.7	148	2	$\frac{3}{2}, \frac{5}{2}$	0.27,0.14	
	(1.154)						
	(1.190)						
1.24	1.243	41.0	40	0	$\frac{1}{2}$	0.05	
1.31	1.310	41.0	29	(2)	$\frac{3}{2}, \frac{5}{2}$	0.04,0.02	
1.37	1.391	35.7	29	(0)	$\frac{1}{2}$	0.04	
1.49		41.0	45	2	$\frac{3}{2}, \frac{5}{2}$	0.07,0.04	
1.57 1.63	1.657	46.0	28				
1.71		41.0	49	2	$\frac{3}{2}, \frac{5}{2}$	0.07,0.03	
1.87	1.865	41.0	170	0	$\frac{1}{2}$	0.17	
1.93	1.934	41.0	25				
1.95	1.956	46.0	42	0	$\frac{1}{2}$	0.04	
	2.063				-		
	2.152						
	2.201						
2.27	2.250	41.0	56	0	$\frac{1}{2}$	0.05	
	2.286						

TABLE II. Results obtained from the ${}^{122}\text{Te}({}^{3}\text{He},d){}^{123}\text{I}$ reaction.

^a Present measurements; uncertainty in excitation energies is ± 8 to ± 10 keV, except in the case of very weak levels. Levels marked with an asterisk were not resolved and their energies were taken from Ref. 8.

^b Nuclear Data Sheets, Ref. 8.

^c Total angular momentum of the transferred proton used in the DWBA calculations.

ness were bombarded with a ³He beam and deuteron spectra were obtained at a laboratory angle of 70°. The measured thicknesses of the two targets differed by 17%, giving rise to a difference of a maximum of 3 keV in the energy loss of the beam in the two targets. The channel difference between the positions of the two ground state peaks was converted into difference in energy using the same energy calibration, yielding a value of 1290 ± 7 keV.

With the known value of 712.0 ± 3.9 keV for the ¹²⁶Te(³He, d)¹²⁷I ground state Q value, the above result, after an estimated correction of 1.5 keV due to the difference in target thicknesses, yields a value of -577 ± 8 keV for the ground state Q value of the ¹²²Te(³He, d)¹²³I reaction. The previ-

		1. 11054115					
Energy ^a (MeV)	Energy ^b (MeV)	θ _{c.m.} (deg)	$d\sigma/d\Omega$ (µb/sr)	l _p	j ^c	Sexp	$s_{ m Theory}$
0.0	0.0	30.6	267	2	<u>5</u> 2	0.40	0.30
0.114	0.114	45.8	49	4	$\frac{7}{2}$	0.51	0.34
0.188	0.188	40.7	18	(2)	$\frac{3}{2}$	0.06	0.10
0.243	0.243	40.7	84	0	$\frac{1}{2}$	0.17	0.24
0.37	0.372	35.6	19	(2)	$\frac{5}{2}, \frac{3}{2}$	0.03,0.06	
0.45	0.454	30.6	10				
1.01	1.007	40.7	103	0	$\frac{1}{2}$	0.16	
				((2)	$\frac{5}{2}, \frac{3}{2}$	0.24,0.48	
1.09 ^d	1.090	40.7	311				
				((5)	$\frac{11}{2}$	0.60	0.41
	(1.108)						
1.21	1,181	35.6	55	2	$\frac{3}{2}, \frac{5}{2}$	0.12,1.06	
1.26	1.264	35.6	27	(2)	$\frac{3}{2}, \frac{5}{2}$	0.05,0.02	
1.36		30.6	69	2	$\frac{3}{2}, \frac{5}{2}$	0.12,0.06	
1.39	1.383	40.7	102	2	$\frac{3}{2}, \frac{5}{2}$	0.22,0.11	
1.44	1.442	40.7	43	2	$\frac{3}{2}, \frac{5}{2}$	0.10,0.05	
1.60	1.561	45.8	20				
1.70		35.6	78	2	$\frac{3}{2}, \frac{5}{2}$	0.13,0.06	
1.82		40.7	56	0	$\frac{1}{2}$	0.07	
1.95		40.7	139	0	$\frac{1}{2}$	0.16	
2.19		30.6	54	0	$\frac{3}{2}, \frac{5}{2}$	0.10,0.05	
2.22		40.7	57	(0)	$\frac{1}{2}$	0.07	

TABLE III. Results obtained from the ${}^{124}\text{Te}({}^{3}\text{He},d){}^{125}\text{I}$ reaction.

^a Present measurements; uncertainty in excitation energies is ± 8 to ± 10 keV, except in the case of very weak levels. Levels marked with an asterisk were not resolved and their energies were taken from Ref. 8.

^b Nuclear Data Sheets, Ref. 8.

^c Total angular momentum of the transferred proton used in the DWBA calculations.

^d Unresolved doublet.

ously accepted²³ value was -550 ± 100 keV. The present measurement corresponds to a mass excess of ¹²³I of -87932 ± 9 keV.

V. DISCUSSION

In the last columns of Tables II and III, the calculated spectroscopic factors for proton transfer, on the basis of the cluster-phonon coupling scheme,¹⁴ are presented, for the levels below 1 MeV excitation. Having in view the large experimental uncertainties for the unresolved triplet around 0.14-0.18 MeV excitation in ¹²³I and the unresolved doublet at 1.09 MeV in ¹²⁵I, it could be concluded that the model is able to predict reasonably well the spectroscopic factors for

the low-lying states in both the nuclei.

A second $\frac{5}{2}^+$ level has been observed¹ in all the heavier iodine isotopes around 0.5-MeV excitation energy. The level at 0.33 MeV in ¹²³I has a $\frac{3}{2}^+$ assignment based on internal conversion data, while in ¹²⁵I, the 0.37-MeV level has been tentatively assigned $\frac{3}{2}^+$ or $\frac{5}{2}^+$ in the present work. The predicted¹⁴ second $\frac{3}{2}^+$ and second $\frac{5}{2}^+$ levels in ¹²³I and ¹²⁵I are at excitation energies of ~1 MeV and ~0.6 MeV, respectively. It may be remarked that if the 0.33-MeV γ ray is pure M1, the measured²⁴ half-life of the 0.33-MeV level $(T_{1/2} = 42 \pm 13 \text{ ps})$ corresponds to $B(M1) \neq (0.25 \pm 0.08) \mu_N^2$, in excellent agreement with the calculated $B(M1; \frac{3}{2}, -\frac{1}{2}, -\frac{1}{$ of the cluster-phonon model.¹⁴ A spin assignment of $\frac{5}{2}^+$ to this level yields a B(M1) of $0.15\mu_N^2$. No data on the transition probability from the 0.37-MeV level in ¹²⁵I are available.

It should be noted that even though the spectroscopic factors predicted for the $1h_{11/2}$ level are in good agreement with the measured values, the predicted excitation energies are almost twice the observed values. Above the excitation energy of 1 MeV, the correspondence between the experimental and the calculated level schemes becomes less obvious.

A more detailed discussion on the wave functions of the ground states of the even Te targets and the ground and the excited levels of $^{123,125}I$,

- *This work is part of a thesis submitted in partial fulfillment of the requirements for the doctoral degree at the University of São Paulo.
- ¹R. L. Auble, J. B. Ball, and C. B. Fulmer, Phys. Rev. 169, 955 (1968).
- ²L. S. Kisslinger and R. A. Sorensen, Rev. Mod. Phys. 35, 853 (1963).
- ³B. S. Reehal and R. A. Sorensen, Phys. Rev. C <u>2</u>, 819 (1970).
- ⁴M. Rustgi, J. Lucas, and S. Mukherjee, Nucl. Phys. A117, 321 (1968).
- ⁵R. Almar, O. Civitarese, and F. Krmpotić, Phys. Rev. C 8, 1518 (1973).
- ⁶V. Paar, Nucl. Phys. <u>A211</u>, 29 (1973).
- ⁷G. Vanden Berghe, Z. Phys. 266, 139 (1974).
- ⁸R. L. Auble, Nucl. Data <u>B7</u>, <u>363</u> (1972).
- ⁹R. L. Auble, Nucl. Data <u>B7</u>, 465 (1972).
- ¹⁰D. Gföller, R. Schönenberg, and A. Flammersfeld, Z. Phys. <u>208</u>, 299 (1968).
- ¹¹R. Stippler, D. Lode, and H. Schrader, Z. Phys. <u>242</u>, 121 (1971).
- ¹²J. S. Geiger, Phys. Rev. 158, 1094 (1967).
- ¹³J. Ludziejewski, J. Kownacki, W. Klamra, J. Chwas-

as well as a comparison with the predicted spectroscopic sum rule limits, will be given in Ref. 14.

ACKNOWLEDGMENTS

The assistance given by the staff of the Pelletron Laboratory is gratefully acknowledged. We express our thanks to Professor Dr. F. Krmpotić for making available the code for the calculation of the theoretical spectroscopic factors and for a critical reading of the manuscript. We would also like to thank Dr. W. Mittig for the use of the peakfitting program.

zczewska, and W. Przyborski, Acta Phys. Polon. <u>36</u>, 939 (1969).

- ¹⁴ F. Krmpotić, M. N. Rao, and A. Szanto de Toledo (unpublished).
- ¹⁵O. Sala and G. Spalek, Nucl. Instrum. Methods <u>122</u>, 213 (1974).
- ¹⁶F. S. Goulding, D. A. Landis, J. Cerny, and R. H. Pehl, Nucl. Instrum. Methods 31, 1 (1964).
- ¹⁷J. M. Cohenca, a computer program for optical-model analysis of nuclear scattering, Univ. of Oxford Nuclear Physics Group Report No. 41, 1968 (unpublished).
- ¹⁸J. W. Luetzelschwab and J. C. Hafele, Phys. Rev. <u>180</u>, 1023 (1969).
- ¹⁹C. M. Perey and F. G. Perey, Phys. Rev. <u>132</u>, 755 (1963).
- ²⁰P. D. Kunz, Univ. of Colorado, 1967 (unpublished).
- ²¹R. H. Bassel, Phys. Rev. <u>149</u>, 791 (1966).
- ²²H. L. Garvin, T. M. Green, and E. Lipworth, Phys. Rev. 111, 534 (1958).
- ²³N. B. Gove and A. H. Wapstra, Nucl. Data <u>A11</u>, 211 (1972).
- ²⁴A. Hogland, S. G. Malmskog, F. Munnich, and H. Schrader, Nucl. Phys. <u>A165</u>, 513 (1971).