

## Coulomb displacement energies of the $A = 4n + 3$ , $T = 1/2$ mirror nuclei in the $1f_{7/2}$ shell\*

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The  $Q$  values of the ( $^3\text{He}, ^6\text{He}$ ) reaction on  $^{46}\text{Ti}$ ,  $^{50}\text{Cr}$ ,  $^{54}\text{Fe}$ , and  $^{58}\text{Ni}$  have been measured, and the excitation energy of levels up to 7 MeV has been determined. Angular distributions from the more strongly populated states have been taken from 4.5 to 27.0° in the laboratory. These angular distributions together with comparison to their  $T_z = +1/2$  mirrors have been used as empirical guides to determine the spin and parity of several of the states. The Coulomb displacement energies of particle-hole states in the  $T = 1/2$  mirrors have been compared to a simple model.

[ NUCLEAR REACTIONS  $^{25}\text{Mg}$ ,  $^{27}\text{Al}$ ,  $^{46}\text{Ti}$ ,  $^{50}\text{Cr}$ ,  $^{54}\text{Fe}$ ,  $^{58}\text{Ni}$ ( $^3\text{He}$ ,  $^6\text{He}$ ),  $E_{^3\text{He}} = 70$  MeV, measured  $Q$ ,  $\sigma(\theta)$ , excitation energies, obtained mass excess of  $^{43}\text{Ti}$ ,  $^{47}\text{Cr}$ ,  $^{51}\text{Fe}$ ,  $^{55}\text{Ni}$ , deduced Coulomb displacement energies. ]

### I. INTRODUCTION

Coulomb displacement energies have been employed in the past to deduce charge radii of nuclei. However, more direct measurements of nuclear charge radii have been provided in recent years by electron scattering and muonic x-ray data. In their review article,<sup>1</sup> Nolen and Schiffer pointed out that the nuclear charge radii extracted from Coulomb displacement energies were too small when compared with other more accurate data. Equivalently, if nuclear charge radii which were determined by electron scattering or muonic x-rays are employed to calculate Coulomb displacement energies, the calculated values are too small by 5–10% throughout the Periodic Table. Nolen and Schiffer pointed out that this discrepancy persists even when both the exchange and electromagnetic spin-orbit terms are included. Several theoretical papers have investigated other correction terms including vacuum polarization, higher order magnetic terms, the finite size of the proton, the proton-neutron mass difference, isospin mixing in the core, and charge symmetry breaking of the nuclear force.<sup>2–11</sup> Despite the refinements of the theoretical model, a solution to the problem has not been found.

The experimental results presented in this paper are of interest because they allow accurate determination of Coulomb displacement energies for the ground and a few excited states of the  $T = \frac{1}{2}$  mirror nuclei throughout the  $1f_{7/2}$  nuclear subshell. Although the displacement energies between isobaric analog states in heavier nuclei are known, the present results include the heaviest known mirror nuclei. The displacement energy of a mirror pair is expected to depend only on the

Coulomb interaction and possibly a charge-symmetry-breaking nuclear force, i.e., a difference in the nuclear part of the  $p$ - $p$  and  $n$ - $n$  interactions. The displacement energy of a nonmirror isobaric analog pair may depend, in addition, upon a charge dependent nuclear force, i.e., a difference in the  $T = 1$ ,  $p$ - $n$  and  $n$ - $n$  interactions. As Sherr and Talmi have shown,<sup>11</sup> it may be possible to extract the  $p$ - $n$  and  $n$ - $n$  difference by comparing the displacement energies of  $T > \frac{1}{2}$  analog pairs with those of the  $T = \frac{1}{2}$  mirror pairs.

The results of the present experiment provide more accurate measurements of the ground state masses of  $^{43}\text{Ti}$ ,  $^{47}\text{Cr}$ ,  $^{51}\text{Fe}$ , and  $^{55}\text{Ni}$  than were obtained previously.<sup>12,13</sup> The accurate determination of the excitation energy of several levels in these nuclei provides the necessary data to extract Coulomb displacement energies of the  $J^\pi = \frac{7}{2}^-$ ,  $\frac{3}{2}^+$ , and  $\frac{1}{2}^+$  levels for the  $T = \frac{1}{2}$  mirror pairs. The angular distributions of these low cross-section reactions and comparison with the  $T_z = +\frac{1}{2}$  mirror nuclei provided evidence for the spin and parity assignments. The displacement energies of the  $\frac{1}{2}^+$  and  $\frac{3}{2}^+$  particle-hole states are compared with a model of Sherr and Bertsch,<sup>14</sup> and excellent agreement is found. However, the data show the same phenomenon which Nolen and Schiffer found in a wide range of nuclei.

### II. EXPERIMENTAL METHOD

The measurement of the reaction  $Q$  values was made by comparing the magnetic rigidity of the  $^6\text{He}$  particles from the reactions of interest with those from the  $^{27}\text{Al}(^3\text{He}, ^6\text{He})^{24}\text{Al}(\text{g.s.})$  and  $^{25}\text{Mg}(^3\text{He}, ^6\text{He})^{22}\text{Mg}(3.3082)$  reactions in a magnetic spectrograph. The  $Q$  values of the calibration re-

TABLE I. Target thickness.

Frame number	Isotope	Thickness <sup>a</sup> ( $\mu\text{g}/\text{cm}^2$ )		Energy loss <sup>b</sup> (keV)		% Enrichment
		Target	Backing <sup>c</sup>	<sup>6</sup> He	<sup>3</sup> He	
426	<sup>50</sup> Cr	82	47	5.5	6.3	96.80(5)
227	<sup>25</sup> Mg	61	30	4.8	4.6	99.21(5)
207	<sup>58</sup> Ni	89	37	6.0	5.5	99.890
632	<sup>46</sup> Ti	40	27	2.9	3.5	81.2
634	<sup>54</sup> Fe	99	31	6.6	5.5	96.81(5)
627	<sup>27</sup> Al	62	27	4.8	4.4	100

<sup>a</sup>The uncertainty in the thicknesses are 10% for the target and 15% for the backing.

<sup>b</sup>The energy loss for <sup>6</sup>He is that of 52 MeV <sup>6</sup>He particles in one-half the target thickness, while for <sup>3</sup>He, the energy loss is that for 70 MeV <sup>3</sup>He particles in one-half the target thickness plus that in the backing.

<sup>c</sup>The measurement of thickness of the backings employed the relative yields from the <sup>12</sup>C(<sup>3</sup>He, <sup>6</sup>Li) reaction, as well as the <sup>6</sup>Li energy loss.

actions  $-19.812(3)$  MeV<sup>15,16</sup> and  $-18.7656(40)$  MeV,<sup>16-19</sup> respectively, are very close to those being measured, and therefore the scaling of the field in the spectrograph contributes very little ( $\sim 1.0$  keV) to the uncertainty in the measured  $Q$  values. A beam of 70 MeV <sup>3</sup>He particles from the Michigan State University cyclotron was employed to induce the reactions on thin isotopically enriched carbon-backed metal foils. The position of the <sup>6</sup>He particles in the focal plane of the spectrograph was measured by a resistive-wire gas-proportional counter. The <sup>6</sup>He particles were identified by their energy loss in two proportional counters, time-of-flight through the spectrograph, and light output from the plastic scintillator which followed the two proportional counters. The method is similar to that described by Kashy *et al.*<sup>20</sup> except for the use of a second proportional counter and event recording the data on magnetic tape in the present experimental arrangement. The target thicknesses were measured by means of the energy loss of 56 MeV <sup>6</sup>Li ions from the <sup>12</sup>C(<sup>3</sup>He, <sup>6</sup>Li) reaction induced on the carbon backings. The targets were rotated so that the carbon backing faced either towards or away from the spectrograph aperture. The difference between <sup>6</sup>Li energies in the two target orientations gives the <sup>6</sup>Li energy loss. Table I gives the results of the target thickness measurements for these thin carbon-backed targets as well as the thicknesses of the backings, which were measured by comparison of the yields with that from a 217  $\mu\text{g}/\text{cm}^2$  carbon foil. The 10% uncertainty in the target thickness implies only about a 1 keV uncertainty in the  $Q$ -value measurements. The  $Q$ -value measurements were made at lab angles of  $6^\circ$  and  $10^\circ$  with a solid angle of  $1.2 \times 10^{-3}$  sr.

### III. RESULTS

The results of the  $Q$ -value measurements and the deduced mass excesses are compared with previous measurements in Table II. The primary differences between the present and previous measurements at MSU are that thinner targets and a second calibration were employed in obtaining the present results while a greater number of repeated measurements were used previously.<sup>12,22</sup> The only substantial difference between the two results is in the <sup>47</sup>Cr ground state mass. This difference is a result of the better resolution obtained which allowed a more accurate determination of the centroid of the previously unresolved ground state. Figures 1 and 2 show the high resolution spectra obtained at  $10^\circ$  in the laboratory.

Table III lists the excitation energies of levels in the final nuclei which have been observed in thin target runs with a cross section greater than about 50 nb/sr at either  $6^\circ$  or  $10^\circ$  in the laboratory or which are observed as isolated peaks in the thick target spectra. The spin and parity assignments have been made for some levels by comparison of the  $T_z = -\frac{1}{2}$  with the  $T_z = \frac{1}{2}$  levels. These assignments are further supported by the comparison of the angular distribution of the states of interest with those from the <sup>42</sup>Ca(<sup>3</sup>He, <sup>6</sup>He)<sup>39</sup>Ca reaction, in which the spins and parities of the final states are well known. Figure 3 illustrates the results of this empirical comparison. The solid lines shown in Fig. 3 are drawn to facilitate comparison of the angular distributions from the various targets. The angular distributions leading to either the  $\frac{7}{2}^-$  or  $\frac{3}{2}^+$  state are quite similar throughout this set. Only the  $L=0$  transfers seem to vary from one case to another. Despite the recent suc-

TABLE II. Mass excesses and  $Q$  values.

Nucleus	Mass excess (MeV)		Average
	Previous <sup>a</sup>	Present	
<sup>43</sup> Ti	-29.328 ± 0.012	-29.305 ± 0.014	-29.319 ± 0.008 <sup>b</sup>
<sup>47</sup> Cr(g.s.)	-34.608 ± 0.040 <sup>c</sup>	-34.553 ± 0.015	-34.561 ± 0.012 <sup>c</sup>
( $\frac{7}{2}^-$ )	-34.386 ± 0.012	-34.371 ± 0.013	-34.379 ± 0.010
<sup>51</sup> Fe(g.s.)	-40.219 ± 0.017	-40.200 ± 0.015	-40.201 ± 0.012 <sup>d</sup>
( $\frac{7}{2}^-$ )	-39.940 ± 0.013	-39.938 ± 0.013	-39.939 ± 0.010
<sup>55</sup> Ni	-45.337 ± 0.011 <sup>e</sup>	-45.327 ± 0.013	-45.333 ± 0.010
Reaction	Q value (MeV)		Present <sup>f</sup>
	Previous <sup>a</sup>		
<sup>46</sup> Ti( <sup>3</sup> He, <sup>6</sup> He) <sup>43</sup> Ti	-17.463 ± 0.012		-17.486 ± 0.014
<sup>50</sup> Cr( <sup>3</sup> He, <sup>6</sup> He) <sup>47</sup> Cr(g.s.)	-18.313 ± 0.040		-18.368 ± 0.014
( $\frac{7}{2}^-$ )	-18.535 ± 0.012		-18.550 ± 0.013
<sup>54</sup> Fe( <sup>3</sup> He, <sup>6</sup> He) <sup>51</sup> Fe(g.s.)	-18.698 ± 0.017		-18.697 ± 0.015
( $\frac{7}{2}^-$ )	-18.969 ± 0.013		-18.971 ± 0.013
<sup>58</sup> Ni( <sup>3</sup> He, <sup>6</sup> He) <sup>55</sup> Ni	-17.555 ± 0.011		-17.565 ± 0.013

<sup>a</sup>Reference 13.

<sup>b</sup>The average mass excess of <sup>43</sup>Ti included the measurement of Ref. 24 (-29.321 ± 0.010 MeV).

<sup>c</sup>In the previous measurement, the <sup>47</sup>Cr g.s. was not resolved. The separation of the  $\frac{7}{2}^-$  and the ground state was taken from the present measurements.

<sup>d</sup>The relative excitation of the  $\frac{7}{2}^-$  and  $\frac{5}{2}^-$  ground state from the present measurement was employed to deduce the <sup>51</sup>Fe and <sup>47</sup>Cr ground state masses.

<sup>e</sup>This value represents an 8.2 keV increase in the mass of <sup>55</sup>Ni from the previous value (Ref. 1) due to the measurement of the <sup>58</sup>Ni mass of Jolivet *et al.* (Ref. 25).

<sup>f</sup> $Q$  values measured relative to the <sup>27</sup>Al(<sup>3</sup>He, <sup>6</sup>He)<sup>24</sup>Al(g.s.) and <sup>25</sup>Mg(<sup>3</sup>He, <sup>6</sup>He)<sup>24</sup>Mg(3.3082) reaction  $Q$  values of -19.812 ± 0.003 MeV (Refs. 15 and 16) and -18.7655 ± 0.004 MeV (Refs. 16-19), respectively.

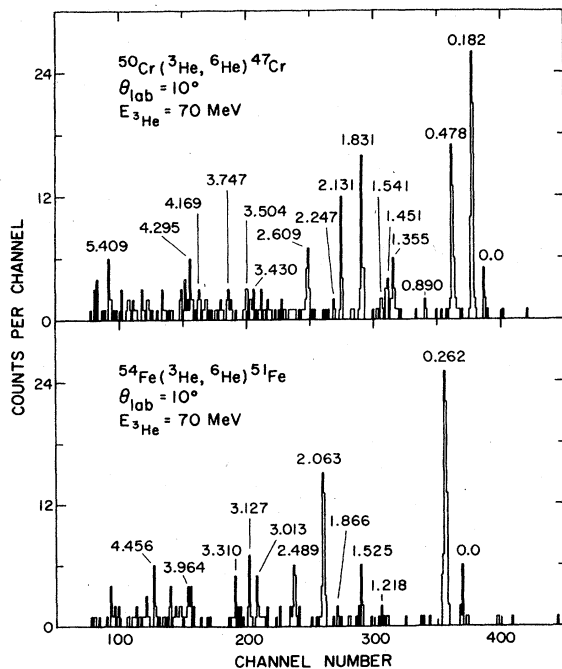


FIG. 1. High resolution spectra of <sup>6</sup>He particles from the <sup>50</sup>Cr(<sup>3</sup>He, <sup>6</sup>He) and <sup>54</sup>Fe(<sup>3</sup>He, <sup>6</sup>He) reactions.

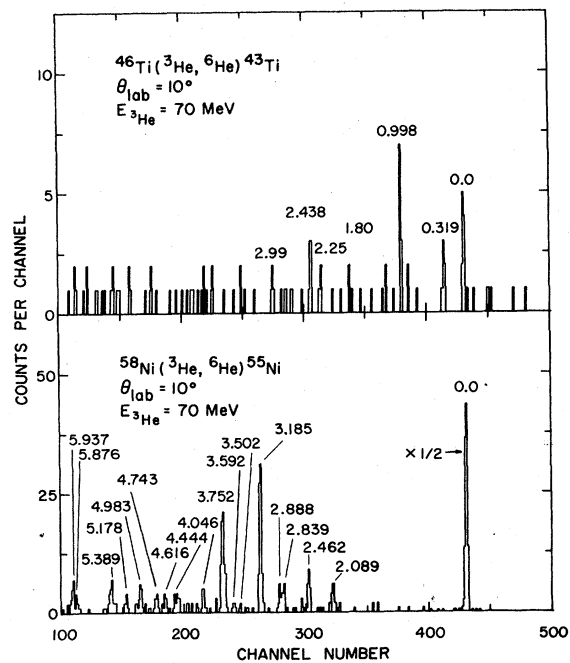


FIG. 2. High resolution spectra of <sup>6</sup>He particles from the <sup>46</sup>Ti(<sup>3</sup>He, <sup>6</sup>He) and <sup>58</sup>Ni(<sup>3</sup>He, <sup>6</sup>He) reactions.

TABLE III. Excitation energies.

$^{55}\text{Ni}$		$^{51}\text{Fe}$		$^{47}\text{Cr}$		$^{43}\text{Ti}$	
$E_x$ (MeV) <sup>a</sup>	$J^\pi$	$E_x$ (MeV) <sup>a</sup>	$J^\pi$	$E_x$ (MeV) <sup>a</sup>	$J^\pi$	$E_x$ (MeV) <sup>a</sup>	$J^\pi$
0.000( 0)	$\frac{7}{2}^-$	0.000( 0)	$\frac{5}{2}^-$	0.000( 0)	$\frac{3}{2}^-$	0.000( 0)	$\frac{7}{2}^-$
2.089( 6)		0.262( 6)	$\frac{7}{2}^-$	0.102(10)	$\frac{5}{2}^-$	0.319( 6)	$\frac{3}{2}^+$
2.462( 5)		1.218(10)		0.182( 7)	$\frac{7}{2}^-$	0.475(10)	
2.839( 5)		1.525( 9)		0.478( 7)	$\frac{3}{2}^+$	0.998(10)	$\frac{1}{2}^+$
2.888( 7)		1.866(13)		0.890(20)		1.160(10)	
3.185( 6)	$\frac{1}{2}^+$	2.063( 7)	$\frac{3}{2}^+$	1.355( 8)		1.470(10)	
3.502(15)		2.489( 8)	$\frac{1}{2}^+$	1.451( 9)		1.800(15)	
3.592(15)		3.013( 9)		1.541(15)		2.250(10)	
3.752( 7)	$\frac{3}{2}^+$	3.127( 9)		1.831( 8)	$\frac{1}{2}^+$	2.438( 9)	
3.784(15)		3.310(10)		2.131( 9)		2.990(15)	
4.046( 9)		3.964(12)	(Doublet)	2.406(10)			
4.444(10)	(Doublet)	4.456(13)		2.557(10)			
4.616(11)				2.609(10)			
4.743(12)				2.661(10)			
4.983(11)				2.848(10)			
5.178(11)				3.430(10)			
5.389(12)				3.504(11)			
5.876(13)				3.747(11)			
5.937(13)				4.169(12)			
6.600(50)				4.295(12)			
6.870(50)				5.409(15)			

<sup>a</sup> Uncertainties in keV are indicated in parentheses.

cess of Delic and Kurath<sup>21</sup> in describing the qualitative features of the  $^{13}\text{C}(^3\text{He}, ^6\text{He})^{10}\text{C}$  reaction by a finite-range distorted-wave Born approximation (DWBA), the  $(^3\text{He}, ^6\text{He})$  reaction mechanism is not yet well understood. So, no attempt to perform a DWBA analysis of these results has been made. The angular distributions are presented in the hope that they may be of some use in the future as the theory of three-nucleon transfer reactions improves.

#### IV. DISCUSSION

The results of the mass measurements and the determination of excitation energies allow the extraction of Coulomb displacement energies listed in Table IV for the  $J^\pi = \frac{7}{2}^-$ ,  $\frac{3}{2}^+$ , and  $\frac{1}{2}^+$  levels in the  $A = 4n + 3$ ,  $T = \frac{1}{2}$  mirror nuclei. Recently Sherr and Bertsch<sup>14</sup> employed the Bansal-French-Zamick model to calculate the Coulomb displacement energies of excited particle-hole states in light nuclei and reported that the level shifts are reproduced to within 50 keV. Using this model, the Coulomb displacement energy of the lowest  $J^\pi = \frac{3}{2}^+$  state in  $^{43}\text{Ti}$  and  $^{43}\text{Sc}$  is given by

$$\Delta E_C(43, \frac{3}{2}^+) = \Delta E_C(39, \frac{3}{2}^+) + 2C(\frac{3}{2}^+, \frac{7}{2}^-)$$

where  $E_C(39, \frac{3}{2}^+)$  is the Coulomb energy difference

of the  $\frac{3}{2}^+$  levels in  $^{39}\text{Ca}$  and  $^{39}\text{K}$ , and  $C(\frac{3}{2}^+, \frac{7}{2}^-)$  is the Coulomb interaction of a  $d_{3/2}$  proton with an  $f_{7/2}$  proton. The factor of 2 in the second term reflects the greater number of  $d_{3/2}$ - $f_{7/2}$  proton interactions in  $^{43}\text{Ti}$  as compared with  $^{43}\text{Sc}$ . The results of predictions using this model for both the  $\frac{1}{2}^+$  and  $\frac{3}{2}^+$  states in the  $A = 4n + 3$ ,  $T = \frac{1}{2}$  mirror nuclei are indicated by the solid lines in Fig. 4. The values  $C(\frac{3}{2}^+, \frac{7}{2}^-) = 296$  keV and  $C(\frac{1}{2}^+, \frac{7}{2}^-) = 302$  keV, were obtained by performing a least squares fit to the data which are indicated by the points. These values of  $C$  are for many-particle-one-hole states, but they can be compared with the 289 and 286 keV values which were obtained in Ref. 14 for one-particle-many-hole states. Recently, it was pointed out that the  $^{39}\text{Ca}$ - $^{39}\text{K}$  pair has an anomalously large Coulomb displacement energy which results from the large binding energy of these nuclei.<sup>22</sup> Hence, it is reasonable to make a fit to the data excluding the  $A = 39$  values. The results are indicated by the dashed lines in Fig. 4. It is then found that  $C(\frac{3}{2}^+, \frac{7}{2}^-) [C(\frac{1}{2}^+, \frac{7}{2}^-)] = 316$  keV [321 keV], and that the predicted Coulomb displacement energy of the  $\frac{3}{2}^+$  [ $\frac{1}{2}^+$ ] states in  $^{39}\text{Ca}$ - $^{39}\text{K}$  is 126 keV [117 keV] below the experimental values. This is consistent with results obtained from the systematics of the series of analog states in the odd mass Ca-K isotopes.<sup>22</sup>

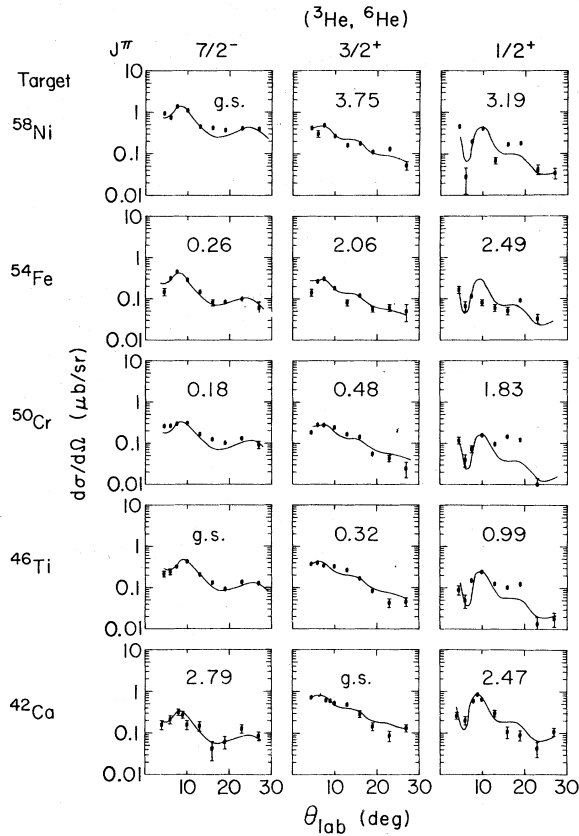


FIG. 3. Angular distributions of the  $({}^3\text{He}, {}^6\text{He})$  reaction at 70 MeV. The  ${}^{42}\text{Ca}({}^3\text{He}, {}^6\text{He})$  results are from Ref. 29.

Calculations of the  $d_{3/2}-f_{7/2}$  and  $s_{1/2}-f_{7/2}$  proton-proton interactions were performed using both harmonic oscillator and Woods-Saxon wave functions. An oscillator parameter of  $0.258 \text{ fm}^{-2}$  was used to obtain the harmonic oscillator wave functions. A Woods-Saxon well depth which reproduced the one-neutron separation energy of  ${}^{43}\text{Sc}$  and a radius consistent with the charge radius obtained in electron scattering experiments<sup>23</sup> were used to obtain the Woods-Saxon wave functions. Table V shows the surprisingly good agreement between the results obtained in the calculations and the experimentally determined values.

The Coulomb displacement energies of the  $A = 4n + 3$ ,  $T = \frac{1}{2}$  mirror nuclei in the  $1f_{7/2}$  shell were calculated using the method outlined by Nolen and Schiffer<sup>1</sup> for the direct term. The depth of a Woods-Saxon well was varied to fit the experimental neutron separation energy of the  $T = +\frac{1}{2}$  nucleus. Then the separation energy of a proton from the  $T_z = -\frac{1}{2}$  nucleus was calculated using the same well depth and assuming a uniformly charged spherical core for the nucleus. The radius of the

TABLE IV. Displacement energies of the  $T = \frac{1}{2}$  mirror pairs in the  $1f_{7/2}$  shell.

A	$J^\pi$	$\Delta E_C$ (MeV)	Reference
41	$\frac{1}{2}^-$	$7.278 \pm 0.005$	16
	$\frac{3}{2}^+$	$7.364 \pm 0.009$	16, 19
43	$\frac{1}{2}^+$	$7.323 \pm 0.007$	16, 19
	$\frac{1}{2}^-$	$7.646 \pm 0.009$	16, present
	$\frac{3}{2}^+$	$7.813 \pm 0.011$	16, 19, present
45	$\frac{1}{2}^+$	$7.789 \pm 0.013$	16, 19, present
	$\frac{1}{2}^-$	$7.906 \pm 0.018$	13, 16
	$\frac{3}{2}^+$	$8.442 \pm 0.013$	16, 26, present
47	$\frac{1}{2}^-$	$8.262 \pm 0.010$	16, 26, present
	$\frac{1}{2}^+$	$8.442 \pm 0.013$	16, 26, present
	$\frac{3}{2}^+$	$8.394 \pm 0.013$	16, 26, present
49	$\frac{1}{2}^-$	$8.487 \pm 0.018$	13, 25
	$\frac{3}{2}^+$	$8.487 \pm 0.018$	16, 27, present
51	$\frac{1}{2}^-$	$8.846 \pm 0.011$	16, 27, present
	$\frac{3}{2}^+$	$9.067 \pm 0.013$	16, 27, present
	$\frac{1}{2}^+$	$9.034 \pm 0.013$	16, 27, present
53	$\frac{1}{2}^-$	$9.073 \pm 0.023$	13, 16
	$\frac{3}{2}^+$	$9.073 \pm 0.023$	25, present
55	$\frac{1}{2}^-$	$9.477 \pm 0.010$	25, present
	$\frac{3}{2}^+$	$9.703 \pm 0.012$	25, 28, present
	$\frac{1}{2}^+$	$9.743 \pm 0.012$	25, 28, present

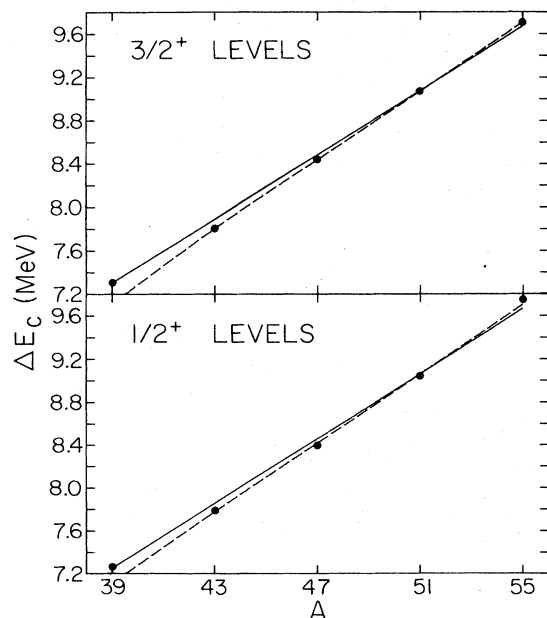


FIG. 4. Coulomb displacement energies versus mass number for  $A = 4n + 3$ ,  $T = \frac{1}{2}$  mirror nuclei in the  $1f_{7/2}$  shell. The points represent the experimental data while the lines connect the predictions discussed in the text.

TABLE V. Coulomb interaction between protons in different shells.

	Exp (keV)	HO <sup>a</sup> (keV)	WS (keV)	
			Direct	Exchange
$f_{7/2}-d_{3/2}$	316	308	338	-16
$f_{7/2}-2s_{1/2}$	321	294	328	-6

<sup>a</sup>Calculation made using the oscillator parameter = 0.258 fm<sup>-2</sup>.

core charge distribution for these nuclei is not experimentally known; however, addition of  $f_{7/2}$  shell neutrons to a nucleus has been shown to have a small effect on the nuclear charge radius. For example in the Ti or Ca isotopes, in which comparison of nuclei having different numbers of  $f_{7/2}$  neutrons is possible, the charge radius varies only about 1% between extremes.<sup>23</sup> Using a charge radius consistent with electron scattering in the above model, we find the calculation of the Cou-

lomb displacement energy to be 450 to 650 keV less than the experimental values found in Table IV. The calculations for the  $\frac{3}{2}^+$  levels agree with the data better than do either the  $\frac{7}{2}^-$  or  $\frac{1}{2}^+$  levels by 100 to 150 keV. Therefore, although the Nolen-Schiffer anomaly persists for these mirror levels, it is interesting that the values for the  $f_{7/2}-d_{3/2}$  and  $f_{7/2}-s_{1/2}$  Coulomb interactions agree so well with the values extracted from Sherr and Bertsch's model.

We hope to be able to extend these results to the hole states in the  $A = 4n + 1$ ,  $T_z = -\frac{1}{2}$  nuclei by means of the (<sup>3</sup>He, <sup>8</sup>Li) or ( $p$ , <sup>6</sup>He) reaction, but resolution as high as in the present experiment will be much more difficult to obtain.

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