Coulomb excitation of levels in ${}^{95}Mo$ and ${}^{97}Mo^{\dagger}$

J. Barrette,* M. Barrette, R. Haroutunian,[‡] G. Lamoureux, and S. Monaro

Laboratoire de Physique Nucléaire and Département de Physique, Université de Montréal, Montréal, Québec, Canada

S. Markiza

Physics Department, Loyola of Montreal, Montreal, Quebec, Canada (Received 25 June 1974)

The properties of the low-lying levels of 95 Mo and 97 Mo have been investigated via Coulomb excitation which was effected by bombarding isotopically enriched thick targets with 6.0 to 10.0 MeV α particles and 43.4 MeV 16 O ions. Sixteen transitions in 95 Mo and twenty three transitions in 97 Mo were observed resulting from direct E2 excitation of eight excited states up to an excitation energy of 1073.7 keV in 95 Mo, and of thirteen excited states up to an excitation energy of 1515.5 keV in 97 Mo. Angular distribution measurements were carried out for several transitions in both nuclei to aid in the assignment of spins and to yield the E2 and M1 contents in these transitions. The level structure of 95 Mo and 97 Mo and the measured E2 and M1 transition rates are compared with the predictions available for these nuclei.

NUCLEAR REACTIONS ^{95,97} Mo ($\alpha, \alpha' \gamma$), E = 6-10 MeV; ^{95,97} Mo (^{16}O , $^{16}O' \gamma$), E = 43.4 MeV; measured $\sigma(E_{\gamma}, \theta_{\gamma})$, ^{95,97} Mo deduced levels, B(E2), B(M1), $T_{1/2}$, J, π , γ mixing, γ branching. Enriched targets.

I. INTRODUCTION

It has become increasingly apparent from recent experimental studies¹⁻⁶ that the molybdenum nuclei provide several interesting features for nuclear model calculations. Several theoretical efforts to explain the nuclear structure of ⁹⁵Mo and ⁹⁷Mo have appeared in the literature.⁷⁻¹⁰ A pure shell-model approach developed by Bhatt and Ball⁷ and Vervier⁸ as well as a theoretical development by Kisslinger and Sorensen,⁹ using a pairing-plusquadrupole interaction, do not successfully account for the complexity of these nuclei. A more recent investigation by Choudhury and Clemens,¹⁰ carried out within the framework of the unified model, seems to give a better fit to the experimental level scheme of ⁹⁵Mo, but totally fails in explaining the rather complicated structure of ⁹⁷Mo as revealed in recent Coulomb excitation experiments⁵ and in an (α, xn) reaction study.⁴ This failure could be explained by the simple assumptions used by those authors to deduce the level scheme of ⁹⁷Mo. Choudhury and Clemens¹⁰ calculated also the E2and M1 transition rates for several transitions in ⁹⁵Mo as well as in ⁹⁷Mo and it is evident that a precise measurement of these quantities would give a more stringent test to their theoretical predictions. A direct approach to the ascertainment of level properties is through Coulomb excitation. Information on the γ -ray transition probabilities of γ rays deexciting levels in ⁹⁵Mo is very limited. The only ones previously reported are the $B(E2\uparrow)$ values for the 203 keV level,¹¹ and for the 786,

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974, and 1073 keV levels.¹² However, the last values¹² are suspect since they were extracted with NaI(Tl) detectors, and the close proximity of other states in the ⁹⁵Mo level structure, not separable with this type of counter, could have yielded an incorrect interpretation of their Coulomb excitation data. In this paper we report the results of Coulomb excitation experiments on ⁹⁵Mo performed with α particles and the use of highresolution large-volume Ge(Li) detectors. Furthermore, information on spins of the excited states and the multipolarity of the decay radiations both in ⁹⁵Mo and ⁹⁷Mo was obtained by angular distribution measurements carried out with α beams. The $B(E2\uparrow)$ values attached to the states of ⁹⁷Mo were reported in a previous paper.⁵ These results will be presented here again in their slightly revised and extended version, since further measurements on this nucleus revealed new γ rays and new excited states in its level structure.

II. EXPERIMENTAL PROCEDURE AND RESULTS

Coulomb excitation was effected by bombarding thick targets of isotopically enriched ⁹⁵Mo (97%) and ⁹⁷Mo (93%), as well as a thick target of natural molybdenum, with 6 to 10 MeV α particles. These targets were in the form of self-supporting metallic rolled foils having a thickness of 45 mg/cm². Singles spectra of the deexcitation γ rays were observed with a 45 and a 36 cm³ Ge(Li) detectors having 2.0 keV resolution at 1.33 MeV, and placed 10 cm from the target at an angle of ±55° with re-



FIG. 1. Direct pulse-height spectrum of the γ rays for 8 MeV α particles on a ⁹⁵Mo target. Energies are in keV. The unlabeled peaks have unknown origin.



FIG. 2. Level schemes of 95 Mo and 97 Mo as deduced from the present Coulomb excitation measurements.

spect to the incoming beam. Some measurements were also performed with a 43.4 MeV ¹⁶O beam. With ¹⁶O ions multiple Coulomb excitation becomes important, and it is difficult to extract B(E2) values from the γ -ray yields because states can be populated by more than one multistep process. However, heavy ion projectiles greatly enhance the excitation cross sections and, thus, are particularly useful in detecting states which are weakly excited with α particles. The ¹⁶O measurements enabled us to gain additional information on B(E2)values and branching ratios of very weakly excited states in ⁹⁵Mo and ⁹⁷Mo.

A. γ -ray spectra and γ -ray yields

A representative γ -ray spectrum, resulting from bombardment of a ⁹⁵Mo enriched target with 8 MeV α particle is shown in Fig. 1 (a γ -ray spectrum of ⁹⁷Mo has been shown elsewhere⁵). The γ rays which are attributed to ⁹⁵Mo and ⁹⁷Mo are presented in the level schemes of Fig. 2.

The energy values given in Fig. 2 have been deduced by taking as internal reference points the 778.22 keV photopeak due to the Coulomb excitation of ${}^{96}Mo^{1}$ and the 1460.75 keV photopeak due to the disintegration of ${}^{40}K$. Furthermore, the energy values of the 203.94, 582.15, and 947.8 keV transitions of ⁹⁵Mo, measured very precisely by Chilosi, Eichler, and Aras,¹³ have been also used as internal reference points. The energies of the 786.21 and 835.14 keV γ rays have also been taken from Chilosi et al.,13 since the former transition is not separated from the 787.5 keV γ ray due to the Coulomb excitation of ⁹⁸Mo⁶ and the latter transition is always mixed with an impurity. The intensity values given in Fig. 2 have been deduced in the present work with the expection of the 786.21 keV transition in ⁹⁵Mo which have been calculated considering the intensity ratio between the 582 and 786 keV γ rays given by Cesareo, Langhoff, and Flammerseld.¹⁴ With respect to our previous investigation on the level structure of ⁹⁷Mo,⁵ two new states at 840 and 1284 keV were found in this work. Comments on individual levels will be given below.

Thick target γ -ray yields for excitation of levels in ⁹⁵Mo and ⁹⁷Mo were measured with 6 to 10 MeV α particles in steps of 1 MeV. The yields were obtained by correcting the areas under the full energy peaks for detector efficiency, absorption of γ rays by the target and target chamber, internal electron conversion, and cascade transitions from the higher energy levels. Details on



FIG. 3. Relative thick-target yields of γ rays observed in the present Coulomb excitation study. The solid curves represent the theoretically predicted E_2 excitation thick-target yields, whereas the points represent the data obtained at each α -particle bombarding energy. ΔE and E_{γ} denote the excitation energy of the state and the γ -ray energy, respectively.

	⁹⁵ Mo		⁹⁷ Mo
Level		Level	
energy	$B(E2^{\dagger})$	energy	$B(E2\dagger)$
(keV)	$(10^{-50} e^2 \mathrm{cm}^4)$	(keV)	$(10^{-50} e^2 \text{ cm}^4)$
203.94	3.80 ± 0.24	480.9	2.05 ± 0.11
765.9	<0.013	658.2	0.047 ± 0.007
786.21	0.325 ± 0.020	679.6	0.46 ± 0.03
820.8	0.060 ± 0.015	719.3	0.39 ± 0.03
947.8	5.25 ± 0.25	721.1	0.168 ± 0.015
1039.3	0.55 ± 0.10	(840.9)	0.030 ± 0.007
1056.8	1.30 ± 0.07	888.1	0.182 ± 0.020
1073.7	3.86 ± 0.21	1024.6	4.53 ± 0.24
		1092.6	0.344 ± 0.025
		1116.7	4.56 ± 0.32
		1268.6	0.95 ± 0.20
		1284.6	0.42 ± 0.09
		1515.5	0.53 ± 0.08

TABLE I. Summary of $B(E2^{\dagger})$ values for levels in 95 Mo and 97 Mo observed via direct E2 Coulomb excitation with α particles.

the methods of calculation have been already reported.^{1,6} The resultant net yield measured for each observed transition in ⁹⁵Mo and ⁹⁷Mo is plotted as a function of α -particle energy in Fig. 3. The $B(E2\uparrow)$ values extracted from the γ -ray yields by means of the first-order perturbation theory of Alder *et al.*¹⁵ are summarized in Table I.

Each $B(E2\dagger)$ value, shown in Table I, represents a weighted average of values obtained for each α particle energy. The yields were observed to vary with the ⁴He energy, within the relative errors, as predicted by the first-order E2 perturbation theory¹⁵ in spite of the fact that by bombarding the targets with α particles at 9 and 10 MeV, transitions produced by the reactions ${}^{95}Mo(\alpha, n\gamma)$ -⁹⁸Ru and ⁹⁷Mo(α , $n\gamma$)¹⁰⁰Ru could be detected in the γ -ray spectra. The identification of these transitions was facilitated by a recent investigation of the level structure of ^{98,100}Ru, through ^{94,96}Mo- $(\alpha, 2n\gamma)$ reactions, by Lederer, Jaklevic, and Hollander.³ The presence of these transitions arising from nuclear reactions shows that nuclear force effects may play a role in the interaction between projectile and target nucleus. However, these effects appear to be negligible since the excitation functions of the strongly excited levels do not diverge from those predicted by the first-order E2 perturbation theory¹⁵ up to a bombarding energy of 10 MeV. Thus, one is justified to employ these functions up to this energy in the calculation of the $B(E2\uparrow)$.

The experimental errors shown in Table I do not include the error introduced by the reorientation effect which is difficult to evaluate since the static quadrupole moment of the various levels is not known. However, the effect due to a static quadrupole moment of 1 e b on the excitation probability of each of the levels in ⁹⁵Mo and ⁹⁷Mo, excited by α particles, was calculated. It was found that the inclusion of this static quadrupole moment value changes the respective cross sections by less than 3%. Theoretical calculations¹⁰ predict that in general the static quadrupole moment val-

Ε. (keV) $(a_4A_4)_{\rm exp}^{\rm a}$ $(a_2 A_2)_{exp}^{a}$ δ a_2 0.020 -0.045 ± 0.002 -0.010 ± 0.002 0.327 0.4 to 1.4 203.94 $\textbf{0.002} \pm \textbf{0.010}$ 0.007 ± 0.013 0.784 -0.044 582.15 -0.048 820.8 -0.030 ± 0.055 0.030 ± 0.068 0.799 0.15 ± 0.17 or $2.7^{+2.5}_{-1.0}$ -0.073 0.42 ± 0.07 or 852.8 0.051 ± 0.009 $\textbf{0.035} \pm \textbf{0.011}$ 0.882 $6.7^{+4.5}_{-2.0}$ 0.02 ± 0.08 or $3.6^{+2.1}_{-1.1}$ 947.8 -0.004 ± 0.002 -0.062 0.01 ± 0.01 b 0.154 ± 0.002 0.846 $0.81^{+0.37}_{-0.28}$ 1056.8 -0.151 ± 0.019 0.027 ± 0.024 0.882 -0.073 $-0.55^{+0.31}_{-0.45}$ -7+ $\rightarrow \frac{5}{2}$ 1073.8 -0.077 ± 0.003 -0.008 ± 0.004 0.887 -0.075 0.72 ± 0.11

TABLE II. Angular distribution results on ⁹⁵Mo.

^a The experimental errors quoted for a_2A_2 and a_4A_4 are statistical only.

 $^{\rm b}\delta(M3/E2).$

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Eγ (keV)	$(a_2A_2)_{\exp}^{a}$	$(a_4A_4)_{\exp}^{a}$	a_2	a_4	$J_i \rightarrow J_f$	δ
238.3	$\boldsymbol{0.056 \pm 0.013}$	0.024 ± 0.017	0.754	-0.036	$\frac{5^+}{2} \rightarrow \frac{3^+}{2}$	0.06 ± 0.06 or
						$2.9^{+0}_{-0.4}$
366.3	$\boldsymbol{0.047 \pm 0.019}$	$\textbf{0.009} \pm \textbf{0.025}$	0.871	-0.070	$\frac{7}{2}^+ \rightarrow \frac{7}{2}^+$	$-0.55\substack{+0\\-0.73}$
397.3 ^b	$\textbf{0.180} \pm \textbf{0.068}$		0.853	-0.064	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	$-0.05\pm0.17~^{c}$
407.0	$\textbf{0.005} \pm \textbf{0.021}$	-0.008 ± 0.028	0.824	-0.055	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	
480.9	$\textbf{0.131} \pm \textbf{0.002}$	0.001 ± 0.002	0.611	-0.008	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	-0.47 ± 0.03 or
						-4.4 ± 0.4
679.6	$\textbf{0.011} \pm \textbf{0.005}$	-0.015 ± 0.006	0.735	-0.032	$\frac{1}{2}^+ \rightarrow \frac{5}{2}^+$	
719.3	$\textbf{0.009} \pm \textbf{0.011}$	$\textbf{0.003} \pm \textbf{0.014}$	0.754	-0.036	$\frac{5}{2}^+ \rightarrow \frac{5}{2}^+$	0.47 ± 0.10 or
						$-10.5_{-4:0}^{+4:5}$
721.1	-0.021 ± 0.015	$\textbf{-0.017} \pm 0.022$	0.755	-0.037	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$ or	0.19 ± 0.09 or
						$2.4^{+0}_{-0.5}$
					$\frac{5^+}{2} \rightarrow \frac{5^+}{2}$ or	0.22 ± 0.14 or
					$\frac{7}{2}^+ \rightarrow \frac{5}{2}^+$	$-3.0^{+1}_{-2.5}$
						0.08 ± 0.23 or
						$4.2^{+\infty}_{-2.4}$
857.3 ^b	$\boldsymbol{0.158 \pm 0.056}$		0.952	-0.098	$\frac{9}{2}^+ \rightarrow \frac{7}{2}^+$	-0.40 ± 0.10 or
						$-4.7^{+1}_{-3.0}$
1024.6	-0.071 ± 0.003	-0.001 ± 0.004	0.871	-0.070	$\frac{7}{2}^+ \rightarrow \frac{5}{2}^+$	$0.54\substack{+0.24\\-0.14}$
1092.6	$\textbf{0.233} \pm \textbf{0.020}$	$\textbf{0.000} \pm \textbf{0.028}$	0.892	-0.077	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	$-0.51^{+0.15}_{-0.24}$ or
						$-3.7^{+1}_{-3.9}$
1116.7	$\textbf{0.163} \pm \textbf{0.004}$	$\textbf{0.001} \pm \textbf{0.006}$	0.899	-0.079	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	0.00 ± 0.01 ^c
1284.6^{b}	$\textbf{-0.163} \pm \textbf{0.032}$		0.899	-0.079	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	$0.81\substack{+0.42\\-0.30}$
1515.5^{b}	$\textbf{0.156} \pm \textbf{0.070}$		0.952	-0.098	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	$0.05\pm0.15\ ^{c}$

TABLE III. Angular distribution results on ⁹⁷Mo.

^a The experimental errors quoted for a_2A_2 and a_4A_4 are statistical only.

^b Angular distribution results obtained with 10 MeV α particles.

 $^{\rm c}\delta(M3/E2)$.

ues are smaller than 1 e b hence their effect will be always within the experimental errors attached to the $B(E2^{\dagger})$ values. Furthermore, the possible effect due to the quadrupole moment of the ground state of ⁹⁵Mo and ⁹⁷Mo (0.12 and 1.1 e b, respectively^{16,17}) was also calculated. It was found again that this effect is also well within the experimental errors of the $B(E2^{\dagger})$ values.

B. Angular distributions

Angular distributions of some of the deexcitation γ rays of ⁹⁵Mo and ⁹⁷Mo were measured at four angles (0, 30, 60, and 90°) with the 45 cm³ Ge(Li) detector at a distance of 15 cm from the target. This large distance was chosen to reduce the finite-angle correction and the effect of any possible uncertainty in the positioning of the target. A 9 MeV α beam was used to carry out these experiments, and in the case of ⁹⁷Mo some measurements with 10 MeV α particles were also performed. In this case the spectra were acquired with the Ge(Li) detector placed at angles of 0 and 90° only. The target was always placed at 45° with respect to the incident beam so as to insure an equal geometry at 0 and 90° and a negligible difference in the γ -ray absorption from the target and target chamber at any angle. A second Ge(Li) detector (the 36 cm³ one) was also placed at -90° with respect to the incoming beam. This detector was used as monitor to normalize the measurements at each angle. The total incident charge

was also collected for the same purpose. The results of these measurements were fitted to the formula $W(\theta) = 1 + \sum_{k=2,4} a_k Q_k A_k P_k(\cos \theta)$ where θ is the γ -ray angle relative to the beam direction, Q_k is the attenuation coefficient of the γ -ray counter,¹⁸ a_k is the Coulomb excitation particle parameter, A_k is the γ - γ directional correlation coefficient for an equivalent cascade, and P_k is the Legendre polynomial. The final results for ⁹⁵Mo and ⁹⁷Mo are summarized in Tables II and III.

The spin sequence(s) of the cascade, previously known or proposed from the present measurements, is (are) given in the sixth column, whereas the measured mixing ratios E2/M1 (or M3/E2) are presented in the seventh column. The δ sign has been determined following the convention of Rose and Brink¹⁹ where the mixing ratio is defined by $\delta = \langle I_i \| \lambda + 1 \| I_f \rangle / \langle I_i \| \lambda \| I_f \rangle$. The value for the 203 keV transition in ⁹⁵Mo is in agreement with the result of McGowan and Stelson¹¹ ($\delta = -0.6 \pm 0.2$; the difference in sign is due to the different sign convention used by those authors) who have measured the angular distribution and the polarization of this transition. However, the 203 keV level has a half-life of 0.756 nsec,²⁰ which is sufficiently long to introduce in the angular distribution of the 203 keV transition an attenuation caused by the deorientation of the excited state. Thus, we have calculated the mixing ratio from the known halflife²⁰ and the $B(E2\uparrow)$ value measured by us. This procedure yields a more precise δ value equal to 0.63 ± 0.04 .

Extensive angular distribution measurements on transitions deexciting levels in ⁹⁵Mo and ⁹⁷Mo have been recently performed by Mesko et al.⁴ Usually their $\boldsymbol{\delta}$ values are in disagreement with those found in the present investigation. In Coulomb excitation measurements, the angular distributions are treated by an exact procedure and their analysis is relatively simple.¹⁵ However, Mesko et al.⁴ obtained their mixing ratio values from angular distributions on emitted γ rays from nuclear states formed in $Zr(\alpha, xn)$ reactions. It is not possible, in this case, to calculate precisely the alignment of the formed excited states. Mesko et al.⁴ employed the approximation that the actual angular distributions are attenuated by a factor $\alpha_{\rm P}$ with respect to those due to completely aligned excited states. These authors suppose that this attenuation factor is a smooth function of the spin of the levels and completely independent on their energy. This approximation is certainly justified for levels with high angular momentum since their alignment is almost total. However, the levels of interest in the present investigation have low angular momentum $(I \leq \frac{7}{2})$ and are very little aligned.

Indeed, our results show that this approximation should be taken with caution. For instance, the $a_2 A_2$ value obtained by us for the 480 keV transition in ⁹⁷Mo (9 MeV α particles) is equal to 0.131 ± 0.002 . The δ value obtained by Mesko *et al.*⁴ for the same transition would correspond to an $a_2 A_2$ coefficient equal to 0.00 to 0.05 which is completely outside the possible experimental errors.

III. DISCUSSION

A. Level properties

The properties of the levels and γ rays shown in Fig. 2 are summarized in Table IV. The admixtures, $\delta = (E2/M1)^{1/2}$, listed in column 4 are those measured by us or those found in previous investigations (see footnotes of Table IV). The reduced E2 and M1 transition rates are given in column 5 and 6, respectively, whereas the final column gives the half-life of the levels. The δ values quoted in square brackets are considered less probable since they would yield M1 transition probabilities strongly hindered. This kind of hindrance is rarely encountered.²¹ The transition whose E2/M1 mixing is not known, have been assumed as pure M1 transitions. In fact, the relationship

$$\frac{T^{E2}}{T^{M1}} = \delta^2 = \frac{3}{100} \left(\frac{\Delta E}{\hbar c}\right)^2 \frac{B(E2\mathbf{1})}{B(M1\mathbf{1})}$$

shows that for constant E2 and M1 reduced transition probabilities, the M1 content of low energy transitions will be favored with respect to the E2content ($\% M1/\% E2 \propto \Delta E^{-2}$). The B(E2*) values corresponding to pure E2 transitions are given in Table V together with their enhancement factors.

Since the most collective transition observed in the present investigation is equal to ~25 W. u. (Weisskopf unit), it can be concluded that the *M*1 component must dominate in these transitions (with the exception of the 458 and 611 keV transitions). It should be mentioned that Behar, Garber, and Grabowski²² recently measured a δ value equal to $-19 \leq \delta \leq -0.64 [M1 + (30 \leq E2 \leq 99.7)\%]$ for the 219 keV transition of ⁹⁵Mo. The choice of the smallest *E*2 content (30%) for this transition would yield a *B*(*E*2+) value equal to $0.29^{+0.31}_{-0.15} e^2 b^2$ (corresponding to 111^{+62}_{-56} W. u.), which is unusually large.

The δ value $3.6^{+2.1}_{-1.1}$ of the 852 keV transition in ⁹⁵Mo and the δ value $2.9^{+0.6}_{-0.4}$ of the 238 keV transition in ⁹⁷Mo have not been included in Table IV since they would give unrealistic values for the E2 reduced transition probabilities. In fact, the former would yield $B(E2*) = 0.42^{+1.65}_{-0.26} e^2 b^2$ (i.e., $1.6^{+4.4}_{-1.0} \times 10^2$ W. u.) and the latter would yield B(E2*)

					D (1411)	
E_{l} (keV)	E_{γ} (keV)	$J_i^{\pi} \rightarrow J_f^{\pi}$	δ	B(E2i) (10 ⁻⁵⁰ e^2 cm ⁴)	$\left[\left(\frac{e\hbar}{2Mc}\right)^2\right]$	<i>T</i> _{1/2} (psec)
			⁹⁵ M	0		
203.94	203.94	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	0.63 ± 0.04 ^a	5.70 ± 0.36	$(4.21 \pm 0.22) \times 10^{-3}$	756 $\pm 14^{a}$
765.9	765.9	$\frac{7}{2}^+ \rightarrow \frac{5}{2}^+$	<0.05 ^b	<0.010	$4.3^{+2.4}_{-1.5}$ × 10 ⁻²	$2.05^{+1}_{-0.70}$
786.21	582.15	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	$0.266_{-0.040}^{+0.052}$ c	$1.0^{+0.6}_{-0.4}$	$(3.2 \pm 0.6) \times 10^{-2}$	4.4 ± 0.6
	786.21	$\frac{1}{2}^+ \rightarrow \frac{5}{2}^+$	E2	0.98 ± 0.06		
820.8	617.4	$\frac{3}{2}^+ \rightarrow \frac{3}{2}^+$	-2.00 ± 0.22 ^c	>0.3	>2.4 $\times 10^{-4}$	<18
				$[0.07^{+0}_{-0.04}]^{07}$	$[4.6^{+5.8}_{-2.8} \times 10^{-3}]$	$[120^{+70}_{-40}]$
	820.8	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	0.15 ± 0.17	$\textbf{0.090} \pm \textbf{0.023}$	>3.1 ×10 ⁻³	
			$[2.7^{+2.5}_{-1.0}]$		$[5.7^{+12}_{-4.7}]^{5}$ × 10 ⁻⁵]	
947.8	181.5	$\frac{9}{2}^+ \rightarrow \frac{7}{2}^+$	Assumed $M1$		$(6.1 \pm 1.7) \times 10^{-3}$	2.34 ± 0.11
	947.8	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	E2	3.15 ± 0.15		
1039.3	219.4 ^d	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	Assumed $M1$		$3.2^{+2.4}_{-1.6} \times 10^{-2}$	0.23 ± 0.06
	253,2	$\frac{1}{2}^+ \rightarrow \frac{1}{2}^+$	Assumed $M1$		$(2.3 \pm 1.1) \times 10^{-1}$	
	835.14	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	0.038 ± 0.019 ^c	$0.07_{-0.05}^{+0.14}$	$(2.6 \pm 0.7) \times 10^{-1}$	
	1039.5	$\frac{1}{2}^+ \rightarrow \frac{5}{2}^+$	E2	1.65 ± 0.30		
1056.8	852.8	$\frac{5}{2}^+ \rightarrow \frac{3}{2}^+$	0.02 ± 0.08	<2.1	$2.3^{+8.5}_{-1.3} \times 10^{-1}$	$0.20\substack{+0\\-0.16}\substack{+26\\-16}$
	1056.8	$\frac{5}{2}^+ \rightarrow \frac{5}{2}^+$	$-0.55_{-0.45}^{+0.31}$	1.30 ± 0.07	$3.3^{+15}_{-2}.5_{4}$ × 10 ⁻²	
1073.7	125.8	$\frac{7^+}{2} \rightarrow \frac{9^+}{2}$	Assumed $M1$		$4.7^{+2}_{-1.5}^{3}$ ×10 ⁻¹	0.46 ± 0.12
	307.8	$\frac{7}{2}^+ \rightarrow \frac{7}{2}^+$	Assumed $M1$		$2.1^{+0.9}_{-0.6}$ × 10 ⁻²	
	1073.8	$\frac{7^+}{2} \rightarrow \frac{5^+}{2}$	0.72 ± 0.11	2.90 ± 0.16	$4.5^{+2.1}_{-1.3}$ × 10 ⁻²	
			⁹⁷ M	0		
480.9	480.9	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	-0.47 ± 0.03	3.07 ± 0.17	$(2.2 \pm 0.4) \times 10^{-2}$	13.0 ± 2.1
658.2	177.97 ^e	$\frac{7}{1}^{+} \rightarrow \frac{3}{2}^{+}$	E2	$7.9^{+4}_{-2}.9$		$2.0 \pm 0.5^{\text{f}}$
	658.2	$\frac{2}{7^+} \rightarrow \frac{2}{5^+}$	$0.04 \pm 0.01^{\text{f}}$	0.035 ± 0.005	$6.9^{+2.3}_{-1.4} \times 10^{-2}$	
679.6	679.6	$2^{2} \rightarrow \frac{2}{5^{+}}$	E2	1.38 ± 0.09	1.1	28.3 ± 1.9
719.3	238.5	$\frac{2}{5^+} \rightarrow \frac{3}{2^+}$	0.06 ± 0.06	<4.2	$6.9^{+5.0}_{-2.5} \times 10^{-2}$	10.4 ± 4.4
		2 2		[<0.5]	$[(1.3 \pm 0.3) \times 10^{-2}]$	$[56 \pm 5]$
	719.3	$\frac{5}{2}^+ \rightarrow \frac{5}{2}^+$	0.47 ± 0.10	0.39 ± 0.03	$6.4^{+4.7}_{-2.4} \times 10^{-3}$	
		2 2	$[-10.5^{+4.5}_{-4.0}]$		$[1.3^{+2.9}_{-0.7} \times 10^{-5}]$	
721.1	721.1	$\left(\frac{3}{2}\right)^+ \rightarrow \frac{5}{2}^+$	0.19 ± 0.09	0.252 ± 0.023	$2.5^{+7.3}_{-1.5} \times 10^{-2}$	$4.0^{+5.2}_{-3.0}$
		2 2	$[2.4^{+0.7}_{-0.5}]$		$[1.6^{+1.2}_{-0.7} \times 10^{-4}]$	$[100 \pm 15]$
888.1	407.0	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	Assumed $M1$		$(2.1 \pm 0.5) \times 10^{-1}$	2.5 ± 0.6
	888.1	$\frac{1}{2}^{+} \rightarrow \frac{5}{2}^{+}$	E2	0.55 ± 0.06		
1024.6	366.3	$\frac{1}{2}^{+} \rightarrow \frac{1}{2}^{+}$	Assumed $M1$		$8.0^{+5.4}_{-3.4} \times 10^{-2}$	$0.32_{-0.13}^{+0.25}$
	543.8	$\frac{1}{2}^{+} \rightarrow \frac{3}{2}^{+}$	E2	$1.3^{+1.4}_{-0.8}$	···	
	1024.6	$\frac{7}{2}^+ \rightarrow \frac{5}{2}^+$	$0.54_{-0.14}^{+0.24}$	3.40 ± 0.18	$8.5_{-3.6}^{+7.9} imes 10^{-2}$	
1092.6	611.9	$\frac{3}{2}^+ \rightarrow \frac{3}{2}^+$	Assumed $M1$		$1.3^{+1.6}_{-0.7} \times 10^{-2}$	$1.3_{-0.6}^{+1.2}$
	1092.6	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	$-0.51^{+0}_{-0.24}$	0.52 ± 0.04	$1.7^{+1.8}_{-1.0}$ $ imes 10^{-2}$	

TABLE IV. Summary of level and γ -ray properties in 95 Mo and 97 Mo.

E _I (keV)	E _γ (keV)	$J_i^{\pi} \rightarrow J_f^{\pi}$	δ	B(E2i) $(10^{-50} e^2 \text{ cm}^4)$	$B(M1\downarrow) \\ \left[\left(\frac{e\hbar}{2Mc} \right)^2 \right]$	T _{1/2} (psec)
1116.7	397.3	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	E2	5.8 ±1.4		1.15 ± 0.08
	458.5	$\frac{9}{2}^+ \rightarrow \frac{7}{2}^+$	Assumed $M1$		$(6.5 \pm 1.2) \times 10^{-3}$	
	1116.7	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	E2	2.74 ± 0.19		
1284.6	1284.6	$\left(\frac{3}{2}\right)^+ \rightarrow \frac{5}{2}^+$	$0.81_{-0.30}^{+0.42}$	0.63 ± 0.14	$1.1^{+2.3}_{-0.7} \times 10^{-2}$	0.43_{-0}^{+0}
1515.5	857.3	$\frac{9}{2}^+ \rightarrow \frac{7}{2}^+$	-0.40 ± 0.10	$0.30_{-0.19}^{+0.33}$	$(1.0 \pm 0.5) \times 10^{-2}$	1.6 ± 0.4
			$[-4.7^{+1}_{-3}]^{5}_{0}]$	$[2.1 \pm 1.0]$	$[5.0^{+9}_{-4.0}]^{0} \times 10^{-4}]$	
	1515.5	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	E2	0.32 ± 0.05		

TABLE IV (Continued)

^a The δ value of the 203.94 keV transition has been calculated from the $B(E2^{\dagger})$ measured in the present work and from the half-life of the 203.94 keV level as given in Ref. 20.

^b The δ value of the 765.9 keV transition has been calculated from the $B(E2\dagger)$ measured in the present work and from the half-life of the 765 keV level as given in Ref. 29.

^c See Ref. 22.

^d The 219.4 keV transition has not been observed in the present work. The calculations have been carried out considering the intensity value given in Ref. 13.

^e The 177.97 keV transition has not been observed in the present work. The calculations have been carried out considering the intensity value given in Ref. 34.

^f The δ value of the 658.2 keV transition has been calculated from the $B(E2^{\dagger})$ measured in the present work and the half-life of the 658.2 keV level as given in Ref. 35.

= $1.49^{+1.06}_{-0.53} e^2 b^2$ (i.e., 560^{+400}_{-200} W. u.) or 0.29 ± 0.05 $e^2 b^2$ (i.e., 110 ± 20 W. u.) depending on the E2/M1ratio of the 719 keV transition. These are exceptionally high enhancement factors encountered only in very deformed nuclei.²¹

By comparing photopeak shapes obtained by Coulomb exciting enriched targets of ⁹⁵Mo and ⁹⁷Mo with ¹⁶O ions, it was possible to discard the δ value $-3.7^{+1.5}_{-3.9}$ of the 1092 keV transition in ⁹⁷Mo. In fact, when these particles are used, several photopeaks show a Doppler broadening at the base of the peak due to the recoil motion of the target nucleus. The larger the fraction of the displaced transition the shorter is the half-life of the level. The comparison of the peak shapes shows that the Doppler shift of the 1092 keV transition is much broader than that of the 947 keV transition (⁹⁵Mo, 2.34 psec) and comparable to the displacement of the 1116 keV transition (⁹⁷Mo, 1.15 psec). Thus, only the δ value $-0.51^{+0.15}_{-0.24}$ (1.3^{+1.2}_{-0.6} psec) is possible for the 1092 keV transition for the other value would yield a half-life equal to $5.9^{+1.0}_{-1.1}$ psec.

³⁵Mo nucleus. All the levels Coulomb excited in the present investigation have been observed both in the decay of ^{95g,m}Tc (Refs. 13 and 14) and in $(\alpha, n\gamma)$ experiments.^{2,4} With the exception of the 1073 keV state, these levels are excited also in (d, p) and (d, t)reaction measurements.^{23,24} Previous Coulomb excitation measurements on ⁹⁵Mo were performed by McGowan and Stelson,¹¹ Alkhazov, Erokhina, and Lemberg,¹² and more recently by Bond.²⁵ The agreement with the results of McGowan and Stelson¹¹ [203 keV, $B(E2\dagger) = (3.5 \pm 0.3) \times 10^{-2} e^2 b^2$] and Bond²⁵ [203 keV, $B(E2\dagger) = 4.3 \pm 0.5$; 765 keV, $B(E2\dagger) = < 0.05$; 786 keV, $B(E2\dagger) = 0.3 \pm 0.1$; 947 keV, $B(E2\dagger) = 5.0 \pm 0.5$; 1073 keV, $B(E2\dagger) = 4.0 \pm 0.5$ in units of $10^{-2} e^2 b^2$] is excellent. On the other hand, the agreement is poor with the results of Alkhazov *et al.*¹² [786 keV, $B(E2\dagger) = 2.0 \pm 0.5$;

TABLE V. B(E2+) and $B(E2+)/B(E2)_{s.p.}$ values calculated for the transitions assumed as pure M1 transitions in Table IV.

		$B(E2\downarrow)$	
Isotope	E_{γ}	$(10^{-50} e^2 \mathrm{cm}^4)$	$B(E2\downarrow)/B(E2)_{s.p.}$ a
⁹⁵ Mo	125.8	42_{-13}^{+21}	$(1.6^{+0}_{-0.5}) \times 10^4$
	181.5	0.27 ± 0.07	$(1.05 \pm 0.27) \times 10^2$
	219.4	$0.95_{-0.48}^{+0.90}$	$3.7^{+2}_{-1.9}$ × 10 ²
	253.2	5.2 ± 2.5	$(2.0 \pm 1.0) \times 10^3$
	307.8	$0.32^{+0}_{-0.09}$	$1.2^{+0}_{-0.3}$ × 10^2
⁹⁷ Mo	366.3	$0.85_{-0.36}^{+0.58}$	$3.2^{+2}_{-1.4}$ × 10 ²
	407.0	1.8^{+0}_{-0}	$6.8^{+1}_{-1}.9_{5} imes 10^{2}$
	458.5	$\textbf{0.045} \pm \textbf{0.008}$	17 ± 3
	611.9	$0.050_{-0.028}^{+0.064}$	19_{-11}^{+24}

^a $B(E2)_{s.p.} = e^2/4\pi [(3/5)^2] R_0^4$, where $R_0 = 1.2 A^{1/3}$ fm.

947 keV, $B(E2\uparrow) = 3.2 \pm 0.7$; 1073 keV, $B(E2\uparrow) = 2.9$ ± 0.6 in units of $10^{-50} e^2 \text{ cm}^4$] particularly for the 786 keV level. The spin $\frac{7}{2}^+$ for the 765 keV level has been established by circular polarization²⁶⁻²⁸ and resonance fluorescence²⁹ measurements. The spin of the 786 $(\frac{1}{2}^+)$ and 1039 $(\frac{1}{2}^+)$ keV levels has been determined recently by Behar et al.22 by angular correlation and polarization experiments. Previous angular correlation measurements on the 582-203 keV cascade yielded a spin $\frac{1}{2}^+$ for the 786 keV state as well.^{20,30} Spins $\frac{1}{2}$, $\frac{3}{2}$, $\frac{5}{2}$, or $\frac{7}{2}$ for the 820 keV level are consistent with the present angular distribution measurements whereas either spin $\frac{3}{2}$ or $\frac{5}{2}$ is consistent for the 1056 keV level. However, Behar et al.²² establish the spin of the 820 keV level as $\frac{3}{2}^+$ and this assignment is confirmed by a recent ⁹⁴Mo(¹³C, ¹²C)⁹⁵Mo reaction study.³¹ On the other hand, Dielh et al.²⁴ favor a spin $\frac{5}{2}^+$ for the 1056 keV level from the value of the ratio S(d, t)/S(d, p).

Spins $\frac{7}{2}^+$ or $\frac{9}{2}^+$ were previously suggested for the 947 keV level.^{13,23,24} Our angular distribution measurements are consistent only with a $\frac{9}{2}^+$ assignment for the 947 keV level, and a $\frac{7}{2}^+$ for the 1073 keV level, in agreement with the results of Mesko *et al.*⁴ and Lederer, Jaklevic, and Hollander.²

⁹⁷Mo nucleus. Since our previous investigation on the level structure of ⁹⁷Mo⁵ another level at 1284 keV has been excited. Furthermore, the existence of a level at 840 keV is also suggested. Either spin $\frac{3}{2}$ or $\frac{5}{2}$ for the 1284 keV level is consistent with our A_2 value for the 1284 keV γ ray (see Table III). However, an appreciable fraction of the $2d_{3/2}$ single-particle state has been assigned to a level at 1.27 MeV.^{32,33} This state cannot be the 1268 keV level since, being excited directly in the ⁹⁷Nb decay,³⁴ its spin must be either $\frac{7}{2}$ ⁺ or $\frac{9}{2}^+$. Hence, spin $\frac{3}{2}^+$ for the 1284 keV level has been taken as the most probable one. A weak transition at 840 keV was observed only in the ⁹⁷Mo spectra. This transition has not been reported in any earlier studies of ⁹⁷Mo and cannot be fitted between any two known levels of this nucleus. The yield of this transition as a function of projectile energy is consistent with an E2 excitation of a possible new state at 840 keV. It is for this reason that the existence of such a state is proposed in this investigation. It is clear, however, that this is merely a suggestion and much additional information is needed to confirm or reject it.

Previous Coulomb excitation measurements on 97 Mo were performed by Alkhazov *et al.*¹² who Coulomb excited two levels at 0.67 and 1.02 MeV $[B(E2^{+})=0.54\pm0.17 \text{ and } 4.3\pm0.9 \text{ in units of } 10^{-50} e^2 \text{ cm}^4]$. These authors associated the 0.67 MeV level to the 658 keV state which is strongly ex-

cited in the 97 Nb decay.³⁴ However, our results show that their level should be associated to the 679 keV state. With this in mind, the agreement between their results and ours becomes satisfactory.

The present angular distribution results establish the spin of the 480 keV state as $\frac{3}{2}$. The A_2 and A_{4} coefficients for the 480 keV transition are consistent with either of the two δ values shown in Table III. These δ values would yield half-lives equal to 13.0 ± 2.1 psec ($\delta = -0.47 \pm 0.03$) and 68 ± 5 psec ($\delta = -4.4 \pm 0.4$). However, Bond³⁵ has recently measured the half-life of some levels in ⁹⁷Mo by the Doppler shift attenuation method following the Coulomb excitation of levels in ⁹⁷Mo by ³⁵Cl projectiles. This author obtained a half-life for the 480 keV level equal to 8.50 ± 0.35 psec. Hence, the larger δ value can be discarded. The 658 keV level is very weakly excited in the Coulomb excitatation measurements. The calculated mixing ratio of the 658 keV transition (see footnote in Table IV) is in agreement with one of the two possible values measured by Behrens and Brodt,³⁶ i.e., $\delta < 0.07$. The angular distributions of the 679 and 407 keV transitions are, within the experimental errors, isotropic, supporting spin $\frac{1}{2}$ for the 679 and 888 keV levels. This assignment is in agreement with data from the reaction ${}^{96}Mo(d, p){}^{97}Mo{}^{32}$ which revealed that the $3s_{1/2}$ quasiparticle excitation is split between levels at about 690 and 890 keV.

The angular distribution of the 238 keV transition is neither consistent with spin $\frac{1}{2}$ nor $\frac{7}{2}$ for the 719 keV level. Furthermore, the placing of the 397 keV cascade transition from the 1116 keV state $(\frac{9}{2}^+$ see below) limits the spin of the 719 keV level to $\frac{5}{2}^+$.

The present angular distribution results are consistent with spins $\frac{3}{2}$, $\frac{5}{2}$, or $\frac{7}{2}$ for the 721 keV level. However, a level corresponding to the excitation of a neutron in the $2d_{3/2}$ shell has been observed by Kent, Cohen, and Moore³³ at 0.73 MeV. If the suggestion of a $\frac{5}{2}^+$ spin for the 719 keV level holds, it is reasonable to propose a spin $\frac{3}{2}^+$ for the 721 keV level.

The 1024 and 1116 keV levels are directly excited by allowed β transitions in the decay of ⁹⁷Nb.³⁴ This establishes the spin of those states as either $\frac{7}{2}$ ⁺ or $\frac{9}{2}$ ⁺. Considering only these two possibilities, the present angular correlation measurements are consistent only with spin $\frac{7}{2}$ ⁺ for the 1024 keV level and spin $\frac{9}{2}$ ⁺ for the 1116 keV level, in agreement with the results of Mesko *et al.*⁴ and Lederer *et al.*²

The present angular distribution results establish the spin of the 1092 keV level as $\frac{3}{2}$. This state, whose existence was proposed also by Mesko *et al.*,⁴ has not been observed in any other previous study of the ⁹⁷Mo level structure.

The spin of the 1268 and 1515 keV levels is either $\frac{7}{2}^+$ or $\frac{9}{2}^+$ since they are excited by allowed β transitions in the decay of ⁹⁷Nb.³⁴ However, Mesko *et al.*⁴ strongly favor a $\frac{7}{2}^+$ assignment for the 1268 keV level. From our Coulomb excitation experiments very little can be said on the properties of this state for it is very weakly excited and no angular distribution measurements could be performed on the transitions deexciting this level. On the other hand, our angular distribution measurements on the 1515 keV transition, carried out with 10 MeV α particles, are consistent only with spin $\frac{9}{2}^+$ in agreement with the proposition of Mesko et al.⁴ These authors also fitted a 246.4 keV γ ray between this level and the 1268.8 keV state. This transition was not detected in the present work.

B. Comparison with nuclear models

The level schemes of ⁹⁵Mo and ⁹⁷Mo calculated for the configurations $(\pi p_{1/2})^2 (\pi g_{9/2})^2 (\nu d_{5/2})^3$ $({}^{95}Mo)^{7,8}$ and $(\pi p_{1/2})^2 (\pi g_{9/2})^2 (\nu d_{5/2})^{-1} ({}^{97}Mo)^8$ are shown in Figs. 4 and 5 (${}^{95}Mo$ and ${}^{97}Mo$, respectively), together with the experimental level schemes obtained in the present investigation.

The only apparent success of these calculations is the prediction of the low-lying $\frac{3}{2}^+$ state in ⁹⁵Mo. This state corresponds essentially to a $|(g_{9/2})^2_0(d_{5/2})^3_{3/2};\frac{3}{2}\rangle$ configuration. Vervier⁸ calculated the *E*2 and *M*1 reduced transition probabilities for the 203 keV transition deexciting the 203 keV state in ⁹⁵Mo. The *B*(*E*2) and *B*(*M*1) values are 8.9 $(10^{-2} e^2 b^2)$ and $8 \times 10^{-3} [(e\hbar/2Mc)^2]$ which should be compared with the 5.70 ± 0.24 and 4.49 ± 0.12 values determined in this work. The order of magnitude for the *B*(*M*1) is correct but the *B*(*E*2) value is too large considering that the same type of calculation predicts *B*(*E*2) values for the even-even molybdenum nuclei 30 to 50% lower than those experimentally measured.^{1,6} As already stated by Vervier, these calculations could be improved by the inclusion of more single-particle states as $1g_{7/2}$, $3s_{1/2}$, and $2d_{3/2}$ in the excitation spectrum of the neutrons.

Kisslinger and Sorensen (KS)⁹ have predicted levels in ⁹⁵Mo and ⁹⁷Mo by considering a shortrange pairing force and a long-range quadrupole force interacting with a spherical core. The KS predictions are compared with the experimental level schemes of ⁹⁵Mo and ⁹⁷Mo in Figs. 4 and 5. From an inspection of Figs. 4 and 5, one can conclude that the model of KS gives a poor description of the nuclear structure of both ⁹⁵Mo and ⁹⁷Mo. This conclusion is also borne out by the B(E2)values recently calculated by Reehal and Sorenson³⁷ for some transitions in ⁹⁵Mo and ⁹⁷Mo. The E2 transition rates calculated by these authors are shown in Table VI with the B(E2) deduced in the present experiment. Since the correspondence



FIG. 4. Comparison of the level scheme of 95 Mo as evinced in this investigation with the theoretical level schemes deduced by Bhatt and Ball (Ref. 7), Vervier (Ref. 8), Kisslinger and Sorensen (Ref. 9), and Choudhury and Clemens (Ref. 10).



FIG. 5. Comparison of the level scheme of 97 Mo as evinced in this investigation with the theoretical level schemes deduced by Vervier (Ref. 8), Kisslinger and Sorensen (Ref. 9), and Choudhury and Clemens (Ref. 10).

Isotope	$J_i^{\pi} \rightarrow J_f^{\pi}$	$\frac{B \left(E2; \boldsymbol{J}_{i} \rightarrow \boldsymbol{J}_{f} \right)_{\text{th}}}{(10^{-50} \ \boldsymbol{e}^{2} \text{ cm}^{4})}$	Eγ (keV)	$ \begin{array}{c} B \left(E2; J_i \rightarrow J_f \right)_{\exp} \\ (10^{-50} \ e^2 \ \mathrm{cm}^4) \end{array} $
⁹⁵ Mo	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	2.42	203.94	5.70 ± 0.36
			820.8	0.090 ± 0.023
	$\frac{1}{2}^+ \rightarrow \frac{5}{2}^+$	12.1	786.21	0.98 ± 0.06
			1039.3	1.65 ± 0.30
	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	10.8	582.15	$1.0^{+0.6}_{-0.4}$
			835.14	0.07^{+0}_{-0}
	$\frac{7^+}{2} \rightarrow \frac{5^+}{2}$	1.18	765.9	<0.010
			1073.8	2.90 ± 0.16
⁹⁷ Mo	$\frac{3}{2}^+ \rightarrow \frac{5}{2}^+$	0.72	480.9	3.07 ± 0.17
			1092.6	0.52 ± 0.04
	$\frac{1}{2}^+ \rightarrow \frac{5}{2}^+$	8.82	679.6	1.38 ± 0.09
			888.1	0.55 ± 0.06
	$\frac{7}{2}^+ \rightarrow \frac{5}{2}^+$	0.18	658.2	0.035 ± 0.005
			1024.6	3.40 ± 0.18
	$\frac{7}{2}^+ \rightarrow \frac{3}{2}^+$	5.84	177.97	7.9^{+4}_{-2}
			543.8	1.3_{-0}^{+1}

TABLE VI. Comparison between the $B(E2; J_i \rightarrow J_f)$ values experimentally determined in this work and those calculated by Reehal and Sorensen for ⁹⁵Mo and ⁹⁷Mo.

between the experimental and theoretical levels is not completely evident, we have sometimes considered the first two states with the same spin. An inspection of Table VI shows that the results of Reehal and Sorensen are not in agreement with experiment.

It is also interesting to compare our data with the predictions of the core excitation model.³⁸ According to this model a multiplet of excited states of spins $\frac{1}{2}$, $\frac{3}{2}$, $\frac{5}{2}$, $\frac{7}{2}$, and $\frac{9}{2}$ should arise from coupling a $2d_{5/2}$ neutron (or hole) to the 2^+ core state identified with the first 2^+ level in the neighboring even nucleus (⁹⁴Mo and ⁹⁶Mo, respectively). The B(E2*) of these states should be nearly equal to the $B(E2; 2^+ \rightarrow 0^+)$ value for the even-core nucleus. These levels should not be excited in one particle transfer reactions. M1 transitions are allowed between members of this multiplet of levels (if ΔI permits), whereas ground state M1 transitions are strictly forbidden. Finally, the sum of the reduced $B(E2\uparrow)$ transitions should be equal to the $B(E2; 0^+ - 2^+)$ value for the even-core nucleus. The comparison of the $B(E2\uparrow)$ values with the core-excitation predictions is summarized in Table VII where the factor F_{ph} is the ratio $B(E2^{\ddagger})/B(E2; 2^{+} \rightarrow 0^{+})_{core}$. The $B(E2; 2^{+} \rightarrow 0^{+})$ value is taken for the next lowest even-mass nucleus, i.e., ⁹⁴Mo and ⁹⁶Mo (see Refs. 1 and 6).

Furthermore the $B(E24)/B(E2)_{s,p.}$ and $B(M14)/B(M1)_{s,p.}$ ratios are also included in the table.

An inspection of Table VII shows that both in ⁹⁵Mo and ⁹⁷Mo the levels with spins $\frac{3}{2}^{+}$, $\frac{7}{2}^{+}$, and $\frac{9}{2}^{+}$ (at 203, 1073, and 947 keV in ⁹⁵Mo, and at 480, 1024, and 1116 keV in ⁹⁷Mo) have a sufficiently large value of F_{ph} to be associated with states due to the excitation of the core. On the other hand, the probable $\frac{5}{2}^{+}$ 1056 keV level in ⁹⁵Mo does not show much of a collective nature (F_{ph} = 0.30), and the 719 keV ($\frac{5}{2}^{+}$) level in ⁹⁷Mo is certainly not consistent with the core excitation model (F_{ph} = 0.069). Furthermore, it seems that the core-excitation strength of the $\frac{1}{2}^{+}$ member of the multiplet is shared between pairs of levels both in ⁹⁵Mo and ⁹⁷Mo (the 786 and 1039 keV levels, and the 679 and 888 keV levels, respectively).

These findings are consistent with (d, p) reaction data. In fact, the 203 and 947 keV levels in ⁹⁵Mo are very weakly excited in (d, p) reaction work²³ and the 1073 keV state is not observed at all, whereas the 786 and 1039 keV states display relatively large (d, p) spectroscopic factors (0.37 and 0.19, respectively). This might indicate that the wave functions describing these levels contain significant mixing of core-excitation and singlequasiparticle component of the $3s_{1/2}$ shell. The 765 $\left(\frac{7}{2}^{+}\right)$ and 820 keV $\left(\frac{3}{2}^{+}\right)$ levels show relatively large spectroscopic factors (0.18 and 0.25, respectively) indicating that these levels might arise as a result of the excitation of a neutron in the $1g_{7/2}$ and $2d_{3/2}$ shells. The 1056 keV $(\frac{5}{2}^+)$ level was not observed in the ${}^{94}Mo(d, p)$ reaction work.²³

A similar picture exists also in ⁹⁷Mo. In fact, Hjorth and Cohen³² have determined a S(d, p) value equal to 1.28 for a $\frac{7}{2}^+$ level at 0.699 MeV which, most probably, corresponds to the very weakly Coulomb excited level at 658 keV. This level can be associated to the excitation of a neutron in the $1g_{7/2}$ shell. The $\frac{1}{2}^+$ levels excited at 0.699 and 0.893 MeV, corresponding to our levels at 679 and 888 keV, have spectroscopic factors of 0.55 and 0.11, respectively. As in ⁹⁵Mo, it is probable that these two levels display appreciable mixing of core-excitation and single-quasiparticle component. The 480 $(\frac{3}{2}^+)$, 1024 $(\frac{7}{2}^+)$, and 1116 keV $(\frac{9}{2}^+)$ levels have not been observed by these authors, and this is consistent with their collective properties. No definite conclusion can be drawn for the 719 $\left(\frac{5}{2}^{+}\right)$ and 721 keV $\left(\frac{3}{2}^{+}\right)$ states. Information on the M1 transition rates of transitions decaying to the ground state in ⁹⁵Mo and ⁹⁷Mo is shown in Table VII, and the data on the M1 transition rates of transitions between excited states are summarized in Table VIII.

An inspection of Table VII and VIII shows that the predictions of the core-excitation model are

Isotope	E _{level} (keV)	J^{π}	F _{ph} ^a	$B(E2\downarrow)/B(E2)_{s.p.}^{b}$	$B(M1\downarrow)/B(M1)_{s.p.}$ c
⁹⁵ Mo	203.94	$\frac{3}{2}^{+}$	1.31 ± 0.11	22.1 ± 1.4	$(2.35 \pm 0.12) \times 10^{-3}$
	765.9	$\frac{\frac{7}{7}}{2}$	<0.002	<0.04	$2.4^{+1}_{-0.8}$ $\times 10^{-2}$
	786.21	$\frac{1}{2}^{+}$	0.22 ± 0.02	3.8 ± 0.2	
	820.8	$\frac{3}{2}^{+}$	$\textbf{0.020} \pm \textbf{0.006}$	0.35 ± 0.09	>1.7 $\times 10^{-3}$ d
	947.8	$\frac{9}{2}^{+}$	0.72 ± 0.06	12.2 ± 0.6	
	1039.3	$\frac{1}{2}^{+}$	0.38 ± 0.08	6.4 ± 1.2	
	1056.8	$(\frac{5}{2})^+$	0.30 ± 0.03	5.0 ± 0.3	1.8^{+8}_{-1} ; $\times 10^{-2}$
	1073.7	$\frac{7}{2}^{+}$	0.66 ± 0.06	11.2 ± 0.6	2.5^{+1}_{-0} ; $^{2}_{7}$ × 10 ⁻²
⁹⁷ Mo	480.9	$\frac{3}{2}^{+}$	0.54 ± 0.05	11.6 ± 0.6	$(1.2 \pm 0.2) \times 10^{-2}$
	658.2	$\frac{7}{2}^{+}$	0.006 ± 0.001	0.13 ± 0.02	$3.9^{+1}_{-0.8}$ $\times 10^{-2}$
	679.6	$\frac{1}{2}^{+}$	0.24 ± 0.02	5.2 ± 0.4	
	719.3	$\frac{5}{2}^{+}$	0.069 ± 0.008	1.47 ± 0.11	$3.6^{+2}_{-1.3}$ × 10 ^{-2 d}
	721.1	$(\frac{3}{2})^+$	0.044 ± 0.005	0.95 ± 0.09	$1.4^{+4}_{-0.8}$ × 10 ^{-2 d}
	888.1	$\frac{1}{2}^{+}$	0.096 ± 0.013	2.1 ± 0.2	
	1024.6	$\frac{7}{2}^{+}$	0.60 ± 0.05	12.8 ± 0.7	4.7^{+4}_{-2}
	1092.6	$\frac{3}{2}^{+}$	0.091 ± 0.009	1.95 ± 0.14	$1.0^{+1}_{-0.6}$ × 10 ⁻²
	1116.7	$\frac{9}{2}^{+}$	0.48 ± 0.05	10.3 ± 0.7	
	1268.6	$\frac{7}{2}^{+}$	0.13 ± 0.03	2.7 ± 0.6	
	1284.6	$(\frac{3}{2})^+$	0.11 ± 0.03	2.4 ± 0.5	$6.0^{+13}_{-4.0} \times 10^{-3}$
	1515.5	$\frac{9}{2}^+$	0.056 ± 0.010	1.2 ± 0.2	

TABLE VII. Enhancements and hindrances of E2 and M1 transitions to the ground states of 95 Mo and 97 Mo.

 ${}^{a}F_{ph}$ is the ratio $B(E_{24})/B(E_{2}; 2^{+} \rightarrow 0^{+})$. The $B(E_{2}; 2^{+} \rightarrow 0^{+})$ values are taken for the next lowest even-mass nuclei, i.e., 94 Mo and 96 Mo (see Refs. 1 and 6).

^b For the definition of $B(E2)_{s.p.}$ see Table V.

 $^{c}B(M1)_{s.p.} = e^{2}/4\pi [(\frac{3}{4})^{2}] \times 10 [(\hbar/2Mc)^{2}].$

^d Only the more probable B(M1+) values has been considered for these transitions. See Table IV and text.

partially supported by the experimental data. The ground-state M1 transitions are retarded. However, this hindrance is expected also within the framework of the shell-model, since M1 transitions are allowed only for levels corresponding to the excitation of the $d_{3/2}$ shell. It appears that the less retarded M1 transitions are those between "members of the multiplet." The fact that the 253 keV transition in ⁹⁵Mo is so strong can be explained by the possible sharing of the one-phonon state between the 786 and 1039 keV levels. The B(M1)values of the 835 and 582 keV transitions (⁹⁵Mo) show that the 1039 keV level has a larger component of the one-phonon state than the 786 keV level. This conclusion is consistent with the F_{ph} and S(d, p) values attached to these states. Finally, we compare the prediction that the sum of the observed E2 strengths should be equal to that of the

 2^+ state of the neighboring even-nuclei (this, in absence of polarization of the nucleus by the oddnucleon which would give rise to a static quadrupole moment Q_g for the ground state of the odd-*A* nucleus). Although the complete set of the multiplet members is not well delineated in both nuclei, the above rule should be applicable under the assumption that all the *E*2 excitation strength is derived from core excitation. The results are shown in Table IX.

It appears that the $\sum B(E2^{\dagger})$ over the observed states in ⁹⁵Mo and ⁹⁷Mo falls far short of such expectations. Attributing the "missing" fraction of the $\sum B(E2^{\dagger})$ to the ground-state quadrupole strength $B(E2; I_g \rightarrow I_g)$, which is given by

$$B(E2; I_g - I_g) = \frac{5}{16\pi} \frac{(I_g + 1)(2I_g + 3)}{I_g(2I_g - 1)} Q_g^2 ,$$

Isotope	<i>E</i> γ (keV)	$E_{l_i} \rightarrow E_{l_f}$	$J_i^{\pi} \rightarrow J_f^{\pi}$	$B(M1)/B(M1)_{s.p.}$
⁹⁵ Mo	125.8 ^a	$1073 \rightarrow 947$	$\frac{7}{2}^+ \rightarrow \frac{9}{2}^+$	$2.6^{+1}_{-0.8}$ × 10 ⁻¹
	181.5 ^a	947 ightarrow 765	$\frac{9}{2}^+ \rightarrow \frac{7}{2}^+$	$(3.4 \pm 1.0) \times 10^{-3}$
	219.4 ^a	1039 → 820	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	$1.8^{+1}_{-0.9}$ × 10^{-2}
	253.2 ^a	$1039 \rightarrow 786$	$\frac{1}{2}^+ \rightarrow \frac{1}{2}^+$	$(1.3 \pm 0.6) \times 10^{-1}$
	307.8 ^a	$1073 \rightarrow 765$	$\frac{7}{2}^+ \longrightarrow \frac{7}{2}^+$	$1.2^{+0}_{-0}:^{5}_{3} \times 10^{-2}$
	582.15	$786 \rightarrow 203$	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	$(1.8 \pm 0.3) \times 10^{-2}$
	617.4 ^b	$820 \rightarrow 203$	$\frac{3}{2}^+ \rightarrow \frac{3}{2}^+$	>1.3 ×10 ⁻⁴
	835.14	$1039 \rightarrow 203$	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	$(1.5 \pm 0.4) \times 10^{-1}$
	852.8	$1056 \rightarrow 203$	$\left(\frac{5}{2}\right)^+ \rightarrow \frac{3}{2}^+$	$1.3^{+4}_{-0.7} \stackrel{8}{\times} 10^{-1}$
⁹⁷ Mo	238.5 ^b	$719 \rightarrow 480$	$\frac{5}{2}^+ \rightarrow \frac{3}{2}^+$	$3.9^{+2}_{-1.4}$ × 10 ⁻²
	366.3	$1024 \rightarrow 658$	$\frac{7}{2}^+ \rightarrow \frac{7}{2}^+$	4.5^{+3}_{-1} ; $^{9}_{9} \times 10^{-2}$
	407.0 ^a	888→480	$\frac{1}{2}^+ \rightarrow \frac{3}{2}^+$	$(1.2 \pm 0.3) \times 10^{-1}$
	458.5 ^a	$1116 \rightarrow 658$	$\frac{9}{2}^+ \rightarrow \frac{7}{2}^+$	$(3.6 \pm 0.7) \times 10^{-3}$
	611.9 ^a	$1092 \rightarrow 480$	$\frac{3}{2}^+ \rightarrow \frac{3}{2}^+$	$7^{+9}_{-4} imes 10^{-3}$
	857.3 ^b	1515→658	$\frac{9}{2}^+ \rightarrow \frac{7}{2}^+$	$(6 \pm 3) \times 10^{-3}$

TABLE VIII. Hindrances of M1 transitions between excited states of 95 Mo and 97 Mo.

^a These γ rays have been assumed as pure *M*1 transitions. See Table IV.

^b Only the more probable B(M1+) value has been considered for these transitions. See Table IV and text.

we have calculated this factor from the known static quadrupole moment of the ground state of ⁹⁵Mo and ⁹⁷Mo.^{16,17} The results are shown in the third column of Table IX. In ⁹⁵Mo the Q_g value is not sufficient to warrant agreement with the theory, whereas in ⁹⁷Mo the $B(E2; I_g + I_g)$ term is already larger than the $B(E2; 0^+ \rightarrow 2^+)_{core}$. The static quadrupole moment values which would warrant agreement with the theory have been calculated and are shown in the last column of Table IX. For ⁹⁷Mo this calculated value is not very different from the experimental one.¹⁷ This arises from the fact that the ground-state quadrupole strength $B(E2; I_g \rightarrow I_g)$ varies rapidly with small variations in Q_g .

TABLE IX. Comparison of the sum of the observed E2 strengths in ⁹⁵Mo and ⁹⁷Mo with $B(E2; 0^+ \rightarrow 2^+)_{\text{core.}}$

Isotope	$\frac{\sum B(E2)^{a}}{B(E2; 0^{+} \rightarrow 2^{+})_{\text{core}}}$	$\frac{B(E2; I_g \rightarrow I_g)_{exp}}{B(E2; 0^+ \rightarrow 2^+)_{core}}$	$Q_{\boldsymbol{g}_{calc}}$ (e b)
⁹⁵ Mo ⁹⁷ Mo	0.70 ± 0.06 0.52 ± 0.06	$\begin{array}{c} 0.02 \pm 0.01 \\ 1.2 \substack{+0.5 \\ -0.4} \end{array}$	$\begin{array}{c} 0.49 \pm 0.06 \\ 0.70 \pm 0.05 \end{array}$

^a The sum $\sum (E2\dagger)$ does not include the $B(E2; I_g \rightarrow I_g)$ term; the $B(E2; 0^+ \rightarrow 2^+)_{core}$ values have been taken from Refs. 1 and 6. See also Table VII.

In conclusion, few of the predictions of the coreexcitation model are in agreement with experiment for ⁹⁵Mo and ⁹⁷Mo, and considerable mixing of states should be invoked to explain the level properties of these nuclei.

The most recent theoretical investigation on the level structure of 95 Mo and 97 Mo is that carried out by Choudhury and Clemens¹⁰ within the frame-work of the unified model. The calculated level schemes of 95 Mo and 97 Mo are compared with the experimental ones in Figs. 4 and 5.

The experimental level density in ⁹⁵Mo is well reproduced by the calculations of Choudhury and Clemens.¹⁰ The fact that the existence of the $\frac{3}{2}^{+}$ level at ~200 keV is well predicted by the model is a direct consequence of the introduction in the calculations of the configuration $(2d_{5/2})^{-3}_{3/2}$. Even though the level sequence is not respected, all the levels observed below 1.2 MeV seem predicted at approximately the proper energy. The theory fails to give agreement with experiment in ⁹⁷Mo. Only the first $\frac{7}{2}^+$ and $\frac{1}{2}^+$ calculated levels seem to be consistent with states observed experimentally at approximately the same energy. As a more stringent test of the theoretical calculations of Choudhury and Clemens,¹⁰ the calculated electromagnetic transition rates for ground-state transitions both in ⁹⁵Mo and ⁹⁷Mo were compared with those deduced in this experiment. The results of this comparison are summarized in Table X.

An inspection of Table X shows that all the M1transition rates are retarded in agreement with experiment. However, this hindrance is due to the fact that M1 transitions are forbidden between the principal components of the wave functions describing these levels. Thus, the calculated M1transition probabilities depend on the amplitude of the weaker components and are very sensitive to small variations in the wave functions. Furthermore, the magnetic dipole operator is a function of an effective orbital and spin gyromagnetic factors for the particles, and of a gyromagnetic factor of the core. These quantities could be considered as parameters of the calculations, hence the comparison with the M1 transition probabilities is not very significant and does not yield very useful information on the nuclear level properties.

As can be seen from Table X, all the calculated E2 transition rates are enhanced. In fact, even if the level energy is much displaced with respect to the calculated energy, all these levels contain a very important part of the one-phonon state. Thus, even for the 203 keV level in ⁹⁵Mo the E2 transition probability arises from the collective component of the wave function. Hence, these E2 transition probabilities show that all these levels should correspond to the most collective states excited in

Isotope	E_1^{a} (keV)	$J_i^{\pi} \rightarrow J_f^{\pi}$	$B(E2\downarrow)_{\rm th}$ (10 ⁻⁵⁰ $e^2 {\rm cm}^4$)	$B(E2\downarrow)_{exp}$ $(10^{-50} e^2 cm^4)$	$B (M1)_{th}$ [$(e\hbar/2Mc)^2$]	B (M1↓ [(eħ/2M	$\left[c\right] ^{2}$
⁹⁵ Mo	203.94	$\frac{3}{2}^+ \rightarrow \frac{5^+}{2}$	5.7	5.70 ± 0.36	1.6×10 ⁻³	(4.21±0.22)×10 ⁻³
	(201) 947.8 (695)	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	5.4	3.15 ± 0.15			5
	(033) 1039.3 (782)	$\frac{1}{2}^+ \longrightarrow \frac{5}{2}^+$	4.2	1.65 ± 0.30			
	(782) 1073.7 (720)	$\frac{7}{2}^+ \longrightarrow \frac{5}{2}^+$	5.0	2.90 ± 0.16	6.6×10^{-4}	$4.5^{+2.1}_{-1.3}$	$\times 10^{-2}$
⁹⁷ Mo	480.9 (948)	$\frac{3}{2}^+ \longrightarrow \frac{5}{2}^+$	3.3	3.07 ± 0.17	2.5×10^{-1}	(2.2 ± 0.4)	×10 ⁻²
	679.6	$\frac{1}{2}^+ \longrightarrow \frac{5}{2}^+$	6.9	1.38 ± 0.09			
	719.3	$\frac{5}{2}^+ \rightarrow \frac{5}{2}^+$	2.8	$\textbf{0.39} \pm \textbf{0.03}$	7.2×10^{-2}	6.4^{+4}_{-2}	×10 ⁻³
	(1013) 1024.6 (646)	$\frac{7^+}{2} \rightarrow \frac{5^+}{2}$	7.2	3.40 ± 0.18	1.8×10^{-1}	$8.5_{-3.6}^{+7.9}$	$\times 10^{-2}$
	(340) 1116.7 (720)	$\frac{9}{2}^+ \rightarrow \frac{5}{2}^+$	5.9	2.74 ± 0.19			

TABLE X. Comparison of the theoretical and experimental electromagnetic transition rates for ground-state transitions in 95 Mo and 97 Mo.

^a The energy values in parentheses are those predicted by Choudhury and Clemens (see Ref. 10).

^b Only the more probable B(M1+) value has been considered for these transitions. See Table IV and text.

this experiment. Under this assumption the first $\frac{7}{2}^+$ level, predicted at 720 keV (⁹⁵Mo) and 646 keV (^{97}Mo) should be associated to the 1073 (^{95}Mo) and 1024 keV (97 Mo) levels, and not to the 765 (95 Mo) and 658 keV (⁹⁷Mo) levels. Similarly, the first $\frac{3}{2}$ state predicted at 948 keV in ⁹⁷Mo shows an E2 transition probability which is more consistent with the 480 keV observed level than with the 1092 keV state. The $\frac{9}{2}^+$ levels predicted at approximately 700 keV in both nuclei should correspond to the excited 947 (95Mo) and 1116 keV (⁹⁷Mo) levels. Finally, an inspection of Table X shows that the calculated E2 transition rates are larger than those deduced experimentally, with the exception of the first excited levels in ⁹⁵Mo and ⁹⁷Mo. This in spite of the fact that we have chosen the levels with the most enhanced E2 transitions.

The logical conclusion arising from the aforementioned points is that the validity of the model of Choudhury and Clemens¹⁰ is less evident when the comparison between the theoretical and experimental electromagnetic transition rates is carried out. This also for ⁹⁵Mo for which there was apparent agreement with experiment in the placing of levels.

C. Comparison with the level structure of ⁹⁹Ru and ¹⁰¹Ru

As a conclusion of the present work, we would like to compare the level schemes of 95Mo and

 ^{97}Mo with those of ^{99}Ru and $^{101}Ru.$ In Fig. 6 the level schemes of ⁹⁵Mo and ⁹⁷Mo are shown with those of ⁹⁹Ru and ¹⁰¹Ru as deduced in Coulomb excitation work.³⁹ The spin-parity assignment for some levels in ⁹⁹Ru and ¹⁰¹Ru is due to Lederer et al.² who studied these nuclei by the ^{98,100}Mo- $(\alpha, 3n\gamma)$ reaction. Except for the fact that the ruthenium isotopes generally display a more pronounced collective nature, and that their level energies are lower than those for the molybdenum isotopes, several common properties appear in these four nuclei whose neutron number ranges from 53 to 57, i.e., 3 to 7 neutrons outside the magic shell of N = 50. For instance: (i) The ground-state has spin $\frac{5}{2}^+$; (ii) the first excited state has spin $\frac{3}{2}^+$, it is strongly collective and lies at a much lower energy than the other states; (iii) the first $\frac{7}{2}^+$ state is very weakly Coulomb excited; (iv) there are three excited levels which display more of a collective nature than the others, i.e., the first $\frac{3^+}{2}$ and $\frac{9^+}{2}$ levels, and the second $\frac{7^+}{2}$ level.

The $\frac{5}{2}$ ⁺ spin of the ground state in ⁹⁵Mo, ⁹⁷Mo, and ⁹⁹Ru is explained by the shell model⁴⁰ which predicts that the first 5 neutrons outside the 50 neutron magic shell fill up the $2d_{5/2}$ shell. Hence, the ground state of these nuclei shows a neutron configuration $(2d_{5/2})^3_{5/2}$ or $(2d_{5/2})^5_{5/2}$. If more neutrons are added, the shell model predicts that the pairing energy will be larger for the two neutrons in the $1g_{7/2}$ shell than in the $2d_{5/2}$ shell. Thus, the ground-state configuration of 101 Ru will be $(1g_{7/2})^2_0$ $(2d_{5/2})^5_{5/2}$. A similar situation exists also in 105 Pd (59 neutrons) and even in 107 Cd (61 neutrons). For these nuclei the ground-state configuration is, most probably, $(1g_{7/2})^4_0 (2d_{5/2})^5_{5/2}$ and $(1g_{7/2})^6_0 (2d_{5/2})^5_{5/2}.^{40}$

The first $\frac{7}{2}^{+}$ excited state, which is weakly excited in Coulomb excitation, could be associated to the excitation of an unpaired neutron of the $2d_{5/2}$ shell to the $1g_{7/2}$ shell. This suggestion is supported for the molybdenum isotopes by the results extracted in (d, p) reaction experiments.^{23,32} Lederer *et al.*² excited levels with large angular

momentum values in all these nuclei, and proposed the existence of a set of states with spins $\frac{7}{2}^+$, $\frac{11}{2}^+$, and $\frac{15}{2}^+$ forming a band having as bandhead the aforementioned $\frac{7}{2}^+$ level. These authors suggest that this band could arise from the coupling of the unpaired neutron in the $1g_{7/2}$ shell to the configuration $(2d_{5/2})_{0^+,2^+,4^+}^{2\,\circ\,r\,4}$. However, one could consider the coupling of this unpaired neutron to the proton configuration $(1g_{9/2})_{0^+,2^+,4^+,6^+,8^+}^{2\,\circ\,r\,4}$, or to the quadrupole vibrations of the even core. Under this assumption, the $\frac{19}{2}^+$ and $\frac{23}{2}^+$ levels observed in 95 Mo and 97 Mo could be included in this same band. If such a band exists, one should have also a band built on the ground state with spins $\frac{5}{2}^+$, $\frac{9}{2}^+$, $\frac{13}{2}^+$, $\frac{17}{2}^+$, ... which could explain the collective char-



FIG. 6. Comparison of the level schemes of 95,97 Mo as evinced in this investigation with those of 99,101 Ru obtained by Coulomb excitation measurements (see Ref. 39). The spin assignment for some levels of 99 Ru and 101 Ru is due to Lederer *et al.* (Ref. 2), whereas the $B(E2^{\dagger})$ values are those obtained in Ref. 39.

acter of the first $\frac{9}{2}^+$ level. Lederer *et al.*² have observed in ⁹⁵Mo and ⁹⁷Mo levels with spins $\frac{13^+}{2}^+$ and $\frac{17^+}{2}^+$ which could be associated with this groundstate band. If two distinct bands exist, intraband M1 transitions should be forbidden whereas E2transitions should be strongly favored between members of the same band ($\Delta I = 2$). Thus, in order to have a better understanding of the level structure of these nuclei, it would be very interesting to determine the transition rates between the levels with large angular momenta.

The calculations of Vervier,⁸ Bhatt and Ball,⁷ as well as of Choudhury and Clemens¹⁰ show that the low-lying $\frac{3}{2}^+$ level in ⁹⁵Mo is due essentially to the neutron configuration $(2d_{5/2})^{\pm 3}_{3/2}$. However, in ⁹⁷Mo, ⁹⁹Ru, and ¹⁰¹Ru there are five neutrons in the $2d_{5/2}$ shell, and it is not possible to have a $J = \frac{3}{2}$ coupling. Vervier⁸ and Choudhury and Clemens¹⁰ show that in ⁹⁷Mo the coupling of neutrons in the configuration $(2d_{5/2})^{5}_{5/2}$ to the configuration $(1g_{9/2})^2_{2^+}$ or to the even core gives rise to a first excited state $\frac{3^+}{2}$ at much higher energy. Since the $1g_{7/2}$ shell is very close to the $2d_{5/2}$ shell, one can explain the $\frac{3^+}{2}$ level by supposing that the configuration of the ground state of the nuclei with 55 and 57 neutrons is given by $(1g_{7/2})^2_0(2d_{5/2})^3_{5/2}$ and $(1g_{7/2})^4_{0}(2d_{5/2})^3_{5/2}$, respectively. Thus, the $\frac{3}{2}^+$ excited state would have the same origin as that for

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- [‡]Present address: Centre National de la Recherche Scientifique, Université de Lyon, Institut de Physique Nucléaire, Lyon, France.
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⁹⁵Mo, i.e., the coupling of three neutrons in the $2d_{5/2}$ shell. Under this hypothesis, the first $\frac{5}{2}^+$ excited state observed in ⁹⁷Mo, ⁹⁹Ru, and ¹⁰¹Ru, at a close energy to the first $\frac{7}{2}^+$ level, could arise from the $(2d_{5/2})^5_{5/2}$ configuration. In this case, it is normal that this $\frac{5}{2}^+$ level is not observed in ⁹⁵Mo, since this nucleus has only three neutrons outside the magic shell N = 50.

With the exception of the existence of a groundstate band $\frac{5}{2}^+$, $\frac{9}{2}^+$, $\frac{13}{2}^+$, ... which could explain the collective nature of the first $\frac{9}{2}^+$ excited state, we have no ready explanation for the existence of the collective levels $\frac{7}{2}^+$ (second one) and $\frac{9}{2}^+$ placed at an energy slightly higher than that of the 2^+ state in the even nuclei. If these levels are supposed to arise from the coupling of the first 2^+ state of the core, or of a proton configuration $J = 2^+$ with the neutron configuration of the ground state, one should also observe collective levels with spin $\frac{1}{2}^+$, $\frac{5}{2}^+$, and $\frac{3}{2}^+$. However, the $\frac{3}{2}^+$ level should be placed at much higher energy than that of the first $\frac{3}{2}^+$ excited state.

It is evident that the Coulomb excitation measurements indicate that the ^{95,97}Mo and ^{99,101}Ru nuclei share many similarities which should be helpful in the development of a more sophisticated model valid in this region of nuclei.

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