

First measurement of ΛN inelastic scattering with Λ from $e^+e^- \rightarrow J/\psi \rightarrow \Lambda \bar{\Lambda}$

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Using an e^+e^- collision data sample of $(10\,087 \pm 44) \times 10^6 J/\psi$ events taken at the center-of-mass energy of 3.097 GeV by the BESIII detector at the BEPCII collider, the process $\Lambda + N \rightarrow \Sigma^+ + X$ is studied for the first time employing a novel method. The Σ^+ hyperons are produced by the collisions of Λ hyperons from J/ψ decays with nuclei in the material of the BESIII detector. The total cross section of $\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X$ is measured to be $\sigma = (37.3 \pm 4.7 \pm 3.5)$ mb with Λ momenta within [1.057, 1.091] GeV/ c , where the uncertainties are statistical and systematic, respectively. This analysis is the first study of Λ -nucleon interactions at an e^+e^- collider, providing information and constraints relevant for the strong-interaction potential, the origin of color confinement, the unified model for baryon-baryon interactions, and the internal structure of neutron stars.

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Describing baryon-baryon interactions within a unified model has always been a challenge in both particle and nuclear physics [1–4]. Strong constraints and well-established models exist for nucleon-nucleon interactions [1,2], but there are still difficulties in precisely modeling hyperon-nucleon scattering, especially hyperon-hyperon interactions, due to the lack of experimental measurements. Until now, there have only been a few measurements for hyperon-nucleon scattering [5–17], and only one for hyperon-hyperon scattering [18], leaving theoretical models largely unconstrained [19–34].

The properties of hyperons in dense matter have attracted much interest due to their close connection with hypernuclei and the hyperon component in neutron stars [4]. Hyperons may exist within the inner layer of neutron stars whose structure strongly depends on the equation of state (EOS) of nuclear matter at supersaturation densities [35]. The appearance of hyperons in the core softens the EOS, resulting in neutron stars with masses lower than $2M_\odot$ [36], where M_\odot is the mass of the sun. However, studies based on observations from the LIGO and Virgo experiments [37] indicate that the EOS can support neutron stars with masses above $1.97M_\odot$. This is the so-called “hyperon puzzle in neutron stars,” warranting further experimental and theoretical studies.

The first attempts to measure hyperon-nucleon interactions ($\Lambda p \rightarrow \Lambda p$, $\Sigma^- p \rightarrow \Sigma^- p/\Lambda n/\Sigma^0 n$, and $\Sigma^+ p \rightarrow \Sigma^+ p$) were made during the 1960s and 1970s using hyperons with momenta less than 1 GeV/ c [5–9]. After a gap of about 20 years, further studies of elastic and inelastic scatterings between hyperons and nucleons were performed using multiple kinds of hyperons with a variety of beam energies [10–17]. The uncertainties on these measurements were, in general, large. On the theoretical side, many models have been proposed to describe the hyperon-nucleon and hyperon-hyperon interactions, including the meson-exchange model (with Jülich [19] or Nijmegen [20] potentials), chiral effective

field theory (χ EFT) approaches [21–28], calculations on the lattice from HALQCD [29,30] and NPLQCD [31,32], low-momentum models [33], and quark-model approaches [34].

Experimental studies of hyperon-nucleon interactions are challenged by the difficulty of obtaining a stable hyperon beam. Firstly, the lifetime of ground-state hyperons is usually of order $O(10^{-10})$ s due to the weak decay, which is too short to provide a stable beam. Meanwhile, hyperons historically used for fixed-target experiments are commonly produced in the collisions between incident protons or K mesons and the target material, with a high background level. Compared with fixed-target experiments, many more hyperons are accessible from the decay of charmonia produced at e^+e^- colliders, which have rarely been used to study hyperon-nucleon scattering because of the lack of both specialized targets and any practical experimental approach. Furthermore, the large number of antihyperons produced in pairs with hyperons bring exciting prospects for probing little-studied antihyperon-nucleon interactions. In this work, the $\Lambda + N \rightarrow \Sigma^+ + X$ process is studied for the first time by a novel method [38,39], where N denotes a certain kind of nucleus and X refers to any possible particles produced accompanying the Σ^+ , using $\Lambda \bar{\Lambda}$ pairs from the decay of $(10\,087 \pm 44) \times 10^6 J/\psi$ events collected by BESIII [40,41]. This method has been applied in a recent BESIII study of Ξ^0 -nucleus interaction [17]. Thanks to the ‘double-tag’ method, a nearly monochromatic hyperon flux of Λ , Σ^+ , Σ^- , Ξ^- , Ξ^0 , Ω^- , and their antiparticles from charmonia decay are accessible that allows for the study of hyperon-nucleon interactions at e^+e^- colliders.

The BESIII detector is a magnetic spectrometer [42] located at the Beijing Electron Positron Collider (BEPCII). The cylindrical core of the BESIII detector consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight (TOF) system, and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0-T magnetic field. Before particles produced in e^+e^- collisions enter the

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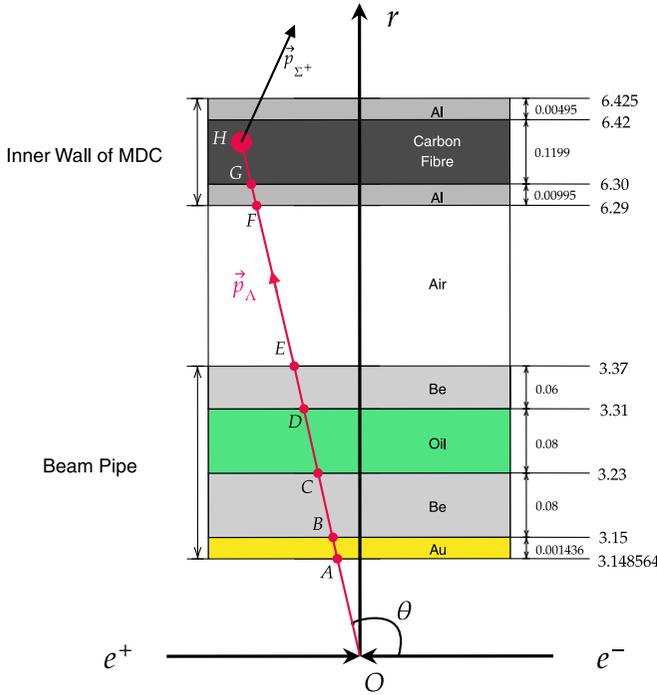


FIG. 1. Illustration of target structure and Λ trajectory inside the target. The target material, composed of the beam pipe and inner wall of the MDC, consists of multiple layers of material, including gold, beryllium, oil, aluminum, and carbon fiber. O is the interaction point of the e^+e^- collision. The horizontal axis is the e^+e^- beam line and the vertical axis (r axis) denotes the distance away from the beam line. The radius and the length of the inner wall of the beam pipe from and along the z axis are 3.148 564 and 100 cm, respectively [42]. The position and the thickness of each layer are listed in the figure, where the units are centimeters. θ is the angle between incident Λ and the z axis. H is the scattering point of Λ and nucleon so that AB, BC, \dots, GH are the Λ track lengths in each layer, where the sum is the total track length inside the target.

spectrometer, they pass through the beam pipe and the inner wall of the MDC, which constitute the scattering targets in the present study. The target structure and the Λ trajectory are shown in Fig. 1, where the Λ hyperons can scatter elastically or inelastically with the nuclei inside these objects. The target is made of multiple layers with different materials, with more detailed information given in Sect. I of the Supplemental Material [43].

Using a GEANT4-based [44] Monte Carlo (MC) package, simulated samples are produced incorporating the geometric description [45] of the BESIII detector and the detector response. An inclusive MC sample containing 1×10^{10} J/ψ decays is used to investigate the potential backgrounds. The production of the J/ψ resonance is simulated by the MC event generator KKMC [46], where the beam-energy spread and the initial-state radiation in the e^+e^- annihilation have been taken into account. The known decay modes are generated by EVTGEN [47,48] using branching fractions taken from the Particle Data Group (PDG) [49], while the unknown decay modes are modeled with LUNDCHARM [50,51]. A signal MC sample with 1×10^6 $\Lambda N \rightarrow \Sigma^+ X$, $\Sigma^+ \rightarrow p\pi^0$ events is generated

to estimate the detection efficiency. The angular distributions of $J/\psi \rightarrow \Lambda \bar{\Lambda}$ and $\bar{\Lambda} \rightarrow \bar{p}\pi^+$ are described by the recently measured decay parameters of the J/ψ and Λ hyperons [52] and $\Lambda N \rightarrow \Sigma^+ X$, $\Sigma^+ \rightarrow p\pi^0$ processes are simulated by the Bertini intranuclear cascade model [53] of the QGSP_BERT physics list defined in GEANT4 [44].

Since Λ and $\bar{\Lambda}$ are produced in pairs from $J/\psi \rightarrow \Lambda \bar{\Lambda}$ decays, the detection of a single $\bar{\Lambda}$ hyperon in an event (called “single-tag”) implies that the recoiling system is a monochromatic Λ hyperon. In this analysis, the $\bar{\Lambda}$ hyperon is reconstructed via $\bar{\Lambda} \rightarrow \bar{p}\pi^+$ and the yield of single-tagged events is obtained by fitting to the recoil-mass distribution of the $\bar{\Lambda}$ hyperon, denoted as N_{ST} . The recoil mass of the $\bar{\Lambda}$ hyperon is defined as $RM_{\bar{p}\pi^+} = \sqrt{|p_{e^+e^-} - p_{\bar{p}} - p_{\pi^+}|^2}$, where $p_{e^+e^-}$, $p_{\bar{p}}$ and p_{π^+} refer to the four-momenta of the initial e^+e^- , \bar{p} , and π^+ particles, respectively. The recoiling Λ hyperon produced together with the reconstructed $\bar{\Lambda}$ hyperon can scatter inelastically with the nucleons in the material and produce a Σ^+ hyperon. We search for such particles through the decay $\Sigma^+ \rightarrow p\pi^0$ among the other tracks and showers in the event, excluding those used to reconstruct the single-tagged $\bar{\Lambda}$ hyperon. The number of double-tagged events (N_{DT}) containing both a reconstructed $\bar{\Lambda}$ hyperon and a Σ^+ hyperon is given by

$$N_{DT} = \mathcal{L}_\Lambda \cdot \sigma(\Lambda N \rightarrow \Sigma^+ X) \cdot \mathcal{B}(\Sigma^+ \rightarrow p\pi^0) \cdot \epsilon_{\text{sig}}, \quad (1)$$

where $\sigma(\Lambda N \rightarrow \Sigma^+ X)$ is the cross section of the inelastic process $\Lambda N \rightarrow \Sigma^+ X$, $\mathcal{B}(\Sigma^+ \rightarrow p\pi^0)$ is the branching fraction of $\Sigma^+ \rightarrow p\pi^0$ decay, and ϵ_{sig} denotes the efficiency of the double-tag reconstruction. The “effective luminosity” \mathcal{L}_Λ is a specially defined quantity to describe the property of the target and the behavior of the incident Λ particle inside the target, which is influenced by several other parameters [15]. Considering the target composition shown in Fig. 1, \mathcal{L}_Λ is calculated event by event as

$$\mathcal{L}_\Lambda = N_{ST} \frac{N_A}{N_{ST}^{\text{MC}}} \sum_j^7 \sum_i^{N_{ST}^{\text{MC}}} \frac{\rho_j^{ij} l^{ij}}{M^j} \mathcal{R}_\sigma^j, \quad (2)$$

where N_A is Avogadro’s number [54], N_{ST}^{MC} is the total number of single-tagged events in the signal MC sample, l^{ij} is the path length of the incident Λ particle of the i th event inside the j th layer, and M^j and ρ_j^j are the molar mass [55] and density, respectively, of the j th layer. Since the contribution from each layer and the cross section for different kinds of nuclei are not the same, the ratio of the scattering cross section (\mathcal{R}_σ) of incident Λ for each category of materials is necessary for normalization. In this Letter, we present the measured cross section of the $\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X$ reaction, with the cross section of each material normalized to that of beryllium. The choice of beryllium as the normalization reference is due to its common use as the target in fixed-target experiments and its significance as the main material of the beam pipe in the BESIII detector. In the case of low and intermediate energy it is assumed that inelastic scattering occurs with single protons on the surface of the nucleus [56–61]. Then \mathcal{R}_σ is proportional to $A^{\frac{2}{3}} \times \frac{Z}{A} = \frac{Z}{A^{\frac{1}{3}}}$, where A and Z are the numbers of nucleons and protons in a single nucleus, respectively. If the material

of a certain layer contains multiple kinds of nuclei, \mathcal{R}_σ must be weighted by the ratio of the numbers of different nuclei per unit volume of the material. The detailed derivation and calculation of \mathcal{L}_Λ can be found in Sec. II of the Supplemental Material [43].

According to Eq. (1), the cross section for interaction with the Be nucleus can be determined as

$$\sigma(\text{Be}) = \frac{N_{\text{DT}}}{\epsilon_{\text{sig}} \mathcal{L}_\Lambda} \frac{1}{\mathcal{B}(\Sigma^+ \rightarrow p\pi^0)}. \quad (3)$$

Since we only reconstruct the Σ^+ on the double-tag side, there may also be contributions from the interactions between the Λ and neutrons. However, the contributions can only arise from three-body reactions such as $\Lambda n \rightarrow \Sigma^+ n\pi^-$. The total energy in the center-of-mass frame of Λ and a stationary neutron is [2.240, 2.249] GeV, while the lowest total energy for the final state $\Sigma^+ n\pi^-$ is 2.269 GeV. Therefore, this process can only occur when the neutrons have relatively large Fermi momenta. As a result, the cross section is suppressed due to the limited phase space. Similar reactions such as $\Lambda p \rightarrow \Sigma^- p\pi^+ / \Sigma^+ p\pi^-$ have been studied [9], which for Λ momentum within [1.057, 1.091] GeV/ c are at least 1 order of magnitude smaller than the measured cross section of $\Lambda p \rightarrow \Sigma^+ X$. Therefore, we neglect the contribution from Λn reactions.

We now describe the selection of signal events. Charged tracks detected in the MDC are required to have a polar angle (θ) satisfying $|\cos \theta| < 0.93$ with respect to the positron beam. The number of good charged tracks must be at least two.

For the single-tag side, $\bar{\Lambda}$ is reconstructed from its decay to \bar{p} and π^+ , which are identified using the measured information in the MDC and TOF. The combined likelihoods (\mathcal{L}) under the proton (antiproton), pion, and kaon hypotheses are calculated. The \bar{p} candidates are required to satisfy $\mathcal{L}(p) > \mathcal{L}(K)$ and $\mathcal{L}(p) > \mathcal{L}(\pi)$, whereas the π^+ candidates are required to satisfy $\mathcal{L}(\pi) > \mathcal{L}(K)$. A vertex fit is performed to constrain all possible $\bar{p}\pi^+$ combinations to a common vertex. The decay length of $\bar{\Lambda}$ is calculated as the distance between the fitted vertex and the interaction point (IP) of the e^+e^- collision. The $\bar{p}\pi^+$ combinations with a vertex-fit χ^2 lower than 200 and a decay length larger than 0 are regarded as $\bar{\Lambda}$ candidates. To further suppress the background, the invariant masses of the $\bar{p}\pi^+$ combinations are required to lie within [1.111, 1.120] GeV/ c^2 and $RM_{\bar{p}\pi^+}$ is required to be within [1.071, 1.153] GeV/ c^2 . If there are multiple candidates passing all the selection criteria above, we select the $\bar{p}\pi^+$ combination with the minimum vertex-fit χ^2 as the best candidate. The number of single-tagged events is determined to be 7207565 ± 3741 by fitting to the $RM_{\bar{p}\pi^+}$ distribution using the sum of two Gaussian distributions and a second-order Chebyshev polynomial, as shown in Fig. 2. The efficiency of the single-tag selection is $(52.16 \pm 0.10)\%$.

In the double-tag selection Σ^+ candidates are reconstructed in the $p\pi^0$ final state. The p is selected using the same criteria as the single-tag selection and the π^0 is reconstructed through EMC showers. The deposited energy of each shower must be more than 25 MeV in the barrel region ($|\cos \theta| < 0.80$) and more than 50 MeV in the end-cap region

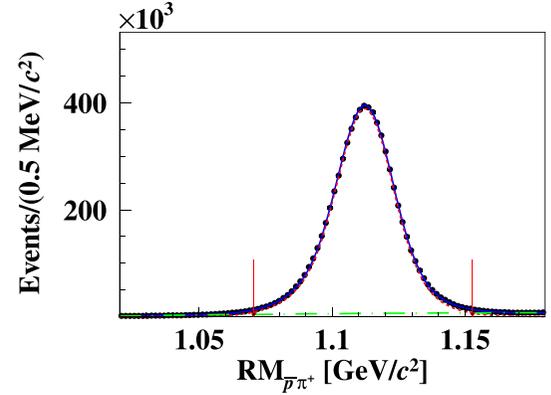


FIG. 2. The $RM_{\bar{p}\pi^+}$ distribution with the fit result superimposed. The black dots with error bars represent the data. The blue solid line is the total fit. The dashed red line is the signal of the single-tag selection and the dot-dashed green line is the background. The red arrows indicate the signal range.

($|\cos \theta| < 0.92$) of the EMC. To suppress electronic noise and showers unrelated to the event, the difference between the EMC time and the event-start time is required to be within [0, 700] ns. The angle between photons and all the other charged tracks should be larger than 10° to suppress the photons from the radiation of charged tracks and other processes. Then a kinematic fit is performed to all possible combinations of two showers by constraining the invariant mass $M_{\gamma\gamma}$ to the known π^0 mass [49]. The combination with the minimum χ^2 from this fit is chosen as the π^0 candidate. The Σ^+ candidate is selected from $p\pi^0$ combinations with invariant mass $M_{p\pi^0} \in [1.12, 1.25]$ GeV/ c^2 that has the maximum value of $\mathcal{L}(p)$ for the proton candidate.

If the incident Λ does not scatter with any nucleons, the recoil mass of $\bar{p}\pi^+p$, $RM_{\bar{p}\pi^+p}$, should be around the known mass of π^- [49] according to the kinematic constraint. For inelastic scattering events, $RM_{\bar{p}\pi^+p}$ has a tendency to be negative, as seen with the signal MC sample and discussed in Sec. III of the Supplemental Material [43]. This behavior is explained by the additional mass and momentum contributed by nucleons in the reaction. To further suppress the background, $RM_{\bar{p}\pi^+p}$ is required to be negative. In addition, the normal event of $J/\psi \rightarrow \Lambda \bar{\Lambda}$ without the hyperon-nucleus scattering can be rejected by identifying a Λ hyperon in the double-tag side after the Σ^+ candidate reconstruction using all possible $p\pi^-$ combinations. The Λ candidate is rejected if $M_{p\pi^-} \in [1.108, 1.124]$ GeV/ c^2 .

The number of double-tagged events is found to be 795 ± 101 by fitting to the distribution of $M_{p\pi^0}$ using a sum of two Gaussian distributions and a third-order Chebyshev polynomial, as is shown in Fig. 3. The parameters and fraction of the two Gaussian distributions are fixed to those obtained from the same fit to the signal MC sample. The efficiency of the double-tag selection is estimated to be $\epsilon_{\text{sig}} = (24.32 \pm 0.15)\%$ by fitting the signal MC sample.

The cross section of $\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X$ is determined through Eq. (3) to be $\sigma(\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X) = (37.3 \pm$

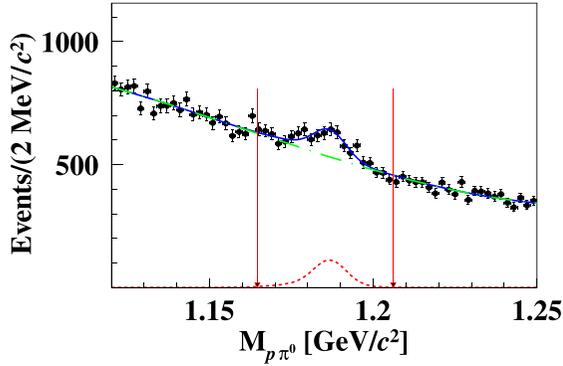


FIG. 3. The $M_{p\pi^0}$ distribution with the fit result overlaid. The black dots with error bars represent the data. The blue solid line is the total fit. The dashed red line is the signal and the dot-dashed green line is the background. The red arrows indicate the signal range.

$4.7_{\text{stat.}} \pm 3.5_{\text{syst.}}$ mb, where $\mathcal{B}(\Sigma^+ \rightarrow p\pi^0)$ is taken from the PDG [49]. Table I lists the inputs used in the calculation.

The systematic uncertainty for the measured cross section is associated with the knowledge of the tracking and particle identification (PID) efficiencies of charged particles, the reconstruction efficiency of π^0 mesons, the number of single-tagged events, the efficiency of the requirement of $RM_{\bar{p}\pi^+p}$ and $M_{p\pi^-}$, the angular distribution of $J/\psi \rightarrow \Lambda\bar{\Lambda}$ and Σ^+ , the size of the signal MC sample, the measured interaction point of the e^+e^- collision, the method to fit the $M_{p\pi^0}$ distribution, and the luminosity (\mathcal{L}_Λ) estimation. The assumption concerning the ratio of cross sections for different kinds of nuclei also introduces a systematic uncertainty.

The systematic uncertainties related to the tracking and PID efficiencies of protons are both 1.0% [62], and for π^0 reconstruction the systematic uncertainty is 1.0% [63]. The systematic uncertainty associated with the number of the single-tagged events is determined to be 0.8% from the inclusive MC. The systematic uncertainties from the $RM_{\bar{p}\pi^+p}$ and $M_{p\pi^-}$ requirements are tested by varying the criteria around the baseline settings to reobtain the measured cross section. The changes of the cross section are denoted as $\Delta = |\sigma - \sigma_{\text{sys.}}|$, where σ and $\sigma_{\text{sys.}}$ refer to the baseline results and the results after changing the criteria. Also calculated are the uncorrelated uncertainties $\omega_{\text{uc.}} = \sqrt{|\omega_\sigma^2 - \omega_{\sigma,\text{sys.}}^2|}$, where ω_σ and $\omega_{\sigma,\text{sys.}}$ correspond to the fit uncertainties of the baseline and systematic test results, respectively. Since the ratio $\Delta/\omega_{\text{uc.}}$ does not show a trending behavior and is less than 2, these two possible sources of systematic bias are considered to be negligible [64]. The systematic uncertainty associated with the

TABLE I. Inputs used to calculate the cross section of $\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X$.

Parameter	Value
N_{DT}	795 ± 101
ϵ_{sig}	24.32%
\mathcal{L}_Λ	$(17.00 \pm 0.01) \times 10^{28} \text{ cm}^{-2}$
$\mathcal{B}(\Sigma^+ \rightarrow p\pi^0)$	$(51.57 \pm 0.30)\%$

knowledge of the angular distribution of $J/\psi \rightarrow \Lambda\bar{\Lambda}$ production is estimated by varying the decay parameters $\alpha_{J/\psi}$, $\Delta\Phi$, α_Λ , and $\alpha_{\bar{\Lambda}}$ within 1 standard deviation [52] and generating new MC data sets to calculate the cross section. The systematic uncertainty from this source can be ignored compared with the statistical uncertainty. The systematic uncertainty associated with the angular distribution of Σ^+ baryons is evaluated by reweighting the angular distribution of the signal MC sample to that of the data and measuring the cross section again, which is determined to be 1.3% as the difference between the reobtained cross section and the baseline value.

The double-tag efficiency has a systematic uncertainty of 0.6% arising from the fitted number of double-tagged events in the signal MC sample. The IP of the e^+e^- collision is used to calculate the track length of Λ inside the target. According to the measured result, the interaction point is distributed around the coordinate origin with an uncertainty of 0.2 cm. We change the IP within ± 0.2 cm away from the original position and take the maximum change of the measured cross section as the systematic uncertainty, which is 4.6%. The systematic uncertainty from the fit method of the $M_{p\pi^0}$ distribution is estimated by changing the background shape from a third-order Chebyshev polynomial to fourth- and fifth-order ones and assigning the uncertainty to be 3.6% as the maximum difference from the baseline result. As well as scattering inside the beam pipe and the inner wall of the MDC, the Λ hyperons may also scatter with a nucleus inside the cooling devices of the BESIII spectrometer. When calculating the luminosity \mathcal{L}_Λ , the cooling pipe is not considered due to its much more complex structure and having less material than the beam pipe and the inner wall of the MDC. We assume a conservative model of the cooling devices and measure the cross section again. The difference from the baseline result is assigned as the systematic uncertainty, which is 6.1%.

In order to estimate the systematic uncertainty caused by the assumption of the ratio of the cross sections for different kinds of nuclei, we measure the cross section again under another assumption that the cross section is proportional to the total number of protons in a nucleus. The difference from our baseline result is taken as the systematic uncertainty, which is determined to be 3.6%.

The total systematic uncertainty on the measured cross section of $\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X$ is computed to be 9.5% by adding the systematic uncertainties listed above in quadrature.

In summary, the inelastic scattering $\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X$ is studied at BESIII using a novel method. The cross section is measured to be $\sigma(\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X) = (37.3 \pm 4.7_{\text{stat.}} \pm 3.5_{\text{syst.}})$ mb for a Be nucleus struck by a Λ hyperon with momentum within [1.057, 1.091] GeV/c. Taking 1.93 as the ratio of the cross section of $\Lambda + {}^9\text{Be} \rightarrow \Sigma^+ + X$ and $\Lambda + p \rightarrow \Sigma^+ + X$ by assuming the the signal process as a surface reaction [56–61], the cross section of $\Lambda + p \rightarrow \Sigma^+ + X$ is determined to be $\sigma(\Lambda + p \rightarrow \Sigma^+ + X) = (19.3 \pm 2.4_{\text{stat.}} \pm 1.8_{\text{syst.}})$ mb.

This is the first discovery and cross-section measurement of $\Lambda + p \rightarrow \Sigma^+ + n$. By virtue of charge independence, the cross sections of $\Lambda + p \rightarrow \Sigma^+ + n$ are just twice that of $\Lambda + p \rightarrow \Sigma^0 + p$ [8]. Our results are consistent with previous experiments regarding the cross-section measurement of

$\Lambda + p \rightarrow \Sigma^0 + p$ [9]. Additionally, this study represents the first attempt to investigate Λ -nucleus interactions at an e^+e^- collider. The result will be valuable for improving the understanding of the potential of strong interaction and the origin of color confinement, as well as providing important constraints for the unified model for baryon-baryon interactions. At BESIII, it is possible to measure the differential cross sections with respect to the momentum of incident hyperons using three-body decays of charmonia with at least one hyperon.

In the future, the Super τ -Charm Facility [65] will produce a J/ψ data set about 100 times larger than the sample collected by BESIII, which will allow for more detailed studies of the mechanism of hyperon-nucleon interactions.

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- [1] I. Vidaña, *Proc. R. Soc. London, Ser. A* **474**, 20180145 (2018).
- [2] E. Hiyama and K. Nakazawa, *Annu. Rev. Nucl. Part. Sci.* **68**, 131 (2018).
- [3] A. Gal, E. V. Hungerford, and D. J. Millener, *Rev. Mod. Phys.* **88**, 035004 (2016).
- [4] L. Tolos and L. Fabbietti, *Prog. Part. Nucl. Phys.* **112**, 103770 (2020).
- [5] F. Eisele, H. Filthuth, W. Foehlich, V. Hepp, and G. Zech, *Phys. Lett. B* **37**, 204 (1971).
- [6] B. Sechi-Zorn, B. Kehoe, J. Twitty, and R. A. Burnstein, *Phys. Rev.* **175**, 1735 (1968).
- [7] G. Alexander, U. Karshon, A. Shapira, G. Yekutieli, R. Engelmann, H. Filthuth, and W. Lughofer, *Phys. Rev.* **173**, 1452 (1968).
- [8] J. A. Kadyk, G. Alexander, J. H. Chan, P. Gaposchkin, and G. H. Trilling, *Nucl. Phys. B* **27**, 13 (1971).
- [9] J. M. Hauptman, J. A. Kadyk, and G. H. Trilling, *Nucl. Phys. B* **125**, 29 (1977).
- [10] J. K. Ahn *et al.* (KEK-PS E-251 Collaboration), *Nucl. Phys. A* **648**, 263 (1999).
- [11] Y. Kondo *et al.* (KEK-PS-E289 Collaboration), *Nucl. Phys. A* **676**, 371 (2000).
- [12] J. K. Ahn, S. Aoki, K. S. Chung, M. S. Chung, H. En'yo, T. Fukuda, H. Funahashi, Y. Goto, A. Higashi, M. Ieiri *et al.* *Phys. Lett. B* **633**, 214 (2006).
- [13] K. Miwa *et al.* (J-PARC E40 Collaboration), *Phys. Rev. C* **104**, 045204 (2021).
- [14] K. Miwa *et al.* (J-PARC E40 Collaboration), *Phys. Rev. Lett.* **128**, 072501 (2022).
- [15] J. Rowley *et al.* (CLAS Collaboration), *Phys. Rev. Lett.* **127**, 272303 (2021).
- [16] T. Nanamura *et al.* (J-PARC E40 Collaboration), *PTEP* **2022**, 093D01 (2022).
- [17] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. Lett.* **130**, 251902 (2023).
- [18] S. Acharya *et al.* (ALICE Collaboration), *Phys. Lett. B* **844**, 137223 (2023).
- [19] J. Haidenbauer and Ulf-G. Meißner, *Phys. Rev. C* **72**, 044005 (2005).
- [20] T. A. Rijken, M. M. Nagels, and Y. Yamamoto, *Prog. Theor. Phys. Suppl.* **185**, 14 (2010).
- [21] H. Polinder, J. Haidenbauer, and U.-G. Meißner, *Nucl. Phys. A* **779**, 244 (2006).
- [22] J. Haidenbauer, S. Petschauer, N. Kaiser, U.-G. Meißner, A. Nogga, and W. Weise, *Nucl. Phys. A* **915**, 24 (2013).
- [23] J. Haidenbauer, U.-G. Meißner, and S. Petschauer, *Nucl. Phys. A* **954**, 273 (2016).
- [24] J. Haidenbauer and U.-G. Meißner, *Eur. Phys. J. A* **55**, 23 (2019).
- [25] J. Haidenbauer, U.-G. Meißner, and A. Nogga, *Eur. Phys. J. A* **56**, 91 (2020).
- [26] J. Haidenbauer, U.-G. Meißner, A. Nogga, and H. Le, *Eur. Phys. J. A* **59**, 63 (2023).
- [27] K. W. Li, X. L. Ren, L. S. Geng, and B. Long, *Phys. Rev. D* **94**, 014029 (2016).

- [28] K. W. Li, X. L. Ren, L. S. Geng, and B. W. Long, *Chin. Phys. C* **42**, 014105 (2018).
- [29] N. Ishii, S. Aoki, and T. Hatsuda, *Phys. Rev. Lett.* **99**, 022001 (2007).
- [30] N. Ishii *et al.* (HAL QCD Collaboration), *Phys. Lett. B* **712**, 437 (2012).
- [31] S. R. Beane *et al.* (NPLQCD Collaboration), *Nucl. Phys. A* **794**, 62 (2007).
- [32] S. R. Beane, W. Detmold, K. Orginos, and M. J. Savage, *Prog. Part. Nucl. Phys.* **66**, 1 (2011).
- [33] B. J. Schaefer, M. Wagner, J. Wambach, T. T. S. Kuo, and G. E. Brown, *Phys. Rev. C* **73**, 011001(R) (2006).
- [34] Y. Fujiwara, Y. Suzuki, and C. Nakamoto, *Prog. Part. Nucl. Phys.* **58**, 439 (2007).
- [35] J. M. Lattimer and M. Prakash, *Astrophys. J.* **550**, 426 (2001).
- [36] D. Lonardonì, A. Lovato, S. Gandolfi, and F. Pederiva, *Phys. Rev. Lett.* **114**, 092301 (2015).
- [37] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **121**, 161101 (2018).
- [38] J. Dai, H.-B. Li, H. Miao, and J.-Y. Zhang, *Chin. Phys. C* (2024), doi:10.1088/1674-1137/ad3dde.
- [39] C. Z. Yuan and M. Karliner, *Phys. Rev. Lett.* **127**, 012003 (2021).
- [40] M. Ablikim *et al.* (BESIII Collaboration), *Chin. Phys. C* **46**, 074001 (2022).
- [41] H. B. Li, *Front. Phys.* **12**, 121301 (2017); **14**, 64001 (2019).
- [42] M. Ablikim *et al.* (BESIII Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **614**, 345 (2010).
- [43] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevC.109.L052201> for additional information and which includes Refs. [15,56–65].
- [44] S. Agostinelli *et al.* (GEANT4 Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **506**, 250 (2003).
- [45] K. X. Huang *et al.*, *Nucl. Sci. Tech.* **33**, 142 (2022).
- [46] S. Jadach, B. F. L. Ward, and Z. Was, *Nucl. Phys. B* **89**, 106 (2000).
- [47] D. J. Lange, *Nucl. Instrum. Methods Phys. Res., Sect. A* **462**, 152 (2001).
- [48] R. G. Ping, *Chin. Phys. C* **32**, 243 (2008).
- [49] R. L. Workman *et al.* (Particle Data Group), *Prog. Theor. Exp. Phys.* **2022**, 083C01 (2022).
- [50] J. C. Chen, G. S. Huang, X. R. Qi, D. H. Zhang, and Y. S. Zhu, *Phys. Rev. D* **62**, 034003 (2000).
- [51] R. L. Yang, R. G. Ping, and H. Chen, *Chin. Phys. Lett.* **31**, 061301 (2014).
- [52] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. Lett.* **129**, 131801 (2022).
- [53] D. H. Wright and M. H. Kelsey, *Nucl. Instrum. Methods Phys. Res., Sect. A* **804**, 175 (2015).
- [54] R. A. Millikan, *Phys. Rev.* **2**, 109 (1913).
- [55] NIST Chemistry webbook, <https://webbook.nist.gov/chemistry/>.
- [56] D. S. Barton, G. W. Brandenburg, W. Busza, T. Dobrowolski, J. I. Friedman, C. Halliwell, H. W. Kendall, T. Lyons, B. Nelson, L. Rosenson *et al.*, *Phys. Rev. D* **27**, 2580 (1983).
- [57] E. D. Cooper, B. K. Jennings, and J. Mares, *Nucl. Phys. A* **585**, 157 (1995).
- [58] M. I. Adamovich *et al.* (WA89 Collaboration), *Z. Phys. C* **76**, 35 (1997).
- [59] E. Botta (OBELIX Collaboration), *Nucl. Phys. A* **692**, 39 (2001).
- [60] M. Astrua, E. Botta, T. Bressani, D. Calvo, C. Casalegno, A. Feliciello, A. Filippi, S. Marcello, M. Agnello, and F. Iazzi, *Nucl. Phys. A* **697**, 209 (2002).
- [61] T. G. Lee and C. Y. Wong, *Phys. Rev. C* **97**, 054617 (2018).
- [62] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. D* **104**, 072007 (2021).
- [63] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. D* **81**, 052005 (2010).
- [64] R. Barlow, [arXiv:hep-ex/0207026](https://arxiv.org/abs/hep-ex/0207026).
- [65] M. Achasov *et al.*, *Front. Phys.* **19**, 14701 (2024).

M. Ablikim,¹ M. N. Achasov,^{5,b} P. Adlarson,⁷⁵ X. C. Ai,⁸¹ R. Aliberti,³⁶ A. Amoroso,^{74a,74c} M. R. An,⁴⁰ Q. An,^{71,58} Y. Bai,⁵⁷ O. Bakina,³⁷ I. Balossino,^{30a} Y. Ban,^{47,g} V. Batozskaya,^{1,45} K. Begzsuren,³³ N. Berger,³⁶ M. Berlowski,⁴⁵ M. Bertani,^{29a} D. Bettoni,^{30a} F. Bianchi,^{74a,74c} E. Bianco,^{74a,74c} A. Bortone,^{74a,74c} I. Boyko,³⁷ R. A. Briere,⁶ A. Brueggemann,⁶⁸ H. Cai,⁷⁶ X. Cai,^{1,58} A. Calcaterra,^{29a} G. F. Cao,^{1,63} N. Cao,^{1,63} S. A. Cetin,^{62a} J. F. Chang,^{1,58} T. T. Chang,⁷⁷ W. L. Chang,^{1,63} G. R. Che,⁴⁴ G. Chelkov,^{37,a} C. Chen,⁴⁴ Chao Chen,⁵⁵ G. Chen,¹ H. S. Chen,^{1,63} M. L. Chen,^{1,58,63} S. J. Chen,⁴³ S. L. Chen,⁴⁶ S. M. Chen,⁶¹ T. Chen,^{1,63} X. R. Chen,^{32,63} X. T. Chen,^{1,63} Y. B. Chen,^{1,58} Y. Q. Chen,³⁵ Z. J. Chen,^{26,h} W. S. Cheng,^{74c} S. K. Choi,¹¹ X. Chu,⁴⁴ G. Cibinetto,^{30a} S. C. Coen,⁴ F. Cossio,^{74c} J. J. Cui,⁵⁰ H. L. Dai,^{1,58} J. P. Dai,⁷⁹ A. Dbeyssi,¹⁹ R. E. de Boer,⁴ D. Dedovich,³⁷ Z. Y. Deng,¹ A. Denig,³⁶ I. Denysenko,³⁷ M. Destefanis,^{74a,74c} F. De Mori,^{74a,74c} B. Ding,^{66,1} X. X. Ding,^{47,g} Y. Ding,³⁵ Y. Ding,⁴¹ J. Dong,^{1,58} L. Y. Dong,^{1,63} M. Y. Dong,^{1,58,63} X. Dong,⁷⁶ M. C. Du,¹ S. X. Du,⁸¹ Z. H. Duan,⁴³ P. Egorov,^{37,a} Y. H. Fan,⁴⁶ J. Fang,^{1,58} S. S. Fang,^{1,63} W. X. Fang,¹ Y. Fang,¹ R. Farinelli,^{30a} L. Fava,^{74b,74c} F. Feldbauer,⁴ G. Felici,^{29a} C. Q. Feng,^{71,58} J. H. Feng,⁵⁹ K. Fischer,⁶⁹ M. Fritsch,⁴ C. D. Fu,¹ J. L. Fu,⁶³ Y. W. Fu,¹ H. Gao,⁶³ Y. N. Gao,^{47,g} Yang Gao,^{71,58} S. Garbolino,^{74c} I. Garzia,^{30a,30b} P. T. Ge,⁷⁶ Z. W. Ge,⁴³ C. Geng,⁵⁹ E. M. Gersabeck,⁶⁷ A. Gilman,⁶⁹ K. Goetzen,¹⁴ L. Gong,⁴¹ W. X. Gong,^{1,58} W. Gradl,³⁶ S. Gramigna,^{30a,30b} M. Greco,^{74a,74c} M. H. Gu,^{1,58} Y. T. Gu,¹⁶ C. Y. Guan,^{1,63} Z. L. Guan,²³ A. Q. Guo,^{32,63} L. B. Guo,⁴² M. J. Guo,⁵⁰ R. P. Guo,⁴⁹ Y. P. Guo,^{13,f} A. Guskov,^{37,a} T. T. Han,⁵⁰ W. Y. Han,⁴⁰ X. Q. Hao,²⁰ F. A. Harris,⁶⁵ K. K. He,⁵⁵ K. L. He,^{1,63} F. H. H. Heinsius,⁴ C. H. Heinz,³⁶ Y. K. Heng,^{1,58,63} C. Herold,⁶⁰ T. Holtmann,⁴ P. C. Hong,^{13,f} G. Y. Hou,^{1,63} X. T. Hou,^{1,63} Y. R. Hou,⁶³ Z. L. Hou,¹ H. M. Hu,^{1,63} J. F. Hu,^{56,i} T. Hu,^{1,58,63} Y. Hu,¹ G. S. Huang,^{71,58} K. X. Huang,⁵⁹ L. Q. Huang,^{32,63} X. T. Huang,⁵⁰ Y. P. Huang,¹ T. Hussain,⁷³ N. Hüskens,^{28,36} N. in der Wiesche,⁶⁸ M. Irshad,^{71,58} J. Jackson,²⁸ S. Jaeger,⁴ S. Janchiv,³³ J. H. Jeong,¹¹ Q. Ji,¹ Q. P. Ji,²⁰ X. B. Ji,^{1,63} X. L. Ji,^{1,58} Y. Y. Ji,⁵⁰ X. Q. Jia,⁵⁰ Z. K. Jia,^{71,58} H. J. Jiang,⁷⁶ P. C. Jiang,^{47,g} S. S. Jiang,⁴⁰ T. J. Jiang,¹⁷ X. S. Jiang,^{1,58,63} Y. Jiang,⁶³ J. B. Jiao,⁵⁰ Z. Jiao,²⁴ S. Jin,⁴³ Y. Jin,⁶⁶ M. Q. Jing,^{1,63} T. Johansson,⁷⁵ X. K.,¹ S. Kabana,³⁴

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