Half-life of ⁷¹Ge and the gallium anomaly

E. B. Norman¹⁰, ¹A. Drobizhev, ²N. Gharibyan⁰, ³K. E. Gregorich, ³Yu. G. Kolomensky⁰, ^{1,2}

B. N. Sammis, N. D. Scielzo, J. A. Shusterman, and K. J. Thomas,

¹University of California, Berkeley, California 94720, USA

²Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

³Lawrence Livermore National Laboratory, Livermore, California 94550, USA

(Received 26 January 2024; accepted 23 April 2024; published 30 May 2024)

Recent discussions about the origin of the so-called gallium anomaly have motivated a remeasurement of the half-life of ⁷¹Ge. We have conducted three separate measurements using dedicated planar Ge detectors—one with ⁵⁵Fe as a standard, one with ⁵⁷Co as a standard, and one standalone ⁷¹Ge measurement. Our results yield a halflife of 11.468 ± 0.008 days, which is consistent with, but significantly more precise than, the currently accepted value. With this experiment, the potential explanation of the gallium anomaly being due to an unexpectedly long ⁷¹Ge half-life has been ruled out, leaving the anomaly's origin as an open question.

DOI: 10.1103/PhysRevC.109.055501

I. INTRODUCTION

The gallium anomaly is based on the fact that several experiments have reported lower than expected (ν_e, e^-) reaction rates on 71 Ga [1–4]. The vast majority of these reactions are thought to involve transitions between the ground states of ⁷¹Ga and ⁷¹Ge. The origin of this discrepancy is not understood, having first been observed in the SAGE [2,5,6] and GALLEX [7,8] experiments, and confirmed with stronger statistical significance recently by the BEST experiment [4]. Given that the predicted reaction rates are believed to be on firm footing, this deficit potentially is an indication of new neutrino physics [2,9]. The cross section for such reactions can be deduced from the electron-capture decay half-life, $t_{1/2}$, of ⁷¹Ge. The most recent evaluated value gave $t_{1/2}$ = 11.43 ± 0.03 days [10], based on measurements done in 1985 [11]. Recently, it was suggested that a somewhat larger value of 12.5-13.5 days could reduce or eliminate this anomaly [12] and that careful new measurements of this half-life were warranted [13]. To thoroughly address this issue, we have conducted three independent, high-precision measurements of the ⁷¹Ge half-life.

II. EXPERIMENT

A. Production of ⁷¹Ge and experimental method

We produced ⁷¹Ge via neutron activation. Two separate Ge targets were irradiated at the TRIGA reactor of the McClellan Nuclear Research Center (MNRC) [14] to produce three distinct counting samples. The first irradiation target was 10.6 mg of natural-abundance germanium oxide GeO2, obtained from Fairmont Chemical Co. sealed in a guartz ampule and irradiated for 8 h at 250 kW in the central core of the reactor. The irradiated sample was transported to the Lawrence Livermore National Laboratory (LLNL) and opened in water to prevent contamination from the dispersible GeO₂ powder. The water

sealed the openings of the two ampule half pieces, allowing for the transfer of irradiated GeO₂ powder with a few drops of ethanol using a fine-tip glass pipette. The ethanol-GeO₂ slurry was placed on a plastic disk and dried slowly under a heat lamp. The dry powder was then taped down against the plastic disk with \sim 30-µm-thick Kapton tape. An additional \sim 30-µm-thick Kapton tape was affixed over the entire disk to ensure sample integrity for an extended period of time. Two such counting samples were prepared from the irradiated GeO₂ powder. The second irradiation target consisted of 0.82 g of detector-grade high-purity Ge $(1.4-1.5\times10^{10} \text{ cm}^{-3})$ net p type) procured from Mirion Technologies Inc. This was cut into three small pieces of approximately $3 \text{ mm} \times 3 \text{ mm} \times 5 \text{ mm}$ dimensions and the surface cleaned via aggressive etching in a 3:1 HNO₃:HF mixture, subsequently quenched in deionized water and rinsed with methanol. This material was irradiated in the graphite reflector of the MNRC reactor for 19 min at 800 kW. Two of these Ge pieces were mounted together on a plastic disk and held in place with two \sim 30-um-thick pieces of Kapton tape. Each of the three irradiated samples were counted on planar detectors at the LLNL Nuclear Counting Facility to assess radiopurity. Initially, the ⁷¹Ge activities were accompanied by a few short-lived isotopes, such as ⁷⁷Ge ($t_{1/2} = 11.3$ h). The three ⁷¹Ge sources were stored for 14 days to allow these short-lived activities to decay away before the half-life measurements began.

B. Results

The decay of ⁷¹Ge to ⁷¹Ga by electron capture was monitored by the pair of K-shell x-ray lines at 9.225 keV/9.252 keV (with total intensity 39.4%) and 10.26 keV/10.264 keV (with total intensity 4.9%) on three planar high-purity germanium (HPGe) detectors at the LLNL Nuclear Counting Facility. Two were ORTEC detectors with crystal diameters of 36 mm and having thin Be windows. The third was a Canberra detector



FIG. 1. Relevant portions of the spectra obtained on day 20 from the three measurements we performed. Top: 71 Ge alone; middle: 71 Ge + 55 Fe; bottom: 71 Ge and 57 Co. Each spectrum represents 24 h of counting.

with crystal diameter of 52 mm and having a thin carbon composite window. The energy resolutions of the three detectors were all approximately 0.35 keV (full width at half maximum) at 5.9 keV. Each detector was housed in its own commercial low-background graded shield.

We performed one absolute ⁷¹Ge half-life measurement and two relative measurements using radioactive standards. We mounted one of the GeO₂ samples approximately 15.4 cm away from the front face of one of the ORTEC detectors. The other GeO₂ sample was mounted together with a weak source of 57 Co ($t_{1/2} = 271.74 \pm 0.06$ days) [15] near the front face of the other ORTEC detector. The Ge wafer pieces were placed together with a weak ⁵⁵Fe source ($t_{1/2} = 2.744 \pm 0.009$ years) [16] near the front face of the Canberra detector. Data were collected from near zero to approximately 300 keV and binned in 4096 channels in 1-day-long time intervals using three separate ORTEC DSPEC data acquisition systems. Energy spectra were stored at the end of each day for offline analysis. Over an 80-day counting period, the shields were never opened and the sources were never moved. Figure 1 illustrates the relevant portions of the spectra we obtained from each of the three detector systems.

From the 80 spectra collected from each of the three detector systems, we utilized two different methods to extract peak areas of the Ga x rays and in the cases of the relative measurements, those of the Mn *K*-shell x rays (⁵⁵Fe) and the 14-keV γ ray (⁵⁷Co). In the first method (analysis 1), the counts in peak and background windows in each spectrum were integrated

and the net peak areas and their uncertainties were then determined by subtraction. To minimize the large uncertainties analysis 1 suffered as a result of signal interference between 71 Ge, 55 Fe, and 57 Co activities, this analysis uses only data collected between day 49 and day 60 (71 Ge + 55 Fe exposure) and between day 1 and day 30 (71 Ge + 57 Co exposure).

In the second method (analysis 2), portions of the spectra containing the peaks of interest were fit using a peak-shape parametrization similar to that suggested by Campbell and Maxwell [17]. The main part of the peak is a Gaussian detector-resolution function,

$$G(x) = H_{\rm G} \exp\left(\frac{-(x-\mu)^2}{2\sigma^2}\right)$$

where *x* is the channel number, H_G is the Gaussian amplitude, μ is the peak centroid, and σ is the standard deviation. An exponential tail on the low energy edge of the peak is introduced to account for charge trapping in detector defects. This exponential tail is truncated at *m* and convoluted with the Gaussian detector resolution,

$$E(x) = \frac{H_{\rm G}R_E}{2} \exp\left(\frac{x-\mu}{\beta} + \frac{\sigma^2}{2\beta^2}\right) \operatorname{erfc}\left(\frac{x-\mu}{\sqrt{2}\sigma} + \frac{\sigma}{\sqrt{2}\beta}\right),$$

where R_E is the ratio of the amplitudes of the unconvoluted exponential to the Gaussian at *m*, and β is the "mean lifetime" of the exponential. E(x) is usually included in the peak area. A step in the background occurs at *m*, due to several effects, including Compton electrons escaping the active detector volume, and coherent scattering in place of Compton scattering. This background step is also convoluted with the Gaussian detector resolution,

$$S(x) = \frac{H_{\rm G}R_s}{2} \operatorname{erfc}\left(\frac{x-\mu}{\sqrt{2}\sigma}\right),$$

where R_S is the ratio of the background step amplitude to the Gaussian amplitude. The peak described by these three functions sits on a smoothly varying background. There are several background function options: none, constant, linear, quadratic, or exponential, selected based on the location of the peak-free background region.

Dead-time corrections, ranging from 0.33% at the start of data taking to 0.14% at the end, were applied to the data obtained from the standalone ⁷¹Ge sample. For the 55 Fe + 71 Ge data, we analyzed the ratio of the Ga and Mn x rays. For the 57 Co + 71 Ge data, we analyzed the ratio of the Ga x rays to the 14-keV γ ray. By using such ratios, the effects of possible variations in detector and/or electronics performance are largely cancelled out. In the course of examining the ${}^{57}\text{Co} + {}^{71}\text{Ge}$ data, we discovered relatively weak Ge K-shell x rays within our analysis windows that appear to have been produced by 14-, 122-, and 136-keV γ rays interacting with the dead layers of our HPGe detectors. After our half-life measurements were completed and the ⁷¹Ge sample was removed, we used the same detector to obtain spectra from just the 57 Co source. These data were then used in both of our analysis methods to correct for the contributions of the Ge x rays to our data. Decay curves from our three measurements and both analyses are shown in Fig. 2.



FIG. 2. Decay curves observed from our three independent measurements of the ⁷¹Ge half-life. Top: Ga *K*-shell x rays as a function of time from the standalone ⁷¹Ge source. Middle: the ratio of the Ga *K*-shell x rays to the Mn *K*-shell x rays from the ⁷¹Ge + ⁵⁵Fe sample. Bottom: ratio of the Ga *K*-shell x rays to the 14-keV γ ray from the ⁷¹Ge + ⁵⁷Co sample. Panels on left are from analysis 1 and panels on right are from analysis 2.

The decay curves observed from each detector were fit using a least squares technique. The data from the standalone ⁷¹Ge source provides a direct measure of the ⁷¹Ge half-life and are well described by an exponential function. In the cases of the relative measurements, a fit to the ratio of activities between ⁷¹Ge and a standard (⁵⁵Fe or ⁵⁷Co) provides a measure of the difference in decay rates between ⁷¹Ge and the that of the standard. The data are also well described by

the exponential function, except for the ${}^{57}\text{Co} + {}^{71}\text{Ge}$ sample in analysis 2, where a constant term is needed to account for the uncertainty in the ⁵⁷Co background subtraction. From the fitted difference in decay rates, we compute the ⁷¹Ge half-life using the accepted values of the half-lives of the standards [15,16]. The results of our three measurements are shown in Table I. For analysis 2, where the goodness of fit metric chi-squared per degree of freedom (χ^2 /d.f.) deviates significantly from unity indicating nonstatistical fluctuations, the uncertainties have been determined by multiplying the fitted statistical uncertainties by the square root of $\chi^2/d.f.$ The relatively large χ^2/d .f. in analysis 2 fits for the ⁷¹Ge + ⁵⁵Fe and $^{71}\text{Ge} + {}^{57}\text{Co}$ arise from (1) the scatter in the decay curves for the Mn x ray and the 14.4-keV γ ray, and (2) the interference from the ⁵⁵Fe and ⁵⁷Co in the Ga x-ray peak-fitting regions. The effect from the latter is visible in the residual plots of Fig. 2.

The two most precise measurements are from the detector exposed only to the 71 Ge source. While the two analysis techniques determine the peak areas differently, the resulting half-life values are highly correlated. We determine the value of the 71 Ge half-life as an arithmetic average of two results without adjusting the uncertainty:

$$t_{1/2}(^{71}\text{Ge}) = 11.4683 \pm 0.0017(\text{stat.}) \text{ days.}$$

C. Systematic uncertainty

Systematics in the measurement can come from the precision of the detector clock, time-dependent detection efficiency (e.g., due to rate-dependent deadtime corrections), and pathologies in background subtraction. The measurements performed with the standard sources allow us to monitor and calibrate out time-dependent effects; moreover, most time-dependent effects cancel in the ratio of the ⁷¹Ge and a standard decay rate. The background-subtraction systematics are amplified in the ratio analysis due to the nontrivial signal interference between the ⁷¹Ge, ⁵⁵Fe, and ⁵⁷Co activities. Therefore, we use the results from the ⁷¹Ge + ⁵⁵Fe and ⁷¹Ge + ⁵⁵Fe and ⁷¹Ge + ⁵⁷Co samples to estimate the systematic uncertainties.

First, we fit the decay rate curves for the ⁵⁵Fe [⁵⁵Mn x-ray peaks in Fig. 1(b)] and ⁵⁷Co [14.4-keV line in Fig. 1(c)] samples to a combination of two exponentials: the primary function with the free decay rate, and the subdominant function with the half-life fixed to our measured value of 11.4683 days to account for spurious contamination of the main peak

TABLE I. Results of the present measurements of the half-life of ⁷¹Ge.

| Sample | Analysis 1 | | Analysis 2 | |
|-------------------------------------|----------------------|---------------|----------------------|---------------|
| | Half-life (days) | $\chi^2/d.f.$ | Half-life (days) | $\chi^2/d.f.$ |
| ⁷¹ Ge | 11.4700 ± 0.0017 | 49.1/58 | 11.4666 ± 0.0018 | 110.7/80 |
| 71 Ge + 55 Fe | 11.477 ± 0.040 | 5.3/9 | 11.479 ± 0.005 | 339.6/61 |
| $^{71}\text{Ge} + {}^{57}\text{Co}$ | 11.4596 ± 0.0039 | 30.8/28 | 11.466 ± 0.007 | 180.5/66 |



FIG. 3. Time dependence of the decay rates for the (a) ⁵⁵Fe and (b) 57 Co data sets.

by the ⁷¹Ge sample. The fits are shown in Fig. 3, and result in the estimates of the $t_{1/2}({}^{55}\text{Fe}) = 2.98 \pm 0.21$ (stat.) yr and $t_{1/2}({}^{57}\text{Co}) = 270.7 \pm 1.9$ (stat.) days. These are in excellent agreement with canonical values [15,16]. If we were to treat the statistical uncertainty on $t_{1/2}({}^{57}\text{Co})$ as a gauge of the size of any potential rate-dependent systematic skewing of our measured half-life from the actual value, it would only contribute ± 0.0034 days to $t_{1/2}$ ⁽⁷¹Ge), owing to the significantly shorter half-life of ⁷¹Ge.

Instead, the systematic error is computed as the standard deviation of the four relative measurements (second and third lines in Table I) with respect to the average absolute measurement (i.e., 11.4683 days), for four degrees of freedom. If we include the absolute measurements also, the result is the same, since the two absolute measurements are highly correlated, and therefore represent one degree of freedom. The resulting systematic error is 0.0082 days; it captures the background-subtraction systematics of the 71 Ge + 55 Fe and 71 Ge + 57 Co samples, and also covers, by construction, ratedependent effects.

PHYSICAL REVIEW C 109, 055501 (2024)



FIG. 4. Results from all reported measurements of the ⁷¹Ge halflife since 1985.

III. CONCLUSIONS

Finally, combining the statistical and systematic uncertainties, we determine the half-life of 71 Ge to be

$$t_{1/2}({}^{/1}\text{Ge}) = 11.4683 \pm 0.0017(\text{stat.}) \pm 0.0082(\text{syst.})$$

= 11.468 ± 0.008 days

Figure 4 compares the present results to those from previous measurements of the ⁷¹Ge half-life.

Our final result for the half-life of ⁷¹Ge is in very good agreement with the accepted value of 11.43 ± 0.03 days [10] and agrees with, but is significantly more precise than, the recently reported 11.46 ± 0.04 day half-life [18]. Thus, as pointed out in two new detailed papers [19,20], the origin of the gallium anomaly remains an open question.

ACKNOWLEDGMENTS

We thank W. Frey and the staff of the MNRC for carrying out the neutron irradiations that produced the ⁷¹Ge used in our measurements. This material was based upon work supported by the U.S. Department of Energy (DOE) Office of Science under Contract No. DE-AC02-05CH11231, and by the DOE Office of Science, Office of Nuclear Physics under Contract No. DE-FG02-08ER41551. This work was performed in part under the auspices of the U.S. Department of Energy by LLNL under Contract No. DE-AC52-07NA27344. This work was partially supported by the Laboratory Directed Research and Development Program at LLNL under Project Tracking Code 23-SI-004.

- [1] J. N. Abdurashitov et al., Measurement of the response of a gallium metal solar neutrino experiment to neutrinos from a ⁵¹Cr source, Phys. Rev. C **59**, 2246 (1999).
- [2] J. N. Abdurashitov et al., Measurement of the response of a Ga solar neutrino experiment to neutrinos from a ³⁷Ar source, Phys. Rev. C 73, 045805 (2006).
- [3] F. Kaether, W. Hampel, G. Heusser, J. Kiko, and T. Kirsten, Reanalysis of the gallex solar neutrino flux and source experiments, Phys. Lett. B 685, 47 (2010).
- [4] V. V. Barinov et al., Results from the baksan experiment on sterile transitions (BEST), Phys. Rev. Lett. 128, 232501 (2022).

- [5] C. Giunti and M. Laveder, Short-baseline active-sterile neutrino oscillations? Mod. Phys. Lett. A 22, 2499 (2007).
- [6] C. Giunti and M. Laveder, Statistical significance of the gallium anomaly, Phys. Rev. C 83, 065504 (2011).
- [7] P. Anselmann and GALLEX, First results from the ⁵¹Cr neutrino source experiment with the GALLEX detector, Phys. Lett. B 342, 440 (1995).
- [8] W. Hampel et al., Final results of the ⁵¹Cr neutrino source experiments in GALLEX, Phys. Lett. B 420, 114 (1998).
- [9] M. Laveder, Unbound neutrino roadmaps, Nucl. Phys. B 168, 344 (2007).

- [10] B. Singh and J. Chen, Nuclear structure and decay data for A = 71 isobars, Nucl. Data Sheets **188**, 1 (2023).
- [11] W. Hampel and L. P. Remsberg, Half-Life of ⁷¹Ge, Phys. Rev. C 31, 666 (1985).
- [12] C. Giunti, Y. F. Li, C. A. Ternes, and Z. Xin, Inspection of the detection cross section dependence of the gallium anomaly, Phys. Lett. B 842, 137983 (2023).
- [13] S. R. Elliott, V. Gavrin, and W. Haxton, The gallium anomaly, arXiv:2306.03299v1.
- [14] https://mnrc.ucdavis.edu
- [15] M. R. Bhat, Nuclear data sheets for $A = 57^*$, Nucl. Data Sheets **85**, 415 (1998).
- [16] H. Junde, Nuclear data sheets for A = 55, Nucl. Data Sheets 109, 787 (2008).

- [17] J. L. Campbell and J. A. Maxwell, A cautionary note on the use of the hypermet tailing function in X-Ray spectrometry with Si(Li) detectors, Nucl. Instrum. Methods Phys. Res. B 129, 297 (1997).
- [18] J. I. Collar and S. G. Yoon, New measurements of ⁷¹Ge decay: Impact on the gallium anomaly, Phys. Rev. C 108, L021602 (2023).
- [19] S. R. Elliott, V. N. Gavrin, W. C. Haxton, T. V. Ibragimova, and E. J. Rule, Gallium neutrino absorption cross section and its uncertainty, Phys. Rev. C 108, 035502 (2023).
- [20] S. R. Elliott, V. N. Gavrin, and W. C. Haxton, The gallium anomaly, Prog. Part. Nucl. Phys. 134, 104082 (2024).