




Isospin symmetry breaking in the charge radius difference of mirror nuclei

Tomoya Naito ^{1,2}, Xavier Roca-Maza ³, Gianluca Colò ³, Haozhao Liang^{1,2} and Hiroyuki Sagawa^{4,5}

¹*RIKEN Interdisciplinary Theoretical and Mathematical Sciences Program (iTHEMS), Wako 351-0198, Japan*

²*Department of Physics, Graduate School of Science, The University of Tokyo, Tokyo 113-0033, Japan*

³*Dipartimento di Fisica, Università degli Studi di Milano, and INFN, Via Celoria 16, 20133 Milano, Italy*

⁴*Center for Mathematics and Physics, University of Aizu, Aizu-Wakamatsu 965-8560, Japan*

⁵*RIKEN Nishina Center, Wako 351-0198, Japan*



(Received 10 February 2022; revised 15 April 2022; accepted 1 December 2022; published 21 December 2022)

Isospin symmetry breaking (ISB) effects in the charge radius difference ΔR_{ch} of mirror nuclei are studied using the test example of ^{48}Ca and ^{48}Ni . This choice allows for a transparent study of ISB contributions since pairing and deformation effects, commonly required for the study of mirror nuclei, can be neglected in this specific pair. The connection of ΔR_{ch} with the nuclear equation of state and the effect of ISB on such a relation are discussed according to an energy density functional approach. We find that nuclear ISB effects may shift the estimated value for the symmetry energy slope parameter L by about 6 to 14 MeV while Coulomb corrections can be neglected. ISB effects on the ground-state energy and charge radii in mirror nuclei have been recently predicted by *ab initio* calculations to be relatively small, pointing to a negligible effect for the extraction of information on the nuclear EoS. These contrasting results call for a dedicated theoretical effort to solve this overarching problem that impacts not only the neutron-skin thickness or the difference in mass and charge radii of mirror nuclei but also other observables such as the isobaric analog state energy.

DOI: [10.1103/PhysRevC.106.L061306](https://doi.org/10.1103/PhysRevC.106.L061306)

There exist important experimental efforts to measure, far from the stability valley, one of the most basic properties of the atomic nucleus: *the charge radius* [1,2]. The study of the charge radius is very much appealing since its determination is free from most nuclear physics uncertainties coming from the strong interaction: the electric charge of a nucleus is determined via electromagnetic probes. Exotic phenomena expected to be observed in those nuclei may help in understanding nuclear structure under extreme conditions of isospin asymmetry [3–5]. At the moment relative isotopic changes in the charge radius can be measured via laser spectroscopy [1] while two projects, SCRIT [6] and ELISE [7], aim at measuring the absolute values.

A newly proposed method to explore and estimate the density dependence of the nuclear equation of state (EoS) of isospin asymmetric matter requires the measurement of the charge radii in mirror mass nuclei [8]. Specifically, it has been shown in [8] on the basis of different energy density functionals (EDFs) that the difference in the charge root-mean-square radius of the nucleus with N neutrons and Z protons, $R_{\text{ch}}^{(N,Z)}$, with respect to its mirror nucleus, that has the number of neutrons and protons interchanged, $\Delta R_{\text{ch}} \equiv R_{\text{ch}}^{(N,Z)} - R_{\text{ch}}^{(Z,N)}$, is connected to the symmetry energy slope parameter L . The latter is *strictly* proportional to the pressure in infinite neutron matter at nuclear saturation density (about 0.16 fm^{-3}) only if isospin symmetry breaking (ISB) effects are neglected. A similar relation was already found by the same author [9]: between the neutron-skin thickness $\Delta R_{np} \equiv R_n^{(N,Z)} - R_p^{(N,Z)}$ of the nucleus with N neutrons and Z protons and the L parameter (cf. also [10]). On this regard, in Ref. [11], it

was shown that the estimation of the neutron-skin thickness in ^{208}Pb via the measurement of the excitation energy of the isobaric analog state (IAS) is clearly dependent on ISB effects: *the larger the neutron-skin in ^{208}Pb , the larger ISB effects must be to reproduce the experimental data on IAS*. If electromagnetic and nuclear ISB contributions are neglected, the excitation energy of the IAS in the nucleus (N, Z) is zero and $\Delta R_{\text{ch}} = -\Delta R_{np}$ being both of the order of a fraction of one fm or less. Hence, the effect of ISB terms other than those originated from the Coulomb interaction may become relevant.

Due to the impact of the nuclear EoS and, in particular, of the L parameter on areas as diverse as nuclear physics and nuclear astrophysics [12–14], the study of ΔR_{np} have fostered different experiments and a number of theoretical investigations along the years (see, e.g., [15–20]). Similar situation is starting to take place regarding the measurement of ΔR_{ch} . As an example, the mirror pairs $^{36}\text{Ca} - ^{36}\text{S}$ and $^{38}\text{Ca} - ^{38}\text{Ar}$ have been analyzed in [21] and $^{54}\text{Ni} - ^{54}\text{Fe}$ in [22] on the basis of nuclear EDFs. Those studies neglect ISB effects as well as pairing correlations, and also deformation is not treated microscopically. Actually, in a recent study based on quantified EDFs [23], ΔR_{ch} has been shown to be influenced by pairing correlations in the presence of low-lying proton continuum—in the proton-rich partner—and the authors concluded that, considering the large theoretical uncertainties, precise data on mirror charge radii cannot provide a stringent constraint on L .

In the present work, we concentrate on a different source of systematic uncertainty with respect to those discussed in Ref. [23]. It will be shown that nuclear ISB contributions

cannot be neglected in the study of the difference of charge radii in mirror nuclei if analyzed on the basis of current EDFs. For that, the specific example ^{48}Ca and ^{48}Ni mirror nuclei is used. We have confirmed by using different Skyrme EDFs that this choice avoids the effects of pairing correlations and deformation on ΔR_{ch} since both nuclei are predicted to be doubly magic in our calculations. The Coulomb plus centrifugal barrier felt by the protons is large enough to avoid large continuum effects on the prediction of ΔR_{ch} (see Supplemental Material [24] and the cited Refs. [11,23,25–28]).

Nuclear model calculations. There exist different theoretical approaches to the description of the charge radii in nuclei. One of the most successful nowadays is based on nuclear density functional theory [29–31]. State-of-the-art nuclear EDFs are known to provide predictions of experimentally known charge radii along the whole nuclear chart which are at the level of 0.02–0.03 fm of average accuracy [14,32–34]. This accuracy is not reached by other approaches available in the literature, hence the suitability of this theoretical framework.

For the present study, we solve the Hartree-Fock equations for the SAMi-J family of EDFs [35] employing the SKYRME_RPA solver [36]. We will see at the end that our main conclusions are independent of the chosen EDFs. Except for the Coulomb interaction, these Skyrme-type EDFs are isospin symmetric—adopting the most standard form found in the literature [29]—and have been calibrated using the fitting protocol of the SAMi EDF [37]. The SAMi-J family has been produced by exploring the optimal parametrization around the minimum (SAMi) in terms of the variation of two parameters that characterize the EoS of asymmetric nuclear matter: the symmetry energy at nuclear saturation density J and the previously introduced L parameter. We will show results for EDFs with J (L) ranging values from 27 (30) MeV to 35 (115) MeV. This range spans the accepted values for these quantities [14]. On top of SAMi-J EDFs, we will first implement and present the effects on ΔR_{ch} originated from the Coulomb interaction in a similar fashion to what has been done in Ref. [11]. As we shall discuss later, Coulomb effects are not accounted for in the nuclear EoS, hence, the L parameter is by construction insensitive to the Coulomb interaction. Subsequently, we will explore and present the effects of ISB contributions coming from the nuclear strong interaction that will affect both the ΔR_{ch} and the properties of the nuclear EoS. Finally, we will present all effects combined.

Coulomb interaction. In standard EDFs it is customary to account for the Coulomb interaction in the atomic nucleus by using the Hartree approximation for the direct term and the Slater approximation for the exchange term. In the literature, this is named local density approximation (LDA) to the Coulomb part of the EDF. While this is reasonable for the description of different observables, it may become inaccurate for the present case. Hence, we will also show results by adopting the generalized gradient approximation (GGA) that accurately reproduces the exact Fock results [38,39].

In addition to that, since ΔR_{ch} is a small quantity, other corrections beyond the GGA could be relevant. Those corrections are the electromagnetic finite size effects of the nucleons and leading order quantum electrodynamic corrections—vacuum

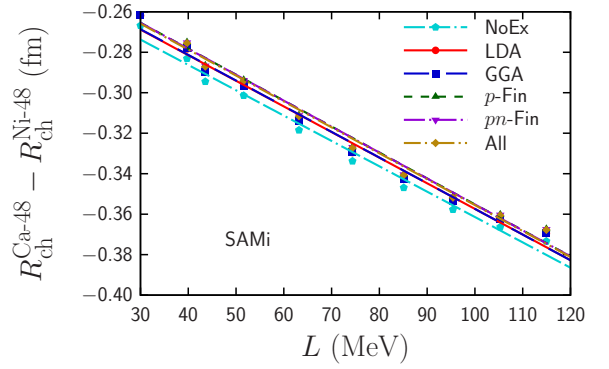


FIG. 1. SAMi-J predictions for the charge radius difference between ^{48}Ca and ^{48}Ni as a function of the L parameter. Different approximations to the Coulomb interaction has been adopted (see text for details).

polarization—to the Coulomb interaction. In Refs. [11,40] these corrections are described in detail.

In Fig. 1 we show that the different Coulomb corrections and approximations taken into account barely modify the values of the difference between the charge radii in ^{48}Ca and ^{48}Ni . The correlation between these values and the L parameter as proposed in [8] is, therefore, also unaffected. For guidance, average linear trends are given by lines. The results shown have been produced with the SAMi-J EDFs, including the unconstrained one: SAMi. In the figure, “NoEx” stands for calculations neglecting the Coulomb exchange term of the functional. Neglecting exchange terms has been postulated as a phenomenological recipe to compensate nuclear ISB effects on the masses of mirror nuclei [9,41,42]. Then, adding to the latter, improving approximations and corrections are implemented. First the Coulomb exchange is taken into account in the LDA and subsequently in the GGA. Two different electromagnetic finite size effects have been implemented in the calculation of the charge radii and Coulomb potential: the first “ p -Fin” takes into account only the electric form factor of the proton while “ pn -Fin” adds to the previous one also the neutron electric form factor effects.

Finally, labeled as “All”, leading order quantum electrodynamic correction to the Coulomb interaction has been added.

Nuclear isospin symmetry breaking terms. The isospin symmetry breaking of the nuclear interaction can be divided into two parts; the charge symmetry breaking (CSB) interaction $V_{\text{CSB}} \equiv V_{nn} - V_{pp}$ and the charge independent breaking (CIB) interaction $V_{\text{CIB}} \equiv (V_{nn} + V_{pp})/2 - V_{pn}$, where V_{pp} , V_{nn} , and V_{pn} denote the proton-proton, neutron-neutron, and proton-neutron nuclear interactions, respectively. Origins of CSB are mainly due to proton-neutron mass difference as well as π^0 - η and ρ^0 - ω mixings in meson exchange models while that of CIB is the mass difference of neutral and charged pions [43].

The form of the CSB and CIB interactions used in this work are [11,44]

$$v_{\text{CSB}}(\mathbf{r}_1, \mathbf{r}_2) = \frac{\tau_{1z} + \tau_{2z}}{4} s_0 (1 + y_0 P_\sigma) \delta(\mathbf{r}_1 - \mathbf{r}_2), \quad (1a)$$

$$v_{\text{CIB}}(\mathbf{r}_1, \mathbf{r}_2) = \frac{\tau_{1z} \tau_{2z}}{2} u_0 (1 + z_0 P_\sigma) \delta(\mathbf{r}_1 - \mathbf{r}_2), \quad (1b)$$

respectively, where $P_\sigma = (1 + \sigma_1 \cdot \sigma_2)/2$ is the spin-exchange operator, σ_i are the Pauli matrices in spin space, and τ_{iz} is the z component of the Pauli matrices in isospin space. These forms are two of the simplest possible yet realistic enough to describe the IAS in different nuclei [11]. Other functional forms of these interactions have been discussed in Refs. [45,46].

Equation of state. The nuclear EoS at zero temperature corresponds to the energy per particle ($e \equiv E/A$) of an infinite sea of neutrons and protons at a fixed constant density where the Coulomb interaction is not taken into account for obvious reasons.

According to the definition above, the Hartree-Fock CSB and CIB contributions to the energy per particle can be derived in terms of the total density $\rho = \rho_n + \rho_p$ and the relative difference $\beta = (\rho_n - \rho_p)/\rho$ between the neutron (ρ_n) and proton (ρ_p) density distributions as [40]

$$e_{\text{CSB}}(\rho, \beta) = \frac{s_0(1 - y_0)}{8} \rho \beta, \quad (2a)$$

$$e_{\text{CIB}}(\rho, \beta) = -\frac{1}{16} u_0 (1 + 2z_0) \rho + \frac{3}{16} u_0 \rho \beta^2, \quad (2b)$$

respectively.

In nuclear physics, it is customary to expand the energy per particle around $\beta \rightarrow 0$ up to $\mathcal{O}[\beta^2]$. This approximation has been shown to be reasonable even for large values of β , provided one remains at densities below two times saturation density [47]. This is actually the situation here. Thus, without losing generality for our current purposes, the EoS can be written as

$$e(\rho, \beta) = e_0(\rho) + e_1(\rho)\beta + e_2(\rho)\beta^2 + \mathcal{O}[\beta^3], \quad (3)$$

from where the symmetry energy is commonly defined as

$$e_{\text{sym}}(\rho) \equiv e(\rho, \beta = 1) - e(\rho, \beta = 0), \quad (4)$$

and, thus,

$$e_{\text{sym}}(\rho) = e_1(\rho) + e_2(\rho), \quad (5)$$

where $e_0(\rho) \equiv e(\rho, \beta = 0)$ is the EoS of symmetric nuclear matter and gets contributions from CIB in Eq. (2b), $e_1(\rho)$ is a contribution originated from the CSB interaction in Eq. (2a) and $e_2(\rho)$ gets a contribution from CIB in Eq. (2b). In the standard definition of the EoS that assumes isospin symmetry (IS): $e_1(\rho)$ would be zero and CIB contributions to $e_0(\rho)$ and $e_2(\rho)$ would also be zero. That is, only the IS terms in $e_2(\rho)$ will contribute to $e_{\text{sym}}(\rho)$. That specific case is when the J and L parameters are customarily defined by expanding $e_2^{\text{IS}}(\rho)$ around saturation density (ρ_0) as

$$e_2^{\text{IS}}(\rho) = J + L\varepsilon + \mathcal{O}[\varepsilon^2], \quad (6)$$

where $\varepsilon \equiv (\rho - \rho_0)/3\rho_0$. Note that ρ_0 would be also affected by ISB effects.

Neutron matter pressure at saturation density. Assuming isospin symmetry, the contribution to the total pressure of neutron matter ($\beta = 1$) at saturation would be proportional to L ,

$$P^{\text{IS}}(\rho_0, \beta = 1) = \rho^2 \left. \frac{\partial e^{\text{IS}}(\rho, \beta)}{\partial \rho} \right|_{\rho=\rho_0} = \frac{1}{3} \rho_0 L, \quad (7)$$

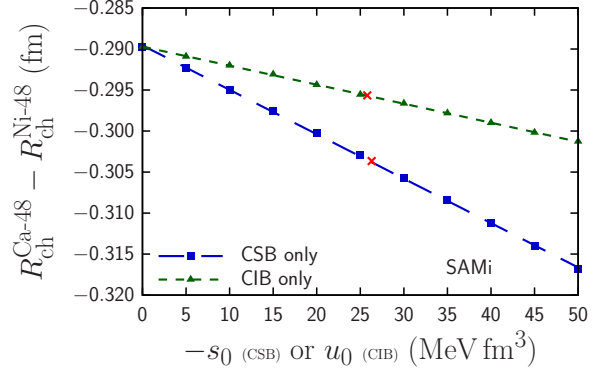


FIG. 2. SAMi EDF predictions for the charge radius difference between ^{48}Ca and ^{48}Ni as a function of the CSB $-s_0$ (blue squares) and CIB u_0 (green triangles) parameters. As a reference, the predictions in Ref. [11] for those parameters are given by red crosses. The values of y_0 and z_0 have been fixed to -1 .

but this is not the case if nuclear ISB terms are included,

$$P(\rho_0, \beta = 1) = \rho^2 \left. \frac{\partial e(\rho, \beta)}{\partial \rho} \right|_{\rho=\rho_0} = \frac{1}{3} \rho_0 (L + L_{\text{CIB}} + L_{\text{CSB}}). \quad (8)$$

In the last equation,

$$L_{\text{CSB}} \equiv \frac{3}{8} s_0 \rho_0 (1 - y_0), \quad (9a)$$

$$L_{\text{CIB}} \equiv \frac{9}{16} u_0 \rho_0. \quad (9b)$$

The value of the CSB parameter s_0 has been studied in the literature in Refs. [11,28] giving results in qualitative agreement, i.e., the values proposed in Ref. [28] have the same sign and are about half of those of Ref. [11]. The value of the CIB parameter u_0 has only been studied in [11]. In more detail, in Ref. [11], the values of the ISB parameters built on top of the SAMi EDF (SAMi-ISB) have been found in a semiphenomenological way. This functional reproduce CIB contributions in symmetric nuclear matter as calculated in [48] while CSB has been fixed to reproduce the IAS in ^{208}Pb . The values are $s_0 = -26.3 \pm 0.7 \text{ MeV fm}^3$ and $u_0 = 25.8 \pm 0.4 \text{ MeV fm}^3$ with y_0 and z_0 fixed to -1 . These values would imply a change in the neutron pressure at saturation in Eq. (7) of about $-0.17 \text{ MeV fm}^{-3}$ due to CSB and $+0.12 \text{ MeV fm}^{-3}$ due to CIB, hence, canceling to a large extent. State-of-the-art *ab initio* calculations in neutron matter does not allow to resolve such ISB contributions to the neutron pressure at saturation (cf. Fig. 3, red band, Ref. [49]). This partial cancellation must be investigated in more detail since the CSB and CIB effects induce fundamental differences between $P(\rho_0, \beta = 1)$ and L .

In Ref. [28] the CSB s_0 parameter was estimated based on the analysis of mirror and triplet displacement energies of different isospin multiplets by using different Skyrme EDFs. The variations of s_0 values proposed in this reference are $-14.9 \pm 3.8 \text{ MeV fm}^3$ for SV-ISB, $-11.2 \pm 2.8 \text{ MeV fm}^3$

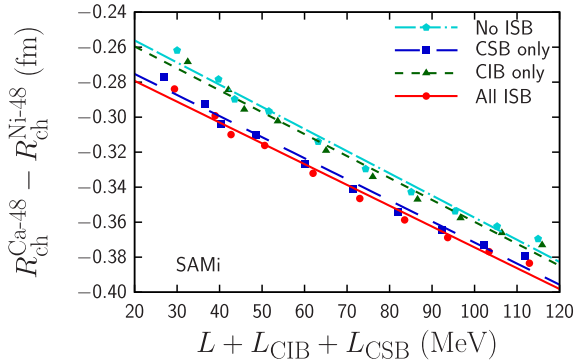


FIG. 3. ΔR_{ch} between ^{48}Ca and ^{48}Ni as a function of the $L + L_{\text{CIB}} + L_{\text{CSB}}$ parameter is shown as predicted by the SAMi-J family of EDFs. Different contributions are shown. Original SAMi-J given by circles and labeled by “No ISB” ($L_{\text{CIB}} = L_{\text{CSB}} = 0$); SAMi-J plus CSB in Eq. (2a) given as squares are labeled by “CSB only” ($L_{\text{CIB}} = 0$); SAMi-J plus CIB in Eq. (2b) given as triangles are labeled by “CIB only” ($L_{\text{CSB}} = 0$); and SAMi-J with all corrections given as circles is labeled as “All ISB”. All calculations include Coulomb within the LDA.

for SkM*-ISB, and $-11.2 \pm 2.2 \text{ MeV fm}^3$ for SLy4-ISB (cf. Table 1 in Ref. [28] where $s_0 = 2r_0^{\text{III}}$).

In Table I of Ref. [50], *ab initio* coupled cluster calculations based on the $\Delta\text{N}^2\text{LO}_{\text{GO}}(394)$ interaction are shown for ΔR_{ch} and binding energy difference (ΔB) in $^{48}\text{Ca} - ^{48}\text{Ni}$. The reported value for ΔB is $66.29(72) \text{ MeV}$ including all effects and $0.72(1) \text{ MeV}$ by neglecting Coulomb effects. The ΔB estimated value from the Atomic Mass Evaluation (AME2020) [51] is $68.67(40) \text{ MeV}$. The EDF proposed in Ref. [11], SAMi-ISB, predicts $\Delta B = 68.72 \text{ MeV}$, with an effect due to ISB of 7.88 MeV . Since ΔB is only due to nuclear ISB when Coulomb is neglected, it is evident that the latter EDF results are not in agreement with *ab initio* calculations in [50]. In more detail, by following the strategy proposed in [52], we have determined an effective s_0 value of -2 MeV fm^3 associated with the *ab initio* results for ΔB in $^{48}\text{Ca} - ^{48}\text{Ni}$ given in [50]. This value is one order of magnitude smaller than those from Refs. [11,28].

Variational Monte Carlo calculations [53] based on AV18 [54] for ΔB in $^{10}\text{Be} - ^{10}\text{C}$ would predict an effective s_0 of about -3 MeV fm^3 when using again the method proposed in [52]. Thus, they give a similar value to the one we have just discussed by using [50].

Regarding ΔR_{ch} in $^{48}\text{Ca} - ^{48}\text{Ni}$, the prediction in Ref. [50] is of $0.238 \pm 0.038 \text{ fm}$ for the full calculation while it is $0.261 \pm 0.035 \text{ fm}$ for the calculation neglecting Coulomb effects. SAMi-ISB predict instead 0.33 fm for the full calculation and 0.28 fm for the calculation neglecting Coulomb effects. These results reflect an opposite trend in ΔR_{ch} . Naively, the Coulomb potential (Ze^2/r) would be expected to increase the charge radius, more in absolute value as larger the Z of the nucleus. Hence, ΔR_{ch} would be expected to be larger when Coulomb is included. These contrasting results call for a dedicated theoretical effort since observables as relevant as the excitation energy of the isobaric analog state, the neutron-skin

thickness, or the difference in mass and charge radii of mirror nuclei would be affected.

In Fig. 2, we show the predictions of the SAMi EDF for the charge radius difference between ^{48}Ca and ^{48}Ni . Nuclear ISB contributions have been included perturbatively. Values of $-s_0$ and u_0 ($y_0 = z_0 = -1$) have been changed from 0 to 50 MeV fm^3 and the effects shown separately in the figure. As a reference, the values suggested in Ref. [11] are given by red crosses. It is important to note that both CSB and CIB are *coherent* and tend to make ΔR_{ch} larger in absolute value; by about 6% if $-s_0 \approx u_0 \approx 25 \text{ MeV fm}^3$.

These trends can be understood from the definition of the ISB interactions in Eq. (2). The CSB average potential felt by protons is proportional to the proton density and $-s_0$. This means that for $s_0 < 0$ protons feel a CSB repulsive potential that grows linearly with $\sim Z$ and, thus, the charge radii tends to increase with Z as well. The CIB average potential felt by protons is proportional to u_0 and to the difference $\sim Z - N/2$. For $u_0 > 0$ protons feel a repulsive CIB average potential, however, the charge radii do not grow as fast as for CSB case.

In Fig. 3, predictions of the SAMi-J family including ISB terms are given for ΔR_{ch} between ^{48}Ca and ^{48}Ni as a function of the L parameter. In this figure, calculations include Coulomb within the LDA and the ISB parameters have been fixed to be the same as for SAMi-ISB. It is seen that the main correction to the charge radius difference between the mirror nuclei ^{48}Ca and ^{48}Ni is due to CSB while CIB remains small. The average horizontal separation between the results is about 14 MeV and rather constant for the large range of values of $L + L_{\text{CIB}} + L_{\text{CSB}}$ displayed in that figure. If the values of s_0 obtained in [28] were considered, the correction on L would be milder and range between 6 and 11 MeV.

Conclusions. The effects discussed here are based on the ISB interactions in Eq. (1) but are independent of the EDF used as a basis. This is shown by the constant shift in Fig. 3. Hence, the different trends can be regarded as general provided the ISB interactions in Eq. (1) are realistic enough for the current purpose. Our results indicate that one must expect a systematic error on L whenever ISB is neglected. That is, whenever the analysis of mirror charge radii is implemented assuming isospin symmetry (L), this may lead to a systematic uncertainty due to the effect of neglected ISB terms (L_{CIB} and L_{CSB}) that can be taken into account by a renormalization of L to smaller values. The correction due to nuclear ISB based on our calculations of the mirror pair $^{48}\text{Ca} - ^{48}\text{Ni}$ would correspond to a shift to lower values of $10 \pm 4 \text{ MeV}$ and, even if not large, it needs to be incorporated—among other corrections [23]—by a sound study of ΔR_{ch} . For the same reasons, the neutron-skin thickness ΔR_{np} in a neutron-rich nucleus is also affected by ISB effects.

The situation is different in *ab initio* calculations [50,53], where the estimated effective value of s_0 seems to be one order of magnitude smaller than those inferred from current EDFs [11,28]. These contrasting results call for a dedicated theoretical effort to solve this overarching problem that impacts the energy of the isobaric analog state, the neutron-skin thickness, or the difference in mass and charge radii of mirror nuclei as well as it may impact astrophysical observables such as the mass, radius, and tidal deformability of a neutron star [55].

Acknowledgments. The authors thank S. Gandolfi and A. Ekström for useful discussions as well as R. B. Wiringa for providing us with Variational Monte Carlo calculations for ΔB in ^{10}Be - ^{10}C . T.N. and H.L. thank the RIKEN iTHEMS program and the RIKEN Pioneering Project: Evolution of Matter in the Universe. T.N. acknowledges the JSPS Grant-in-Aid for Research activity Start-up under Grant No. 22K20372, the RIKEN Special Postdoctoral Researchers Program, and the Science and Technology Hub

Collaborative Research Program from RIKEN Cluster for Science, Technology and Innovation Hub (RCSTI). H.L. acknowledges the JSPS Grant-in-Aid for Early-Career Scientists under Grant No. 18K13549 and the Grant-in-Aid for Scientific Research (S) under Grant No. 20H05648. H.S. acknowledges the Grant-in-Aid for Scientific Research (C) under Grant No. 19K03858. The numerical calculations were performed on cluster computers at the RIKEN iTHEMS program.

-
- [1] P. Campbell, I. Moore, and M. Pearson, Laser spectroscopy for nuclear structure physics, *Prog. Part. Nucl. Phys.* **86**, 127 (2016).
- [2] T. Suda and H. Simon, Prospects for electron scattering on unstable, exotic nuclei, *Prog. Part. Nucl. Phys.* **96**, 1 (2017).
- [3] R. F. Garcia Ruiz *et al.*, Unexpectedly large charge radii of neutron-rich calcium isotopes, *Nat. Phys.* **12**, 594 (2016).
- [4] C. Gorges, L. V. Rodríguez, D. L. Balabanski, M. L. Bissell, K. Blaum, B. Cheal, R. F. Garcia Ruiz, G. Georgiev, W. Gins, H. Heylen, A. Kanellakopoulos, S. Kaufmann, M. Kowalska, V. Lagaki, S. Lechner, B. Maaß, S. Malbrunot-Ettenauer, W. Nazarewicz, R. Neugart, G. Neyens *et al.*, Laser Spectroscopy of Neutron-Rich Tin Isotopes: A Discontinuity in Charge Radii Across the $N = 82$ Shell Closure, *Phys. Rev. Lett.* **122**, 192502 (2019).
- [5] S. Chen, J. Lee, P. Doornenbal, A. Obertelli, C. Barbieri, Y. Chazono, P. Navrátil, K. Ogata, T. Otsuka, F. Raimondi, V. Somà, Y. Utsuno, K. Yoshida, H. Baba, F. Browne, D. Calvet, F. Château, N. Chiga, A. Corsi, M. L. Cortés *et al.*, Quasifree Neutron Knockout from ^{54}Ca Corroborates Arising $N = 34$ Neutron Magic Number, *Phys. Rev. Lett.* **123**, 142501 (2019).
- [6] K. Tsukada, A. Enokizono, T. Ohnishi, K. Adachi, T. Fujita, M. Hara, M. Hori, T. Hori, S. Ichikawa, K. Kurita, K. Matsuda, T. Suda, T. Tamae, M. Togasaki, M. Wakasugi, M. Watanabe, and K. Yamada, First Elastic Electron Scattering from ^{132}Xe at the Scrit Facility, *Phys. Rev. Lett.* **118**, 262501 (2017).
- [7] A. Antonov, M. Gaidarov, M. Ivanov, D. Kadrev, M. Aïche, G. Barreau, S. Czajkowski, B. Jurado, G. Belier, A. Chatillon, T. Granier, J. Taïeb, D. Doré, A. Letourneau, D. Ridikas, E. Dupont, E. Berthoumieux, S. Panebianco, F. Farget, C. Schmitt *et al.*, The electron-ion scattering experiment ELISe at the International Facility for Antiproton and Ion Research (FAIR)-A conceptual design study, *Nucl. Instrum. Methods Phys. Res. A* **637**, 60 (2011).
- [8] B. A. Brown, Mirror Charge Radii and the Neutron Equation of State, *Phys. Rev. Lett.* **119**, 122502 (2017).
- [9] B. Brown, W. Richter, and R. Lindsay, Displacement energies with the Skyrme Hartree-Fock method, *Phys. Lett. B* **483**, 49 (2000).
- [10] X. Roca-Maza, M. Centelles, X. Viñas, and M. Warda, Neutron Skin of ^{208}Pb , Nuclear Symmetry Energy, and the Parity Radius Experiment, *Phys. Rev. Lett.* **106**, 252501 (2011).
- [11] X. Roca-Maza, G. Colò, and H. Sagawa, Nuclear Symmetry Energy and the Breaking of the Isospin Symmetry: How Do They Reconcile with Each Other? *Phys. Rev. Lett.* **120**, 202501 (2018).
- [12] M. Baldo and G. Burgio, The nuclear symmetry energy, *Prog. Part. Nucl. Phys.* **91**, 203 (2016).
- [13] M. Oertel, M. Hempel, T. Klahn, and S. Typel, Equations of state for supernovae and compact stars, *Rev. Mod. Phys.* **89**, 015007 (2017).
- [14] X. Roca-Maza and N. Paar, Nuclear equation of state from ground and collective excited state properties of nuclei, *Prog. Part. Nucl. Phys.* **101**, 96 (2018).
- [15] M. B. Tsang, J. R. Stone, F. Camera, P. Danielewicz, S. Gandolfi, K. Hebeler, C. J. Horowitz, J. Lee, W. G. Lynch, Z. Kohley, R. Lemmon, P. Möller, T. Murakami, S. Riordan, X. Roca-Maza, F. Sammarruca, A. W. Steiner, I. Vidaña, and S. J. Yennello, Constraints on the symmetry energy and neutron skins from experiments and theory, *Phys. Rev. C* **86**, 015803 (2012).
- [16] C. J. Horowitz, E. F. Brown, Y. Kim, W. G. Lynch, R. Michaels, A. Ono, J. Piekarewicz, M. B. Tsang, and H. H. Wolter, A way forward in the study of the symmetry energy: Experiment, theory, and observation, *J. Phys. G: Nucl. Part. Phys.* **41**, 093001 (2014).
- [17] F. J. Fattoyev, J. Piekarewicz, and C. J. Horowitz, Neutron Skins and Neutron Stars in the Multimessenger Era, *Phys. Rev. Lett.* **120**, 172702 (2018).
- [18] S. Abrahamyan *et al.* (PREX Collaboration), Measurement of the Neutron Radius of ^{208}Pb through Parity Violation in Electron Scattering, *Phys. Rev. Lett.* **108**, 112502 (2012).
- [19] D. Adhikari, H. Albataineh, D. Androic, K. Aniol, D. S. Armstrong, T. Averett, C. Ayerbe Gayoso, S. Barcus, V. Bellini, R. S. Beminiwattha, J. F. Benesch, H. Bhatt, D. Bhatta Pathak, D. Bhetuwal, B. Blaikie, Q. Campagna, A. Camsonne, G. D. Cates, Y. Chen, C. Clarke, and X. Zheng *et al.* (PREX Collaboration), Accurate Determination of the Neutron Skin Thickness of ^{208}Pb through Parity-Violation in Electron Scattering, *Phys. Rev. Lett.* **126**, 172502 (2021).
- [20] H. Sotani, N. Nishimura, and T. Naito, New constraints on the neutron-star mass and radius relation from terrestrial nuclear experiments, *Prog. Theor. Exp. Phys.* **2022**, 041D01 (2022).
- [21] B. A. Brown, K. Minamisono, J. Piekarewicz, H. Hergert, D. Garand, A. Klose, K. König, J. D. Lantis, Y. Liu, B. Maaß, A. J. Miller, W. Nörtershäuser, S. V. Pineda, R. C. Powel, D. M. Rossi, F. Sommer, C. Sumithrarachchi, A. Teigelhöfer, J. Watkins, and R. Wirth, Implications of the $^{36}\text{Ca} - ^{36}\text{S}$ and $^{38}\text{Ca} - ^{38}\text{Ar}$ difference in mirror charge radii on the neutron matter equation of state, *Phys. Rev. Res.* **2**, 022035(R) (2020).
- [22] S. V. Pineda, K. König, D. M. Rossi, B. A. Brown, A. Incorvati, J. Lantis, K. Minamisono, W. Nörtershäuser, J. Piekarewicz, R. Powel, and F. Sommer, Charge Radius of Neutron-Deficient ^{54}Ni and Symmetry Energy Constraints Using the Difference in Mirror Pair Charge Radii, *Phys. Rev. Lett.* **127**, 182503 (2021).

- [23] P.-G. Reinhard and W. Nazarewicz, Information content of the differences in the charge radii of mirror nuclei, *Phys. Rev. C* **105**, L021301 (2022).
- [24] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevC.106.L061306> for a detailed analysis on deformation and pairing effects in ^{48}Ni .
- [25] M. Stoitsov, N. Schunck, M. Kortelainen, N. Michel, H. Nam, E. Olsen, J. Sarich, and S. Wild, Axially deformed solution of the Skyrme-Hartree-Fock-Bogoliubov equations using the transformed harmonic oscillator basis (ii) HFBTHO v2.00d: A new version of the program, *Comput. Phys. Commun.* **184**, 1592 (2013).
- [26] E. Chabanat, P. Bonche, P. Haensel, J. Meyer, and R. Schaeffer, A Skyrme parametrization from subnuclear to neutron star densities. Part II. Nuclei far from stabilities, *Nucl. Phys. A* **635**, 231 (1998).
- [27] J. Bartel, P. Quentin, M. Brack, C. Guet, and H.-B. Håkansson, Towards a better parametrisation of Skyrme-like effective forces: A critical study of the SKM force, *Nucl. Phys. A* **386**, 79 (1982).
- [28] P. Bączyk, J. Dobaczewski, M. Konieczka, W. Satuła, T. Nakatsukasa, and K. Sato, Isospin-symmetry breaking in masses of $N = Z$ nuclei, *Phys. Lett. B* **778**, 178 (2018).
- [29] M. Bender, P.-H. Heenen, and P.-G. Reinhard, Self-consistent mean-field models for nuclear structure, *Rev. Mod. Phys.* **75**, 121 (2003).
- [30] G. Colò, Nuclear density functional theory, *Adv. Phys.: X* **5**, 1740061 (2020).
- [31] *Energy Density Functional Methods for Atomic Nuclei*, edited by N. Schunck (IOP Publishing, Bristol, 2019), pp. 2053–2563.
- [32] S. Goriely, N. Chamel, and J. M. Pearson, Further explorations of Skyrme-Hartree-Fock-Bogoliubov mass formulas. XIII. The 2012 atomic mass evaluation and the symmetry coefficient, *Phys. Rev. C* **88**, 024308 (2013).
- [33] A. V. Afanasjev and S. E. Agbemava, Covariant energy density functionals: Nuclear matter constraints and global ground state properties, *Phys. Rev. C* **93**, 054310 (2016).
- [34] P.-G. Reinhard and W. Nazarewicz, Nuclear charge densities in spherical and deformed nuclei: Toward precise calculations of charge radii, *Phys. Rev. C* **103**, 054310 (2021).
- [35] X. Roca-Maza, M. Brenna, B. K. Agrawal, P. F. Bortignon, G. Colò, L. G. Cao, N. Paar, and D. Vretenar, Giant quadrupole resonances in ^{208}Pb , the nuclear symmetry energy, and the neutron skin thickness, *Phys. Rev. C* **87**, 034301 (2013).
- [36] G. Colò, L. Cao, N. Van Giai, and L. Capelli, Self-consistent RPA calculations with Skyrme-type interactions: The `skyrme_rpa` program, *Comput. Phys. Commun.* **184**, 142 (2013).
- [37] X. Roca-Maza, G. Colò, and H. Sagawa, New Skyrme interaction with improved spin-isospin properties, *Phys. Rev. C* **86**, 031306(R) (2012).
- [38] T. Naito, R. Akashi, and H. Liang, Application of a Coulomb energy density functional for atomic nuclei: Case studies of local density approximation and generalized gradient approximation, *Phys. Rev. C* **97**, 044319 (2018).
- [39] T. Naito, X. Roca-Maza, G. Colò, and H. Liang, Coulomb exchange functional with generalized gradient approximation for self-consistent Skyrme Hartree-Fock calculations, *Phys. Rev. C* **99**, 024309 (2019).
- [40] T. Naito, X. Roca-Maza, G. Colò, and H. Liang, Effects of finite nucleon size, vacuum polarization, and electromagnetic spin-orbit interaction on nuclear binding energies and radii in spherical nuclei, *Phys. Rev. C* **101**, 064311 (2020).
- [41] B. A. Brown, New Skyrme interaction for normal and exotic nuclei, *Phys. Rev. C* **58**, 220 (1998).
- [42] S. Goriely and J. M. Pearson, Further explorations of Skyrme-Hartree-Fock-Bogoliubov mass formulas. VIII. role of Coulomb exchange, *Phys. Rev. C* **77**, 031301(R) (2008).
- [43] G. Miller, B. Nefkens, and I. Šlaus, Charge symmetry, quarks and mesons, *Phys. Rep.* **194**, 1 (1990).
- [44] H. Sagawa, N. Van Giai, and T. Suzuki, Isospin mixing and the sum rule of super-allowed fermi beta-decay, *Phys. Lett. B* **353**, 7 (1995).
- [45] P. Bączyk, W. Satuła, J. Dobaczewski, and M. Konieczka, Isobaric multiplet mass equation within nuclear density functional theory, *J. Phys. G: Nucl. Part. Phys.* **46**, 03LT01 (2019).
- [46] P. Bączyk and W. Satuła, Mirror energy differences in $T = 1/2$ $f_{7/2}$ -shell nuclei within isospin-dependent density functional theory, *Phys. Rev. C* **103**, 054320 (2021).
- [47] I. Vidaña, C. Providência, A. Polls, and A. Rios, Density dependence of the nuclear symmetry energy: A microscopic perspective, *Phys. Rev. C* **80**, 045806 (2009).
- [48] H. Müther, A. Polls, and R. Machleidt, Isospin symmetry breaking nucleon-nucleon potentials and nuclear structure, *Phys. Lett. B* **445**, 259 (1999).
- [49] D. Lonardoni, I. Tews, S. Gandolfi, and J. Carlson, Nuclear and neutron-star matter from local chiral interactions, *Phys. Rev. Res.* **2**, 022033(R) (2020).
- [50] S. J. Novario, D. Lonardoni, S. Gandolfi, and G. Hagen, Trends of neutron skins and radii of mirror nuclei from first principles (2021), [arXiv:2111.12775](https://arxiv.org/abs/2111.12775).
- [51] M. Wang, W. Huang, F. Kondev, G. Audi, and S. Naimi, The AME 2020 atomic mass evaluation (II). Tables, graphs and references, *Chin. Phys. C* **45**, 030003 (2021).
- [52] T. Naito, G. Colò, H. Liang, X. Roca-Maza, and H. Sagawa, Toward *ab initio* charge symmetry breaking in nuclear energy density functionals, *Phys. Rev. C* **105**, L021304 (2022).
- [53] R. B. Wiringa (private communication).
- [54] R. B. Wiringa, V. G. J. Stoks, and R. Schiavilla, Accurate nucleon-nucleon potential with charge-independence breaking, *Phys. Rev. C* **51**, 38 (1995).
- [55] G. Selva, X. Roca-Maza, and G. Colò, Isospin symmetry breaking effects on the mass-radius relation of a neutron star, *Symmetry* **13**, 144 (2021).