Distinct sequential and massive transfer processes for production of neutron-rich $N ≈ 126$ nuclei in $23\sqrt{8}$ U + 198 Pt reactions

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To investigate the underlying mechanisms responsible for the enhanced production of new neutron-rich $N \approx 126$ nuclei in the reaction ²³⁸U + ¹⁹⁸Pt, detailed simulations of the system at an incident energy of 8 MeV/nucleon using the improved quantum molecular dynamics model have been performed. Sequential and massive transfer processes, responsible for the production of targetlike and projectilelike *n*-rich $N \approx 126$ fragments, respectively, have been recognized. Compared to sequential transfer, the contribution from the massive transfer process plays an almost equal role for the production of new nuclei with atomic number $Z \leq 76$. The two processes show distinct features in the angular and kinetic energy distributions in the laboratory system and hopefully can be disentangled experimentally.

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The properties of neutron-rich $N \approx 126$ nuclei are essential for understanding the astrophysical *r*-process abundance peak around $A = 195$ [\[1\]](#page-4-0) and the evolution of the $N = 126$ neutron shell closure far from the β-stability line $[2,3]$. Multinucleon transfer (MNT) reaction has been proposed as an alternative approach of great potential to synthesize these $N = 126$ *r*-process waiting-point nuclei [\[4,5\]](#page-4-0). Considering that the ground-state *Q* values favor the transfer of protons from lead to xenon in the reaction $136Xe + 208Pb$, Zagrebaev and Greiner proposed to take advantage of the stabilizing effects of the neutron closed shells at $N = 82$ for ¹³⁶Xe and $N = 126$ for ²⁰⁸Pb to enhance the production of $N \approx 126$ isotones below ^{208}Pb [\[4\]](#page-4-0). However, no evidence for such multiproton transfer was found in the experiments performed at Dubna and Argonne [\[6,7\]](#page-4-0). The GRAZING code calculations showed a significant advantage of the system $136Xe + 198Pt$ over 136 Xe + 208 Pb for producing new $N = 126$ isotopes because of larger neutron transfer probability compared to

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proton [\[8\]](#page-4-0). In the experiment of $^{136}Xe + ^{198}Pt$ at the incident energy of ≈ 8 MeV/nucleon performed at GANIL [\[9\]](#page-4-0), the cross sections for $N = 126$ isotones were deduced and MNT reactions showed an obvious advantage over the fragmentation of the ²⁰⁸Pb beam on the Be target $[10]$ in the production of very neutron-rich nuclei with proton number $Z \leqslant 77$. MNT reactions between symmetric massive nuclei, such as ²⁰⁴Hg with 198 Pt and 208 Pb, were performed at Argonne [\[11,12\]](#page-4-0). Rather neutron-rich transfer products were populated but no new isotopes in this region were observed up to now.

The dynamical processes involved in the MNT reactions attracted much interest in theoretical studies using different approaches. The effects of dynamical deformation on the potential energy surface and the mass distribution were investigated in the dinuclear system (DNS) framework [\[13–15\]](#page-4-0). In the calculations performed with the improved quantum molecular dynamics (ImQMD) model, the energy dissipation in the 136 Xe + 198 Pt system was found to be strongly associated with the incident energy $[16]$. In the stochastic mean-field approach, the mass distribution of primary fragments and the production of isotopes heavier than the target in the multinucleon transfer of $^{136}Xe + ^{208}Pb$

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were better reproduced by considering the quantal diffusion mechanism [\[17,18\]](#page-4-0).

The reaction between 238 U and 198 Pt was initially suggested as an alternative for the production of $N \approx 126$ neutron-rich nuclei by Zagrebaev and Greiner [\[19\]](#page-4-0). The calculated production cross sections for these neutron-rich nuclei were on average higher than those in the collision of $136Xe$ with ^{208}Pb or ^{198}Pt by the Langevin approach [\[19\]](#page-4-0) and the DNS model [\[20\]](#page-4-0). And such cross-section enhancement was confirmed by our recent calculations using the ImQMD model [\[21\]](#page-4-0). Due to the complicated dynamical processes involved, such as the coupling of single-particle and collective degrees of freedom, sequential nucleon transfer was assumed to play a main role in mass rearrangement in the Langevin approach [\[19\]](#page-4-0), and only one nucleon transfer was considered in the DNS model [\[20\]](#page-4-0). Compared to the single-nucleon transfer, the transfer of massive clusters was proposed and supported by the observed large cross sections for the production of heavier actinides in Ref. [\[22\]](#page-4-0). The sequential transfer and the simultaneous transfer of several nucleons were also discussed based on the experimental measurements of reactions with the target 232 Th [\[23,24\]](#page-4-0). However, the detailed dynamical mechanisms of two transfer processes and their effects on the production of primary fragments are still unclear.

In the investigation of the underlying mechanism responsible for the favored production of neutron-rich $N \approx 126$ species in the reaction system $^{238}U + ^{198}Pt$, the dynamical process of massive transfer is revealed by using the ImQMD model in the present work. In the model, a variety of degrees of freedom, such as neck formation, nucleon transfer, deformations of two colliding nuclei, and different types of separation of the composite system, can be considered simultaneously [\[25\]](#page-4-0). Over 3 000 000 events of the system $^{238}U + ^{198}Pt$ are simulated at an incident energy of 8 MeV/nucleon and different impact parameters. At the initial time of reaction, the distance between the centers of mass of the projectile and the target is taken to be 30 fm. The decays of primary fragments produced in the ImQMD model are described by the statistical evaporation model (HIVAP code) [\[26,27\]](#page-5-0). A detailed description of the method of ImQMD + HIVAP can be found in Ref. [\[21\]](#page-4-0).

Here we take the production of the primary fragment 204 Pt $(N = 126)$ as an example and plot two different events at an impact parameter of $b = 6.0$ fm of the ²³⁸U + ¹⁹⁸Pt reaction at an incident energy of 8 MeV/nucleon in Fig. 1. They are the snapshots at three moments, namely, the touching of the projectile and the target, a moment in the multinucleon transfer process, and the reseparation of the composite system. Nucleons originated from the projectile and the target are represented in red and green, respectively. Event I presents a simple scenario where the targetlike fragment ²⁰⁴Pt is produced by the transfer of six neutrons from the projectile to the target. Event II illustrates the transfer of a large number of nucleons from the projectile to the target. The remaining nucleons of the projectile ²³⁸U and several nucleons transferred from the target 198 Pt form the primary projectilelike fragment 204 Pt in event II. In Fig. 1, the *z* axis is set as the beam direction and the *x* axis as the impact parameter. In the two cases, the pictures of the systems are quiet similar at

FIG. 1. The snapshots at three different moments of two examples producing primary fragments 204Pt at an impact parameter of $b = 6.0$ fm in the ²³⁸U + ¹⁹⁸Pt reaction at an incident energy of 8 MeV/nucleon.

the touching point, but very different at the reseparation of the composite systems. The fragment 204Pt is produced along the trajectory of the target in event I, while it is produced along that of the projectile in event II.

Figure 2 depicts the density along the axis of the system, which passes the centers of the projectilelike fragments (PLFs) and the targetlike fragments (TLFs), at different reaction times in the two events of Fig. 1. The neck region, having the smallest density between the two centers, is denoted in blue. In event I, the neck can be recognized easily as the density is always lower than 0.04 fm⁻³, which is consistent with the picture of the sequential transfer of a few nucleons between two colliding nuclei. The neck position barely changed from the touching of the projectile and the target to the reseparation of the composite system. In event II, a bulky mass shifting from the projectile to the target with a high-density region over 0.14 fm^{-3} (denoted in red) occurs. It corresponds to the collective transfer of a large number of nucleons. It results in the shift of the neck region by about 4 fm towards the projectile in a short time. Therefore, two completely different dynamical processes are revealed in events I and II, leading to the production of the same primary fragment 204 Pt.

FIG. 2. The density evolution around the neck region for the two events shown in Fig. 1. The density is calculated along the axis of the system, which passes the centers of the PLFs and the TLFs.

FIG. 3. (a) The nucleon exchange rates, (b) the average lifetimes of the composite systems (c.s.), and (c) the cross sections for producing the primary fragment 204Pt as a function of impact parameters for different ξ groups.

In most events, the primary fragment 204 Pt is produced by the exchange of nucleons between the projectile and the target in both directions. To investigate the feature of the production mechanisms of primary fragments, we define a variable to describe the extent of nucleon transfer as $\xi = A_F^P/A_F$, where A_F is the mass number of the fragment and A_F^P is the number of nucleons coming from the projectile in this fragment. We take $A_{\text{ex}}/\tau_{\text{c.s.}}$ as the nucleon exchange rate, i.e., the average number of exchanged nucleons per unit time, where *A*ex is the total number of nucleons exchanged between the projectile and the target. $\tau_{\text{c.s.}}$ is the lifetime of the composite system (c.s.), which is defined as the time interval between touching of two colliding nuclei and reseparation of the composite system. Figure 3 displays the average values of $A_{ex}/\tau_{c.s.}$, $\tau_{\text{c.s.}}$, and the corresponding production cross sections for the primary fragment ²⁰⁴Pt. They are grouped according to ξ values as functions of the impact parameters. As shown in Fig. $3(a)$, the nucleon exchange rates for the production of PLFs ($\xi > 0.5$) and TLFs ($\xi < 0.5$) at large impact parameters are very different: the former is almost twice the latter. As the impact parameter decreases, the nucleon exchange rates for both increase and saturate to nearly an identical value. It is noted that the production of the 204 Pt PLFs requires the net transfer of 34 nucleons, while only 6 nucleons are required for the production of the ²⁰⁴Pt TLFs. In Fig. $3(b)$, the average lifetimes of the composite systems for five groups of ξ decrease monotonically with increasing the impact parameter. The longest corresponds to the central collision where more nucleons are exchanged, while the shortest corresponds to peripheral collisions where the primary fragments are produced as either TLFs with the smallest ξ or PLFs with the largest ξ . For TLFs of ξ < 0.5, they can be understood by the

FIG. 4. The angular distributions of (a) primary and (b) residual fragments of 204 Pt produced in the 238 U + 198 Pt system at 8 MeV/nucleon in the laboratory system. Panels (c) and (d) present the distributions of kinetic energies of primary and residual 204 Pt, respectively.

sequential transfer of nucleons between two colliding nuclei. The transfer of more nucleons needs a longer lifetime of the composite system and generally occurs at smaller impact parameters. The group with the largest ξ (PLFs are denoted by red diamonds) is produced at similar impact parameters with the smallest ξ group (TLFs are denoted by black squares). In these PLFs, at least 34 nucleons are transferred from the projectile 238 U to the target for producing the primary fragment 204 Pt. The sequential transfer of nucleons cannot explain the short lifetime of the composite system denoted by the red diamonds. As Fig. [2](#page-1-0) shows, large mass collective transfer plays a critical role in both the production of these PLFs and the evolution of the corresponding composite system. In Fig. $3(c)$, the production cross-section curve has a parabolalike shape for each group. The biggest contribution comes from TLFs produced in peripheral collisions at large impact parameters.

The different production mechanisms of 204 Pt in $^{238}U + ^{198}Pt$ revealed above are also present in the distributions of emitting angles and kinetic energies. In Fig. 4, we divide the production processes of 204 Pt into two groups, i.e., PLFs with $\xi > 0.5$ and TFLs with $\xi < 0.5$. Figures $4(a)$ and $4(b)$ illustrate the angular distributions of primary and residual ²⁰⁴Pt fragments by blue lines in the laboratory system. For both primary and residual fragments, two peaks located at 30◦ and 53◦ come from the PLFs and TLFs, respectively. The distributions of kinematic energies in the laboratory system are shown in Figs. $4(c)$ and $4(d)$. The PLF and TLF components are also distinguishable, corresponding to the two bumps at about 1200 and 600 MeV.

Similar behavior is also found in the angular distributions of new isotopes of Os, Re, W, and Ta (see Fig. [5\)](#page-3-0). Open

FIG. 5. The angular distributions of new isotopes in primary and residual fragments of elements (a) Os, (b) Re, (c) W, and (d) Ta in the laboratory system.

and solid symbols represent primary and residual fragments, respectively. For new neutron-rich isotopes with lower atomic number, the contributions of the PLFs are significantly enhanced relative to TLFs compared to 204 Pt. However, the two peaks get closer to each other with decreasing atomic number and are less distinguishable for neutron-rich Ta isotopes. The production cross sections for these residual fragments depend on the cross sections for primary fragments and their excitation energies. Figure 6 shows the average excitation energies of the primary fragments as a function of ξ . The excitation energies of primary fragments peak around $\xi = 0.5$, corresponding to central collisions with the maximum number of nucleons exchanged and the longest lifetime of the composite system. The smallest and largest ξ values corresponding to peripheral collisions induce lower excitation energies. This is consistent with the correlation between the lifetime of the

FIG. 6. The distributions of the average excitation energies of primary fragments of (a) Os, (b) Re, (c) W, and (d) Ta.

FIG. 7. The distributions of the average number of neutrons evaporated from primary fragments of (a) Os, (b) Re, (c) W, and (d) Ta.

composite system and ξ shown in Fig. [3\(b\).](#page-2-0) In the case of a shorter lifetime, large mass collective transfer leads to lower excitation energies of primary fragments. The residual fragments of new neutron-rich nuclei are mainly produced by the evaporation of neutrons in the decay of the above primary fragments of Os, Re, W, and Ta. The average numbers of neutrons evaporated from per primary fragment of Os, Re, W, and Ta are presented in Fig. 7. Figure 7 shows a similar distribution to the excitation energies presented in Fig. 6. The largest excitation energies around $\xi = 0.5$ lead to the evaporation of more than ten neutrons. Fewer neutrons are evaporated in the decay of PLFs with larger ξ or TLFs with smaller ξ , both of which contribute to the survival of new neutron-rich nuclei. Figure 7 also indicates that the projectilelike fragments play a significantly important role in the production of these nuclei.

To summarize, the underlying mechanism responsible for the enhanced production of neutron-rich $N \approx 126$ nuclei with $Z \le 78$ in the reaction ²³⁸U + ¹⁹⁸Pt at an incident energy of 8 MeV/nucleon has been investigated by using the ImQMD model. In addition to TLFs, the contribution from PLFs to the production cross sections for these fragments has been found. Distinct dynamical processes are revealed in the production of PLFs and TLFs. Sequential transfer of nucleons plays a key role in producing TLFs, while massive transfer of nucleons plays a key role in producing PLFs. The difference between them manifests itself not only in the dynamical processes but also in the angular and kinetic energy distributions. The latter originated from PLF and TLF components can be distinguished in the experimental measurements.

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