Cross sections of photoneutron reactions on ¹⁸¹Ta at $E_{\nu max}$ up to 95 MeV

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The total bremsstrahlung flux-averaged cross sections $\langle \sigma(E_{\gamma \max}) \rangle$ for the photonuclear reactions ${}^{181}\text{Ta}(\gamma, xn; x \leq 8)^{181-x}\text{Ta}$ have been measured in the range of end-point energies $E_{\gamma \max}$ up to 95 MeV. The experiments were performed with the beam from the NSC KIPT electron linear accelerator LUE-40 with the use of the activation and offline γ -ray spectrometric technique. The calculation of average cross sections was carried out using the cross section values computed with the TALYS1.95 code for different level density models LD 1–6. A comparison between the experimental total cross sections $\langle \sigma(E_{\gamma \max}) \rangle$ and the theoretical values has shown satisfactory agreement for the ${}^{181}\text{Ta}(\gamma, xn)$ reactions with the escape of 1–7 neutrons.

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I. INTRODUCTION

Studies into multiparticle photonuclear reactions in the energy range above the giant dipole resonance (GDR) and up to the pion production threshold ($E_{\rm th} \approx 145$ MeV) are of particular interest. This is because in the energy region under consideration a change in the mechanism of photonuclear interaction takes place; i.e., detailed knowledge can be obtained about the competition between two mechanisms of nuclear photodisintegration, namely, through the GDR excitation and the quasideuteron photoabsorption [1].

To describe the mechanism of multiparticle photonuclear reactions, various theoretical models have been developed. For example, a combined model of photonucleon reactions was worked out in Ref. [2], which united the semiempirical model of oscillations, the quasideuteron model of photoabsorption, the exciton and evaporation models. For illustration, that model was tested using the data on relative yields from the 181 Ta(γ , xn) ${}^{181-x}$ Ta reactions with emission of up to six neutrons and also from the reactions ${}^{181}\text{Ta}(\gamma, p) {}^{180\text{m}}\text{Hf}$ and 181 Ta (γ, pn) 179m Hf with the charged particle in the outlet channel [3]. The combined-model calculations were also compared with the yields of isotopes produced in the photonuclear reactions on natural molybdenum at the end-point energy of the bremsstrahlung spectrum, $E_{\gamma max} = 67.7$ MeV [4]. Rodrigues et al. [5] proposed the Monte Carlo multicollisional intranuclear cascade model to study photonuclear reactions at intermediate energies ($20 \le E \le 140$ MeV); the model predictions were compared with the experimental total photoabsorption cross sections for the nuclei Sn, Ce, Ta, and Pb (see Ref. [6]) and with the calculated data from Ref. [1] in the energy range E = 25 to 132 MeV.

The modern Hauser-Feshbach nuclear reaction codes such as EMPIRE [7], TALYS [8], CCONE [9], and COH3 [10], used to calculate photoinduced reaction cross sections, also call for testing in a wide range of atomic masses and energies. Although at present there is a sufficient dataset on the experimental cross sections in the GDR energy region [11,12], the use of the data on single- or two-particle reactions only precludes testing various theoretical concepts, because the results of calculations by different models (e.g., nuclear level density computations *LD* 1–6 in the TALYS1.95 code) differ from each other only slightly. With the increase in the number of particles in the outlet channel of the reaction, the distinctions between different theoretical models become more prominent. This enables one to choose the optimum version of the computational model using the reaction cross-section data with $x \ge 3$. However, the experimental cross sections for photonuclear reactions with emission of a large number of particles are thus far still lacking.

The multiparticle photonuclear reactions that have relatively low cross sections can be observed with the availability of intense incident γ -quantum fluxes. These fluxes can be provided by electron linear accelerators with the use of targets-converters for bremsstrahlung generation. It should be noted that the experiments on bremsstrahlung beams substantially complicate the procedure of determining the photonuclear reaction cross sections. First of all, it is necessary to determine precisely the γ -quantum flux density to comply with the real experimental conditions. To this end, modern computational codes (e.g., GEANT4 or MCNP) should be used. Besides, the experiment implies the measurement of the integral characteristics of the reactions, and this calls for additional mathematical processing of the results. And yet, despite the arising difficulties, the bremsstrahlung beams are an important tool in the studies of photonuclear reactions.

Tantalum is used in structural, shielding, and bremsstrahlung target materials. Natural tantalum consists of a mixture of two isotopes, ¹⁸¹Ta and ^{180m}Ta, in the ratio of 8300 to 1. ¹⁸¹Ta presents a heavily deformed nucleus with the quadrupole deformation parameter $\beta = 0.26$ [11]. The deformation can give rise, for example, to a complex structure in the energy dependence of the ¹⁸¹Ta(γ , n) ¹⁸⁰Ta reaction cross section, which exhibits two peaks in the GDR region. The ^{180m}Ta isotope is the only stable isomer (within the sensitivity of current techniques), which comes under the so-called bypassed nuclei, the existence of which in nature poses the problem of search/investigation of the processes of heavy nuclei formation, which are not associated with the neutron capture.

The photodisintegration of ¹⁸¹Ta in the GDR range was experimentally investigated using beams of quasimonochromatic and bremsstrahlung γ quanta [6,13–19]. The result was that the total photoabsorption cross-section values for $\sigma(\gamma, abs)$ and $\sigma(\gamma, sn)$ were determined. The cross sections for photoneutron reactions on ¹⁸¹Ta were obtained by the method of direct neutron registration in the GDR region for (γ, n) and $(\gamma, 2n)$ (see Ref. [14]). In [15], measurements were made of the cross sections for the (γ, n) , $(\gamma, 2n)$, and $(\gamma, 3n)$ reactions, and also for the $(\gamma, 4n)$ reaction up to an energy of 36 MeV. Paper [20] presents the experimental results from NEW Subaru studies for the ¹⁸¹Ta(γ , xn; $x \leq 4$) reaction, and draws a comparison between the data obtained at different laboratories. The observed difference in the absolute values of the reaction cross sections determined by different methods gives impetus to conducting additional studies on tantalum photodisintegration. Note that the cross sections for photoproton and photoneutron reactions with x > 4 on the ¹⁸¹Ta nucleus have not been measured [12].

Several photonuclear reaction studies were carried out on the ¹⁸¹Ta nucleus with the use of γ -bremsstrahlung beams at energies higher than the GDR energy. The experiments have given the weighted average yield values at end-point energies of the bremsstrahlung spectrum, $E_{\gamma max} = 40$ and 55 MeV [21], and the relative yields at $E_{\gamma max} = 67.7$ MeV [3].

In work [22], the bremsstrahlung flux-averaged cross sections $\langle \sigma(E_{\gamma \text{max}}) \rangle$ were measured for photoneutron reactions on ¹⁸¹Ta with emission of up to 8 neutrons at $E_{\gamma \text{max}} = 80$ to 95 MeV. Along with that, a comparison with the TALYS1.9based computations was made. Note that the crosssection maxima for these reactions lie at energies below 80 MeV. The $\langle \sigma(E_{\gamma \text{max}}) \rangle$ data extension towards lower $E_{\gamma \text{max}}$ will make it possible to test the calculations in the region of cross-section maxima for the $x \leq 8n$ reactions, just as this was done, e.g., in Ref. [23] for the ¹⁸¹Ta(γ , 3n) ¹⁷⁸Ta reaction.

The present paper is concerned with measurements of the total average cross sections $\langle \sigma(E_{\gamma \max}) \rangle$ for photoneutron reactions on the ¹⁸¹Ta nucleus with emission of up to eight neutrons at end-point γ -bremsstrahlung energies $E_{\gamma \max} = 35$ to 80 MeV. The results obtained in this work are compared with our earlier data measured in the range $E_{\gamma \max} = 80-95$ MeV, and also with the calculations using the cross sections $\sigma(E)$ computed with the TALYS1.95 code for different nuclear level density models *LD* 1–6 [8].

II. EXPERIMENTAL PROCEDURE

A. Experimental setup

Experimental tantalum photodisintegration studies were carried out through measurements of the residual γ activity of the irradiated sample, which enables one to obtain simultaneously the data from different channels of photonuclear



FIG. 1. Schematic block diagram of the experiment. The upper part shows the measuring room, where the exposed target (red color) and the target monitor (blue color) are extracted from the capsule and are arranged in turn before the HPGe detector for induced γ -activity measurements. The lower part shows the accelerator LUE-40, the Ta converter, Al absorber, and exposure chamber.

reactions. This technique is well known and has been described in a variety of papers concerned with the investigation of multiparticle photonuclear reactions, e.g., on the nuclei ²⁷Al [24], ⁹³Nb [25–27], ¹⁸¹Ta [22,23].

The experimental setup is presented in Fig. 1. The γ -ray bremsstrahlung beam was generated by means of the NSC KIPT electron linac LUE-40 RDC Accelerator [28,29]. Electrons of the initial energy E_e were incident on the target-converter made from a 1.05 mm thick natural tantalum plate, measuring 20 by 20 mm. To remove electrons from the bremsstrahlung flux, a cylindrical aluminum absorber, 100 mm in diameter and 150 mm in length, was used.

The targets of diameter 8 mm, placed in the aluminum capsule, were arranged behind the Al absorber on the electron beam axis. For transporting the targets to the place of irradiation and back for induced activity registration, a pneumatic tube transfer system was used. On delivery of the irradiated targets to the measuring room, the samples are extracted from the aluminum capsule and are transferred one by one to the detector for the measurements. Taking into account the time of target delivery and extraction from the capsule, the cooling time for the sample under study took no more than 3 minutes.

The induced γ activity of the irradiated targets was registered by the semiconductor high-purity germanium (HPGe) detector Canberra GC-2018 with the resolutions of 0.8 and 1.8 keV (FWHM) for the energies $E_{\gamma} = 122$ and 1332 keV, respectively. Its efficiency was 20% relative to the NaI(Tl) detector, 3 inches in diameter and 3 inches in thickness. The absolute registration efficiency of the GC-2018 detector was calibrated with a standard set of γ -ray radiation sources: ²²Na, ⁶⁰Co, ¹³³Ba, ¹³⁷Cs, ¹⁵²Eu, and ²⁴¹Am.

The bremsstrahlung spectra of electrons were calculated by using the GEANT4.9.2 code [30] with due regard for the real geometry of the experiment, where consideration was given to spatial and energy distributions of the electron beam. The program code GEANT4.9.2 *PhysList G4LowEnergy* allows one to perform calculations taking properly into account all

Nuclear reaction	$E_{\rm th}~({\rm MeV})$	J^{π} of nucleus product	$T_{1/2}$	E_{ν} (keV)	I_{γ} (%)
$\frac{181}{180g}$	7 58	1+	8.152 ± 0.006 h	103557 ± 0.007	0.81 ± 0.16
181 Ta (γ, n) 180m Ta	7.65	1 9-	$>1.2 \times 10^{15} \text{ v}$	105.557 ± 0.007	0.01 ± 0.10
181 Ta $(\gamma, 2n)$ 179 Ta	14.22	7/2+	1.82 ± 0.03 y	54.611	13.6 ± 0.4
			•	55.790	23.7 ± 0.7
181 Ta $(\gamma, 3n)$ 178g Ta	22.05	1^{+}	$9.31 \pm 0.03 \text{ min}$	1350.68 ± 0.03	1.18 ± 0.03
181 Ta $(\gamma, 3n)^{178m}$ Ta	22.35	$(7)^{-}$	$2.36\pm0.08~\mathrm{h}$	426.383 ± 0.006	97.0 ± 1.3
181 Ta $(\gamma, 4n)$ 177 Ta	29.01	$7/2^+$	56.56 ± 0.06 h	112.9498 ± 0.0005	7.2 ± 0.8
181 Ta $(\gamma, 5n)$ 176 Ta	37.44	$(1)^{-}$	$8.09\pm0.05~\mathrm{h}$	1159.28 ± 0.09	25.00 ± 0.15^{a}
181 Ta $(\gamma, 6n)$ 175 Ta	44.46	7/2+	10.5 ± 0.2 h	348.5 ± 0.5	12.0 ± 0.6
181 Ta $(\gamma, 7n)$ 174 Ta	53.21	3+	$1.05\pm0.03~\mathrm{h}$	1205.92 ± 0.04	4.9 ± 0.4
181 Ta $(\gamma, 8n)$ 173 Ta	60.63	$5/2^{-}$	3.14 ± 0.13 h	172.2 ± 0.1	18.00 ± 0.15^{a}
100 Mo(γ , n) 99 Mo	8.29	$1/2^{+}$	$65.94\pm0.01~\mathrm{h}$	739.50 ± 0.02	12.13 ± 0.12

TABLE I. Spectroscopic data [31] on the nuclei products from the reactions ${}^{181}\text{Ta}(\gamma, xn; x = 1-8){}^{181-x}\text{Ta}$ and the monitoring reaction ${}^{100}\text{Mo}(\gamma, n){}^{99}\text{Mo}$.

^aError of intensity I_{γ} for the 1159.28 and 172.2 keV γ lines were determined as half-value spreads according to the databases of [31] and [32].

physical processes for the case of an amorphous target. Similarly, GEANT4.9.2 *PhysList QGSP BIC HP* makes it possible to calculate the neutron yield due to photonuclear reactions from targets of different thicknesses and atomic charges. In addition, the bremsstrahlung gamma fluxes were monitored by the yield of the ¹⁰⁰Mo(γ , n) ⁹⁹Mo reaction. For this purpose, the natural molybdenum target monitor, placed close by the target under study, was simultaneously exposed to radiation.

In the experiment, natural tantalum/molybdenum samples were exposed to radiation at end-point bremsstrahlung energies $E_{\gamma max}$ ranging from 35 to 80 MeV with an energy step of \approx 5 MeV. The masses of tantalum and molybdenum targets were, respectively, \approx 43 and \approx 60 mg. The time of irradiation, $t_{\rm irr}$, and the time of residual γ -activity spectrum measurement, $t_{\rm meas}$, were both 30 min.

Figure 2 shows the long-term measurement gamma spectrum from reaction products of the tantalum target in the E_{γ} range from 40 to 1500 keV.

Table I lists the parameter values of the reaction $^{181}\text{Ta}(\gamma, xn; x \leq 8)^{181-x}\text{Ta}$ and the monitoring reaction $^{100}\text{Mo}(\gamma, n)^{99}\text{Mo}$ according to the data from [31]: E_{th} are reaction thresholds; $J, \pi, T_{1/2}$ denote the spin, parity, and half-life period of the nuclei products, respectively; E_{γ} are the energies of the γ lines under study and their intensities are I_{γ} .

B. Calculation formulas for the flux-average cross sections

The cross sections $\langle \sigma(E_{\gamma \text{max}}) \rangle$ averaged over the bremsstrahlung γ flux $W(E, E_{\gamma \text{max}})$ from the threshold E_{th} of the reaction under study to the end-point energy of the spectrum $E_{\gamma \text{max}}$ were calculated with the use of the theoretical cross-section values $\sigma(E)$ computed with the TALYS1.95 code [8]. The theoretical bremsstrahlung flux-averaged cross section $\langle \sigma(E_{\gamma \text{max}}) \rangle$ in a given energy interval and the experimental ones were calculated by the formulas (1) and (2), respectively:

$$\langle \sigma(E_{\gamma \max}) \rangle = \Phi^{-1}(E_{\gamma \max}) \int_{E_{th}}^{E_{\gamma \max}} \sigma(E) W(E, E_{\gamma \max}) dE, \qquad (1)$$

$$\langle \sigma(E_{\gamma \max}) \rangle = \frac{\lambda \Delta A}{N_n I_\gamma \ \varepsilon \ \Phi(E_{\gamma \max}) [1 - \exp(-\lambda t_{irr})] \exp(-\lambda t_{cool}) [1 - \exp(-\lambda t_{meas})]}, \tag{2}$$

where $\triangle A$ is the number of counts of γ quanta in the full absorption peak, λ is the decay constant $(\ln 2/T_{1/2})$, N_n is the number of target atoms, I_{γ} is the absolute intensity of the analyzed γ quanta, ε is the absolute detection efficiency for the analyzed γ quanta energy, $\Phi(E_{\gamma \max}) = \int_{E_{\rm th}}^{E_{\gamma \max}} W(E, E_{\gamma \max}) dE$ is the integrated bremsstrahlung flux $W(E, E_{\gamma \max})$ in the energy range from the reaction threshold $E_{\rm th}$ of the corresponding reaction up to the maximum energy of γ quanta $E_{\gamma \max}$; $t_{\rm irr}$, $t_{\rm cool}$, and $t_{\rm meas}$ are the irradiation time, cooling time, and measurement time, respectively. A more detailed description of all the calculation procedures necessary for the determination of $\langle \sigma(E_{\gamma \max}) \rangle$ can be found in [26,33].

If the nucleus product has the isomeric state, the value of the total average cross section for the reaction under study $\langle \sigma(E_{\gamma \max}) \rangle_{\text{tot}}$ [hereinafter referred to as $\langle \sigma(E_{\gamma \max}) \rangle$] is calculated as the sum of $\langle \sigma(E_{\gamma \max}) \rangle_{\text{g}}$ and $\langle \sigma(E_{\gamma \max}) \rangle_{\text{m}}$, being, respectively, the average cross sections for the ground state and isomeric state.

In our calculations of average reaction cross sections, all radioactive isotopes were assumed to be produced as a result of photonuclear reactions on ¹⁸¹Ta, considering that the ^{180m}Ta content of the natural tantalum mixture is negligibly small (0.012%). The self-absorption of reaction-product γ rays in the target was computed in the GEANT4.9.2 code.



FIG. 2. γ -ray spectrum from the 43.7 mg ¹⁸¹Ta target after exposure for 30 min to the bremsstrahlung γ flux at $E_{\gamma max} = 80.7$ MeV.



FIG. 3. Fragment of the γ -ray spectrum from the 56.7 mg Mo target after its exposure to the bremsstrahlung γ flux at $E_{\gamma max} = 80.7$ MeV for $t_{irr} = 30$ min; $600 \le E_{\gamma} \le 900$ keV.

C. Bremsstrahlung γ -flux monitoring

The bremsstrahlung gamma flux monitoring against the 100 Mo(γ , n) 99 Mo reaction yield was performed by comparing the experimentally obtained average cross-section values with the computation data. To determine the experimental $\langle \sigma(E_{\gamma \max}) \rangle_{\exp}$ values by Eq. (2), we have used the $\triangle A$ activity value for the $E_{\gamma} = 739.50$ keV γ line and the absolute intensity $I_{\nu} = 12.13\%$ (see Table I and the example spectrum in Fig. 3). The theoretical values of the average cross section $\langle \sigma(E_{\nu \max}) \rangle_{\text{th}}$ were calculated by Eq. (1) using the cross sections $\sigma(E)$ with the TALYS1.95 code with the default options. The normalization (monitoring) factor k_{monitor} , derived from the ratios of $\langle \sigma(E_{\gamma \max}) \rangle_{\text{th}}$ to $\langle \sigma(E_{\gamma \max}) \rangle_{\exp}$, represent the deviation of the GEANT4.9.2-computed bremsstrahlung γ flux from the real flux falling on the target. The determined k_{monitor} values were used for normalizing the cross sections for photonuclear reactions on the ¹⁸¹Ta nucleus. The monitoring procedure has been detailed in [25,26].

The Ta converter and Al absorber used in the experiment generate the neutrons that can cause the reaction ${}^{100}Mo(n, 2n) {}^{99}Mo$. Calculations were made of the neutron energy spectrum and the fraction of neutrons of energies above the threshold of this reaction, similarly to [34]. The contribution of the ${}^{100}Mo(n, 2n) {}^{99}Mo$ reaction to the induced activity of the ${}^{99}Mo$ nucleus has been estimated and is negligible compared to the contribution of ${}^{100}Mo(\gamma, n) {}^{99}Mo$. The contribution of the reaction ${}^{100}Mo(\gamma, n) {}^{99}Mo$. The contribution of the reaction ${}^{100}Mo(\gamma, p) {}^{99}Nb, {}^{99}Nb \xrightarrow{\beta^-} {}^{99}Mo$ is also negligible.

D. Experimental accuracy of the average cross sections $\langle \sigma(E_{\gamma max}) \rangle$, $\langle \sigma(E_{\gamma max}) \rangle_g$, and $\langle \sigma(E_{\gamma max}) \rangle_m$

The uncertainty in measurements of experimental values of the average cross sections $\langle \sigma(E_{\gamma \max}) \rangle$, $\langle \sigma(E_{\gamma \max}) \rangle_g$ and $\langle \sigma(E_{\gamma \max}) \rangle_m$ was determined as a quadratic sum of statistical and systematical errors. The statistical error in the observed γ activity is mainly due to statistics calculation in the total absorption peak of the corresponding γ line, which varies within 1% to 10%. This error varies depending on the γ -line intensity and the background conditions of spectrum measurements. The intensity of the line depends on the detection efficiency, the half-life period, and the absolute intensity I_{γ} . The background is generally governed by the contribution of the Compton scattering of quanta.

The systematical errors are due to the following uncertainties:

- (1) Time of exposure and the electron current $\approx 0.5\%$.
- (2) γ -ray registration efficiency of the detector, $\approx 2-3\%$, which is generally associated with the gamma radiation source error. The error is greater at γ -quantum energies $E_{\gamma} = 50-200$ keV, this being due to a small γ -line quantity in this energy range and the intricate shape of the efficiency curve.
- (3) The half-life time $T_{1/2}$ of the reaction products and the absolute intensity of the analyzed γ quanta $I_{\gamma} =$ 1.3–20%, as is noted in Table I according to the data from [31]. For the case of ¹⁸¹Ta(γ , 5*n*) ¹⁷⁶Ta and ¹⁸¹Ta(γ , 8*n*) ¹⁷³Ta reactions, the errors of γ -line intensities were determined as half-value spreads from the databases of [31] and [32]. The errors amounted to 0.6% and 1.4% for 1159.28 keV (¹⁷⁶Ta) and 172.2 keV (¹⁷³Ta), respectively.
- (4) Normalization of the experimental data to the yield of the monitoring reaction ${}^{100}\text{Mo}(\gamma, n) {}^{99}\text{Mo}$ made up to 5–6%. It should be noted that the systematic error in yield monitoring of the ${}^{100}\text{Mo}(\gamma, n) {}^{99}\text{Mo}$ reaction stems from three unavoidable errors, each running to $\approx 1\%$. These are the unidentified isotopic composition of natural molybdenum, the uncertainty in the γ -line intensity used, I_{γ} , and the statistical error in the determination of the area under the normalizing γ -line peak. In our calculations, we have used the percentage value of ${}^{100}\text{Mo}$ isotope abundance equal to 9.63% (see Ref. [30]).

Thus, the statistical and systematical errors differ for different ${}^{181}\text{Ta}(\gamma, xn; x \leq 8){}^{181-x}\text{Ta}$ reactions. The total uncertainty of the experimental data is given in Fig. 5 and Tables II, III, and IV.

III. ¹⁸¹Ta(γ , xn; $x \leq 8$)^{181-x}Ta REACTION CROSS SECTIONS RESULTING FROM THE TALYS1.95 CODE COMPUTATIONS

The theoretical values of total and partial crosssections $\sigma(E)$ for the ${}^{181}\text{Ta}(\gamma, xn){}^{181-x}\text{Ta}$ reactions with emission of up to eight neutrons were taken for the monochromatic photons from computations by the TALYS1.95 code [8] installed on the Linux distribution Ubuntu 20.04. The computations were performed for different level density models *LD* 1–6. There are three phenomenological level density models and three options for microscopic level densities:

*LD*1: Constant temperature + Fermi gas model. In this model introduced by Gilbert and Cameron, the excitation energy range is divided into a low energy part from E_0 up to a matching energy E_M , where the so-called constant temperature law applies, and a high energy part above, where the Fermi gas model applies.



FIG. 4. Total cross sections $\sigma(E)$ for the ¹⁸¹Ta($\gamma, xn; x \leq 8$)^{181-x}Ta reactions from TALYS1.95 computations for different level density models *LD* 1–6.

*LD*2: Backshifted Fermi gas model. In the backshifted Fermi gas model, the pairing energy is treated as an adjustable parameter and the Fermi gas expression is used down to E_0 .

LD3: Generalized superfluid model (GSM). The model takes superconductive pairing correlations into account ac-

cording to the Bardeen-Cooper-Schrieffer theory. The phenomenological version of the model is characterized by a phase transition from a superfluid behavior at low energy, where pairing correlations strongly influence the level density, to a high energy region which is described by the Fermi



FIG. 5. Total average cross sections $\langle \sigma(E_{\gamma \text{max}}) \rangle$ for the reactions ¹⁸¹Ta($\gamma, xn; x \leq 8$)^{181-x}Ta. Full circles are our present data. Empty squares show our earlier results [22]; in the case of the ¹⁸¹Ta($\gamma, 3n$)¹⁷⁸Ta reaction data are taken from [23]. The curves show the TALYS1.95 computations of average cross sections using different level density models *LD* 1–6.

gas model. The GSM thus resembles the constant temperature model to the extent that it distinguishes between low energy and a high energy region, although for the GSM this distinction follows naturally from the theory and does not depend on specific discrete levels that determine matching energy. Instead, the model automatically provides a constant temperature-like behavior at low energies.

TABLE II. Experimental average cross-section values for the 181 Ta $(\gamma, xn; x = 1, 3)^{181-x}$ Ta reactions.

TABLE III.	Experimental	average	cross-section	values	for	the
⁸¹ Ta(γ , xn ; $x =$	$(2, 4, 5)^{181-x}$ T	a reaction	ns			

Nuclear	$E_{\gamma \max}$	$\langle \sigma(E_{\gamma \max}) \rangle$ (mb)			
reaction	(MeV)	ground	meta	total ^a	
181 Ta (γ, n)	35.1	97.3 ± 19.9		106.4 ± 21.7	
	39.9	96.6 ± 19.7		105.6 ± 21.6	
	45.1	80.4 ± 16.4		87.8 ± 17.9	
	50.0	75.1 ± 15.3		82.0 ± 16.8	
	55.2	78.0 ± 15.9		85.3 ± 17.4	
	60.1	78.3 ± 16.0		85.6 ± 17.5	
	64.6	74.7 ± 15.3		81.7 ± 16.7	
	70.3	71.7 ± 14.6		78.3 ± 14.6	
	75.2	68.5 ± 14.0		74.8 ± 15.3	
	80.2	71.7 ± 14.5		78.4 ± 15.8	
	80.7	73.2 ± 15.0		80.0 ± 16.4	
	84.9	67.1 ± 13.6		73.4 ± 14.8	
	85.6	67.4 ± 13.6		73.7 ± 14.9	
	90.5	64.0 ± 12.9		69.9 ± 14.1	
	90.9	67.0 ± 13.5		73.2 ± 14.8	
	95.0	65.4 ± 13.2		71.5 ± 14.4	
181 Ta $(\gamma, 3n)$	35.1	8.59 ± 0.70	2.63 ± 0.17	11.22 ± 0.72	
	39.9	9.57 ± 0.67	2.92 ± 0.18	12.49 ± 0.69	
	45.1	7.30 ± 0.49	2.50 ± 0.16	9.80 ± 0.52	
	50.0	6.98 ± 0.45	2.23 ± 0.14	9.20 ± 0.47	
	55.2	6.33 ± 0.50	2.12 ± 0.13	8.45 ± 0.52	
	60.1	6.21 ± 0.57	2.08 ± 0.13	8.29 ± 0.59	
	64.6	5.29 ± 0.43	2.00 ± 0.12	7.28 ± 0.45	
	70.3	5.20 ± 0.48	1.81 ± 0.11	7.01 ± 0.49	
	75.2	4.86 ± 0.45	1.69 ± 0.11	6.55 ± 0.46	
	80.2	4.96 ± 0.47	1.85 ± 0.10	6.81 ± 0.48	
	80.7	4.82 ± 0.39	1.74 ± 0.11	6.56 ± 0.40	
	84.9	4.77 ± 0.67	1.71 ± 0.09	6.48 ± 0.68	
	85.6	4.78 ± 0.46	1.81 ± 0.10	6.59 ± 0.47	
	90.5	4.64 ± 0.63	1.60 ± 0.09	6.24 ± 0.63	
	90.9	4.49 ± 0.43	1.73 ± 0.09	6.22 ± 0.44	
	95.0	4.56 ± 0.46	1.70 ± 0.09	6.26 ± 0.47	

^aThe experimental result for the total cross section of the ¹⁸¹Ta(γ , n)¹⁸⁰Ta reaction is given using the value $\langle \sigma(E_{\gamma max}) \rangle_g / \langle \sigma(E_{\gamma max}) \rangle = 0.915$; for the ¹⁸¹Ta(γ , 3n)¹⁷⁸Ta reaction the total cross section is determined as the sum $\langle \sigma(E_{\gamma max}) \rangle_g$ and $\langle \sigma(E_{\gamma max}) \rangle_m$.

*LD*4: Microscopic level densities (Skyrme force) from Goriely's tables. Using this model allows reading tables of microscopic level densities from the RIPL database. These tables were computed by Gorielyon based on Hartree-Fock calculations for excitation energies up to 150 MeV and for spin values up to I = 30.

LD5: Microscopic level densities (Skyrme force) from Hilaire's combinatorial tables. The combinatorial model includes a detailed microscopic calculation of the intrinsic state density and collective enhancement. The only phenomenological aspect of the model is a simple damping function for the transition from spherical to deformed.

*LD*6: Microscopic level densities (temperature-dependent HFB, Gogny force) from Hilaire's combinatorial tables.

Nuclear reaction	$E_{\gamma \max}$ (MeV)	$\langle \sigma(E_{\gamma \max}) \rangle$ (mb)
181 Ta $(\gamma, 2n)$	35.1	89.7 ± 5.5
	39.9	85.2 ± 5.2
	45.1	
	50.0	63.2 ± 3.9
	55.2	59.2 ± 3.6
	60.1	59.9 ± 3.7
	64.6	57.5 ± 3.5
	70.3	51.5 ± 3.2
	75.2	50.8 ± 3.1
	80.2	47.4 ± 2.9
	80.7	
	84.9	41.4 ± 2.5
	85.6	45.4 ± 2.8
	90.5	
	90.9	45.8 ± 2.8
	95.0	44.7 ± 2.7
181 Ta $(\gamma, 4n)$	50.0	6.15 ± 1.09
	55.2	5.15 ± 1.08
	60.1	5.18 ± 0.84
	64.6	5.08 ± 0.89
	70.3	5.26 ± 0.85
	75.2	3.96 ± 0.73
	80.2	5.19 ± 0.73
	80.7	3.32 ± 0.51
	84.9	4.26 ± 0.72
	85.6	4.23 ± 0.54
	90.5	4.16 ± 0.71
	90.9	4.37 ± 0.62
	95.0	4.19 ± 0.63
181 Ta $(\gamma, 5n)$	50.0	2.14 ± 0.18
	55.2	3.50 ± 0.27
	60.1	4.13 ± 0.31
	64.6	4.36 ± 0.33
	70.3	4.19 ± 0.31
	75.2	3.66 ± 0.27
	80.2	4.09 ± 0.28
	80.7	3.79 ± 0.30
	84.9	3.59 ± 0.26
	85.6	3.92 ± 0.27
	90.5	3.32 ± 0.23
	90.9	3.83 ± 0.26
	95.0	3.67 ± 0.25

The TALYS1.95 computation data on the total cross sections for the ¹⁸¹Ta(γ , xn; $x \leq 8$)^{181-x}Ta reactions are presented in Fig. 4. The data were obtained for different level density models. It is obvious from the figures that for the (γ , n) and (γ , 2n) reactions the variants of calculations for *LD* 1–6 are closely located. With the increase in the number of neutrons in the outlet channel, the behavior of the cross sections with energy for the *LD*5 and *LD*6 models is different from that for the other models, viz., the maxima of cross sections are somewhat lower, while their positions are shifted towards higher energy.

TABLE IV. Experimental average cross-section values for the 181 Ta $(\gamma, xn; x = 6, 7, 8)^{181-x}$ Ta reactions

Nuclear		
reaction	$E_{\gamma \max}$ (MeV)	$\langle \sigma(E_{\gamma \max}) \rangle$ (mb)
$\overline{^{181}}$ Ta $(\gamma, 6n)$	60.1	1.46 ± 0.22
	64.6	2.41 ± 0.23
	70.3	2.26 ± 0.19
	75.2	2.20 ± 0.18
	80.2	2.76 ± 0.20
	80.7	2.49 ± 0.19
	84.9	2.61 ± 0.30
	85.6	2.88 ± 0.30
	90.5	2.42 ± 0.28
	90.9	2.77 ± 0.19
	95.0	2.59 ± 0.19
181 Ta $(\gamma, 7n)$	75.2	0.99 ± 0.10
	80.2	1.16 ± 0.12
	80.7	1.01 ± 0.09
	84.9	1.28 ± 0.16
	85.6	1.30 ± 0.14
	90.5	1.30 ± 0.28
	90.9	1.40 ± 0.15
	95.0	1.40 ± 0.19
181 Ta $(\gamma, 8n)$	80.2	0.16 ± 0.12
	84.9	0.44 ± 0.16
	85.6	0.38 ± 0.14
	90.5	0.60 ± 0.28
	90.9	0.79 ± 0.15
	95.0	0.74 ± 0.19

IV. RESULTS AND DISCUSSION

In the present work, we obtained the experimental values of the total average cross sections $\langle \sigma(E_{\gamma \text{max}}) \rangle$ for the $^{181}\text{Ta}(\gamma, xn; x \leq 8)^{181-x}\text{Ta}$ reaction in the range of end-point bremsstrahlung γ -quantum energies $E_{\gamma \text{max}} = 35-80$ MeV. The found cross sections are compared with the theoretical values of the average cross sections calculated by Eq. (1) using bremsstrahlung fluxes corresponding to real experimental conditions and cross sections from TALYS1.95 for level density models *LD* 1–6. Thus, each cross section $\langle \sigma(E_{\gamma \text{max}}) \rangle$ of the $^{181}\text{Ta}(\gamma, xn; x \leq 8)^{181-x}\text{Ta}$ reactions corresponds to six variants of calculation.

The experimental and theoretical cross sections $\langle \sigma(E_{\gamma \text{max}}) \rangle$ (*LD* 1–6) are shown in Fig. 5. For completeness, this figure shows earlier results of our studies at $E_{\gamma \text{max}} = 80-95$ MeV [22], and for the ¹⁸¹Ta(γ , 3n)¹⁷⁸Ta reaction at $E_{\gamma \text{max}} =$ 35–95 MeV from [23]. Within the limits of experimental errors, the data of this work and from [22] are in satisfactory agreement for all the reactions under consideration. Thus, the energy range of end-point bremsstrahlung γ -quantum energies $E_{\gamma \text{max}} = 35-95$ MeV is covered.

The cross sections $\langle \sigma(E_{\gamma \max}) \rangle$ for x = 2, 4-8 are determined in the experiment directly from the yields of the corresponding reactions. In the case of reactions (γ, n) and $(\gamma, 3n)$, the procedure for determining the total cross section is somewhat more complicated.

In the experiment for the ¹⁸¹Ta(γ , n)¹⁸⁰Ta reaction, only the average cross section $\langle \sigma(E_{\gamma max}) \rangle_g$ for the ground-state population of the ^{181g}Ta nucleus can be measured. The total experimental average cross section $\langle \sigma(E_{\gamma max}) \rangle$ for this reaction can be estimated through the use of the theoretical values of the total cross section $\langle \sigma(E_{\gamma max}) \rangle$ and for the ground-state one $\langle \sigma(E_{\gamma max}) \rangle_g$. The cross-section ratios $\langle \sigma(E_{\gamma max}) \rangle_g / \langle \sigma(E_{\gamma max}) \rangle$, computed with the TALYS1.95 code were found to be 0.915, 0.915, 0.922, 0.92, 0.875, and 0.90 for the level density models *LD* 1–6, respectively. This spread in the ratios leads to uncertainty of the total cross-section estimated values of $\approx 5\%$.

Note that the main contribution (> 90%) to the total cross section comes from the cross section for the ground state, while the addition of the metastable state is insignificant. In Fig. 5(a), the experimental result is given using the value $\langle \sigma(E_{\gamma max}) \rangle_g / \langle \sigma(E_{\gamma max}) \rangle = 0.915$. As can be seen, in the case of the reaction (γ , n), the difference between the variants of calculation by different level density models *LD* 1–6 is inconsiderable. Any variant of the calculation is consistent with the experimental results within the error limits.

The experimental and calculated total cross sections $\langle \sigma(E_{\gamma \text{max}}) \rangle$ for the reaction $^{181}\text{Ta}(\gamma, 2n)^{179}\text{Ta}$ are shown in Fig. 5(b). Here, too, the difference between the calculations for different models of the level density *LD* 1–6 is insignificant. As in the case of the (γ, n) reaction, it is impossible to single out the preferred model for describing the experimental results.

For the ¹⁸¹Ta(γ , 3*n*)¹⁷⁸Ta reaction, the total cross section is determined as the sum of the experimental values of the average cross sections of the ground $\langle \sigma(E_{\gamma max}) \rangle_{g}$ and metastable $\langle \sigma(E_{\gamma max}) \rangle_{m}$ states. The values $\langle \sigma(E_{\gamma max}) \rangle_{g}$ and $\langle \sigma(E_{\gamma max}) \rangle_{m}$ are measured directly in the experiment.

The total average cross sections $\langle \sigma(E_{\gamma \text{max}}) \rangle$ for the ¹⁸¹Ta(γ , 3n)¹⁷⁸Ta reaction [23] are shown in Fig. 5(c). The theoretical values of the total average cross section for the reaction (γ , 3n) according to *LD*1 and *LD*6 models differ by 20–30%, forming a corridor in which all experimental data $\langle \sigma(E_{\gamma \text{max}}) \rangle$ are located. The best agreement between experiment and theory is observed in the case of the *LD*5 model calculation: the experimental cross sections for the formation of a nucleus in the isomeric state $\langle \sigma(E_{\gamma \text{max}}) \rangle_{\text{m}}$ is located below all theoretical curves, but closest to calculations using the *LD*5 and *LD*6 models, and the values $\langle \sigma(E_{\gamma \text{max}}) \rangle_{\text{g}}$ lie above all calculations in the 35–60 MeV range, but at 65–95 MeV there is good agreement with the calculation for the *LD*5 model [23].

With the increase in the number of neutrons in the reaction outlet channel the difference between the theoretical curves becomes more appreciable [Fig. 5(d)–5(h)]. At first glance, it becomes possible to single out a calculation model that most optimally agrees with the experimental data. But for x >3, the reaction cross sections decrease, and the experimental error increases, which complicates the analysis. In the case of reactions (γ , 4n) and (γ , 6n), there is a significant scatter in the experimental data, which does not allow us to choose one of the level density models. The results for (γ , 5n) and (γ , 8n) do not agree with any of the theoretical curves, although the experimental cross sections for $(\gamma, 7n)$ and $(\gamma, 8n)$ are closest to the calculation by the *LD5* model.

None of the models *LD* 1–6 of the TALYS1.95 code allow a satisfactory description of the entire array of experimental data obtained for the x = 1–8 reactions. As a result of the analysis using the χ^2 method, it was shown that in the case of the reaction (γ , n), the best agreement between the experimental ($\sigma(E_{\gamma max})$) values and the theoretical TALYS1.95-based computations using the *LD*3 model was achieved; for (γ , 2n) *LD*3; for (γ , 3n) *LD*5; for (γ , 4n) *LD*1; for (γ , 5n) *LD*1; for (γ , 6n) *LD*5; for (γ , 7n) *LD*5; and for (γ , 8n) *LD*5. This does not allow us to select the optimal model for describing all reactions ¹⁸¹Ta(γ , xn).

Note also the tendency to the satisfactory agreement between the experimental and calculated data on the total cross sections $\langle \sigma(E_{\gamma max}) \rangle$ for photoneutron reactions on ¹⁸¹Ta, in which the nuclei products are produced with positive parity π in the ground state. For the reactions ¹⁸¹Ta(γ , 3n) ^{178m}Ta, ¹⁸¹Ta(γ , 5n) ¹⁷⁶Ta, and ¹⁸¹Ta(γ , 8n) ¹⁷³Ta, which resulted in the formation of nuclei with negative parity, the experimental results do not agree with the calculations.

The numerical values of the experimental total average cross sections $\langle \sigma(E_{\gamma \max}) \rangle$ for the ¹⁸¹Ta($\gamma, xn; x \leq 8$)^{181-x}Ta reactions in the range of end-point bremsstrahlung γ -quanta energies $E_{\gamma \max} = 35-95$ MeV are presented in Tables II, III, and IV.

V. CONCLUSIONS

The present work is concerned with the study of photoneutron reactions on the ¹⁸¹Ta nucleus with emission of up to eight neutrons at end-point bremsstrahlung γ -quantum energies $E_{\gamma max} = 35-80$ MeV with the use of the activation and offline γ -ray spectrometric technique (residual activity

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technique). The experimentally determined total average cross sections $\langle \sigma(E_{\gamma \max}) \rangle$ of the reactions have been compared with the theoretical values computed with TALYS1.95 code for different level density models *LD* 1–6 and satisfactory agreement has been shown for the ¹⁸¹Ta(γ , *xn*) reactions with the escape of 1–7 neutrons. The result of the χ^2 -method analysis did not allow us to select the optimal *LD* model for a compatible description of the experimental $\langle \sigma(E_{\gamma \max}) \rangle$ values for all reactions ¹⁸¹Ta(γ , *xn*; $x \leq 8$)^{181–x}Ta.

The tendency toward satisfactory agreement between the experimental and calculated data on the total cross sections $\langle \sigma(E_{\gamma max}) \rangle$ for photoneutron reactions on ¹⁸¹Ta, in which the nuclei products are produced with positive parity π in the ground state, was observed. For the reactions ¹⁸¹Ta(γ , 3n) ^{178m}Ta, ¹⁸¹Ta(γ , 5n) ¹⁷⁶Ta, and ¹⁸¹Ta(γ , 8n) ¹⁷³Ta, which resulted in the formation of nuclei with negative parity, the experimental results do not agree with any TALYS1.95 computation for the models *LD* 1–6.

The experimental data on average cross sections $\langle \sigma(E_{\gamma max}) \rangle$, $\langle \sigma(E_{\gamma max}) \rangle_m$, $\langle \sigma(E_{\gamma max}) \rangle_g$ for the reactions in the energy range $E_{\gamma max} = 35-80$ MeV were obtained for the first time. The present results extend the range of the values obtained previously at $E_{\gamma max} = 80-95$ MeV towards the lower-energy region, where the cross-section maxima for the reactions under study lie.

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