

Quenching of jets tagged with W bosons in high-energy nuclear collisions

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(Received 20 December 2021; accepted 21 April 2022; published 3 May 2022)

We carry out detailed calculations of jet production associated with W gauge bosons in Pb + Pb collisions at the Large Hadron Collider (LHC). In our calculations, the production of W + jet in $p + p$ collisions as a reference is obtained by SHERPA, which performs next-to-leading-order matrix-element calculations matched to the resummation of parton shower simulations, while jet propagation and medium response in the quark-gluon plasma are simulated with the linear Boltzmann transport (LBT) model. We provide numerical predictions on seven observables of W + jet production with jet quenching in Pb + Pb collisions: the medium modification factor for the tagged jet cross sections I_{AA} , the distribution in invariant mass between the two leading jets in $N_{\text{jets}} \geq 2$ events m_{jj} , the missing p_T or the vector sum of the lepton and jet transverse momentum $|\vec{p}_T^{\text{Miss}}|$, the summed scalar p_T of all the jets in an event S_T , transverse momentum imbalance x_{jW} , average number of jets per W boson R_{jW} , and azimuthal angle between the W boson and jets $\Delta\phi_{jW}$. The distinct nuclear modifications of these seven observables in Pb + Pb relative to that in $p + p$ collisions are presented with detailed discussions.

DOI: [10.1103/PhysRevC.105.054902](https://doi.org/10.1103/PhysRevC.105.054902)

I. INTRODUCTION

Jet quenching due to strong interaction between energetic partons and the dense QCD medium has long been proposed as an excellent hard probe of the properties of the quark-gluon-plasma (QGP) created in relativistic heavy-ion collisions (HICs) [1–28]. Among a wealth of jet quenching observables, the production of jets in association with a gauge boson has been regarded as a “golden channel” due to some of its unique features [29,30]. Since gauge bosons produced in the initial hard scattering do not participate in strong interactions with the medium, the transverse momentum of the boson closely reflects the initial energy of the leading jets before they interact with the medium. In addition, jets associated with a gauge boson are dominated by quark jets, which can help constrain the flavor dependence of parton energy loss. Recently γ/Z -jet correlations [31–47], and H + jet processes [48,49] have already been investigated within several theoretical models and by experiments in Pb + Pb collisions at

$\sqrt{s} = 5.02$ TeV. In this paper, we perform a quantitative study of W + jets in high-energy heavy-ion collisions.

At the leading order (LO) in perturbation theory, jet production associated with W bosons attributes mainly to two subprocesses: quark-antiquark annihilation $q\bar{q}' \rightarrow Wg$ and Compton process $qg \rightarrow Wq$. At very large momentum transfer, the Compton process dominates, therefore, jets recoiling from a W boson are predominately quark jets. In this respect, W + jet can help further constrain the flavor dependence of jet quenching. When a W boson is produced in the center-of-mass frame at LO, its momentum component transverse to the beam axis is balanced by a back-to-back jet with the same momentum in the transverse plane, resulting in the divergence of transverse momentum imbalance at $x_{jW} = p_T^{\text{jet}}/p_T^W \simeq 1$ and azimuthal angle correlation at $\Delta\phi_{jW} = |\phi_{\text{jet}} - \phi_W| = \pi$ [38,41,47]. With higher-order perturbative corrections [50–53], additional hard and soft gluon radiations may affect the W -jet correlations, for instance, the balance of transverse momentum is smeared and azimuthal angle correlation is broadened.

As in Z + jets [41,44,47], the next-to-leading-order (NLO) calculation does not take the resummation of soft and collinear radiation into account and has only limited number of final particles. Although the NLO calculation can describe transverse momentum spectra of jets, it is, however, insufficient to study W -jet correlations in azimuthal angle which suffer from divergence in the large-angle region. Monte Carlo (MC) event generator PYTHIA which employs leading-order matrix elements (MEs) merged with a parton shower (PS) contains some high-order corrections from both real and virtual

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contributions. It is, however, short of additional hard or wide-angle radiation from high-order matrix element calculations. Simulations matching the NLO with PS [41,44,47,54–56], on the other hand, provide a satisfactory description of a wide variety of experimental observables of $W^\pm/Z/\gamma + \text{jet}$ in the whole phase space. Therefore, we will utilize an improved reference of gauge boson tagged jet production in proton-proton ($p + p$) collisions to study W -jet correlations in relativistic heavy-ion collisions (HICs) at the Large Hadron Collider (LHC).

In this paper, we carry out a systematic study of $W + \text{jets}$ in both $p + p$ and heavy-ion collisions (Pb + Pb) at $\sqrt{s_{\text{NN}}} = 5.02$ TeV. With the MC event generator SHERPA [57], which can perform NLO matrix element calculations matched to the resummation of parton showers, we provide excellent baselines of $p + p$ collisions at 5.02 TeV. We then use the linear Boltzmann transport (LBT) model [58–60] to simulate jet propagation and medium response and predict the medium modifications of several specific observables of $W + \text{jet}$ in HIC: the distribution in invariant mass between the two leading jets in $N_{\text{jets}} \geq 2$ events m_{jj} , the medium modification of jet spectra in different p_T^W intervals, the modification of the distributions in $|\vec{p}_T^{\text{Miss}}|$ which is the vector sum of the lepton and jets transverse momentum, and the summed scalar p_T^{jets} of all the jets in the event S_T . We will also provide numerical results for several familiar observables of W -jet correlations in HICs, which have been utilized to investigate $Z + \text{jet}$ in HICs [41]: the shift of the transverse momentum imbalance of $W + \text{jet}$ as well as its mean value between $p + p$ and Pb + Pb collisions, the modification of azimuthal angle correlations, and the number of tagged jets per W boson.

The rest of the paper is organized as follows: In Sec. II we present the framework for the calculation of jet production in association with W bosons both in $p + p$ and Pb + Pb collisions. We also describe how jets tagged by a W boson are produced in SHERPA and transported in LBT. In Sec. III we present medium modifications of seven observables of $W + \text{jet}$ in Pb + Pb relative to that in $p + p$ collisions. In Sec. IV we summarize our study.

II. FRAMEWORK DESCRIPTION

A. $W + \text{jets}$ in $p + p$ collisions at next-to-leading order with parton showers

In our calculations, jet productions in association with a W boson in $p + p$ collisions are simulated within a MC event generator SHERPA 2.24 [57], which can perform NLO ME calculations matched to the PS with several merging schemes. AMEGIC++ [61] and COMIX [62] are SHERPA's original matrix-element generators which provide tree-level matrix elements and create the phase-space integration as well. MC programs OPENLOOPS [63] is interfaced with SHERPA to provide the virtual matrix-elements. The MEPS@NLO merging method [64–66] is used to yield improved matrix elements for multiple jets production at NLO matched to the resummed parton showers [67,68]. LHAPDE is interfaced with SHERPA and the parton distribution function (PDF) set ‘‘CT14 NLO’’ [69]

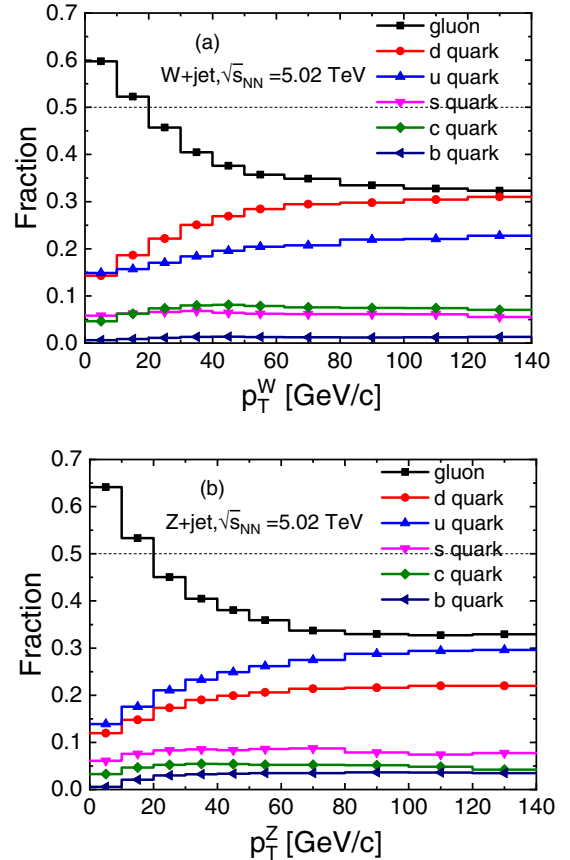


FIG. 1. Fraction of leading parton flavor triggered by (a) W boson and (b) Z boson as a function of gauge boson transverse momentum p_T^V .

is used to provide the PDF for partons that participate in the hard interaction in $p + p$ collisions.

Although W and Z bosons have a lot in common, W bosons have some unique properties as compared with Z bosons. For instance, W bosons carry electric charge and would change the flavor of the jet parton. As a result, the flavors of jets associated with W 's are different from a Z boson. We have classified the flavor of the leading parton triggered by a Z boson and W bosons in Fig. 1. As can be seen, the quark fractions increase significantly with the transverse momentum of the gauge boson. At high gauge boson energy, the jets are dominated by quark jets. Compared with jet production associated with a Z boson, the fraction of the leading parton flavor tagged with W bosons is quite different. For instance, the fraction of u quark associated with W bosons is almost the same as the fraction of d quark associated with a Z boson and the fraction of s quark associated with a Z boson is almost the same as the fraction of c quark associated with a W boson as a result of isospin symmetry. The different parton flavor fractions would lead to different fractions of hadrons as well as different jet properties. The comparison between $W + \text{jet}$ and $Z + \text{jet}$ would provide new opportunities to explore the jet tomography of the QGP. The difference in the flavor fraction is a result of different production mechanisms of W and Z boson in hard scattering. In this regard, W 's associated with jets or hadrons can be used to constrain nonperturbative

hadronization models in both $p + p$ and Pb + Pb collisions as well as the flavor dependence of jet quenching, which is beyond the scope of this paper and will be discussed in the future.

To compare with experimental measurements, we select the W bosons and associated jets according to the kinematic cuts adopted by the ATLAS experiment [70]. The electrons are constrained in the phase space $p_T > 25$ GeV/ c and $|\eta| < 2.47$ and are rejected in the transition region ($1.37 < |\eta| < 1.52$). Muons are required to have $p_T > 25$ GeV/ c and $|\eta| < 2.4$. Additionally, jets are reconstructed using the anti- k_T algorithm [71,72] with a radius parameter $R = (\Delta\eta^2 + \Delta\phi^2)^{1/2} = 0.4$ using all final-state partons. Jets are required to have $p_T > 30$ GeV/ c and $|y| < 4.4$ and are removed if a jet is within $\Delta R = 0.5$ of an electron or muon. Furthermore, since the W boson eventually decays into an electron and a neutrino, events are required to have significant missing transverse momentum and large transverse mass to compensate the missing information of the neutrino, which cannot be detected directly by experiment. The missing transverse momentum is defined as the negative vector sum of the transverse momentum of leptons, photons, and jets as well as the soft deposits in the calorimeter and is required to have $E_T^{\text{Miss}} = -|\vec{p}_T^l + \vec{p}_T^\nu + \sum \vec{p}_T^{\text{jets}} + \vec{p}_T^{\text{soft}}| > 25$ GeV/ c [70,73]. Transverse mass is defined as $m_T = \{2p_T^l p_T^\nu [1 - \cos(\phi^l - \phi^\nu)]\}^{1/2}$ and required to have $m_T > 40$ GeV/ c .

The differential cross section of jet production associated with a W boson as a function of jet transverse momentum calculated by SHERPA is compared with the experimental data [70] in Fig. 2(a). The distribution in dijet invariant mass $m_{jj} = [(E^L + E^{\text{Sub}L})^2 - (\vec{p}^L + \vec{p}^{\text{Sub}L})^2]^{1/2}$ between the two leading jets in $N_{\text{jets}} \geq 2$ events is also calculated and compared with experimental data in Fig. 2(b). The jet distributions in association with a W boson production from SHERPA show excellent agreement with the experimental data and can be used as references and inputs for the energy-loss models to study jet-medium interactions in heavy-ion collisions. The jet spectrum monotonically decreases as a function of jet transverse momentum. However, the distribution as a function of the dijet invariant mass increases when $m_{jj} < M_W$ and decreases steeply when $m_{jj} > M_W$, which is similar to the W boson mass distribution and quite different from inclusive dijet mass distribution which is a monotonic function of m_{jj} .

B. $W + \text{jet}$ in Pb + Pb collisions within the linear Boltzmann transport model

For a quantitative investigation of the jet properties associated with a vector gauge boson in heavy-ion collisions, cold nuclear matter (CNM) effects should also be taken into consideration. In our calculations, we use the EPPS16 [74] nuclear parton distribution functions (nPDFs) in the LHAPDF library to investigate the cold nuclear matter effect due to nuclear modification of the parton distribution functions. Cold nuclear matter effects are negligible in the distribution of γ or $Z + \text{jets}$ in the kinematic ranges we are interested in. However, the cross section of jet production associated with a W boson is rather sensitive to the isospin dependence of nPDF due to the production of the charged W gauge bosons.

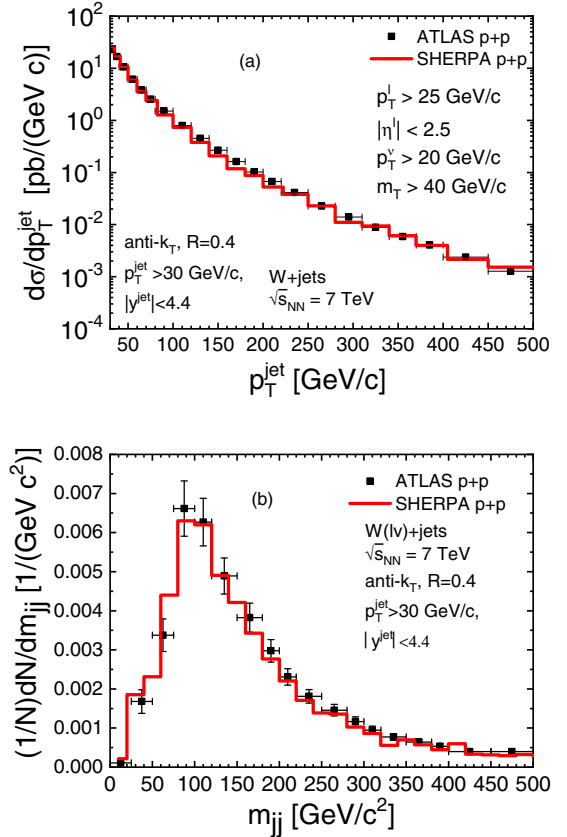


FIG. 2. (a) Differential cross section for the production of $W + \text{jets}$ as a function of the transverse momentum of the associated jets at $\sqrt{s_{NN}} = 7$ TeV and the comparison with the ATLAS experimental data (black). (b) Normalized distributions of events passing the $W + \text{jet}$ selection cut as a function of the dijet invariant mass m_{jj} between the two leading jets in $N_{\text{jets}} \geq 2$ events and the comparison with the ATLAS experimental data (black).

The nuclear modification factors for the jet p_T distribution due to CNM are calculated and shown in Fig. 3. As one can see, W^- is enhanced by 20% while W^+ is suppressed by 20% due

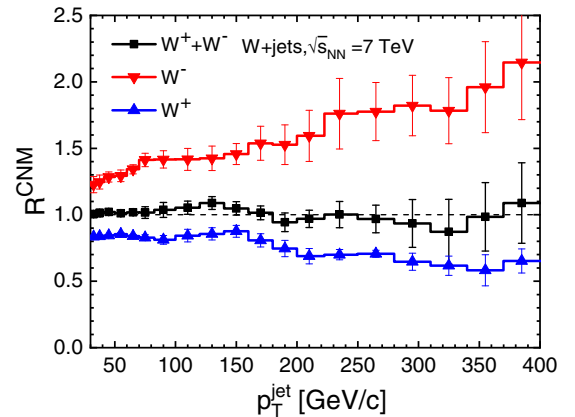


FIG. 3. The modification of jet spectrums tagged by W^+ , W^- and $W^+ + W^-$ due to the cold nuclear effect with EPPS16 modified CT14nlo pdf set.

to the isospin dependence of nPDF in Pb nuclei. However, the CNM effect beyond the isospin dependence of nPDF is negligible, as seen in the modification factor for the sum of W^+ - and W^- -triggered jets. Similar conclusions are reached in Ref. [75]. Therefore, the isospin dependence of nPDF must be taken into account for the study of nuclear modification of jet production associated with W^+ or W^- bosons. However, CNM effect becomes negligible when the final results are averaged over W^+ and W^- .

In our study, jet propagation, parton energy loss and the medium response in hot and dense QCD medium due to jet-medium interactions are simulated within the linear Boltzmann transport (LBT) model [58–60], which is based on the Boltzmann equation,

$$\begin{aligned} & p_1 \cdot \partial f_a(p_1) \\ &= - \int \frac{d^3 p_2}{(2\pi)^3 2E_2} \int \frac{d^3 p_3}{(2\pi)^3 2E_3} \int \frac{d^3 p_4}{(2\pi)^3 2E_4} \\ & \quad \times \sum_{b(c,d)} [f_a(p_1) f_b(p_2) - f_c(p_3) f_d(p_4)] |M_{ab \rightarrow cd}|^2 \\ & \quad \times S_2(s, t, u) (2\pi)^4 \delta^4(p_1 + p_2 - p_3 - p_4), \end{aligned} \quad (1)$$

for parton propagation in the QGP medium, where f_i are phase-space distributions of medium parton. $S_2(s, t, u)$ is a Lorentz-invariant regulation condition to regulate all soft and collinear divergency. Elastic scatterings are simulated with the corresponding matrix elements $|M_{ab \rightarrow cd}|$ which include the complete set of leading order $2 \rightarrow 2$ elastic scattering processes.

The induced gluon radiation from inelastic scattering is numerically incorporated into LBT according to the high-twist formalism [76–78]:

$$\frac{dN_g}{dx dk_\perp^2 dt} = \frac{2\alpha_s C_A P(x) \hat{q}}{\pi dk_\perp^4} \left(\frac{k_\perp^2}{k_\perp^2 + x^2 M^2} \right)^2 \sin^2 \left(\frac{t - t_i}{2\tau_f} \right), \quad (2)$$

where x and k_\perp are the energy fraction and transverse momentum of the radiated gluon, respectively, $P(x)$ is the splitting function, \hat{q} is the jet transport coefficient which is calculated from the elastic scattering, and $\tau_f = 2Ex(1-x)/(k_\perp^2 + x^2 M^2)$ is the formation time of the radiated gluon. The medium information is provided by 3 + 1D CLVisc hydrodynamics [79,80] with the initial condition provided by the AMPT [81] Monte Carlo model. LBT has been successful in describing experimental data on the suppression of large- p_T hadrons [59,60], inclusive jets [82], γ -hadron or jets [38,42,43] correlations, and Z + jet production [41].

III. NUMERICAL RESULTS AND DISCUSSIONS

In this section, we will present predictions about the modifications of W + jets event distributions and the correlations between the recoil W boson and the associated jets in 0%–30% central Pb + Pb collisions at the LHC energy within our framework. In our calculations, the only parameter α_s that controls the effective coupling strength between jet and medium is set to 0.2, which is the value we fixed in our

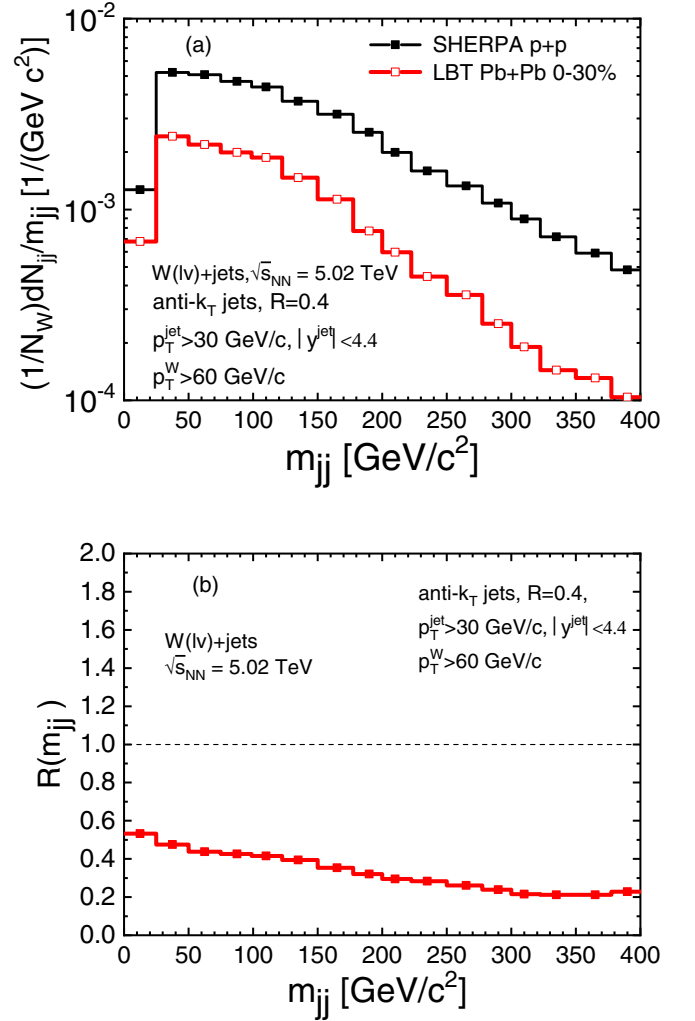


FIG. 4. (a) Normalized distributions of events passing the W + jets selection cut as a function of the dijet invariant mass m_{jj} between the two leading jets in $N_{\text{jets}} \geq 2$ events in $p + p$ and the scaled distributions in Pb + Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV. (b) The ratio of normalized distribution of m_{jj} in Pb + Pb to that in $p + p$ collisions at $\sqrt{s_{NN}} = 5.02$ TeV.

previous studies of Z + jets correlations [41] in Pb + Pb collisions.

A. Attenuation of W -jet in Pb + Pb

We first investigate the distribution in dijet invariant mass m_{jj} between the two leading jets in W -jet events with $N_{\text{jets}} \geq 2$ and medium modification of the m_{jj} distribution, which is defined as

$$R_{AA}(m_{jj}) = \frac{1}{\langle N_{\text{coll}} \rangle} \frac{dN^{AA}/dm_{jj}}{dN^{pp}/dm_{jj}}. \quad (3)$$

In Fig. 4, we present the normalized dijet invariant-mass distribution for events passing the W -jet selection in $p + p$ and the scaled distributions in Pb + Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV as well as the nuclear modification factor. Since the dijet invariant mass is proportional to the virtuality [17,23]

of the initial hard scattering, the suppression of the modified invariant-mass distribution in Pb + Pb relative to $p + p$ collisions is mainly due to the effects of jet quenching. We note that the m_{jj} distribution is significantly suppressed due to jet quenching and the modification factor tends to decrease with increasing m_{jj} , as shown in Fig. 4. The suppression of this dijet invariant-mass distribution is due to the reduction of the dijet events that pass all the selection cuts in Pb + Pb collisions due to jet quenching. The m_{jj} dependance of the suppression factor also indicates that the effective invariant mass of the dijets that pass the selection cuts is suppressed due to the broadening of each individual jet and their relative momentum.

We also calculate another nuclear modification factor for the double-differential cross section of $W + \text{jet}$ production:

$$I_{AA} = \frac{(1/N_W^{\text{Pb+Pb}})dN^{\text{Pb+Pb}}/dp_T^W dp_T^{\text{jet}}}{(1/N_W^{p+p})dN^{p+p}/dp_T^W dp_T^{\text{jet}}}, \quad (4)$$

which is defined as the ratio of the double-differential tagged jet spectra in central Pb + Pb collisions to that in $p + p$ collisions. The double-differential tagged jet spectra in both 0%–30% central Pb + Pb and $p + p$ collisions are shown in Fig. 5(a) and the modification factors are shown in Fig. 5(b) in four p_T^W intervals.

In LO calculations, the jet is produced in the opposite direction of the recoil W boson with the same momentum in the transverse plane. The tagged jet spectra will fall off rapidly above the cutoff value of p_T^W . With high-order corrections from NLO perturbative matrix element calculations of hard emissions as well as resummation of soft and collinear radiations, the tagged jet spectra are smeared but have a maximum value at around the p_T^W interval. The jet energy loss in Pb + Pb collisions will lead to a shift of the tagged jet spectra to a smaller value of p_T . This results in the suppression at low p_T^{jet} and the enhancement at high p_T^{jet} of the nuclear modification factor I_{AA} . Consequently, the nuclear modification factor is quite sensitive to the transverse momentum cut for the W boson and reach its minimum value in $p_T^{\text{jet}} \simeq p_T^W$ region. This is similar to the jet spectra tagged by direct photon or Z boson.

Since the W boson eventually decays into an electron and a neutrino, the existence of the neutrino with missing energy would make the reconstruction of the W boson relatively more difficult than that of Z^0 boson, particularly in Pb + Pb collisions with enhanced production of low- p_T particles [73]. When correlation of $W + \text{jets}$ in heavy-ion collisions is concerned, the situation may be further complicated due to the attenuation of jet energies in the QGP.

To facilitate the experimental study of $W + \text{jets}$ in Pb + Pb, we define

$$\vec{p}_T^{\text{Miss}} = -\left(\vec{p}_T^l + \sum \vec{p}_T^{\text{jets}}\right), \quad (5)$$

which represents the vector sum of the lepton and jets in a $W + \text{jets}$ event, and propose to measure the nuclear modification of \vec{p}_T^{Miss} distribution as given by

$$R_{AA}(p_T^{\text{Miss}}) = \frac{1}{\langle N_{\text{coll}} \rangle} \frac{dN^{AA}/dp_T^{\text{Miss}}}{dN^{pp}/dp_T^{\text{Miss}}}. \quad (6)$$

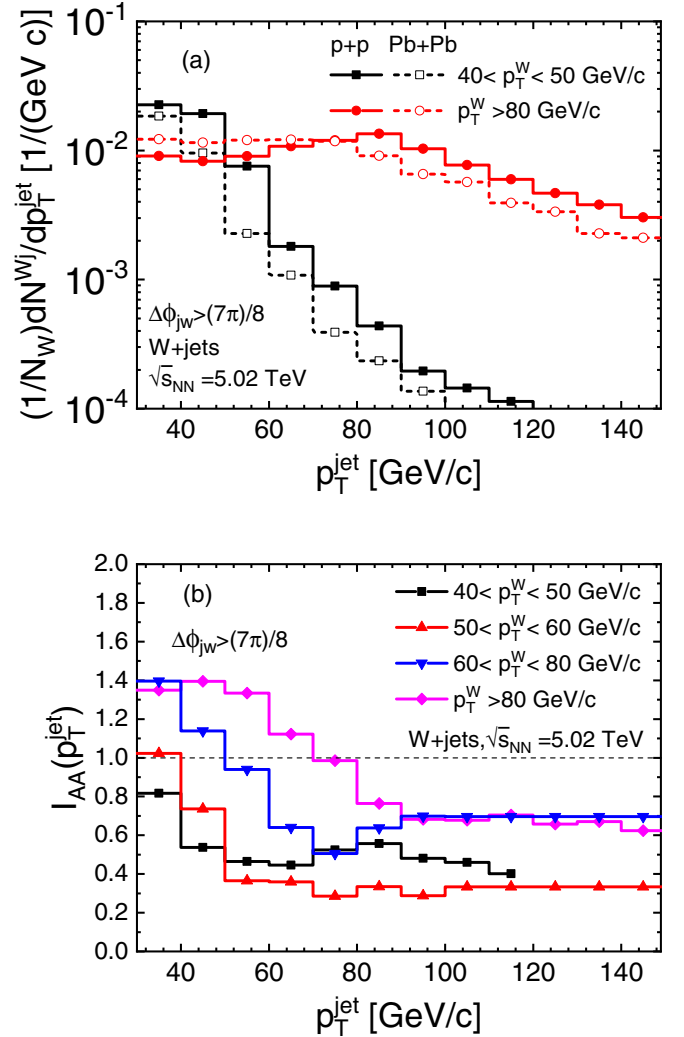


FIG. 5. (a) The double-differential transverse momentum spectrums of $W + \text{jets}$ in $p + p$ and Pb + Pb collisions in different p_T^W intervals. (b) Ratio of the transverse momentum of jets associated with a W boson in 0%–30% central Pb + Pb collisions to that in $p + p$ collisions in different transverse momentum ranges of W boson denoted by different-color lines, as a function of jet transverse momentum at $\sqrt{s_{NN}} = 5.02$ TeV.

The missing transverse momentum \vec{p}_T^{Miss} excludes neutrino and only includes lepton and jets. Therefore, it should be much easier to be measured. In $p + p$ collisions, it is equal to the transverse momentum of the neutrino because of momentum-energy conservation. In Pb + Pb collisions, it represents the vector sum of the transverse momentum that is outside of the jet cone and the neutrino. This missing energy in Pb + Pb collisions reflects directly the amount and the direction of energy that jets loses in the $W + \text{jets}$ event in Pb + Pb collisions. The distributions of events passing the $W + \text{jets}$ kinematic selection cut as a function of \vec{p}_T^{Miss} in Pb + Pb to that in $p + p$ collisions at $\sqrt{s} = 5.02$ TeV is plotted in Fig. 6(a) while their ratio is illustrated in Fig. 6(b). One observe that both distributions peak around p_T^W , and the jet-quenching effect in Pb + Pb may shift the peak to

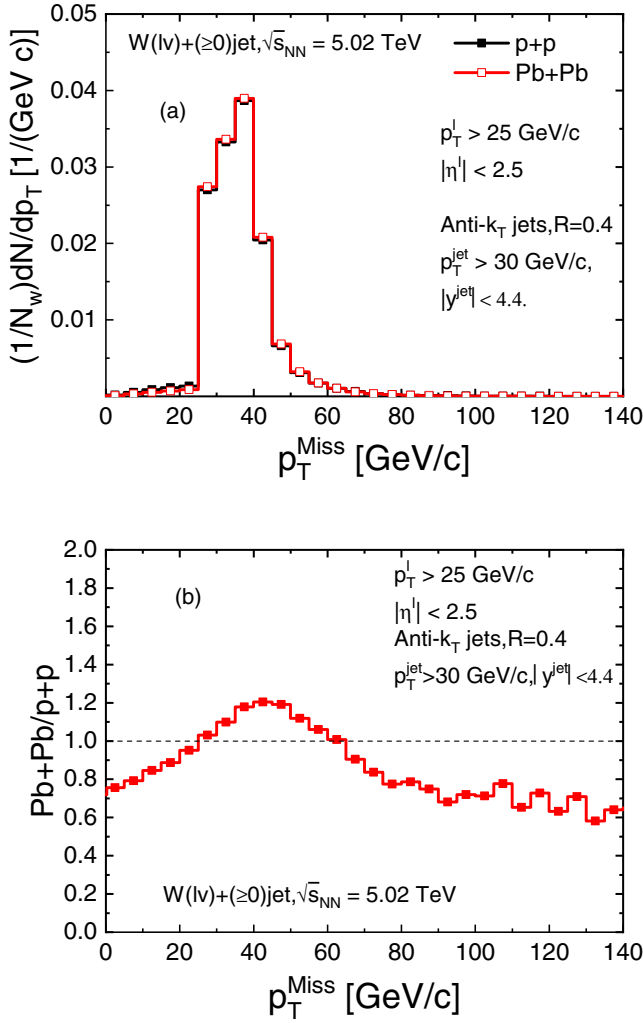


FIG. 6. (a) Normalized distributions of events passing the $W + \text{jet}$ selection cut as a function of the \vec{p}_T^{Miss} which is defined as the vector sum of the lepton and jets in $\text{Pb} + \text{Pb}$ and in $p + p$ collisions at $\sqrt{s_{NN}} = 5.02 \text{ TeV}$. (b) The ratio of distributions of events passing the $W + \text{jet}$ selection as a function of the \vec{p}_T^{Miss} in $\text{Pb} + \text{Pb}$ to that in $p + p$ collisions at $\sqrt{s_{NN}} = 5.02 \text{ TeV}$.

a smaller value of p_T^{Miss} . This shift is caused by transverse energy transfer outside the jet cone due to elastic and inelastic scattering with the medium and the direction of the energy carried by radiated partons outside the jet cone in the opposite direction of the neutrino or W boson. As a consequence, the modification factor $R_{AA}(p_T^{\text{Miss}})$ increases as a function of \vec{p}_T^{Miss} in the region $\vec{p}_T^{\text{Miss}} < 50 \text{ GeV}/c$ and decreases with increasing \vec{p}_T^{Miss} in the region $\vec{p}_T^{\text{Miss}} > 50 \text{ GeV}/c$, and is greater than one in the region $30 < \vec{p}_T^{\text{Miss}} < 60 \text{ GeV}/c$.

To quantify the relative energy loss of $W + \text{jet}$ events due to jet-medium interaction, we start with the nuclear modification for the summed scalar p_T of all reconstructed jets that pass the kinematic cut in an event S_T , which should be sensitive to the total transverse momentum broadening of $W + \text{jets}$ events.

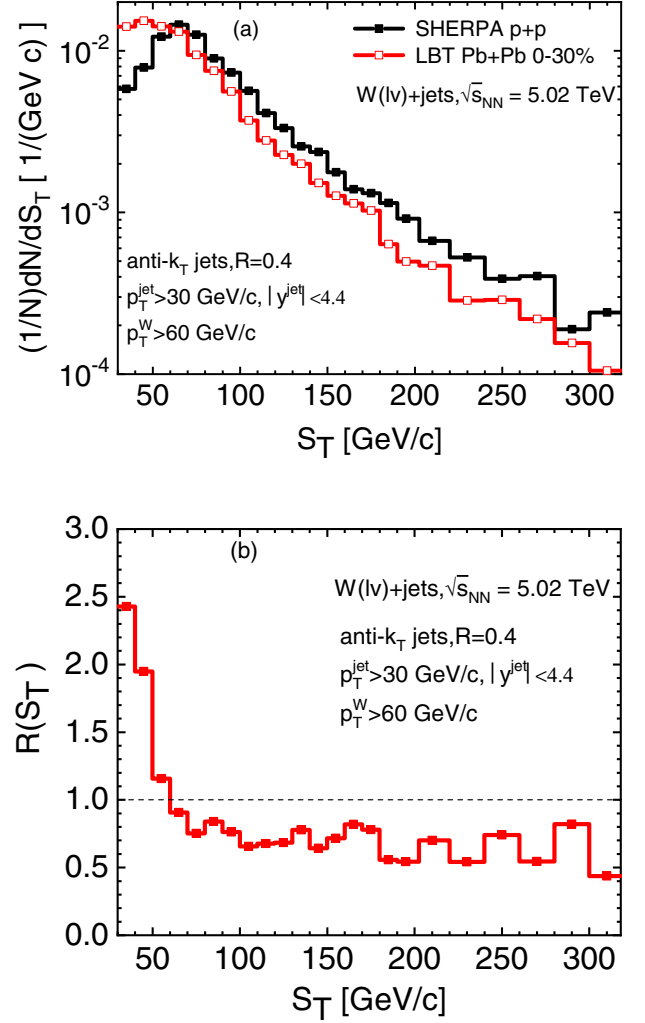


FIG. 7. (a) The normalized distributions of events passing the $W + \text{jets}$ selection as a function of the summed scalar p_T of all reconstructed jets. (b) The ratio of S_T distribution in $\text{Pb} + \text{Pb}$ to that in $p + p$ collisions at $\sqrt{s_{NN}} = 5.02 \text{ TeV}$.

The distributions in $\text{Pb} + \text{Pb}$ and $p + p$ collisions and the nuclear modification factor,

$$R_{AA}(S_T) = \frac{1}{\langle N_{\text{coll}} \rangle} \frac{dN^{AA}/dS_T}{dN^{pp}/dS_T}, \quad (7)$$

as a function of $S_T = \sum p_T^{\text{jets}}$ at $\sqrt{s_{NN}} = 5.02 \text{ TeV}$ are shown in Fig. 7. We note that $R_{AA}(S_T)$ is smaller than one if no cut is adopted on the transverse momentum of the W boson. However, the distributions of S_T is enhanced in the region $S_T < 60 \text{ GeV}/c$, and suppressed in the region $S_T > 60 \text{ GeV}/c$ if we adopt a kinematic cut $p_T^W > 60 \text{ GeV}/c$. $R_{AA}(S_T)$ has similar behavior as I_{AA} for tagged jet spectra because of the steeply falling cross section when $S_T > p_T^W = 60 \text{ GeV}/c$. Compared with inclusive jet transverse momentum, the suppression of R_{AA} is a result of the reduction of jet yields as well as the reduction of the jet energy in the QGP. However, S_T is the scalar summed of all the final states jets, the difference of S_T

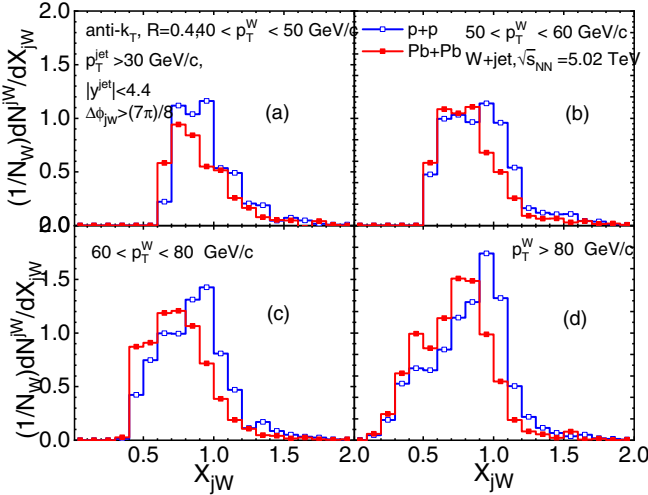


FIG. 8. Transverse momentum asymmetry x_{jW} of W + jets in Pb + Pb and $p + p$ collisions at $\sqrt{s_{NN}} = 5.02$ TeV in four p_T^W intervals (a)–(d).

between $p + p$ and Pb + Pb collisions is the total transverse momentum loss or broadening due to jet-medium interactions.

B. Modified correlations of W + jet in Pb + Pb

In this section we turn to correlations between the jet and the recoil W^\pm boson. First, the imbalance in the transverse momentum between a W boson and the associated jet $x_{jW} = p_T^{\text{jet}}/p_T^W$ is calculated in four p_T^W bins and is shown in Fig. 8. We only consider the most back-to-back W + jet pairs which are required to have azimuthal angle difference $\Delta\phi_{jW} > 7\pi/8$. Even in $p + p$ collisions, the jet energy does not exactly balance the W boson energy because of next-to-leading order effects and some of the quark's energy may extend outside of the jet cone. Compared with $p + p$ collisions, there is a significant displacement of the peak position of the momentum imbalance x_{jW} towards a smaller value in Pb + Pb collisions. The shift of the transverse momentum asymmetry is a direct consequence of the energy loss of the jet associated with the W boson with energy above the threshold. The transverse momentum of the W boson is unattenuated in the QGP, while the jet loses energy to the outside of the jet cone due to elastic and inelastic interactions with the hot-medium constituents. This leads to a smaller value of x_{jW} in Pb + Pb compared with that in $p + p$ collisions.

To quantify the relative shift in the asymmetry distribution between $p + p$ and central Pb + Pb collisions, the mean value of the momentum imbalance $\langle x_{jW} \rangle$ in different transverse momentum interval of the recoil W boson is calculated as shown in Fig. 9(a). We see that the mean value decreases as a function of the transverse momentum of the W boson. When p_T^W is in the interval 40–50 GeV/c, the mean value is about 0.98, and the energy of the W trigger is almost equal to the momentum of the associated jet in the transverse plane. When $p_T^W > 80$ GeV/c, the mean value is about 0.85, and the jet energy is noticeably smaller than the energy of the recoil W boson as a result of additional soft or hard emissions from

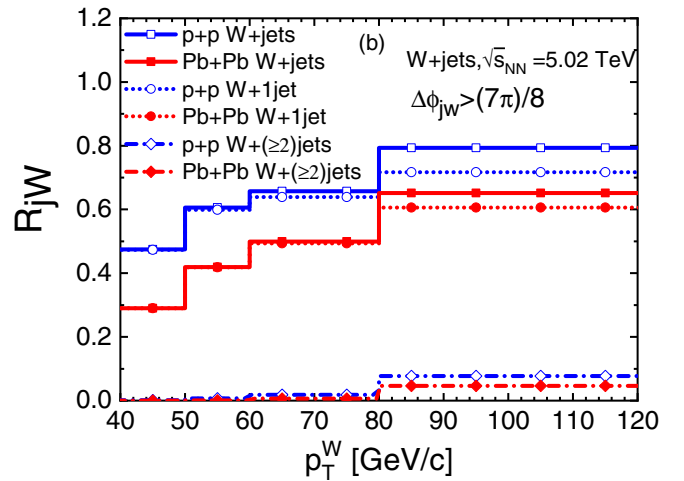
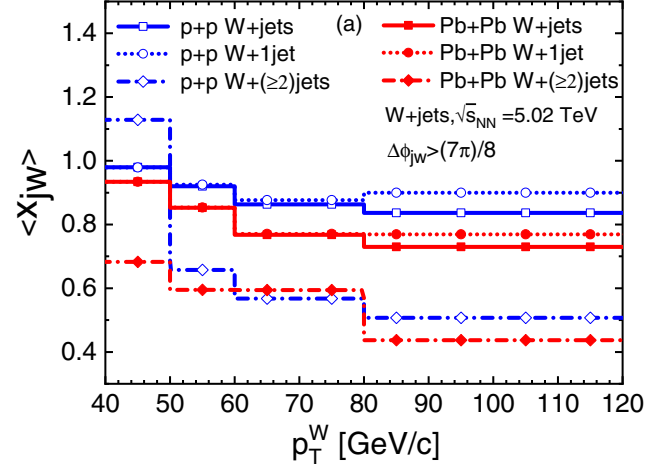


FIG. 9. The distribution of (a) the mean value of the momentum imbalance $x_{jW} = p_T^{\text{jet}}/p_T^W$ and (b) average number of triggered jets with transverse momentum greater than 30 GeV/c per W boson R_{jW} in Pb + Pb and $p + p$ collisions at $\sqrt{s_{NN}} = 5.02$ TeV as a function of the transverse momentum of W boson.

high-order corrections. We can also calculate the mean value for a W plus only one jet process (denoted as “ $W + 1$ jet”) and a W in association with more than one jets (denoted as “ $W + (\geq 2)$ jets”) as shown by the dotted lines and dash dotted lines. We see that the mean value in $W + (\geq 2)$ jets processes is about 0.5 for a high energy W boson, indicating that the jet energy in the multijet event is only half of the energy of the W boson. The mean value in $W + (\geq 2)$ jets processes is greater than 1 when $p_T^W < 60$ GeV/c. There is a very small probability that a W boson is associated with more than one jets in the back-to-back region with energy greater than p_T^W . In those processes, a W boson may be radiated from one of the jets as a fragmentation W boson.

It is not a surprise that the mean value of the momentum imbalance in Pb + Pb collisions is much smaller than that in $p + p$ collisions due to jet-medium interactions. The reduction of this mean value in Pb + Pb collisions from that in $p + p$ collisions $\Delta\langle x_{jW} \rangle$ and fraction of the reduction of the mean

TABLE I. Relative shift of the mean value of momentum imbalance of $W + \text{jet}$ pair (x_{jW}) between $p + p$ collisions and central Pb + Pb collisions at 5.02 TeV.

p_T^W (GeV/c)	40–50	50–60	60–80	80–120
$\Delta \langle x_{jW} \rangle$	0.045	0.068	0.096	0.107
$\Delta \langle x_{jW} \rangle / \langle x_{jW} \rangle_{pp}$	4.6%	7.4%	11.1%	12.8%
$p_T^W * \Delta \langle x_{jW} \rangle \simeq$ (GeV/c)	2.0	3.7	6.8	10.7

value $\Delta \langle x_{jW} \rangle / \langle x_{jW} \rangle_{pp}$ are tabulated in Table I. We see the reduction increases as a function of the transverse momentum of the W boson. It indicates that jets tagged by higher energy W bosons lose a larger fraction of their energy.

The amount of jet energy loss in Pb + Pb collisions is also shown in the last line in Table I. We see that the average jet energy loss increases with the energy of the recoil W boson. With the increased energy of the trigger W boson, the initial transverse momentum of the recoil jet is also larger and it has a higher probability to interact with the medium and loses larger fraction of its energy to the outside of the jet cone. However, our results of average jet energy loss in $W + \text{jet}$ processes is smaller than the Bayesian extraction from $\gamma + \text{jet}$ [83]. The underlying reason of the difference come from two aspects. First, the quark fraction in $W + \text{jets}$ processes is larger than that in $\gamma + \text{jet}$. In addition, jet cone size R used in our calculation is 0.4 while $R = 0.3$ is used in Ref. [83].

Another direct consequence of jet quenching is the reduction of the absolute jet yields above the kinematic threshold in Pb + Pb collisions, which can be investigated through calculating the average number of jet partners per W boson R_{jW} . The dependence of R_{jW} on the transverse momentum of the W boson p_T^W is shown in Fig. 9(b). As can be seen, the average number of tagged jets per W boson that pass the selection cut is overall suppressed in Pb + Pb due to jet quenching compared with that in $p + p$ collisions. We also calculated the fraction of jet that fall below the kinematic selection threshold and shown in Table II. We see that high-energy W bosons lose a smaller fraction of jets.

In addition to the transverse momentum correlations, we also calculate the azimuthal angle correlation of jets and the recoil W boson in four p_T^W intervals in both $p + p$ and Pb + Pb collisions, as shown in Fig. 10. Compared with $p + p$ collisions, the correlation is moderately suppressed at small azimuthal angle (relative to the W boson) in Pb + Pb collisions. The distribution is normalized to the number of W bosons that pass the selection cut rather than the number of $W + \text{jet}$ pairs, and one boson maybe cannot find any

TABLE II. Reduction of average number of jet partners per W boson (R_{jW}) between $p + p$ collisions and central Pb + Pb collisions at 5.02 TeV.

p_T^W (GeV/c)	40–50	50–60	60–80	≥ 80
$\Delta \langle R_{jW} \rangle$	0.19	0.19	0.16	0.14
$\Delta \langle R_{jW} \rangle / \langle R_{jW} \rangle_{pp}$	0.39	0.31	0.24	0.18

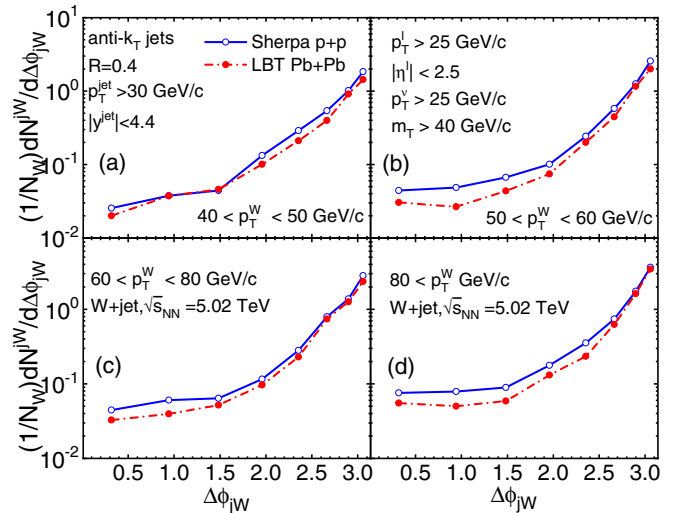


FIG. 10. Azimuthal angle correlation $\Delta\phi_{jW}$ of $W + \text{jets}$ in Pb + Pb and $p + p$ collisions at $\sqrt{s_{NN}} = 5.02$ TeV in four p_T^W intervals (a)–(d).

associated jets or can have more than one associated jets, so the integration of the azimuthal angle correlation may be less than or greater than one. The suppression of the small angle correlation of $W + \text{jets}$ is mainly due to the suppression of the secondary or multiple jets by jet quenching similar to the γ or $Z + \text{jet}$ correlation [38,41].

To illustrate the mechanism of this suppression, the contributions from W plus only one jet and W in association with more than one jet to the transverse momentum asymmetry and azimuthal angle correlation are also calculated as shown by the dotted line and the dash-dotted line both in $p + p$ and Pb + Pb collisions, respectively, in Fig. 11. We see that $W + 1$ jet processes dominate the large-angle region where the jet is opposite to the direction of the W boson in the transverse plane. However, in the small angle region, it is the W plus more than one jet processes that dominate the correlation. Compared with W plus only one jet, the azimuthal angle correlation of W associated with more than one jet is much broadened. This is because W plus only one jet processes mainly come from leading-order matrix element and the W boson is balanced by only one jet with azimuthal angle around 180° relative to the recoil W boson. On the other hand, W production associated with more than one jet mainly originates from NLO matrix elements which contain hard emissions at large angles. These multiple jets with relatively lower energy can easily lose energy due to jet quenching and shift their final energy below the kinematic cut. This leads to the suppression of $W + \text{jets}$ correlations at small azimuthal angle.

We observe a moderately broadened W -jet correlation in these events in Pb + Pb relative to $p + p$ collisions, which is different with the results of $Z + \text{jets}$ [41], where no modification is observed in Z plus only one jet process between $p + p$ and Pb + Pb collisions. The underlying reason for the difference is that the kinematic threshold used in those calculations is different, especially the cut on the jet rapidity. Figure 12 shows the azimuthal angle correlation $\Delta\phi_{jW}$ of

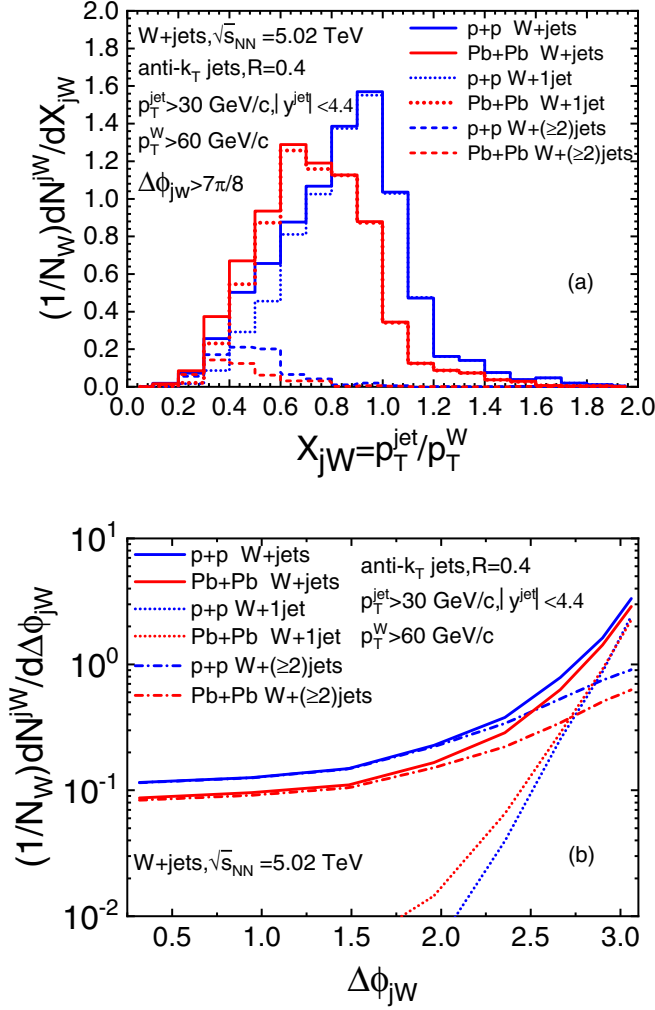


FIG. 11. (a) Transverse momentum asymmetry x_{jW} and (b) azimuthal angle correlation $\Delta\phi_{jW}$ of $W + \text{jets}$ in $\text{Pb} + \text{Pb}$ and $p + p$ collisions at $\sqrt{s_{NN}} = 5.02$ TeV. The contributions from W plus only one jet and W associated with more one jets to $\Delta\phi_{jW}$ and x_{jW} are calculated and shown by a dotted line and a dash-dotted line, respectively.

W plus only one jets (up) and W associated with more one jets (bottom) with jet rapidity $|y^{\text{jet}}| < 1.6$ and $|y^{\text{jet}}| < 4.4$ and the comparison between $p + p$ and $\text{Pb} + \text{Pb}$ collisions. We see $W + 1$ jets is much broader with jet rapidity $|y^{\text{jet}}| < 1.6$ compared with $|y^{\text{jet}}| < 4.4$, while contributions from $W + 2$ jets is much enhanced with jet rapidity $|y^{\text{jet}}| < 4.4$ compared with $|y^{\text{jet}}| < 1.6$. This is because a larger-rapidity cut would include more jets as a result of which the W event in association with only one jet with constraint $|y^{\text{jet}}| < 1.6$ would become an event in which W is associated with more than one jet with condition $|y^{\text{jet}}| < 4.4$. With constraint $|y^{\text{jet}}| < 1.6$, no significant difference between the $\Delta\phi_{jW}$ in $W + 1$ jet is observed between $p + p$ and $\text{Pb} + \text{Pb}$ collisions as in $Z + \text{jets}$ [41]. However, a moderately broadened W -jet correlation is seen with constraint $|y^{\text{jet}}| < 4.4$ in $\text{Pb} + \text{Pb}$ compared with $p + p$ collisions. This is because the energy of the jets with large rapidity in W plus multijets events is relatively small.

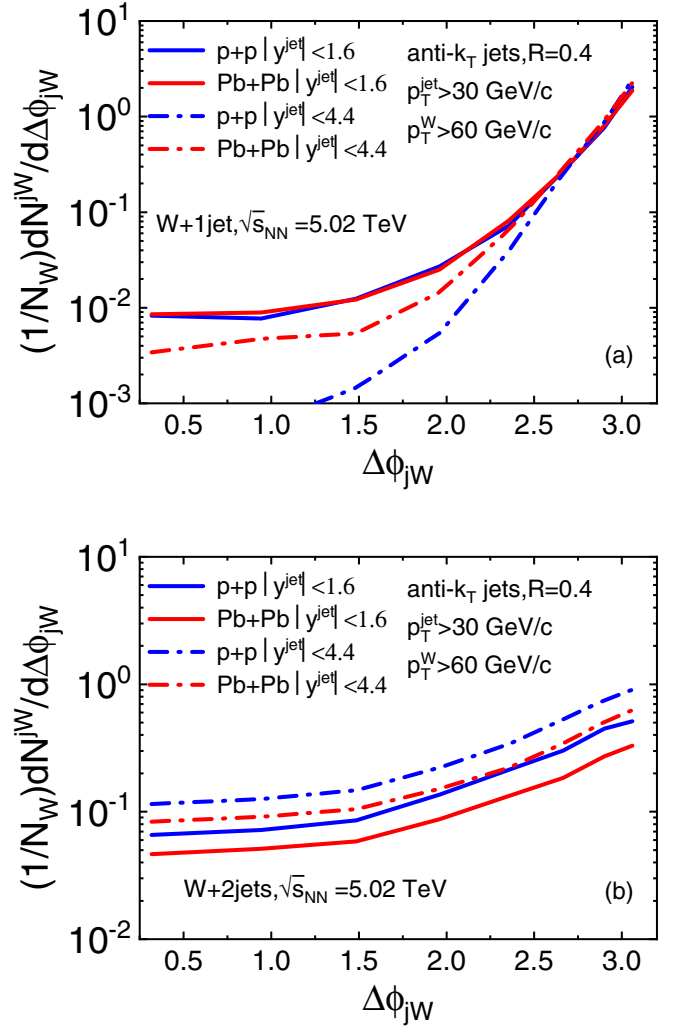


FIG. 12. Azimuthal angle correlation $\Delta\phi_{jW}$ (a) W plus only one jet and (b) W associated with more than one jet in $\text{Pb} + \text{Pb}$ and $p + p$ collisions at $\sqrt{s_{NN}} = 5.02$ TeV. The $\Delta\phi_{jW}$ distributions with $|y|$ cut 1.6 and 4.4 are shown by the solid line and the dash-dotted line, respectively.

Some of those jets lose energy and get easily lost in $\text{Pb} + \text{Pb}$ collisions. Some of these W plus multijets events in $p + p$ collisions would become $W + 1$ jet process in $\text{Pb} + \text{Pb}$ collisions due to jet quenching. This leads to the enhancement of $W + 1$ jet azimuthal correlation in the small-angle region with kinematic constraint $|y^{\text{jet}}| < 4.4$ in $\text{Pb} + \text{Pb}$ relative to $p + p$ collisions.

IV. CONCLUSION

We have carried out the systematic study of jet production in association with a W boson in both $p + p$ and $\text{Pb} + \text{Pb}$ collisions at the LHC energy. We use a Monte Carlo event generator SHERPA to generate reference $W + \text{jet}$ production in $p + p$ collisions with NLO ME matched to PS. Our calculations show excellent agreement with the experimental data in $p + p$ collisions. Jet propagation and medium response in the hot and dense medium are simulated by LBT and the medium

information is provided by 3 + 1D CLVisc hydrodynamics. We investigated the medium effect on the dijet invariant mass m_{jj} between the two leading jets. We also studied the nuclear modification of jet spectra associated with a W boson in different W transverse momentum intervals. Jet-medium interactions lead to an enhancement in small p_T^{jet} region and a suppression in large- p_T^{jet} region due to the steep falling of the jet spectra. We also presented the modification of the missing transverse momentum in W + jets events. The shift of this distribution to a smaller value indicates that jets lose large fraction of their energy in the opposite direction of the neutrino or W boson. We demonstrate that the shift of the scalar sum of transverse momentum S_T reflects the absolute jet energy loss in Pb + Pb collisions. Furthermore, we have

investigated the shift of W + jet p_T imbalance distribution x_{jW} due to jet energy loss, the suppression of jet partners per W trigger R_{jW} due to the reduction of jets yields, as well as the modification of W + jet azimuthal angle correlations $\Delta\phi_{jW}$ resulting from the suppression of multijets in heavy-ion collisions.

ACKNOWLEDGMENTS

The authors would like to thank H. Zhang, T. Luo, P. Ru, and G. Ma for helpful discussions. This research is supported by Guangdong Major Project of Basic and Applied Basic Research No. 2020B0301030008, Natural Science Foundation of China with Projects No. 11935007 and No. 11805167.

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- [1] X. N. Wang and M. Gyulassy, *Phys. Rev. Lett.* **68**, 1480 (1992).
 - [2] M. Gyulassy, I. Vitev, X. N. Wang, and B. W. Zhang, *Quark-Gluon Plasma* **3**, 123 (2004).
 - [3] G. Y. Qin and X. N. Wang, *Int. J. Mod. Phys. E* **24**, 1530014 (2015).
 - [4] I. Vitev, S. Wicks, and B. W. Zhang, *J. High Energy Phys.* **11** (2008) 093.
 - [5] I. Vitev and B. W. Zhang, *Phys. Rev. Lett.* **104**, 132001 (2010).
 - [6] G. Y. Qin and B. Muller, *Phys. Rev. Lett.* **106**, 162302 (2011).
 - [7] J. Casalderrey-Solana, J. G. Milhano, and U. A. Wiedemann, *J. Phys. G* **38**, 035006 (2011).
 - [8] C. Young, B. Schenke, S. Jeon, and C. Gale, *Phys. Rev. C* **84**, 024907 (2011).
 - [9] Y. He, I. Vitev, and B. W. Zhang, *Phys. Lett. B* **713**, 224 (2012).
 - [10] C. E. Coleman-Smith and B. Muller, *Phys. Rev. C* **86**, 054901 (2012).
 - [11] K. C. Zapp, F. Krauss, and U. A. Wiedemann, *J. High Energy Phys.* **03** (2013) 080.
 - [12] G. L. Ma, *Phys. Rev. C* **87**, 064901 (2013).
 - [13] F. Senzel, O. Fochler, J. Uphoff, Z. Xu, and C. Greiner, *J. Phys. G* **42**, 115104 (2015).
 - [14] J. Casalderrey-Solana, D. C. Gulhan, J. G. Milhano, D. Pablos, and K. Rajagopal, *J. High Energy Phys.* **10** (2014) 019; **09** (2015) 175.
 - [15] J. G. Milhano and K. C. Zapp, *Eur. Phys. J. C* **76**, 288 (2016).
 - [16] N. B. Chang and G. Y. Qin, *Phys. Rev. C* **94**, 024902 (2016).
 - [17] A. Majumder and J. Putschke, *Phys. Rev. C* **93**, 054909 (2016).
 - [18] L. Chen, G. Y. Qin, S. Y. Wei, B. W. Xiao, and H. Z. Zhang, *Phys. Lett. B* **782**, 773 (2018).
 - [19] L. Chen, G. Y. Qin, S. Y. Wei, B. W. Xiao, and H. Z. Zhang, *Phys. Lett. B* **773**, 672 (2017).
 - [20] Y. He, L. G. Pang, and X. N. Wang, *Phys. Rev. Lett.* **125**, 122301 (2020).
 - [21] Y. T. Chien and I. Vitev, *Phys. Rev. Lett.* **119**, 112301 (2017).
 - [22] L. Apolinario, J. G. Milhano, M. Ploskon, and X. Zhang, *Eur. Phys. J. C* **78**, 529 (2018).
 - [23] M. Connors, C. Nattrass, R. Reed, and S. Salur, *Rev. Mod. Phys.* **90**, 025005 (2018).
 - [24] W. Dai, S. Wang, S. L. Zhang, B. W. Zhang, and E. Wang, *Chin. Phys. C* **44**, 104105 (2020).
 - [25] S. Wang, W. Dai, B. W. Zhang, and E. Wang, *Eur. Phys. J. C* **79**, 789 (2019).
 - [26] S. Y. Chen, B. W. Zhang, and E. K. Wang, *Chin. Phys. C* **44**, 024103 (2020).
 - [27] J. Yan, S. Y. Chen, W. Dai, B. W. Zhang, and E. Wang, *Chin. Phys. C* **45**, 024102 (2021).
 - [28] S. Y. Chen, W. Dai, S. L. Zhang, Q. Zhang, and B. W. Zhang, *Eur. Phys. J. C* **80**, 865 (2020).
 - [29] X. N. Wang, Z. Huang, and I. Sarcevic, *Phys. Rev. Lett.* **77**, 231 (1996).
 - [30] X. N. Wang and Z. Huang, *Phys. Rev. C* **55**, 3047 (1997).
 - [31] G. Y. Qin, J. Ruppert, C. Gale, S. Jeon, and G. D. Moore, *Phys. Rev. C* **80**, 054909 (2009).
 - [32] W. Dai, I. Vitev, and B. W. Zhang, *Phys. Rev. Lett.* **110**, 142001 (2013).
 - [33] X. N. Wang and Y. Zhu, *Phys. Rev. Lett.* **111**, 062301 (2013).
 - [34] J. Casalderrey-Solana, D. C. Gulhan, J. G. Milhano, D. Pablos, and K. Rajagopal, *J. High Energy Phys.* **03** (2016) 053.
 - [35] R. K. Elayavalli, and K. C. Zapp, *Eur. Phys. J. C* **76**, 695 (2016).
 - [36] Z. B. Kang, I. Vitev, and H. Xing, *Phys. Rev. C* **96**, 014912 (2017).
 - [37] L. Chen, G. Y. Qin, L. Wang, S. Y. Wei, B. W. Xiao, H. Z. Zhang, and Y. Q. Zhang, *Nucl. Phys. B* **933**, 306 (2018).
 - [38] T. Luo, S. Cao, Y. He, and X. N. Wang, *Phys. Lett. B* **782**, 707 (2018).
 - [39] R. B. Neufeld, I. Vitev, and B.-W. Zhang, *Phys. Rev. C* **83**, 034902 (2011).
 - [40] R. B. Neufeld and I. Vitev, *Phys. Rev. Lett.* **108**, 242001 (2012).
 - [41] S. L. Zhang, T. Luo, X. N. Wang, and B. W. Zhang, *Phys. Rev. C* **98**, 021901(R) (2018).
 - [42] W. Chen, S. Cao, T. Luo, L. G. Pang, and X. N. Wang, *Phys. Lett. B* **777**, 86 (2018).
 - [43] W. Chen, S. Cao, T. Luo, L. G. Pang, and X. N. Wang, *Phys. Lett. B* **810**, 135783 (2020).
 - [44] S. L. Zhang, T. Luo, X. N. Wang, and B. W. Zhang, *Nucl. Phys. A* **982**, 599 (2019).
 - [45] A. M. Sirunyan *et al.* (CMS Collaboration), *Phys. Lett. B* **785**, 14 (2018).
 - [46] A. M. Sirunyan *et al.* (CMS Collaboration), *Phys. Rev. Lett.* **119**, 082301 (2017).

- [47] S. Chatrchyan *et al.* (CMS Collaboration), *Phys. Lett. B* **722**, 238 (2013).
- [48] E. L. Berger, J. Gao, A. Jueid, and H. Zhang, *Phys. Rev. Lett.* **122**, 041803 (2019).
- [49] L. Chen, S. Y. Wei, and H. Z. Zhang, *Eur. Phys. J. C* **80**, 1136 (2020).
- [50] R. Boughezal, X. Liu, and F. Petriello, *Phys. Rev. D* **94**, 113009 (2016).
- [51] M. Czakon, A. Mitov, M. Pellen, and R. Poncelet, *J. High Energy Phys.* **06** (2021) 100.
- [52] R. Boughezal, C. Focke, X. Liu, and F. Petriello, *Phys. Rev. Lett.* **115**, 062002 (2015).
- [53] S. Kallweit, J. M. Lindert, P. Maierhofer, S. Pozzorini, and M. Schönherr, *J. High Energy Phys.* **04** (2016) 021.
- [54] P. Sun, B. Yan, C. P. Yuan, and F. Yuan, *Phys. Rev. D* **100**, 054032 (2019).
- [55] Y. T. Chien, D. Y. Shao, and B. Wu, *J. High Energy Phys.* **11** (2019) 025.
- [56] Z. B. Kang, K. Lee, J. Terry, and H. Xing, *Phys. Lett. B* **798**, 134978 (2019).
- [57] T. Gleisberg, S. Hoeche, F. Krauss, M. Schonherr, S. Schumann, F. Siegert, and J. Winter, *J. High Energy Phys.* **02** (2009) 007.
- [58] H. Li, F. Liu, G. I. Ma, X. N. Wang, and Y. Zhu, *Phys. Rev. Lett.* **106**, 012301 (2011).
- [59] Y. He, T. Luo, X. N. Wang, and Y. Zhu, *Phys. Rev. C* **91**, 054908 (2015).
- [60] S. Cao, T. Luo, G. Y. Qin, and X. N. Wang, *Phys. Rev. C* **94**, 014909 (2016).
- [61] F. Krauss, R. Kuhn, and G. Soff, *J. High Energy Phys.* **02** (2002) 044.
- [62] T. Gleisberg and S. Hoeche, *J. High Energy Phys.* **12** (2008) 039.
- [63] F. Cascioli, P. Maierhofer, and S. Pozzorini, *Phys. Rev. Lett.* **108**, 111601 (2012).
- [64] S. Höche, F. Krauss, S. Schumann, and F. Siegert, *J. High Energy Phys.* **05** (2009) 053.
- [65] S. Höche, F. Krauss, M. Schonherr, and F. Siegert, *J. High Energy Phys.* **08** (2011) 123.
- [66] S. Höche, F. Krauss, M. Schonherr, and F. Siegert, *J. High Energy Phys.* **04** (2013) 027.
- [67] T. Gleisberg and F. Krauss, *Eur. Phys. J. C* **53**, 501 (2008).
- [68] S. Schumann and F. Krauss, *J. High Energy Phys.* **03** (2008) 038.
- [69] T. J. Hou *et al.*, *J. High Energy Phys.* **03** (2017) 099.
- [70] G. Aad *et al.* (ATLAS Collaboration), *Eur. Phys. J. C* **75**, 82 (2015).
- [71] M. Cacciari, G. P. Salam, and G. Soyez, *Eur. Phys. J. C* **72**, 1896 (2012).
- [72] M. Cacciari, G. P. Salam, and G. Soyez, *J. High Energy Phys.* **04** (2008) 063.
- [73] G. Aad *et al.* (ATLAS Collaboration), *Eur. Phys. J. C* **79**, 935 (2019).
- [74] K. J. Eskola, P. Paakkinen, H. Paukkunen, and C. A. Salgado, *Eur. Phys. J. C* **77**, 163 (2017).
- [75] P. Ru, B. W. Zhang, L. Cheng, E. Wang, and W. N. Zhang, *J. Phys. G* **42**, 085104 (2015).
- [76] X. F. Guo and X. N. Wang, *Phys. Rev. Lett.* **85**, 3591 (2000).
- [77] B. W. Zhang and X. N. Wang, *Nucl. Phys. A* **720**, 429 (2003).
- [78] B. W. Zhang, E. Wang, and X. N. Wang, *Phys. Rev. Lett.* **93**, 072301 (2004).
- [79] L. Pang, Q. Wang, and X. N. Wang, *Phys. Rev. C* **86**, 024911 (2012).
- [80] L. G. Pang, Y. Hatta, X. N. Wang, and B. W. Xiao, *Phys. Rev. D* **91**, 074027 (2015).
- [81] Z. W. Lin, C. M. Ko, B. A. Li, B. Zhang, and S. Pal, *Phys. Rev. C* **72**, 064901 (2005).
- [82] Y. He, S. Cao, W. Chen, T. Luo, L. G. Pang, and X. N. Wang, *Phys. Rev. C* **99**, 054911 (2019).
- [83] Y. He, L. G. Pang, and X. N. Wang, *Phys. Rev. Lett.* **122**, 252302 (2019).