Coulomb excitation of the $|T_z| = \frac{1}{2}$, $A = 23$ mirror pair

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Background: Electric-quadrupole (*E*2) strengths relate to the underlying quadrupole deformation of a nucleus and present a challenge for many nuclear theories. Mirror nuclei in the vicinity of the line of $N = Z$ represent a convenient laboratory for testing deficiencies in such models, making use of the isospin symmetry of the systems. **Purpose:** Uncertainties associated with literature $E2$ strengths in ²³Mg are some of the largest in $T_z = |\frac{1}{2}|$ nuclei in the *sd* shell. The purpose of the present paper is to improve the precision with which these values are known, to enable better comparison with theoretical models.

Methods: Coulomb-excitation measurements of ²³Mg and ²³Na were performed at the TRIUMF-ISAC facility using the TIGRESS spectrometer. They were used to determine the *E*2 matrix elements of mixed *E*2/*M*1 transitions.

Results: Reduced *E*2 transition strengths, $B(E2)$, were extracted for ²³Mg and ²³Na. Their precision was improved by factors of approximately 6 for both isotopes, while agreeing within uncertainties with previous measurements.

Conclusions: A comparison was made with both shell-model and *ab initio* valence-space in-medium similarity renormalization group calculations. Valence-space in-medium similarity renormalization group calculations were found to underpredict the absolute *E*2 strength, in agreement with previous studies.

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I. INTRODUCTION

Electric-quadrupole $(E2)$ transitions strengths are a powerful probe of nuclear structure, relating directly to the underlying quadrupole deformation of the nucleus. Simultaneously, they present a challenge to valence-space based theoretical models, with significant contributions to *E*2 strength arising from particle-hole excitations out of the model space. In the vicinity of the line of $N = Z$, mirror nuclei (nuclei with inverted numbers of protons and neutrons) are an excellent laboratory for nuclear physics, with isospin symmetry enforcing analogous structures for both nuclei. Studies of transition strengths in isobaric analog transitions have been employed for a huge range of nuclei, from low-mass systems such as ⁷Be and ⁷Li [\[1\]](#page-4-0), through the $f_{7/2}$ shell (e.g., Ref. [\[2\]](#page-4-0)), and extending into the upper *f p* and *g*⁹/² model spaces (e.g., Ref. [\[3\]](#page-4-0)).

Within the *sd* shell, one is able to compare modern *ab initio* techniques such as the valence-space in-medium similarity renormalization group (VS-IMSRG) to calculations utilizing exceptionally successful empirical shell-model interactions such as the USDB [\[4\]](#page-4-0). Systematic studies of deficiencies

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in such models require, however, high-quality experimental data. In this paper, we build on our previous studies of ^{22}Mg $[5]$ and ²¹Mg $[6]$ by presenting an improved experimental measurement of the low-lying *E*2 strength in the $|T_z| = \frac{1}{2}$, $A = 23$ mirror pair, ²³Mg and ²³Na. Prior to the present paper, the $B(E2)$ value between the ground and first excited state in ²³Mg [\[7,8\]](#page-5-0) was the most imprecisely measured of all $T_z = -\frac{1}{2}$, *sd*-shell nuclei [\[9\]](#page-5-0). A detailed systematic study comparing VS-IMSRG and shell-model calculations to the available data within the *sd* shell is the subject of a separate publication [\[10\]](#page-5-0).

The precision to which *E*2 strengths are determined in oddmass *sd*-shell nuclei is often limited by the fact that decays are of a mixed *E*2/*M*1 nature. When the decay is dominated by $M1$ strength, as is the case in ²³Mg and ²³Na, the leading uncertainty in determining the *E*2 strength is typically the mixing ratio δ between *E*2 and *M*1 contributions determined, for example, from the angular correlations between emitted γ rays. By performing a Coulomb excitation measurement, rather than determining the *E*2 strength from the decay properties, this source of uncertainty can be largely eliminated, allowing for a higher level of precision.

II. EXPERIMENTAL DETAILS

 23 Mg and 23 Na were investigated through Coulomb excitation using the TIGRESS facility $[11]$ at TRIUMF ISAC. ²³Mg nuclei were produced by the impinging of 480-MeV protons onto a SiC ISAC target. The Mg atoms produced were then selectively laser ionized using three step resonant excitation (285.3 to 880.8 to 291.6 nm) into an autoionizing state and extracted. 23 Na contamination was suppressed by the use of the ion-guide laser ion source (IG-LIS) [\[12\]](#page-5-0). A repeller plate is held at 40 V to suppress the extraction of surface-ionized contaminants by factors of up to 10^6 . ²³Na ions were produced by the surface ion source of the TRIUMF offline ion source (OLIS) [\[13\]](#page-5-0). The beams were then accelerated by the TRI-UMF ISAC accelerator chain and delivered to TIGRESS. The 23 Mg/²³Na cocktail beam had an energy of 42.9 MeV, while the ²³Na beam provided by OLIS was provided at energies of both 42.9 and 39.4 MeV. The total beam intensity for the 23 Mg portion of the experiment was maintained at roughly 3×10^5 particles per second—this includes a component from the remaining 23 Na contamination. The 23 Na beam intensity was maintained at approximately 6×10^7 particles per second.
The beams were then impinged onto a 0.44-mg/cm²-thick natTi target at the center of the TIGRESS array. Scattered beamlike and targetlike nuclei were detected in an S3-type [\[14\]](#page-5-0) silicon detector, mounted 31 mm downstream of the target position. Gamma rays were detected using the TIGRESS array, which for the present measurement was composed of 14 clover-type HPGe detectors. The high-purity germanium (HPGe) detectors were operated in their withdrawn configuration, with the face of the detectors 14.5 cm from the target and the bismuth germanate (BGO) suppression shields forward, providing the best possible peak-to-background ratio and Doppler correction.

While the use of IG-LIS heavily suppresses extraction of 23 Na, a degree of contamination remains which was monitored in two ways. First, a Bragg detector was used to provide

FIG. 1. Tail of the silicon-time laser-time distribution (see text for details), least-squares fit with an exponential plus constant background. The integral of the background is used to determine the surface ionized contamination originating from 23 Na. Shown in the inset is the total time structure arising from the laser ionization in the present measurement with the fitted area indicated.

an instantaneous measure of the beam composition. While the composition is being determined in this way experimental data cannot be acquired. For the second method, the 10-kHz signal used to synchronize the laser ionization system was used, with every second pulse triggering the generation of a ramping waveform, which could then be digitized. The amplitude of the digitized waveform thereby gave a proxy for the time of the detection relative to the laser-ionization pulse and could thus be used to distinguish laser-ionized beam components which had a 10-kHz pulsed structure from the continuous surface ionized contaminants. This method allowed for a continuous determination of contamination, allowing us to monitor for sudden changes in the ISAC target behavior. Based on these analyses, the ²³Na contribution to the beam cocktail was determined to be 15.2(9)% of the total, with the uncertainty being predominantly systematic and arising from the choice of fitting region. Figure 1 shows the laser timing distribution, the tail of which was fit with an exponential and baseline to determine the relative contributions to the beam cocktail.

III. ANALYSIS

The data were unpacked using the GRSISORT [\[15\]](#page-5-0) soft-ware package, built in a ROOT [\[16\]](#page-5-0) framework. Gamma-ray events were Doppler corrected event by event on the basis of the beam and target kinematics determined from the hit location in the annular silicon detectors and whether the detected particle had beamlike or targetlike kinematic properties. Gamma-ray spectra for ²³Na at 39.4 MeV and the ²³Mg + $2²³$ $2²³$ Na cocktail beam are shown in Figs. 2 and [3,](#page-2-0) respectively. Relative γ -ray detection efficiencies for TIGRESS were determined using a standard suite of 152 Eu, 133 Ba, and 60 Co sources. ²³Na data were split into 48 groups: 12 angular bins for both beamlike and targetlike detection, repeated for both beam energies. The 23 Mg data were binned in 12 groups, six

FIG. 2. Doppler-corrected γ -ray spectra on the basis of ²³Na (red) and 48 Ti (black) kinematics for a 23 Na beam energy of 39.4 MeV. Top: Detection of a targetlike recoil (⁴⁸Ti) in the downstream annular silicon detector. Bottom: Detection of a beamlike recoil (^{23}Na) in the downstream annular silicon detector. The additional width of the 23 Na peak in the top figure arises from the wide angles at which the scattering occurs, leading to significant slowing in the target material. Other lines in the titanium corrected (black) spectra arise from isotopes of titanium with a lower natural abundance than 48Ti (73.8%).

angular groups each for beamlike and targetlike scattering. Yields were adjusted for the natural abundance of ⁴⁸Ti.

In the beamlike scattering data the ²³Mg and ²³Na γ -ray lines were readily distinguished and were fitted individually, as shown in Fig. 4. The observed 48 Ti yield was then adjusted for the observed 23 Na component on the basis of the 42.9-MeV 23 Na data. For the target scattering data the two components of the $A = 23$ γ -ray peak were not always distinguishable. The 23 Na component was therefore determined and subtracted on the basis of the observed component in the beamlike scattering data and of the 42.9 -MeV pure 23 Na data taken with OLIS. 23 Na contamination could thereby be handled empirically, without requiring assumptions about beam composition and minimizing the introduction of systematic uncertainties.

The Coulomb-excitation analysis was performed in the coupled-channels GOSIA2 code [\[17\]](#page-5-0) used to simultaneously

FIG. 3. As Fig. 2 but for a cocktail ²³Mg (\approx 85%) and ²³Na $(\approx 15\%)$ beam at an energy of 42.9 MeV.

FIG. 4. Fit of the γ -ray peaks observed in TIGRESS corresponding to the deexcitation of the first excited state in 23Mg and the analog state in the stable contaminant and mirror nucleus, 23 Na. These data were coincident with events from the first four rings of the downstream annular silicon detector, corresponding to angles of 19.5◦–25.8◦. This fitting method can be used for all cases where the beamlike particle was detected. See the text for details of the analysis for targetlike particle detection.

FIG. 5. Low-lying levels in ^{23}Mg and ^{23}Na relevant to the present analysis. The $5/2^+ \rightarrow 3/2^+$ transition (red) was investigated and other transitions were included within the GOSIA analysis. Gray transitions indicate mixed *E*2/*M*1. Data taken from Ref. [\[9\]](#page-5-0).

analyze beamlike and targetlike data. The levels included in the GOSIA2 analysis are shown in Fig. 5. Ground-state spectroscopic quadrupole moments for both 23 Na and 23 Mg were taken at their evaluated values [\[18\]](#page-5-0). For each beam all data were analyzed simultaneously, maximizing sensitivity. The $\langle \frac{3}{2}^+ | E2 | \frac{5}{2}^+ \rangle$ and $\langle \frac{5}{2}^+ | E2 | \frac{5}{2}^+ \rangle$ matrix elements were varied in order to construct χ^2 surfaces to incorporate any mutual dependence. χ^2 surfaces for ²³Mg and ²³Na are shown in Figs. 6 and 7, respectively. Little sensitivity was found to the diagonal matrix element beyond an indication of the sign in 23 Na. Matrix elements to higher-lying states were fixed to their literature values during the minimization procedure, however their 1σ limits were investigated to quantify any impact on the result and are incorporated as a systematic uncertainty.

IV. DISCUSSION

Extracted matrix elements are summarized in Table I, along with other properties derived from the present results.

FIG. 7. χ^2 surface resulting from the GOSIA2 analysis of ²³Na from which transition and diagonal matrix elements were extracted.

We compare the present results with those calculated from two theoretical models. VS-IMSRG calculations were performed using the EM1.8/2.0 interaction $[19,20]$, which was generated by similarity renormalization group (SRG) evolution [\[21\]](#page-5-0) of the chiral N³LO NN interaction of Entem and Machleidt [\[22\]](#page-5-0), and adding a nonlocally regulated N^2LO 3N interaction with the low energy constants adjusted to reproduce the triton binding energy and the 4He matter radius. Calculations are performed in a harmonic oscillator basis of $\hbar \omega$ = 20 MeV with $2n + \ell \le e_{\text{max}} = 12$ and with a truncation on the three-body matrix elements $e_1 + e_2 + e_3 \leq E_{3\text{max}} = 16$. All operators are truncated at the normal-ordered two-body level. A diagonalization was then performed using the NUSHELLX [\[23\]](#page-5-0) code. Shell-model calculations were also performed in NUSHELLX, making use of the USDB interaction [\[4\]](#page-4-0) with effective charges of $e_\pi = 1.36$ and $e_\nu = 0.45$.

TABLE I. *E*2 matrix elements, *B*(*E*2) values, spectroscopic quadrupole moments, and mixing ratios deduced from the present paper with statistical and systematic uncertainties quoted, in that order. Where available, literature values are shown for comparison. Mixing ratios were deduced on the basis of the literature lifetimes and the presently determined *B*(*E*2) values.

^{23}Na	This paper	Literature	Ref.
$\langle \frac{3}{2}^+ E2 \frac{5}{2}^+ \rangle$ eb	$0.252 \pm 0.003 \pm 0.004$	$0.237^{+0.014}_{-0.015}$	$\lceil 9 \rceil$
$B(E2; \frac{5}{2}^+ \rightarrow \frac{3}{2}^+) e^2$ fm ⁴	$106 \pm 3 \pm 3$	93 ± 12	[9]
$\langle \frac{5}{2}^{+} E2 \frac{5}{2}^{+} \rangle$ eb	$-0.29_{-0.29}^{+0.32} \pm 0.05$		
$Q_s(\frac{5}{2}^+)$ eb	$-0.22_{-0.22}^{+0.25} \pm 0.04$		
$\delta_{E2/M1}^2$	0.0038 ± 0.0004	$0.0034^{+0.0004}_{-0.0003}$	$\lceil 9 \rceil$
23 Mg			
$\langle \frac{3}{2}^{+} E2 \frac{5}{2}^{+} \rangle$ eb	$0.285 \pm 0.015 \pm 0.004$	$0.23^{+0.07}_{-0.10}$	$\lceil 9 \rceil$
$B(E2; \frac{5}{2}^+ \rightarrow \frac{3}{2}^+) e^2$ fm ⁴	135^{+15}_{-14} ± 4	86 ± 58	$\lceil 9 \rceil$
$\langle \frac{5}{2}^{+} E2 \frac{5}{2}^{+} \rangle$ eb	$-0.2_{-1.3}^{+2.0} \pm 0.05$		
$Q_s(\frac{5}{21}^+)$ eb	$-0.15_{-1.00}^{+1.50} \pm 0.04$		
$\delta_{E2/M1}^2$	0.0056 ± 0.0006	$0.0036_{-0.0028}^{+0.0028}$	$\lceil 9 \rceil$

TABLE II. $B(E2)$ values determined in the present paper compared to those calculated using the VS-IMSRG method and the nuclear shell model using the USDB interaction.

Isotope	$B(E2) \downarrow (e^2 \text{ fm}^4)$					
	J_i^{π}	J^{π}_{τ}	Expt.	VS-IMSRG	USDB	
^{23}Mg	$5+$ 21	$3+$ 21	135(15)	75.2	117.3	
^{23}Na		3^{+}	106(4)	56.9	109.1	

Table II shows the present results compared to those calculated using the aforementioned models. The shell-model (USDB) calculations well reproduce the observed *B*(*E*2) values. VS-IMSRG values, meanwhile, are considerably lower than the experimentally determined ones. This deficiency is consistent with that observed in our previous studies of $|T_z| = 1$ mirror pairs [5]. While the VS-IMSRG values are deficient, it should be noted that the relative $B(E2)$ strengths are better reproduced by the *ab initio* calculations. Defining the ratio $R = \frac{B(E2\frac{5}{2}^{+} \rightarrow \frac{3}{2}^{+})[^{23}Mg]}{B(E2\frac{5}{2}^{+} \rightarrow \frac{3}{2}^{+})[^{23}Na]}$ $\frac{B(E_2 \frac{3}{2} \rightarrow \frac{3}{2} + \frac{1}{2})}{(25 \times 10^{-23} \text{ kg})}$, we find that $R_{\text{exp}} = 1.27(14)$, whereas $R_{\text{USDB}} = 1.06$ and $R_{\text{VS-IMSRG}} = 1.34$. In order to understand the relative behavior of *E*2 strengths across mirror pairs, a systematic study is required, which is the subject of a separate work [\[10\]](#page-5-0).

V. CONCLUSIONS

 23 Mg and 23 Na have been studied by Coulomb excitation using particle- γ coincidences at TRIUMF-ISAC. The relative insensitivity of the Coulomb excitation methodology to the *M*1 transitions which dominate the decay of the first excited states allowed for the extraction of *E*2 transition strengths with superior precision to that previously achieved, while

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agreeing within uncertainties with literature values. Calculations were performed, employing both the shell model with the USDB interaction, and the *ab initio* VS-IMSRG methodology. Consistent with previous work, it was found that the VS-IMSRG calculations significantly underpredict the *E*2 transition strength. A detailed, systematic investigation of deficiencies in *E*2 strength from VS-IMSRG calculations is the subject of a separate study [\[10\]](#page-5-0).

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