Evidence against the Efimov effect in ¹²C from spectroscopy and astrophysics

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Background: The Efimov effect is a universal phenomenon in physics whereby three-body systems are stabilized via the interaction of an unbound two-body subsystems. A hypothetical state in ¹²C at 7.458-MeV excitation energy, comprising a loose structure of three α particles in mutual two-body resonance, has been suggested in the literature to correspond to an Efimov state in nuclear physics. The existence of such a state has not been demonstrated experimentally.

Purpose: Using a combination of γ spectroscopy, charged-particle spectroscopy, and astrophysical rate calculations allowing for strict limits on the existence of such a state to been established here.

Method: Using the combined data sets from two recent experiments, one with the TexAT (Texas Active Target) TPC (Time Projection Chamber) to measure α decay and the other with Gammasphere to measure γ decay of states in ¹²C populated by ¹²N and ¹²B β decay, respectively, we achieve high sensitivity to states in close proximity to the α threshold in ¹²C.

Results: No evidence of a state at 7.458 MeV is seen in either data set. Using a likelihood method, the 95% confidence limit γ -decay branching ratio is determined as a function of the β -decay feeding strength relative to the Hoyle state. In parallel, calculations of the 3α reaction rate show the inclusion of the Efimov corresponds to a large increase in the reaction rate around 5×10^7 K.

Conclusion: From decay spectroscopy—at the 95% confidence limit, the Efimov state cannot exist at 7.458 MeV with any γ -decay branching ratio unless the β strength is less than 0.7% of the Hoyle state. This limit is evaluated for a range of different excitation energies and the results are not favorable for existence of the hypothetical Efimov state in ¹²C. Furthermore, the 3α reaction rate with the inclusion of a state between 7.43 and 7.53 MeV exceeds the rate required for stars to undergo the red giant phase.

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The Efimov effect is a universal quantum phenomena present in several areas of physics. The effect is observed for three-body systems that are comproed of subsystems where the subunit two-body systems are unbound but have a large *s*-wave scattering length. Vitaly Efimov found that under these conditions the long-range three-body attraction arises and that this attraction can support a family of three-body states. A detailed review of Efimov physics and experimental evidence for it can be found in Ref. [1]. The classical interpretation is that

the three-body force binds the system via the "shuttling" back and forth of one of the particles. This then creates an infinite series of states given by a universal scaling law. While predicted 50 years ago, this phenomenon took 35 years to observe experimentally. The first clear evidence for Efimov effect was reported for the system of ultracold gas of caesium atoms in an external magnetic field [2]. In nuclear systems, which were the original focus of Efimov's investigation, the situation is more complicated. In principle, a $J^{\pi} = 0^+$ (corresponding to L =0) 3α state in ¹²C, where the 2α subsystems are unbound but form a long-lived resonant state, can be seen as Efimov trimer. In his original paper Efimov argued that the 0^+ excited state at

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7.65 MeV in ¹²C (Hoyle state) possibly originates due to this interesting three-body quantum phenomena which we now call the Efimov effect [3]. Microscopic three-body continuum calculations that utilize phenomenological α - α potential [4] indicate that the three-body potential is small compared to the nuclear and Coulomb potentials and as a result the Hoyle state is probably not related to the Efimov effect. Faddeev calculations for the 3α system have previously been performed and do not predict an additional near-threshold 0^+ that would correspond to an Efimov state [5]. More recently, existence of an Efimov state in ${}^{12}C$ at an excitation energy that corresponds to a mutual ⁸Be(g.s.) resonance for all three α particles was suggested in Refs. [6,7]. This excitation energy is given, in units of MeV, by the following simple relation which takes into account that the narrow resonance of ⁸Be(g.s.) is unbound by 91.84 keV with respect to decay to two α particles:

$$E = \frac{2}{3} \sum_{i}^{3} E_{\text{rel}_{i}} - Q = 2 \times 0.09184 + 7.2747 = 7.458.$$
(1)

The main goal of this paper is to search for any evidence of this hypothetical state or, if not, place experimental limits on its existence. We utilize the results of two recent experiments. The first one is the study that is sensitive to three α -particle decay channels of the near α -threshold excited states in ¹²C populated in the β^+ decay of ¹²N [8,9]. The second is the γ -spectroscopy study of states in ¹²C populated in β^- decay of ¹²B [10]. Combining these two data sets we demonstrate that there is no evidence for a resonance at or near 7.458 MeV. Stringent experimental limits on its existence have been established. We also examine the astrophysical implications of such a state existing below the Hoyle state using a simplistic model to calculate the 3α reaction rate and demonstrate the incompatibility of this result with current astrophysical observations.

Experimental limits of an Efimov state. There has not been a large amount of experimental activity to investigate if there is a resonance in ${}^{12}C$ below the Hoyle state. One investigation claiming to observe an Efimov state in a heavy-ion Zn+Zn/Ni+Ni collisions at 35 MeV/u was recently published [11]. By examining events with three α particles and measuring their relative energies, potential Efimov states were found by looking at three α -particle triplets where the relative energy between all α particles is consistent with 92 keV. Due to the reaction mechanism used, there is a dominant contribution from uncorrelated α particles which are required to be accounted for via mixing. The remaining spectrum is then accounted for using an arbitrary fit function on top of Breit Wigner peaks which show up around 0.1 MeV suggested mutual ⁸Be resonances. Due to low statistics and dependence on this fit function, it is therefore difficult to definitely claim evidence of a peak. However, this study represented a dedicated effort to experimentally observe such a state. While in-medium effects afforded by a heavy-ion reaction may enhance the production of an Efimov state, the reaction complexity also introduces numerous sources of background that are difficult to account for. A cleaner population method is through the β decay of ${}^{12}N / {}^{12}B$ which populates 0^+ , 1^+ , and 2^+ states in accordance to the β -decay selection rules.



FIG. 1. Excitation function obtained from 3α decay energy deposition. The dotted red line corresponds to a Gaussian fit for the Hoyle state contribution. The yield above this is conservatively taken as possibly arising from additional states such as the Efimov state (ES). The peak around 7.3 MeV corresponds to deposition events on the cathode.

Through the recently developed β -delayed charged-particle decay technique using the TexAT (Texas Active Target) TPC (Time Projection Chamber) [8], one is afforded a good probe on any resonance existing at a low relative energy above the 3α threshold. This has not been previously identified due to the difficulties associated with low-energy measurements using implantation in silicon detector arrays. Despite the advantages afforded using this technique, the measurement of a three-particle final state only 180 keV above threshold is still challenging.

Efimov state limits from β -delayed charged-particle decays in a TPC. To establish a limit on the population of the Efimov state via β decay of ¹²N, the TexAT TPC was used to study the β -delayed charged-particle decay of ¹²N [8]. A beam of ¹²N with an energy of 24 MeV was stopped inside of the active-area of the TexAT TPC by 20 Torr of CO₂ gas. This was achieved on a single implantation decay basis which allowed for the matching between the implantation event and the subset of events where the β decay populates states above the α threshold in ¹²C. The trigger condition for the decay was that more than one Micromegas pad fired. The trigger threshold is 10 keV and therefore one is sensitive to decay events down to $E_x \approx 7.38$ MeV, below which the subsequent ⁸Be decay (for $E_x > 7.37$ MeV) releases 92 keV of energy which would also trigger the detector providing 100% efficiency for $E_x >$ 7.38 MeV and $E_x < 7.37$ MeV. The three-dimensional tracks from the three α particles arising from these events were then reconstructed and the total energy deposited was used to calculate the excitation energy. This is shown in Fig. 1, where the majority of events seen are from the Gaussian tails of the Hoyle state at 7.654 MeV. One may also determine the energy of any 3α decay by looking at the total length of the tracks and converting the range of the α particles to an energy and summing. Taking events which lay within the region of interest for both of these plots, one may then manually check events to deduce the origin of these counts. The peak in



FIG. 2. The 95% C.L. exclusion plot for a 7.458-MeV Efimov state. The γ and α experimental limits exclude regions of the plot relating to the strength of the β -feeding strength relative to the Hoyle state (abscissa) and the γ -ray branching ratio (ordinate). With a particular range of the γ branching ratio, the existence of a state cannot be conclusively excluded if the β -feeding strength ratio is $<7 \times 10^{-3}$.

Fig. 1 just above the threshold corresponds to events where the implanting beam is scattered (primarily off the entrance window) and the ¹²N beam is implanted either on the cathode or anode. When it subsequently decays, part of the energy of the event is lost as one or two α particles deposit their energy into the anode or cathode directly rather than liberating electrons in the gas volume. To determine the contribution from states between the absolute threshold at the Hoyle state, a Gaussian tail was fitted for the Hoyle state contribution using the previously obtained experimental resolution of 55 keV. To remain conservative, any background above this Gaussian component was counted as a potential Efimov contribution: 137.1 counts in total. The 95% confidence limit (C.L.) was therefore taken as 160.5 for α events from Poisson statistics.

To convert this into a limit, the expected number of 3α Efimov-state (ES) decays is given by:

$$N_{\rm ES} = N_{\rm Hoyle} \frac{\beta_{\rm ES}}{\beta_{\rm Hoyle}} \frac{{\rm BR}_{\alpha}({\rm ES})}{{\rm BR}_{\alpha}({\rm Hoyle})},$$
(2)

where β_i describes the β -decay feeding strength from ¹²N and $BR_{\alpha} = \frac{\Gamma_{\alpha}}{\Gamma_{tot}}$ for the ES and the Hoyle state. Rearranging the terms, one arrives at:

$$\frac{\beta_{\rm ES}}{\beta_{\rm Hoyle}} BR_{\alpha}({\rm ES}) = BR_{\alpha}({\rm Hoyle}) \frac{N_{\rm ES}}{N_{\rm Hoyle}}.$$
 (3)

The factor on the left-hand side of Eq. (3) allows us to place a limit on the α branching ratio multiplied by the β -feeding strength relative to the Hoyle state. Inserting the values, BR_{α}(Hoyle) = 99.9%, N_{Hoyle} = 23,276, and N_{ES} < 160.5. This 95% confidence limit is represented in Fig. 2 (slanted-right blue hash region) where the abscissa, $x = \frac{\beta_{ES}}{\beta_{Hoyle}}$, is plotted against the ordinate, $y = BR_{\gamma}(ES) = 1 - BR_{\alpha}(ES)$. The product of the β strengths (x) and the α branching ratio



FIG. 3. Gammasphere energy spectrum gated on 4439-keV transition. The peak at 3214 keV is from the Hoyle $\rightarrow 2_1^+$ transition. The yield in the 3014-keV region (red arrow) shows no sign of a peak from the Efimov $\rightarrow 2_1^+$ transition. Data from Ref. [10].

(1 - y) gives $(\frac{\beta_{\text{ES}}}{\beta_{\text{Hoyle}}} \text{BR}_{\alpha}(\text{ES})) < 0.69\%$ from Eq. (3) therefore constraining x(1 - y) < 0.69% in the exclusion plot.

Efimov state limits from β -delayed γ spectroscopy. Aside from observation in the 3α channel, there have been studies of the γ -decay spectrum associated with β -delayed population of ¹²C using ¹²B [10]. By using Gammasphere to study for coincident γ rays with the 4.44-MeV first-excited state in ¹²C, one may examine any possible contribution from ¹²C(ES) \rightarrow ¹²C(2⁺₁) which should correspond to $E_{\gamma} =$ (7.458–4.444) MeV = 3.014 MeV. Examining the region of interest from these previous data [10], no such yield can be seen in Fig. 3. The yield from a potential Efimov state is <11.4 counts at 95% C.L. in comparison to the Hoyle state which has a yield of 58 ± 9. Following the same prescription above, the number of γ rays from Efimov state decays is given by:

$$N_{\rm ES} = N_{\rm Hoyle} \frac{\beta_{\rm ES}}{\beta_{\rm Hoyle}} \frac{{\rm BR}_{\gamma}({\rm ES})}{{\rm BR}_{\gamma}({\rm Hoyle})}.$$
 (4)

Separating the unknowns onto the left-hand side from those known on the right-hand side, one gets:

$$\frac{\beta_{\rm ES}}{\beta_{\rm Hoyle}} BR_{\gamma}({\rm ES}) = BR_{\gamma}({\rm Hoyle}) \frac{N_{\rm ES}}{N_{\rm Hoyle}}.$$
 (5)

The known values are $N_{\rm ES} < 11.4$, $N_{\rm Hoyle} = 58 \pm 9$, and $BR_{\gamma}({\rm Hoyle}) = 0.042\%$. This allows for an additional exclusion region from the product of the β strengths and the γ branching ratio of <0.008% (red left-slanted hash region in Fig. 2).

The combination of the γ and α measurements in Fig. 2 demonstrates that an Efimov state at 7.458 MeV is excluded at the 95% C.L. unless the β -feeding strength is $<7 \times 10^{-3}$ the strength of the Hoyle state and has a specific decay γ -decay branch. Requiring the γ branching ratio to be $\approx 100\%$, this 95% C.L. extends down to $<10^{-4}$.

The existence of an Efimov state at an energy other than 7.458 MeV may also be examined using the same approach as detailed above. The product of the β strengths and the



FIG. 4. Triple- α reaction rates as a function of the astrophysical temperature using the NACRE formulism [14]. The dot-dashed black line corresponds to the preexisting NACRE rate. The solid blue line includes the Hoyle state and the 2⁺₂ state in ¹²C using the latest accepted values. The third line, dashed red, also includes an additional state corresponding to the Efimov state using parameters from Table I. The upper limit calculated from Suda [17] is shown as a green triangle whereby the red giant phase requires a reaction rate of less than $\approx 10^{-29}$ cm⁻⁶ s⁻¹ mol⁻² at a temperature of 10^{7.8} K. The inclusion of the Efimov state clearly violates this reaction rate limit.

 γ branching-ratio at the 95% C.L. does not exceed 0.016%. The technique used for the α limit is robust up until the separation of the Hoyle peak from any potential second peak is roughly 2.35 σ , i.e., up until E_x = 7.525 MeV where the γ and α branching ratios are comparable. The γ limit is highly applicable until the γ branching ratio is such that the predicted number of Efimov γ decays is less than the 95% C.L. or our detection limit. Given that Hoyle state is well measured via γ decays in the Gammasphere data and the background is fairly flat around the Hoyle peak, this implies an excitation energy exceeding the Hoyle state is required whereby the γ branching ratio continues to rapidly decrease, and as such, this scenario may be definitely excluded.

Astrophysical limitations on low-lying states. In the 3α process, there is a strong contribution from low-lying 0⁺ states [12,13]. It is for this reason that the Hoyle state so successfully enhances the 3α reaction rate by 7 orders of magnitude, overcoming the A = 5, 8 bottleneck in helium-burning stars. Any additional low-lying state therefore must also contribute to a large degree, particularly at lower temperatures. To understand the role that the Efimov state may have, one can examine the expected astrophysical reaction rate including such a resonance in addition to the Hoyle state. The NACRE formulation was used [14] and three cases were examined, the results of which appear in Fig. 4.

The first case (dashed-dotted black line) is the NACRE parameter case [14] which shows the current reaction rate. The second case (solid blue line) uses the most up-to-date parameters for the Hoyle state, the 2^+_2 in 12 C and the 8 Be (g.s.) [15,16,18]. The main influence corresponds to the modified radiative and α widths of the Hoyle state and the revised width of the 8 Be (g.s.). The final case (dashed red line) is whereby, in

TABLE I. Naïve estimates of the Efimov decay mechanism. The α widths, Γ_{α} , assume the same reduced width and the radiative width assumes the dominance of the *E*2 transition to the 4.44 MeV 2⁺ state and is scaled as E_{ν}^{5} .

Parameter	Hoyle state	Efimov state
$\overline{E_x}$	7.654 MeV	7.458 MeV
Γ_{α}	9.3 eV [15]	79.8 neV
$\Gamma_{\rm rad}$	5.1 meV [18]	3.72 meV
$\Gamma_{\alpha}/\Gamma_{\rm tot}$	>99.9%	0.002%

addition to the states included in the second case, an additional resonance corresponding to the Efimov state was included. For such a state, in Table I, naïve estimates of the widths are calculated via assuming the same underlying reduced width and radiative width for the Efimov state as the Hoyle state when scaled appropriately by their energies (for penetrability and E_{γ}^{5} for the α and γ widths accordingly). This is verified by more developed investigations into the properties of an Efimov state [6]. For the Efimov state, $\Gamma_{rad} \gg \Gamma_{\alpha_0}$ so $\Gamma_{rad} \approx \Gamma_{tot}$. Therefore, the rate is driven predominantely by Γ_{α_0} .

The contribution of the additional Efimov resonance in the third case clearly demonstrates a phenomenal increase (a factor of $\approx 40\,000$ at 5×10^7 K) in the reaction rate at lower temperatures which are vitally important for many stars. Understanding the role that the 3α reaction rate has on the dynamics of stars has previously been examined [17] and it was concluded that the reaction rate at $10^{7.8}$ K must be less than $\approx 10^{-29}$ cm⁻⁶ s⁻¹ mol⁻² in order for stars to undergo the red giant phase. This astrophysical limit on the rate is shown in Fig. 4 as an upside-down green triangle and the rate from case three (including the Efimov state) can clearly be seen to exceed this limit and does so by a factor of ≈ 24 . As such, the existence of such a state is incompatible with current astrophysical models. Given the contribution of the Efimov state is limited by Γ_{α} , to quench the contribution of this state to be compatible with the reaction rate limit, this width is required to be decreased by an order of magnitude. The Efimov state has a well-developed cluster structure and therefore a partial α width a factor of 10 lower than the Hoyle state is clearly not possible. Such a state is additionally excluded down to an extremely small β -feeding ratio of 10^{-4} from the combined α/γ spectroscopy for such a state.

Modifying the energy of this additional state results in a rate of more than 10^{-29} cm⁻⁶ s⁻¹ mol⁻² for energies of 7.43 < E_x < 7.53 MeV and therefore resonances in this region may also be explicitly excluded.

Conclusion. Using combined data from particle and γ decay from ${}^{12}N/{}^{12}B$, one may place incredibly restrictive limits on the β -feeding strength and therefore existence of an Efimov state below the Hoyle state in carbon-12. An Efimov state in such close proximity to the α threshold would decay almost solely via γ decay and therefore the β -feeding strength relative to the Hoyle state is expected to be $<10^{-4}$ at the 95% C.L. Furthermore, it can clearly be seen that the Efimov state has a tremendous impact on stellar evolution. A low-lying state 0⁺ (whether Efimov or merely an α -clustered

state) would have a significant impact on stellar abundances that the existence of such a resonance is incompatible with current astrophysical models whereby the modified 3α reaction rate would eliminate the red-giant phase of stars.

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- [1] P. Naidon and S. Endo, Rep. Prog. Phys. 80, 056001 (2017).
- [2] T. Kraemer, M. Mark, P. Waldburger, J. G. Danzl, C. Chin, B. Engeser, A. D. Lange, K. Pilch, A. Jaakkola, H.-C. Nägerl, and R. Grimm, Nature 440, 315 (2006).
- [3] V. Efimov, Phys. Lett. B 33, 563 (1970).
- [4] H. Suno, Y. Suzuki, and P. Descouvemont, Phys. Rev. C 91, 014004 (2015).
- [5] O. Shinsho and K. Hiroyuki, Nucl. Phys. A 493, 91 (1989).
- [6] H. Zheng, A. Bonasera, M. Huang, and S. Zhang, Phys. Lett. B 779, 460 (2018).
- [7] H. Zheng and A. Bonasera, J. Phys. Commun. 4, 085011 (2020).
- [8] J. Bishop, G. V. Rogachev, S. Ahn, E. Aboud, M. Barbui, P. Baron, A. Bosh, E. Delagnes, J. Hooker, C. Hunt, H. Jayatissa, E. Koshchiy, R. Malecek, S. Marley, R. O'Dwyer, E. Pollacco, C. Pruitt, B. Roeder, A. Saastamoinen, L. Sobotka, and S. Upadhyayula, Nucl. Instrum. Methods A 964, 163773 (2020).
- [9] J. Bishop, G. V. Rogachev, S. Ahn, E. Aboud, M. Barbui, A. Bosh, C. Hunt, H. Jayatissa, E. Koshchiy, R. Malecek, S. T. Marley, E. C. Pollacco, C. D. Pruitt, B. T. Roeder, A. Saastamoinen, L. G. Sobotka, and S. Upadhyayula, Phys. Rev. C 102, 041303(R) (2020).
- [10] M. Munch, M. Alcorta, H. O. U. Fynbo, M. Albers, S. Almaraz-Calderon, M. L. Avila, A. D. Ayangeakaa, B. B. Back, P. F. Bertone, P. F. F. Carnelli, M. P. Carpenter, C. J. Chiara, J. A. Clark, B. DiGiovine, J. P. Greene, J. L. Harker, C. R. Hoffman, N. J. Hubbard, C. L. Jiang, O. S. Kirsebom, T. Lauritsen,

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K. L. Laursen, S. T. Marley, C. Nair, O. Nusair, D. Santiago-Gonzalez, J. Sethi, D. Seweryniak, R. Talwar, C. Ugalde, and S. Zhu, Phys. Rev. C **93**, 065803 (2016).

- [11] S. Zhang, A. Bonasera, M. Huang, H. Zheng, D. X. Wang, J. C. Wang, L. Lu, G. Zhang, Z. Kohley, Y. G. Ma, and S. J. Yennello, Phys. Rev. C 99, 044605 (2019).
- [12] S. Ishikawa, Phys. Rev. C 87, 055804 (2013).
- [13] N. B. Nguyen, F. M. Nunes, I. J. Thompson, and E. F. Brown, Phys. Rev. Lett. **109**, 141101 (2012).
- [14] C. Angulo, M. Arnould, M. Rayet, P. Descouvemont, D. Baye, C. Leclercq-Willain, A. Coc, S. Barhoumi, P. Aguer, C. Rolfs, R. Kunz, J. Hammer, A. Mayer, T. Paradellis, S. Kossionides, C. Chronidou, K. Spyrou, S. Degl'Innocenti, G. Fiorentini, B. Ricci, S. Zavatarelli, C. Providencia, H. Wolters, J. Soares, C. Grama, J. Rahighi, A. Shotter, and M. Lamehi Rachti, Nucl. Phys. A 656, 3 (1999).
- [15] J. Kelley, J. Purcell, and C. Sheu, Nucl. Phys. A 968, 71 (2017).
- [16] D. Tilley, J. Kelley, J. Godwin, D. Millener, J. Purcell, C. Sheu, and H. Weller, Nucl. Phys. A 745, 155 (2004).
- [17] T. Suda, R. Hirschi, and M. Y. Fujimoto, Astrophys. J. 741, 61 (2011).
- [18] T. Kibédi, B. Alshahrani, A. E. Stuchbery, A. C. Larsen, A. Görgen, S. Siem, M. Guttormsen, F. Giacoppo, A. I. Morales, E. Sahin, G. M. Tveten, F. L. B. Garrote, L. C. Campo, T. K. Eriksen, M. Klintefjord, S. Maharramova, H.-T. Nyhus, T. G. Tornyi, T. Renstrøm, and W. Paulsen, Phys. Rev. Lett. 125, 182701 (2020).