

**Fission dynamics of compound nuclei: Pairing versus fluctuations**Yu Qiang,<sup>1</sup> J. C. Pei,<sup>1,\*</sup> and P. D. Stevenson<sup>2</sup><sup>1</sup>*State Key Laboratory of Nuclear Physics and Technology, School of Physics, Peking University, Beijing 100871, China*<sup>2</sup>*Department of Physics, University of Surrey, Guildford, Surrey GU2 7XH, United Kingdom*

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Energy dependence of fission observables is a key issue for wide nuclear applications. We studied real-time fission dynamics from low-energy to high excitations in the compound nucleus  $^{240}\text{Pu}$  with the time-dependent Hartree-Fock + BCS approach. It is shown that the evolution time of the later phase of fission towards scission is considerably lengthened at finite temperature. As the role of dynamical pairing is vanishing at high excitations, the random transition between single-particle levels around the Fermi surface to mimic thermal fluctuations is indispensable to drive fission. The obtained fission yields and total kinetic energies with fluctuations can be divided into two asymmetric scission channels, namely, S1 and S2, which explain well experimental results and give microscopic support to the Brosa model. With increasing fluctuations, the S2 channel takes over the S1 channel and the spreading fission observables are obtained.

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A deeper understanding of fission from a droplet of condensed nuclear matter splitting into fragments is still strongly motivating, even though its discovery occurred more than 80 years ago [1]. First, fission studies are crucial for increasingly wide nuclear applications [2], as well as for basic sciences such as synthesis of superheavy elements [3,4] and constraints on the  $r$ -process in neutron-star mergers [5–7]. However, fission measurements are very difficult and energy-dependent fission data are sparse in major nuclear data libraries [8]. Second, the fission process is extremely complex from the microscopic view as a probe of nonequilibrium quantum many-body dynamics [9–11].

It is known that the pioneer Bohr-Wheeler statistical theory is very successful but not applicable for highly excited fission with experimental observations of exceeding prescission neutron multiplicities [12]. Strong viscosity and dissipation in hot nuclear matter has to be invoked [13]. The realistic fission of compound nuclei is not only determined by the barrier but also the later phase of fission evolutions towards scission becomes important [14]. In addition, the quantum effects such as shell effects and pairing gradually fade away as excitation energies increase [4,15]. There have been studies based on temperature-dependent fission barriers [4,15,16] or energy-dependent level densities [17]; however, a fully microscopic fission dynamics in terms of excitation energy dependence is still absent.

For experiments, the well-known semiempirical model by Brosa *et al.* [18] is the primary tool for the evaluation of fission data with high accuracy. This model has great physics intuition on the multichannel fission and the random neck-rupture assumptions, which is well established by detailed fission observations, in particular correlations between distributions

of mass yields, total kinetic energies (TKE), and neutron multiplicities. However, as a major obstacle for extrapolations when experiments are absent, the origin and pathways of two asymmetric standard channels (denoted S1 and S2) in the Brosa model are ambiguous, although shell effects are present in nascent fragments [10,19]. For shape dynamics models [16,20–23] based on complex potential energy surfaces (PES), it is still difficult to identify the pathways of these two modes. Therefore, the validation of physics assumptions of the Brosa model from microscopic dynamical models would be significant.

The microscopic time-dependent density functional theory (TD-DFT) is promising to describe the later phase of fission from saddle to scission [24–28]. TD-DFT has provided valuable clues about the overdamped assumption [29], nonadiabatic effects [30], the excitations of fragments [28], and the role of shell effects [19] and pairing effects [28], but the lack of fluctuations undermines TD-DFT to reproduce distributions of fission yields [29,31]. It is an evident defect that strongly dissipated fission has no dissipation-fluctuation correspondence. At low excitations, the probability of orbital exchanges is connected to the Landau-Zener effect and is dependent on the pairing gap [24]. At high excitations, as the pairing is vanishing, it is expected that thermal fluctuations are the main source of orbital changes. There are efforts such as the stochastic TD-DFT with initial fluctuations [31,32] or by including dynamical density fluctuations [33], aiming to bridge the Langevin descriptions [21]. The time-dependent random-phase approximation [34] can describe particle-number fluctuations but not actual distributions of fission observables [30,35]. In addition to quantal fluctuations, it is essential to include thermal fluctuations based on TD-DFT which would become significant in fission of compound nuclei. Thermal fluctuations in the mean-field picture can be naturally linked to random transitions be-

\*peij@pku.edu.cn

tween single-particle levels around Fermi surfaces. Actually the fluctuations in single-particle and collective motions are intertwined in the TD-DFT approach.

In this Letter, we study the energy dependence of various fission observables of the compound nucleus  $^{240}\text{Pu}$  with microscopic TD-DFT, including dynamical pairing and thermal fluctuations. This is an attempt to develop a unifying fission framework by connecting microscopic dynamical models and statistical Langevin models. As a reward, it turns out that our results can explain the origin of the two asymmetric fission channels of the Brosa model.

We describe the fission of compound nuclei with the time-dependent Hartree-Fock + BCS (TD-BCS) approach [36,37]. The initial configuration of the compound nucleus  $^{240}\text{Pu}$  is obtained by finite-temperature Hartree-Fock + BCS calculations [15,38]. The evolution of compound nuclei is similar to that of the zero-temperature time-dependent Hartree-Fock-Bogoliubov (TD-HFB) formalism [36],

$$i\hbar \frac{d\mathcal{R}}{dt} = [H, \mathcal{R}], \quad (1)$$

where  $H$  is the HFB Hamiltonian, and  $\mathcal{R}$  is the general density matrix. The initial  $H$  and  $\mathcal{R}$  are associated with a finite temperature [38]. The time-dependent Hartree-Fock + BCS equations can be obtained by using the BCS basis or the canonical basis [36,37]. Note that TD-BCS can describe dynamical pairing approximately compared to the fully dynamical pairing in TD-HFB.

In TD-BCS, the evolution of densities is actually related to the evolution of occupation numbers of single-particle levels. In the mean-field picture, the single-particle levels around Fermi surfaces are active for orbital exchanges due to dynamical pairing fluctuations [28]. To mimic thermal fluctuations, we implement random transitions between single-particle levels without explicit external forces, in which the occupation number  $n_k$  is modified with a random additive,  $\delta n_{kj}$ . The random  $\delta n_{kj}$  is designed as a transition so that the total particle number is strictly conserved. The transition occurs as a random Gaussian noise around Fermi surfaces. The transition amplitude  $\delta n_{kj} = q_r C_{kj} \exp(-\frac{|\varepsilon_k - \varepsilon_j|}{T})$ , where  $e^{-|\varepsilon_k - \varepsilon_j|/T}$  is a symmetric Boltzmann distribution,  $T$  is an effective temperature, and  $\varepsilon_k$  and  $\varepsilon_j$  are single-particle energies. The transition amplitudes are also constrained by the Pauli exclusion principle. For two levels with occupation numbers  $n_k$  and  $n_j$ , we take  $C_{kj} = \min(n_k, 1 - n_j)$ , which is the maximum allowed symmetric transition amplitude. The transition occurs randomly as a jump up or a jump down, which is determined by another random number,  $q_r \in [-1.0, 1.0]$ . The random transitions simulate nucleon-nucleon collisions and also act as a remedy to truncated correlations, while the exact treatment of collision terms beyond the time-dependent Hartree-Fock (TDHF) approach is very sophisticated [39]. The effective temperature in fluctuations is not necessarily the initial temperature of compound nuclei. Note that fluctuations can be considerable even in spontaneous fission [40]. At high temperatures, the orbital exchanges are mainly induced by thermal fluctuations, even when two levels are not close.

The calculations are performed with the time-dependent Hartree-Fock solver SKY3D [41,42] with the addition of our

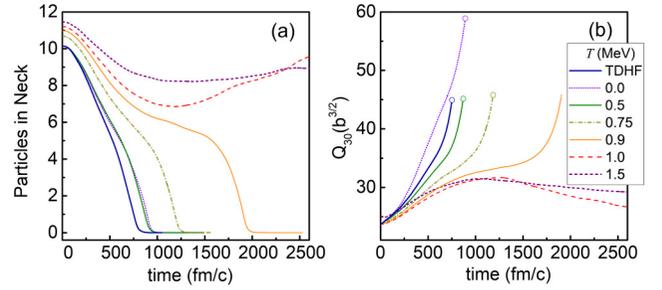


FIG. 1. (a) TD-BCS evolutions of the number of particles in a neck of 2 fm in length at the density minimum. (b) The octupole deformation  $Q_{30}$  (in units of  $b = 100 \text{ fm}^2$ ) of  $^{240}\text{Pu}$  with different initial temperatures  $T$ . TDHF results without pairing are also shown.

modifications of TD-BCS plus thermal fluctuations. The initial configurations at finite temperatures are obtained using the SKYAX solver [15,43] to interface with SKY3D [44]. There is a pairing cutoff in SKYAX as described in Ref. [45]. The excitation energy of compound nuclei is related to the initial temperature [4,38]. The time evolution operator is based on the Taylor expansion at the fourth order and the time step is taken as 0.1 fm/c. The box size ( $x, y, z$ ) is taken as  $48 \times 48 \times 64$  fm and the grid space is 0.8 fm. The nuclear interaction we adopted is the widely used SkM\* parametrization [46] and the pairing interaction is the mixed pairing [47]. More details of the methods are given in the Supplemental Material [48].

We first studied the fission of the compound nucleus  $^{240}\text{Pu}$  with different initial temperatures with TD-BCS. The initial deformation in this work adopts the dimensionless quadrupole-octupole deformations as  $\beta_2 = 2.3$  and  $\beta_3 = 1.0$  (see the definition in Ref. [49]). The timescale is an important quantity characterizing nuclear dynamics with dissipations and fluctuations [50]. Figure 1(a) displays the evolutions of the number of particles in the neck. The zero-temperature TD-BCS calculations are slower than TDHF calculations due to its longer fission pathway. With increasing temperatures  $T$ , the evolution times become considerably lengthened. Note that fission would not occur above  $T = 0.9$  MeV within TD-BCS. At  $T = 0.9$  MeV, corresponding to an excitation energy of 16.1 MeV, the evolution takes 1900 fm/c, or  $6.3 \times 10^{-21}$  s. It can be seen that timescales of the later phase of fission are indeed considerable compared to the statistical model at high excitations. For example, the timescale is about  $10^{-20-21}$  s by statistical models for fission of highly excited superheavy nuclei [51]. Figure 1(b) displays the evolutions of octupole deformations. TD-BCS calculations at zero temperature result in a larger octupole deformation at scission. At high excitations, shape evolutions become very slow as an indication of increasing viscosities.

There is great concern about the role of dynamical pairing in fission of compound nuclei when the initial static pairing is vanishing. Figure 2 displays the evolution of pairing energies with different initial temperatures. We see that both initial pairing and dynamical pairing are very small at high excitations. Note that the pairing above the critical temperature is not strictly zero [52]. It has been known that in some cases fission can happen within TD-BCS or TD-HFB but not within

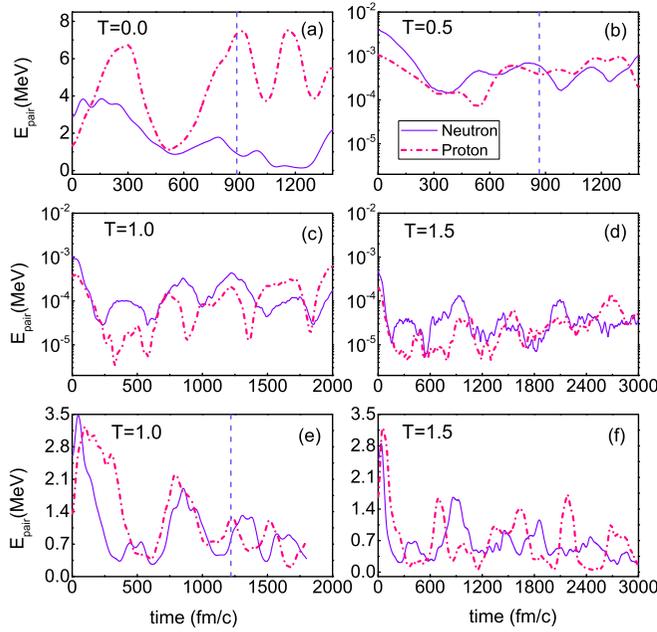


FIG. 2. The evolutions of neutron and proton pairing energies (in MeV) within TD-BCS at different initial temperatures of  $T = 0$  MeV (a), 0.5 MeV (b), 1.0 MeV (c), and 1.5 MeV (d). TD-BCS results with the initial pairing field at zero temperature are also shown for  $T = 1.0$  MeV (e) and 1.5 MeV (f).

TDHF [30,53]. For tests, we also performed TD-BCS calculations at high temperatures but with an initial pairing field at zero temperature [see Figs. 2(e) and 2(f)]. Dynamical pairing fluctuations in Figs. 2(e) and 2(f) are suppressed compared to zero-temperature results in Fig. 2(a). In hot nuclei, we see that pairing energies dissipate rapidly at the beginning stage of evolutions. Furthermore, the damping time from  $T = 1.0$  to 1.5 MeV decreases, which indicates increasing viscosities

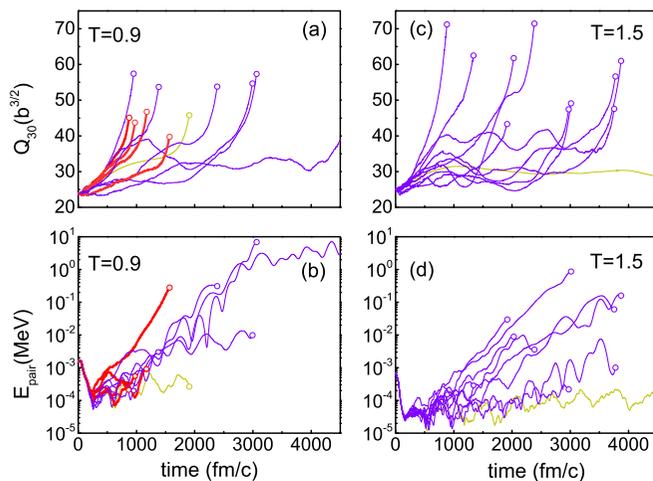


FIG. 3. The evolutions of  $Q_{30}$  and pairing energies within TD-BCS plus thermal fluctuations at temperatures of 0.9 and 1.5 MeV. Results of  $T = 0.9$  MeV with small scission deformations (S1 channel) are shown in thick red (gray) lines. Results without fluctuations in yellow (light gray) lines are also shown for comparison.

and dissipations as temperature increases. This also implies that the initial lubricant pairing can reduce viscosity to some extent. The fission now happens at  $T = 1.0$  and 1.25 MeV with initial pairings, but still does not happen at  $T = 1.5$ . In this case, thermal fluctuations have to be invoked.

Figure 3 displays the evolutions of octupole deformations and pairing energies at  $T = 0.9$  and 1.5 MeV with thermal fluctuations. The resulting evolution times of different pathways are distributed widely. At  $T = 1.5$  MeV, the fission now occurs with thermal fluctuations as an indispensable driving source. The resulting scission deformations are widely distributed compared to those of  $T = 0.9$  MeV, as a result of larger effects of thermal fluctuations at higher temperatures. Pairing energies decrease at the beginning due to dissipations and then induced dynamical pairing (not superfluid pairing) increases towards the scission due to thermal fluctuations, exhibiting interesting competing roles of dissipation and fluctuation. The induced pairing becomes prominent after long time evolutions. It has also been shown that the reentrance of pairing can happen in hot rotating nuclei [54].

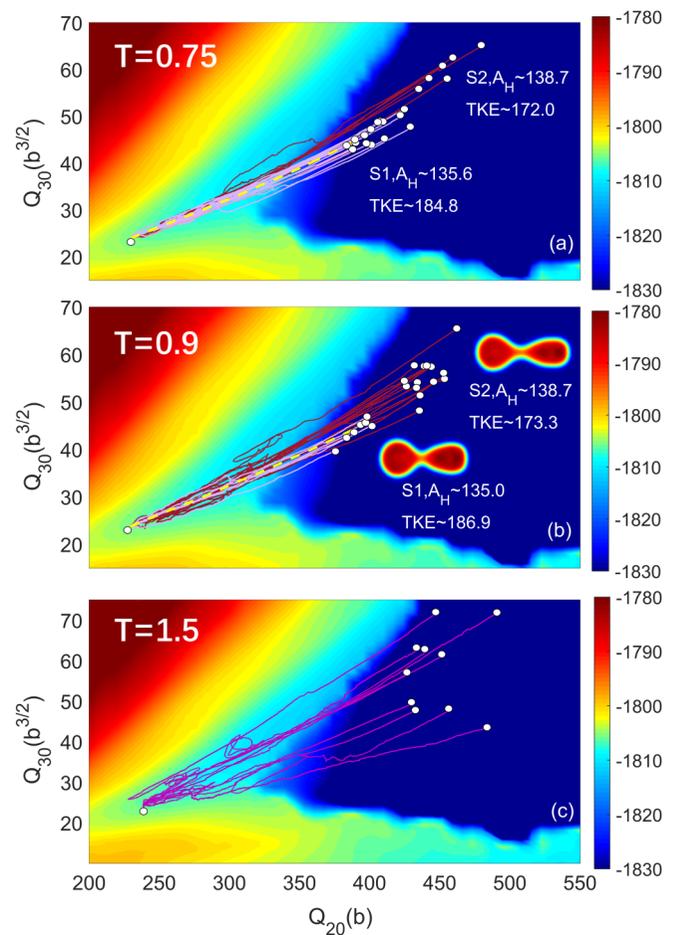


FIG. 4. The fission pathways of  $^{240}\text{Pu}$  within TD-BCS plus thermal fluctuations in the space of quadrupole-octupole deformations ( $Q_{20}$ ,  $Q_{30}$ ), at temperatures of 0.75 MeV (a), 0.9 MeV (b), and 1.5 MeV (c). At  $T = 0.75$  and 0.9 MeV, the fission pathways without fluctuations (dashed yellow line) are also shown. Specific results of the S1 and S2 channels are also shown inside.

TABLE I. Calculated fission observables of  $^{240}\text{Pu}$  at different initial temperatures  $T$  (MeV) and associated excitation energies  $E^*$ , including mass of heavy fragment  $A_H$ , excitation energies of heavy fragments  $E_H^*$  and light fragments  $E_L^*$ , and TKE. All energies are in MeV. TDHF results are also listed. TD-BCS results with an initial pairing of zero temperature are listed for comparison. With thermal fluctuations, averaged values and standard deviations in parentheses are shown.

$T$ ( $E^*$ )	$A_H$	$E_H^*$	$E_L^*$	TKE
TDHF	134.9	9.9	12.0	186.9
TD-BCS with temperature				
0.5 (4.7)	135.3	9.1	19.3	186.9
0.75 (10.6)	135.8	13.8	21.3	185.3
0.9 (16.1)	135.6	17.8	24.8	185.6
TD-BCS with initial pairing				
0.0	138.6	10.6	22.6	172.1
0.75 (10.6)	137.7	13.5	25.1	175.6
1.0 (20.5)	138.4	19.8	28.8	174.2
1.25 (34.6)	137.0	28.9	32.9	176.9
TD-BCS with thermal fluctuations				
0.75 (10.6)	136.5(1.8)	14.5(2.5)	24.8(3.2)	180.9(6.9)
0.9 (16.1)	137.5(2.4)	20.5(3.3)	27.4(2.7)	177.4(6.9)
1.5 (53.2)	138.5(4.9)	41.4(5.7)	42.3(4.9)	172.6(3.9)

One of the key issues is the distribution of outcomes of TD-BCS calculations with thermal fluctuations. Figure 4 shows the fission pathways in the quadrupole-octupole deformation space. At  $T = 0.75$  MeV ( $E^* = 10.6$  MeV) and  $T = 0.9$  MeV ( $E^* = 16.1$  MeV), the fission yields are mainly distributed around two asymmetric channels. For example, the average masses of heavy fragments at  $T = 0.9$  MeV are around  $A_H = 135.0$  and  $138.7$  for the S1 and S2 channels, respectively. The associated average TKE are around  $186.9$  and  $173.3$  MeV, respectively. This is exactly the two standard asymmetric fission channels of  $^{240}\text{Pu}$  in the Brosa model [18]. The two channels of pathways are close in the deformation space while S2 corresponds to a larger deformation or a longer neck. The onset of two asymmetric channels is mainly due to dynamical fluctuations; however, it would be difficult to identify them by models based on static PES. It is understandable that the longer neck structure leads to smaller TKE and wider distributions. The longer S2 pathways also lead to more dissipations and higher excitations of fragments (see the Supplemental Material [48] for details), leading to the slope of the sawtooth structure of neutron multiplicities. At  $T = 1.5$  MeV ( $E^* = 53.2$  MeV), the splitting of S1 and S2 is not clear any more. The distributions of scission deformations and masses are much wider than those of  $0.75$  and  $0.9$  MeV. This demonstrated that the splitting of S1 and S2 disappears due to increasing fluctuations at high excitations. In Fig. 4,

S1 is dominated at  $T = 0.75$  MeV and S2 is dominated at  $T = 0.9$  MeV. Systematic analysis of experiments has also found that S2 is dominated and the percentage of the S1 channel decreases with increased energies [55].

Finally, Table I displays calculated fission observables. The complete results of all fluctuated pathways are given in the Supplemental Material [48]. In experiments, the averaged TKE of  $^{239}\text{Pu}(n, f)$  is about  $175$  MeV and slightly decreases with increasing excitation energies [56]. It is related to larger scission deformations and decreased S1 percentage at higher excitations as shown in Fig. 4. The experimental averaged mass of heavy fragments  $A_H$  is about  $140$  [18] rather than the magic number  $132$ . It is shown that TKE and  $A_H$  from TD-BCS with temperatures and TDHF are about  $186$  MeV and  $135.5$ , which are around the S1 channel. On the other hand, TKE and  $A_H$  from TD-BCS with initial pairing are about  $175$  MeV and  $138$ . We see that a considerable initial pairing is favorable for the S2 channel. Without thermal fluctuations, the resulting fission observables are close to the S1 channel. With increasing thermal fluctuations, the S2 channel gradually takes over the S1 channel, and finally the averaged TKE and  $A_H$  come back to experimental values with considerable spreading widths. We have demonstrated the essential role of thermal fluctuations in fission of compound nuclei when initial pairings vanish and dissipations increase. It is also of great interest to obtain excitation energies of fragments, which are relevant to neutron multiplicities. In Table I, heavy fragments have less excitation energies at low excitations but become close to those of light fragments at high excitations, which is reasonable as the sawtooth structure would fade away at high excitations [57]. In conclusion, it is promising to develop a unifying framework for various energy-dependent fission observables with more pathways, a suitable effective temperature for fluctuations, and also varying initial deformations [29,53]. Our work sheds a new light on the intuitive Brosa model for extrapolations and provides valuable clues towards a predictive microscopic fission theory.

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- [1] L. Meitner and O. R. Frisch, Disintegration of uranium by neutrons: A new type of nuclear reaction, *Nature (London)* **143**, 239 (1939).  
 [2] L. A. Bernstein, D. A. Brown, A. J. Koning, B. T. Rearden, C. E. Romano, A. A. Sonzogni, A. S. Voyles, and W. Younes,

Our future nuclear data needs, *Annu. Rev. Nucl. Part. Sci.* **69**, 109 (2019).

- [3] J. H. Hamilton, S. Hofmann, and Y. T. Oganessian, Search for superheavy nuclei, *Annu. Rev. Nucl. Part. Sci.* **63**, 383 (2013).

- [4] J. C. Pei, W. Nazarewicz, J. A. Sheikh, and A. K. Kerman, Fission Barriers of Compound Superheavy Nuclei, *Phys. Rev. Lett.* **102**, 192501 (2009).
- [5] M. Eichler, A. Arcones, A. Kelic, O. Korobkin, K. Langanke, T. Marketin, G. Martinez-Pinedo, I. V. Panov, T. Rauscher, S. Rosswog, C. Winteler, N. T. Zinner, and F. K. Thielemann, The role of fission in neutron star mergers and its impact on the  $r$ -process peaks, *Astrophys. J.* **808**, 30 (2015).
- [6] S. Goriely, The fundamental role of fission during  $r$ -process nucleosynthesis in neutron star mergers, *Eur. Phys. J. A* **51**, 22 (2015).
- [7] J. Sadhukhan, S. A. Giuliani, Z. Matheson, and W. Nazarewicz, Efficient method for estimation of fission fragment yields of  $r$ -process nuclei, *Phys. Rev. C* **101**, 065803 (2020).
- [8] M. B. Chadwick *et al.*, ENDF/B-VII.1 nuclear data for science and technology: Cross sections, covariances, fission product yields and decay data, *Nucl. Data Sheets* **112**, 2887 (2011).
- [9] M. Bender *et al.*, Future of nuclear fission theory, *J. Phys. G: Nucl. Part. Phys.* **47**, 113002 (2020).
- [10] K. H. Schmidt and B. Jurado, Review on the progress in nuclear fission—experimental methods and theoretical descriptions, *Rep. Prog. Phys.* **81**, 106301 (2018).
- [11] N. Schunck and L. M. Robledo, Microscopic theory of nuclear fission: a review, *Rep. Prog. Phys.* **79**, 116301 (2016).
- [12] M. Thoennessen and G. F. Bertsch, Threshold for Dissipative Fission, *Phys. Rev. Lett.* **71**, 4303 (1993).
- [13] P. Paul and M. Thoennessen, Fission time scales from giant dipole resonances, *Annu. Rev. Nucl. Part. Sci.* **44**, 65 (1994).
- [14] P. Fröbrich, I. I. Gontchar, and N. D. Mavlitov, Langevin fluctuation-dissipation dynamics of hot nuclei: Prescission neutron multiplicities and fission probabilities, *Nucl. Phys. A* **556**, 281 (1993).
- [15] Y. Zhu and J. C. Pei, Thermal fission rates with temperature dependent fission barriers, *Phys. Rev. C* **94**, 024329 (2016).
- [16] J. Zhao, T. Nikšić, D. Vretenar, and S. G. Zhou, Microscopic self-consistent description of induced fission dynamics: Finite-temperature effects, *Phys. Rev. C* **99**, 014618 (2019).
- [17] D. E. Ward, B. G. Carlsson, T. Døssing, P. Möller, J. Randrup, and S. Åberg, Nuclear shape evolution based on microscopic level densities, *Phys. Rev. C* **95**, 024618 (2017).
- [18] U. Brosa, S. Grossmann, and A. Müller, Nuclear scission, *Phys. Rep.* **197**, 167 (1990).
- [19] G. Scamps and C. Simenel, Impact of pear-shaped fission fragments on mass-asymmetric fission in actinides, *Nature (London)* **564**, 382 (2018).
- [20] D. Regnier, N. Dubray, N. Schunck, and M. Verriere, Fission fragment charge and mass distributions in  $^{239}\text{Pu}(n, f)$  in the adiabatic nuclear energy density functional theory, *Phys. Rev. C* **93**, 054611 (2016).
- [21] K. Sekimoto, Langevin equation and thermodynamics, *Prog. Theor. Phys. Suppl.* **130**, 17 (1998).
- [22] J. Randrup and P. Möller, Energy dependence of fission-fragment mass distributions from strongly damped shape evolution, *Phys. Rev. C* **88**, 064606 (2013).
- [23] L. L. Liu, X. Z. Wu, Y. J. Chen, C. W. Shen, Z. X. Li, and Z. G. Ge, Study of fission dynamics with a three-dimensional Langevin approach, *Phys. Rev. C* **99**, 044614 (2019).
- [24] S. E. Koonin and J. R. Nix, Microscopic calculation of nuclear dissipation, *Phys. Rev. C* **13**, 209 (1976).
- [25] J. W. Negele, S. E. Koonin, P. Möller, J. R. Nix, and A. J. Sierk, Dynamics of induced fission, *Phys. Rev. C* **17**, 1098 (1978).
- [26] T. Nakatsukasa, K. Matsuyanagi, M. Matsuo, and K. Yabana, Time-dependent density-functional description of nuclear dynamics, *Rev. Mod. Phys.* **88**, 045004 (2016).
- [27] C. Simenel and A. S. Umar, Heavy-ions collisions and fission dynamics with the time-dependent Hartree-Fock theory and its extensions, *Prog. Part. Nucl. Phys.* **103**, 19 (2018).
- [28] A. Bulgac, P. Magierski, K. J. Roche, and I. Stetcu, Induced Fission of  $^{240}\text{Pu}$  within a Real-Time Microscopic Framework, *Phys. Rev. Lett.* **116**, 122504 (2016).
- [29] A. Bulgac, S. Jin, K. J. Roche, N. Schunck, and I. Stetcu, Fission dynamics of  $^{240}\text{Pu}$  from saddle to scission and beyond, *Phys. Rev. C* **100**, 034615 (2019).
- [30] G. Scamps, C. Simenel, and D. Lacroix, Superfluid dynamics of  $^{258}\text{Fm}$  fission, *Phys. Rev. C* **92**, 011602(R) (2015).
- [31] D. Lacroix and S. Ayik, Stochastic quantum dynamics beyond mean field, *Eur. Phys. J. A* **50**, 95 (2014).
- [32] S. Ayik, A stochastic mean-field approach for nuclear dynamics, *Phys. Lett. B* **658**, 174 (2008).
- [33] A. Bulgac, S. Jin, and I. Stetcu, Unitary evolution with fluctuations and dissipation, *Phys. Rev. C* **100**, 014615 (2019).
- [34] R. Balian and M. Vénéroni, Fluctuations in a time-dependent mean-field approach, *Phys. Lett. B* **136**, 301 (1984).
- [35] K. Godbey, C. Simenel, and A. S. Umar, Microscopic predictions for the production of neutron-rich nuclei in the reaction  $^{176}\text{Yb} + ^{176}\text{Yb}$ , *Phys. Rev. C* **101**, 034602 (2020).
- [36] S. Ebata, T. Nakatsukasa, T. Inakura, K. Yoshida, Y. Hashimoto, and K. Yabana, Canonical-basis time-dependent Hartree-Fock-Bogoliubov theory and linear-response calculations, *Phys. Rev. C* **82**, 034306 (2010).
- [37] G. Scamps, D. Lacroix, G. F. Bertsch, and K. Washiyama, Pairing dynamics in particle transport, *Phys. Rev. C* **85**, 034328 (2012).
- [38] A. L. Goodman, Finite-temperature HFB theory, *Nucl. Phys. A* **352**, 30 (1981).
- [39] C. Y. Wong and H. H. K. Tang, Dynamics of nuclear fluid. V. Extended time-dependent Hartree-Fock approximation illuminates the approach to thermal equilibrium, *Phys. Rev. C* **20**, 1419 (1979).
- [40] J. Sadhukhan, W. Nazarewicz, and N. Schunck, Microscopic modeling of mass and charge distributions in the spontaneous fission of  $^{240}\text{Pu}$ , *Phys. Rev. C* **93**, 011304(R) (2016).
- [41] J. A. Maruhn, P.-G. Reinhard, P. D. Stevenson, and A. S. Umar, The TDHF code Sky3D, *Comput. Phys. Commun.* **185**, 2195 (2014).
- [42] B. Schuetrumpf, P.-G. Reinhard, P. D. Stevenson, A. S. Umar, and J. A. Maruhn, The TDHF code Sky3D version 1.1, *Comput. Phys. Commun.* **229**, 211 (2018).
- [43] P.-G. Reinhard, B. Schuetrumpf, and J. A. Maruhn, The Axial Hartree-Fock + BCS Code SkyAx, *Comput. Phys. Commun.* **258**, 107603 (2020).
- [44] M. Pancic, Y. Qiang, J. C. Pei, and P. Stevenson, Shape evolutions in fission dynamics within time-dependent Hartree-Fock approach, *Front. Phys.* **8**, 351 (2020).
- [45] M. Bender, K. Rutz, P.-G. Reinhard, and J. A. Maruhn, Pairing gaps from nuclear mean-field models, *Eur. Phys. J. A* **8**, 59 (2000).
- [46] J. Bartel, P. Quentin, M. Brack, C. Guet, and H. B. Håkansson, Towards a better parametrisation of Skyrme-like effective forces: A critical study of the SkM force, *Nucl. Phys. A* **386**, 79 (1982).

- [47] J. Dobaczewski, W. Nazarewicz, and M. V. Stoitsov, Nuclear ground-state properties from mean-field calculations, *Eur. Phys. J. A* **15**, 21 (2002).
- [48] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevC.103.L031304> for detailed theoretical methods and fission observables of individual events obtained from TD-BCS calculations.
- [49] M. Bender, K. Rutz, P.-G. Reinhard, J. A. Maruhn, and W. Greiner, Potential energy surfaces of superheavy nuclei, *Phys. Rev. C* **58**, 2126 (1998).
- [50] C. Simenel, K. Godbey, and A. S. Umar, Timescales of Quantum Equilibration, Dissipation and Fluctuation in Nuclear Collisions, *Phys. Rev. Lett.* **124**, 212504 (2020).
- [51] P. H. Chen, Z. Q. Feng, J. Q. Li, and H. F. Zhang, A statistical approach to describe highly excited heavy and superheavy nuclei, *Chin. Phys. C* **40**, 091002 (2016).
- [52] E. Khan, N. Van Giai, and N. Sandulescu, Pairing interactions and vanishing pairing correlations in hot nuclei, *Nucl. Phys. A* **789**, 94 (2007).
- [53] P. Goddard, P. Stevenson, and A. Rios, Fission dynamics within time-dependent Hartree-Fock: Deformation-induced fission, *Phys. Rev. C* **92**, 054610 (2015).
- [54] D. J. Dean, K. Langanke, H. Nam, and W. Nazarewicz, Pairing Reentrance Phenomenon in Heated Rotating Nuclei in the Shell-Model Monte Carlo Approach, *Phys. Rev. Lett.* **105**, 212504 (2010).
- [55] U. Brosa, H. H. Knitter, T. S. Fan, J. M. Hu, and S. L. Bao, Systematics of fission-channel probabilities, *Phys. Rev. C* **59**, 767 (1999).
- [56] K. Meierbachtol, F. Tovesson, D. L. Duke, V. Geppert-Kleinrath, B. Manning, R. Meharchand, S. Mosby, and D. Shields, Total kinetic energy release in  $^{239}\text{Pu}(n, f)$  post-neutron emission from 0.5 to 50 MeV incident neutron energy, *Phys. Rev. C* **94**, 034611 (2016).
- [57] M. Albertsson, B. G. Carlsson, T. Døssing, P. Möller, J. Randrup, and S. Åberg, Excitation energy partition in fission, *Phys. Lett. B* **803**, 135276 (2020).