Structure of 46,47 Ca from the β^- decay of 46,47 K in the framework of the nuclear shell model

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In the present work, we report a comprehensive theoretical study of the log ft values for the allowed and forbidden β^- decay transitions of ⁴⁶K and ⁴⁷K corresponding to recently available experimental data from the GRIFFIN spectrometer at TRIUMF-ISAC [Phys. Rev. C **100**, 054327 (2019); **102**, 054314 (2020)]. We perform the nuclear shell-model calculation in sdpf-valence space, with the SDPF-MU interaction, to calculate low-lying energy spectra of ^{46,47}K and ^{46,47}Ca. For further investigation, we also calculate spectroscopic properties of ^{46,47}K and ^{46,47}Ca and compare the results with the experimental data. We suggest the spin-parity of several levels, which was previously tentative, in both the calcium isotopes. Based on the energy and log ft values, we conclude that the state at 3.984 MeV in ⁴⁶Ca could be either 3⁻ or 2⁺ and a state at 4.432 MeV might be 3⁻. The spin-parity of the states at 2.875, 3.951, and 4.453 MeV are predicted to be $1/2^-$, $3/2^-$, and $1/2^-$ or $1/2^+$, respectively, in ⁴⁷Ca. We also give the confirmation to the spin-parity of 2.850, 3.889, and 4.606 MeV states for ⁴⁷Ca. Our results of level schemes of ^{46,47}K are in reasonable agreement with the experimental data, while the agreement of calculated log ft values for the β^- decay with the experimental data is limited.

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I. INTRODUCTION

Understanding the formation of shell structure across an isotopic chain (from proton drip line to neutron drip line) is a key challenge in nuclear physics. New experiments have revealed the appearance of new shell closures N = 16, 32, 34 [1–8] and the disappearance of the magic numbers N = 8, 20, 28 [9–11]. The evolution of the shell structure in calcium isotopes has been a crucial area of investigation in nuclear structure over the past few decades and is still in progress from both experimental and theoretical perspectives. Accurate experimental data for level energies, spins, and parities is of utmost importance to obtain complete spectroscopic information of the calcium isotopes apart from helping us to determine the nature of interactions among the nucleons therein and set a benchmark for our theoretical calculations.

The study of β decay is a very important tool to determine the structure of atomic nuclei. In β decay, transitions are classified into two categories [12]: allowed and forbidden, based on the value of orbital angular momentum l of the emitted leptons. Transitions with l = 0 correspond to allowed and those with l > 0 to forbidden transitions. Allowed transitions are characterized by a change in total angular momentum $\Delta J =$ 0, 1 and no change in parity ($\Delta \pi = +1$). Forbidden β decays are further classified into forbidden unique (FU) and forbidden nonunique (FNU) transitions. For the *K*th-FU transition, $\Delta J = K + 1$, while $\Delta J \leq K$ for the *K*th-FNU transition and $\Delta \pi = (-1)^{K}$ in both the cases. For both allowed and forbidden transitions, log *ft* values, shape factors, and electron spectra have been calculated with the effective value of axialvector coupling constant g_A , obtained corresponding to their mass region, earlier in β -decay studies in Refs. [13–18]. Study of second-FNU β^- decay of ²⁴Na(4⁺) \rightarrow ²⁴Mg(2⁺) and ³⁶Cl(2⁺) \rightarrow ³⁶Ar(0⁺) has been reported recently in Ref. [19].

Several experiments have been performed to investigate the excited states of ^{46,47}Ca, of which some are nuclearreaction-based experiments [20–24] while others are β -decay measurements [25–29]. Although several excited states have been identified in these experiments, experimental assignments of spin-parity to all the states could not be made. In some instances, tentative assignments are given and in others, no assignment could be made.

Recently, an experiment has been carried out at TRIUMF in which high-statistic data from the β^- decay of the ground state (g.s.) $J^{\pi} = 2^-$ of ⁴⁶K into ⁴⁶Ca has been measured with the GRIFFIN spectrometer [30], where 42 excited states were populated and β -feeding branching ratios into excited states of ⁴⁶Ca were also observed. From analysis of these data, it was possible to assign the spin-parity of excited states. From the same experiment, the β^- decay of the g.s. $J^{\pi} = 1/2^+$ of ⁴⁷K into ⁴⁷Ca was studied in which the spin-parity of eight excited states were assigned along with the precise measurement of the half-life of ⁴⁷K [31]. These experiments measure simultaneously the probability of electromagnetic transitions among the states of a nucleus and β -decay feeding of these states from neighboring nuclei. Studying them together is a real stringent test for the nuclear shell model.

The study of nuclear structures up to Z = 20 and beyond using first principles or *ab initio* approaches has gained momentum over the past few years [32–38]. In Ref. [39], a coupled-cluster (CC) method with two-nucleon (*NN*) and

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three-nucleon (3N) interaction from chiral effective-field theory (EFT) [40-43] has been used to treat the many-body system of calcium isotopes. Their results [39] confirm a shell closure in ⁴⁸Ca, a subshell closure in ⁵²Ca, and a weak subshell closure in 54 Ca. It has been shown that 3N forces play an important role in explaining the magic number N = 28 in calcium isotopes [44]. In Ref. [45], Holt et al. calculated the energy spectra of neutron-rich calcium isotopes using manybody perturbation theory (MBPT) with NN and NN + 3Nforces for pf and $pfg_{9/2}$ valence spaces. They also performed shell-model calculations using the phenomenological pf-shell interactions such as GXPF1A [46] and KB3G [47] and compared results with the experimental data. For ⁴⁶Ca, their results are in good agreement with the experimental data; however, 4^+ and 6^+ states are ≈ 1 MeV higher for the NN + 3N interaction in the $pfg_{9/2}$ model space than the experimental values. A significant spread in the spectra was obtained, indicating the need to incorporate cross-shell degrees of freedom. Furthermore, they are unable to reproduce negative-parity states and the 0^+_2 state, which was expected to be dominated by the *sd* shell. Thus, the *sd pf*-model space is crucial for the study of these states. For ⁴⁷Ca, they concluded that the pf-valence space gives compressed spectra and the best results are obtained with NN + 3N forces in $pfg_{9/2}$ space. This establishes that the extended space $pfg_{9/2}$ with 3N forces improves the energy spectra.

In Ref. [30], the authors extended the work of Holt *et al.* wherein they have used a nonstandard valence space for ⁴⁶Ca in which protons occupy $s_{1/2}d_{3/2}f_{7/2}p_{3/2}$ orbitals and neutrons occupy $s_{1/2}d_{3/2}f_{7/2}p_{3/2}p_{1/2}$ orbitals above a ²⁸Si core. They reproduced correctly the 0⁺₂ state and also the negative-parity states but obtained a significantly compressed spectra, and their results show that proton excitations from the *sd* shell are dominant. These calculations reveal that the protons are no longer inactive despite having a robust shell closure with Z = 20.

Other *ab initio* methods such as the in-medium similarity renormalization group (IM-SRG) targeted for a particular nucleus [48] and the self-consistent Green's function (SCGF) [49] theory have also been applied to study the calcium isotopes. Bhoy *et al.* have used the shell model with the GXPF1Br + V_{MU} interaction [50] for calculating energy spectra of ^{47–58}Ca [51] where they have used *pf*, *pf* g_{9/2}, and *pf* g_{9/2}d_{5/2} model spaces to show the dependence of states on the inclusion of the higher orbitals.

The nuclear charge radius is an important observable to describe the shell evolution in nuclei. An experiment at ISOLDE-CERN based on laser spectroscopy has been performed to measure the charge radius of ⁵²Ca [52], which was found to be much larger than expected for a doubly magic nucleus. From *ab initio* CC theory [52], these results are well reproduced. This reflects a breaking of magicity at N = 32 in calcium isotopes. A recent shell-model study [53] for calcium isotopes was reported to find the location of the drip line of calcium isotopes and showed that the calcium isotope chain is bound up to ⁷⁰Ca.

In the present work we calculated the log ft values for the allowed and forbidden β^- decay of 46 K and 47 K, corresponding to the available experimental data of the TRIUMF experiment [30,31] and using the shell model with the *sd pf*-model space. For these calculations, we also extracted the effective value of g_A by using the chi-squared fitting method. We also studied the energy spectra, quadrupole moment, magnetic moment, and transition strengths of ^{46,47}K and ^{46,47}Ca isotopes. A comparison of our theoretically predicted results with the experimental results is also presented. Wave functions of various states in both calcium isotopes have also been studied to determine the contribution from each configuration and to deduce the role of the *sd*-model space.

Our work is the first theoretical description of energy spectra of 47 Ca corresponding to recently available experimental data [31], which refined our knowledge regarding the level scheme of 47 Ca. This study is the first shell-model calculation of the log *ft* values for allowed and forbidden β^- decay of 46,47 K [30,31].

This paper is organized as follows: In Sec. II, we explain the shell-model Hamiltonian with the adopted model space and theoretical formalism for allowed and forbidden nuclear β decay. Also, we extract the effective value of g_A by using the chi-squared fitting method for β -decay study. In Sec. III, we present theoretically calculated level structures and the spectroscopic properties of ^{46,47}K and ^{46,47}Ca. Also, we report the log *ft* results of the β^- decay of ⁴⁶K and ⁴⁷K. In Sec. IV, conclusions are drawn.

II. FORMALISM

A. Shell-model Hamiltonian

The nuclear shell-model Hamiltonian contains a singleparticle energy and a two-nucleon-interaction terms. The shell-model Hamiltonian can be written as

$$H = T + V = \sum_{\alpha} \epsilon_{\alpha} c_{\alpha}^{\dagger} c_{\alpha} + \frac{1}{4} \sum_{\alpha\beta\gamma\delta} v_{\alpha\beta\gamma\delta} c_{\alpha}^{\dagger} c_{\beta}^{\dagger} c_{\delta} c_{\gamma}, \quad (1)$$

where $\alpha = \{n, l, j, t\}$ is a single-particle state and the corresponding single-particle energy is ϵ_{α} , c_{α}^{\dagger} and c_{α} are the creation and annihilation operators, and $v_{\alpha\beta\gamma\delta} = \langle \alpha\beta | V | \gamma\delta \rangle$ are the antisymmetrized two-body matrix elements.

We have used the nuclear shell model to determine the nuclear structure properties of ^{46,47}K and ^{46,47}Ca. It has been found that including cross-shell excitations in the valence space is necessary to correctly reproduce the energy spectra of ^{46,47}K and ^{46,47}Ca [30,45]. We have thus used a phenomenological SDPF-MU interaction [54] for *sdpf*-model space in the shell-model calculations with ¹⁶O as an inert core. In this interaction, there are seven orbitals ($d_{5/2}$, $s_{1/2}$, $d_{3/2}$, $f_{7/2}$, $p_{3/2}$, $f_{5/2}$, and $p_{1/2}$) corresponding to two major shells, available for the valence nucleons to occupy. This allows us to calculate both the positive- and negative-parity states of ^{46,47}K and ^{46,47}Ca. For unnatural-parity states, we have allowed either one proton or one neutron excitation from the *sd* shell to the *pf* shell, known as the 1p-1h excitation.

B. β -decay theory for allowed and forbidden transitions

A detailed theoretical formalism of nuclear β decay has been presented in Refs. [55,56]. A relatively simple approach in describing β decay involves the impulse approximation, according to which the decaying nucleon experiences just the weak interaction at the moment of decay and does not interact strongly with the remaining A - 1 nucleons. As such, the A - 1 nucleons are referred to as spectator nucleons with respect to the weak interaction. In the initial and final nuclear many-body states, however, the active nucleon does participate in strong interactions [12]. The nuclear β^- decay process is described with an effective point-like interaction vertex with an effective coupling constant G_F , known as the Fermi coupling constant. The probability of the emitted electron for the β^- decay process to lie in an energy range W_e to $W_e + dW_e$ is given by

$$P(W_e)dW_e = \frac{G_F^2}{(\hbar c)^6} \frac{1}{2\pi^3 \hbar} C(W_e) p_e c W_e (W_0 - W_e)^2 \times F_0(Z, W_e) dW_e,$$
(2)

where W_0 is the endpoint energy of the β spectrum which corresponds to the maximum energy taken by the electron in a transition, the factor $F_0(Z, W_e)$ is the Fermi function, and Z is the proton number of the daughter nucleus. The p_e and W_e are the momentum and energy of the emitted electron, respectively, and $C(W_e)$ is the shape factor that contains information about the nuclear structure. The partial half-life of the decay process is related to the transition probability as

$$t_{1/2} = \frac{\ln(2)}{\int_{m_e c^2}^{W_0} P(W_e) dW_e},$$
(3)

where m_e is the rest mass of the electron and the integral in the denominator is called the decay rate or transition probability per unit time. To simplify this integration, we introduce the dimensionless quantities $w_0 = W_0/m_ec^2$, $w_e = W_e/m_ec^2$, and $p = p_ec/m_ec^2 = (w_e^2 - 1)^{1/2}$, which are kinematical quantities divided by the electron rest mass. Now, the partial half-life is related to shape function as

$$ft_{1/2} = \kappa, \tag{4}$$

where *f* is the dimensionless integrated shape function, and the value of the constant κ [57] is

$$\kappa = \frac{2\pi^3 \hbar' \ln(2)}{m_e^5 c^4 (G_{\rm F} \cos\theta_{\rm C})^2} = 6289 \,\text{s},\tag{5}$$

where $\theta_{\rm C}$ is the Cabibbo angle.

The dimensionless integrated shape function f can be written as

$$f = \int_{1}^{w_0} C(w_e) p w_e (w_0 - w_e)^2 F_0(Z, w_e) dw_e.$$
(6)

For the allowed (Gamow-Teller) transition, the shape factor $C(w_e)$ can be expressed as

$$C(w_e) = B(GT) = \frac{g_A^2}{2J_i + 1} |\mathcal{M}_{GT}|^2,$$
(7)

where \mathcal{M}_{GT} is the Gamow-Teller nuclear matrix element (NME) of $\sigma \tau$ and B(GT) is the reduced transition probability (details of which can be found in Ref. [12]), g_A is the axial-vector coupling constant, and J_i is the angular momentum of the initial state. For such a transition, the reduced half-life is

calculated by multiplying the half-life with the phase-space factor (Fermi integral) given by

$$f_0 = \int_1^{w_0} p w_e (w_0 - w_e)^2 F_0(Z, w_e) dw_e.$$
(8)

We then take the logarithm of the *ft value*, also known as the reduced half-life or comparative half-life, as the *ft value* is generally a large quantity:

$$\log ft \equiv \log(f_0 t_{1/2} s).$$

The shape factor $C(w_e)$ for the forbidden transition has the form of

$$C(w_{e}) = \sum_{k_{e},k_{v},K} \lambda_{k_{e}} \bigg[M_{K}(k_{e},k_{v})^{2} + m_{K}(k_{e},k_{v})^{2} - \frac{2\gamma_{k_{e}}}{k_{e}w_{e}} M_{K}(k_{e},k_{v})m_{K}(k_{e},k_{v}) \bigg],$$
(9)

where k_e and k_v (=1, 2, 3, ...) are related to the partial-wave expansion of the leptonic wave functions, and *K* is the order of forbiddenness of the transition. The entities $M_K(k_e, k_v)$ and $m_K(k_e, k_v)$ are written in terms of the NME and leptonic phase-space factors [14,55]. The quantities

$$\gamma_{k_e} = \sqrt{k_e^2 - (\alpha Z)^2}$$
 and $\lambda_{k_e} = F_{k_e-1}(Z, w_e)/F_0(Z, w_e),$

where λ_{k_e} is the Coulomb function, in which $F_{k_e-1}(Z, w_e)$ is the generalized Fermi function [14,15]. The log *ft* values for forbidden transitions are calculated in a similar manner as that in the case of allowed transitions by using the phasespace factor corresponding to the concerned transitions (more details can be found in Ref. [55]). The NME contain all the information about nuclear-structure and can be expressed as

$$= \frac{\sqrt{4\pi}}{\hat{J}_i} \sum_{pn}^{V/A} m_{KLS}^{(N)}(pn)(k_e, m, n, \rho)$$

$$= \frac{\sqrt{4\pi}}{\hat{J}_i} \sum_{pn}^{V/A} m_{KLS}^{(N)}(pn)(k_e, m, n, \rho)(\Psi_f || [c_p^{\dagger} \tilde{c}_n]_K || \Psi_i),$$

$$(10)$$

where the summation in Eq. (10) runs over the proton (p)and neutron (n) single-particle states with $\hat{J}_i = \sqrt{2J_i + 1}$. The quantity *m* is the total power of $(m_e R/\hbar)$, $(W_e R/\hbar)$, and αZ ; *n* is the total power of $(W_e R/\hbar)$ and αZ ; ρ is the power of αZ . The functions ${}^{V/A}m_{KLS}^{(N)}(pn)(k_e, m, n, \rho)$ are the single-particle matrix elements (SPMEs) that do not depend on the nuclear models and $(\Psi_f || [c_p^{\dagger} \tilde{c}_n]_K || \Psi_i)$ are the one-body transition densities (OBTDs) between the initial (Ψ_i) and final (Ψ_f) states. The SPME expressions used in this work are taken from Refs. [14,15] and the OBTDs are computed from the shell-model code NUSHELLX [58].

C. Quenching factor

The bare values of the two coupling constants $g_V = 1.0$ (vector coupling constant) and $g_A = 1.27$ (axial-vector coupling constant) associated with the β -decay theory are determined from conserved vector current (CVC) and partial conserved axial-vector current (PCAC), respectively. In the nuclear shell-model calculations, the renormalizations due to

the truncation of model space and possible meson-exchange current contributions are taken into account by using effective values of the coupling constants. In this paper, we have calculated the quenching factor for g_A . The averaged shape factor [55] is defined as

$$\overline{C(w_e)} = f/f_0. \tag{11}$$

The expressions for f and f_0 are written in Eqs. (6) and (8). For Gamow-Teller transitions, $\overline{C(w_e)}$ is B(GT) and that for first-forbidden transitions is [59,60]

$$\overline{C(w_e)}(fm^2) = \frac{6289\lambda_{Ce}^2}{ft} = \frac{9378 \times 10^5}{ft},$$
 (12)

where, λ_{Ce} is the reduced Compton wavelength of electron. For first-forbidden β decays, there are six operators for NME, given by

$$O(0^{-}) : g_{A}(\boldsymbol{\sigma} \cdot \boldsymbol{p}_{e}), \ g_{A}(\boldsymbol{\sigma} \cdot \boldsymbol{r}),$$

$$O(1^{-}) : g_{V}\boldsymbol{p}_{e}, \ g_{A}(\boldsymbol{\sigma} \times \boldsymbol{r}), \ g_{V}\boldsymbol{r},$$

$$O(2^{-}) : g_{A}[\boldsymbol{\sigma}\boldsymbol{r}]_{2},$$
(13)

where \mathbf{r} and \mathbf{p}_e are the radial coordinate and electron momentum, respectively. The operators $O(0^-)$, $O(1^-)$, and $O(2^-)$ correspond to the $\Delta J = 0$, 1, and 2 transitions, respectively. The operator $\boldsymbol{\sigma} \cdot \mathbf{p}_e$ is the axial-charge nuclear matrix element γ_5 . For first-forbidden nonunique $J^+ \leftrightarrow J^-$ transitions, γ_5 NME is enhanced due to nuclear-medium effects in the form of meson-exchange currents. This enhancement factor in γ_5 is represented by ϵ_{MEC} , which is defined as the ratio of the axial-charge matrix element to its impulse-approximation value. The one-body impulse NME $M_0^T = \langle J_f || - g_A \frac{1}{M} \vec{\sigma} \cdot \vec{p}_e t_- || J_i \rangle$, where M is the nucleon mass and $t_- |n\rangle = |p\rangle$, is multiplied by an effective coupling constant ϵ_{MEC} to take into account the contributions from the meson-exchange currents [61,62]. We have taken the value of ϵ_{MEC} to be 1.6, which is consistent with Refs. [59,63].

In Table I, we have shown theoretical and experimental log ft values and averaged shape factors corresponding to transitions ${}^{46}\text{K} \rightarrow {}^{46}\text{Ca}$ and ${}^{47}\text{K} \rightarrow {}^{47}\text{Ca}$. These calculations are done by using free coupling constants (quenching factor q = 1.0). We have also included mesonic enhancement factor $\epsilon_{\text{MEC}} = 1.6$ for the matrix element M_0^T in 0^- transitions. In the present calculations, we have also included next-to-leading-order terms of the β -decay shape function, similar to Refs. [13,14]. In Fig. 1, theoretical and experimental $\overline{C(w_e)}^{1/2}$ values are plotted. We have extracted the effective value of $g_A = q \times g_A^{\text{free}} = 0.72$ corresponding to quenching factor q = 0.57 from the chi-squared fitting method.

III. RESULTS AND DISCUSSION

We have performed shell-model calculations to study nuclear structures of 46,47 K and 46,47 Ca in the *sd pf*-model space. Low-lying energy spectra of 46 K and 46 Ca obtained from the shell model are compared with the experimental data in Fig. 2. The experimental spin-parity of the g.s. is tentative for 46 K. Our theoretical calculations predict the g.s. as 2^- . The g.s. of 46 K has the configuration of $\pi(d_{5/2}^{6}s_{1/2}^2d_{3/2}^3) \otimes$

TABLE I. Comparison of computed log ft values and average shape factors for Gamow-Teller and first-forbidden transitions with experimental data [30,31]. Only confirmed transitions for ${}^{46}\text{K} \rightarrow {}^{46}\text{Ca}$ and ${}^{47}\text{K} \rightarrow {}^{47}\text{Ca}$ are presented. Calculated values are obtained by using the quenching factor q = 1.00 and enhancement factor $\epsilon_{\text{MEC}} = 1.6$ for 0^- transitions.

Transition		$\log ft$		$\overline{[C(w)]}$	$\overline{[C(w_e)]}^{1/2}$	
Initial	Final	Expt.	Theory	Expt.	Theory	
$^{46}K(2^{-})$	${}^{46}\text{Ca}(2^+_1)$	6.92	6.439	10.62	18.47	
	${}^{46}Ca(0_2^+)$	10.27	9.525	0.22	0.53	
	${}^{46}\text{Ca}(4^+_1)$	9.70	7.405	0.43	6.075	
	${}^{46}Ca(2_2^+)$	8.01	8.298	3.03	2.17	
	${}^{46}Ca(3_1^-)$	8.04	5.755	0.0076	0.105	
	${}^{46}Ca(2_3^+)$	8.13	6.879	2.64	11.135	
	${}^{46}Ca(4_2^+)$	>11.5	8.868	0.054	1.13	
47 K(1/2 ⁺)	$^{47}Ca(3/2_1^-)$	>6.5	7.831	17.22	3.72	
	$^{47}Ca(3/2_1^+)$	5.457	5.690	0.1482	0.11	
	$^{47}Ca(1/2_1^+)$	4.807	4.386	0.3132	0.51	

 $\nu(d_{5/2}^6 s_{1/2}^2 d_{3/2}^4 f_{7/2}^7)$ with 70.24% probability. In Fig. 3, lowlying energy spectra corresponding to ⁴⁷K and ⁴⁷Ca are shown and also compared with the experimental data. The shellmodel calculations with the SDPF-MU interaction correctly reproduce the g.s. spin-parity for ⁴⁷K. The g.s. configuration of ⁴⁷K is $\pi(d_{5/2}^6 s_{1/2}^1 d_{3/2}^4) \otimes \nu(d_{5/2}^6 s_{1/2}^2 d_{3/2}^4 f_{7/2}^8)$ with probability of 71.21%. The calculated energy spectra of ⁴⁷K is in good agreement with the experimental one.

We have computed electromagnetic transition strengths B(E2) for transitions from excited states to the g.s. in 46,47 K



FIG. 1. Comparison of calculated and experimental average shape factors for Gamow-Teller and first-forbidden transitions to obtain the quenching factor. For extraction of the quenching factor, we have used only confirmed transitions of ^{46,47}Ca.



FIG. 2. Comparison of theoretical and experimental energy spectra of ⁴⁶K and ⁴⁶Ca. Experimental data are taken from Refs. [31,64].

and 46,47 Ca, which are shown in Table II. In case of 46 Ca, B(E2) value for $2^+_1 \rightarrow 0^+_1$ transition is 0.4 W.u., while the experimental value is 3.63 W.u., which is quite far from theory, but $B(E2 \ 3/2^-_1 \rightarrow 7/2^-_1)$ in 47 Ca is 0.2 W.u., which agrees with the experimental value (<0.28 W.u.). We have also predicted experimentally unknown transition strength $B(E2; 3/2^-_2 \rightarrow 7/2^-_1)$ for 47 Ca. In Table III, we have reported quadrupole and magnetic

In Table III, we have reported quadrupole and magnetic moments obtained from the shell model with the SDPF-MU interaction for selected states of 46,47 K and 46,47 Ca.

We have then compared these values with the experimental ones [64,65] and found that the magnetic moments of 2^+ , $1/2^+$, and $7/2^-$ states are consistent with experimental values for ⁴⁶Ca, ⁴⁷K, and ⁴⁷Ca, respectively, for $g_s^{\text{eff}} = 0.85g_s^{\text{free}}$. Also, we obtain the magnetic moment of the g.s. 2^- for ⁴⁶K to be -0.478(-0.585) for $g_s^{\text{eff}} = 0.85(0.7)g_s^{\text{free}}$. As the quenching factor for g_s is found to be 0.9 in the fp shell for the GXPF1 interaction [66] and 0.92–0.93 in the sd-shell for the USDB interaction [67], the value of 0.85 is a reasonable one for SDPF-MU. We have predicted quadrupole and magnetic



FIG. 3. Comparison of theoretical and experimental energy spectra of 46 K and 46 Ca. Experimental data are taken from Refs. [31,64].

TABLE II. Comparison of theoretical and experimental reduced electric-quadrupole transition probabilities from excited states to the g.s. in 46,47 K and 46,47 Ca. Effective charges are taken as $e_p = 1.35e$ and $e_n = 0.35e$. Experimental values are taken from Refs. [64,65].

		B(E2) (W.u.)		
Nucleus	Transition	Expt.	SDPF-MU	
⁴⁶ K	$4^1 ightarrow 2^1$	NA	2.70	
⁴⁶ Ca	$2^+_1 \rightarrow 0^+_1$	3.63	0.40	
⁴⁷ K	$5/2^+_1 \to 1/2^+_1$	NA	2.5	
⁴⁷ Ca	$3/2^1 \to 7/2^1$	< 0.28	0.2	
	$3/2_2^- \rightarrow 7/2_1^-$	NA	0.30	

moments for several states of ^{46,47}Ca from the shell-model which are experimentally not yet measured.

So, our energy spectra and magnetic moments corresponding to the adopted interaction are in a reasonable agreement with the experimental data. Thus, the SDPF-MU interaction is a suitable interaction for calculating nuclear properties of these nuclei. It means that we can use the wave functions, obtained from the SDPF-MU interaction, to compute the NME needed for the log ft calculations.

In Table IV, we have presented the calculated log ft values for β^- decay from 2^- of 46 K to various excited states of 46 Ca. There are two possible spin-parities: 2^+_4 and 3^-_2 , corresponding to the state at 3984.07(16) keV. Accordingly, the spin-parity and log ft values of the subsequent states are determined. For instance, if the state at 3984.07(16) keV is 2^+_4 , then the spin-parity and log ft value of the state at 4385.91(15) keV are 2^+_5 and 9.132, respectively. On the other hand, if the state at 3984.07(16) keV is considered to be 3^-_2 , then, the 4385.91(15) keV state would be 2^+_4 with a log ft value of 9.137. We have also listed the experimentally obtained spin-parity J^+_{π} , excitation energy, branching ratio,

TABLE III. Comparison of theoretical and experimental quadrupole and magnetic moments of selected states for 46,47 K and 46,47 Ca. The effective charges are taken as $e_p = 1.35e$ and $e_n = 0.35e$. For the magnetic-moment calculations, two sets of g_s^{eff} are employed: $g_s^{\text{eff}} = 0.7g_s^{\text{free}}$ and $g_s^{\text{eff}} = 0.85g_s^{\text{free}}$, separated by a solidus (/). Experimental data are taken from Refs. [64,65].

			$\mu(\mu_N)$	Q(eb)		
Nuclei	J_f^π	Expt.	SDPF-MU	Expt.	SDPF-MU	
⁴⁶ K	$2^{-}_{g.s.}$	-1.051(6)	-0.585/-0.478	NA	0.061	
⁴⁶ Ca	2_{1}^{+}	-0.52(12)	-0.425/-0.517	NA	-0.043	
	3_{1}^{+}	NA	-1.009/-1.225	NA	0.002	
	4_{1}^{+}	NA	-1.176 /-1.429	NA	-0.015	
⁴⁷ K	$1/2_{g.s.}^+$	1.933(9)	1.583/1.953			
⁴⁷ Ca	$7/2_1^-$	-1.38(3)	-1.026/-1.246	0.021(4)	0.051	
	$5/2_{1}^{-}$	NA	-0.734/-0.892	NA	-0.014	
	$3/2_1^-$	NA	-1.060/-1.287	NA	-0.026	

and log ft values of final states. Furthermore, we have also presented the corresponding modes of decay. Transition from initial state to final state could be either allowed or FU, or FNU based on the selection rules of β decay.

In computing log ft, we have used the effective value of $g_A = 0.72$. Experimental values are used for the β -decay (ground state to ground state) Q values for ⁴⁶K and ⁴⁷K as well as for the excitation energies in ⁴⁶Ca and ⁴⁷Ca for the evaluations of the log ft values. The Q values of 7.716 and 6.632 MeV are used for ⁴⁶K and ⁴⁷K, respectively. The g.s. spin-parity of ⁴⁶Ca is well reproduced with the

SDPF-MU interaction. The energy difference between experimental and theoretical 2^+_1 is 0.513 MeV, as can be seen in Fig. 2(b), and the calculated log ft value is 6.862, which is very close to the experimental value of 6.92(4). Transition from 2^- of 46 K to 0^+_2 of 46 Ca is of the first FU type for which calculated log ft value is 10.017, which agrees well with the experimental value of 10.27(2). The difference between the theoretically and experimentally obtained energies of 3_1^- is 0.022 MeV, which is very small. Spin-parity corresponding to the state with energy 3.984 MeV is unconfirmed. For this state, experimentally, it is found that the spin-parity based on the log ft value is constrained to be either 2^+ or 3^+ , or 3⁻. If we assume this state to be 2^+ , then the log ft value corresponding to the β^- decay to this state is 9.080. By assuming this state to be 3^+ , we obtain log ft = 10.457. If the allowed transition is assumed, then this state would be 3^{-} along with a log ft value of 6.009. The energy difference between calculated and experimental value for this state is 47 keV, as shown in Fig. 2(b). Thus, shell-model calculations with the SDPF-MU interaction establish this state to be either 3^- or 2^+ . The spin-parity of the state at 4.432 MeV is likewise unconfirmed from experiments. So, we have taken all possibilities into account and calculated the corresponding log ft values. Theoretically, we predict this state to be 3^- on the basis of the log *ft* value.

In Table V, we have reported calculated $\log ft$ results for the allowed, FU, and FNU β^- decay from $1/2^+$ of 47 K to various excited states of 47 Ca. The $7/2^-$ state is the g.s. of ⁴⁷Ca which is correctly reproduced with SDPF-MU interaction. The order of experimental $3/2_1^-$ and $3/2_1^+$ states is reversed in theoretical prediction by the shell model, as shown in Fig. 3(b). The calculated log ft for the $3/2^{-}_{2}$ state is 8.201 which is very near to experimental $\log ft$ of 8.46(4) for the $(3/2)^{-}$ state. The experimental $(3/2)^{-}$ state is at 2.850 MeV while the theoretical value of energy for this state is 3.030 MeV, which means that the shell model confirms this state to be $3/2^{-}$. The next unconfirmed state is at 2.875 MeV, which is constrained to be $(1/2^{-}, 3/2^{-})$, experimentally. If this state is considered to be $3/2^-$ then the calculated log ft is 9.846, while for $1/2^-$, log ft is 8.487, which is very close to the experimental log ft, i.e., 8.40(9). Also, the excitation energy for $1/2^{-1}$ is 3.237 MeV which is quite close to the experimental value. So, we predict a state at 2.875 MeV to be $1/2^-$. Experimental first $5/2^-$ with log ft value of 10.28(2) can be assigned as a shell model $5/2_1^-$ state. We also get a confirmation between theory and experiment for a $(5/2)^{-1}$ state at 3.889 MeV. For this state, the calculated $\log ft$ is 10.045, while the experimental value is >10.1.

TABLE IV. Computed log ft values for the allowed, FU, and FNU β^- decay from ${}^{46}K(2^-) \rightarrow {}^{46}Ca(J_f)$. The results are obtained by using the quenching factor of q = 0.57 for g_A . Experimental and theoretically predicted spin-parities are also mentioned. Experimental excitation energies E, β^- branching ratios, and log ft values are taken from Ref. [30].

		E (keV)	Mode of decay		$\log ft$	
J_f^{π} (Expt.)	J_f^{π} (SM)			β^- branching	Expt.	Theory
2+	2_{1}^{+}	1346.00(14)	1st FNU	27.4(21)	6.92(4)	6.862
0^{+}	0_{2}^{+}	2421.98(22)	1st FU	0.38(1)	10.27(2)	10.017
4+	4_{1}^{+}	2574.53(16)	1st FU	1.15(14)	9.70(6)	7.898
2^{+}	2^{+}_{2}	3020.67(14)	1st FNU	0.55(20)	8.01(16)	8.772
3-	3_{1}^{-}	3610.51(15)	Allowed	0.28(14)	8.04(22)	6.248
2^{+}	2_{3}^{+}	3638.38(15)	1st FNU	0.22(2)	8.13(4)	7.370
4+	4_{2}^{+}	3857.51(17)	1st FU	< 0.003	>11.5	9.361
(2+,3)	$2_4^+/3_2^-$	3984.07(16)	1st FNU (2_4^+) /Allowed (3_2^-)	0.47(3)	7.63(3)	9.080/6.009
3+	3_{1}^{+}	4257.26(15)	1st FNU	0.092(9)	8.20(5)	10.512
2^{+}	$2_5^+/2_4^+$	4385.91(15)	1st FNU	4.39(16)	6.44(2)	9.132/9.137
3-	$3^{-}_{2}/3^{-}_{3}$	4404.48(15)	Allowed	5.09(22)	6.37(2)	6.009/6.040
2^{+}	$2_6^+/2_5^+$	4428.02(14)	1st FNU	0.017(14)	8.80(40)	9.941/9.133
$(3, 4^+)$	$3_3^-/3_4^-$	4432.05(16)	Allowed	2.59(7)	6.65(2)	6.040/7.779
2+	$2^+_7/2^+_6$	4487.05(16)	1st FNU	0.46(2)	7.36(2)	9.173/9.947

For a state at 3.951 MeV in 47 Ca, there are two possibilities, see Fig. 3(b). It could be either $3/2^-$ or $5/2^-$. If this state is assumed as $5/2^-$ then there occurs first FU transition and calculated log *ft* is 13.170 which is far from the experimental log *ft* value of 9.3(2). If we consider this state as $3/2^-$, then transition is to be the first FNU type and the calculated log ft value is 9.896, while the experimental value is 7.9(2). The state is more likely to be $3/2^-$. There are four possibilities of spin-parity for a state at 4.453 MeV excitation energy. This could be either $1/2^-$, $1/2^+$, $3/2^-$, or $3/2^+$. The calculated

TABLE V. Computed log ft values for the allowed, FU, and FNU β^- decay from ${}^{47}K(1/2^+) \rightarrow {}^{47}Ca(J_f)$. The results are obtained by using the quenching factor of q = 0.57 for g_A . Experimental and theoretically predicted spin-parities are also mentioned. Experimental excitation energies (E), β^- branching ratios, and log ft values are taken from Ref. [31].

J_f^{π} (Expt.)	J_{f}^{π} (SM)	E (keV)	Mode of decay	β^- branching	$\log ft$	
					Expt.	Theory
3/2-	$3/2_1^-$	2013.4(3)	1st FNU	<2.9	>6.5	7.956
$3/2^+$	$3/2_1^+$	2578.1(3)	Allowed	18.4(3)	5.457(8)	6.183
$1/2^{+}$	$1/2_{1}^{+}$	2599.2(3)	Allowed	80(2)	4.807(9)	4.879
$(3/2)^{-}$	$3/2_{2}^{-}$	2849.9(3)	1st FNU	0.013(1)	8.46(4)	8.201
$(1/2^{-}, 3/2^{-})$	$1/2_{1}^{-}$	2874.7(3)	1st FNU	0.015(3)	8.40(9)	8.487
$5/2^{-}$	$5/2_{1}^{-}$	3266.3(3)	1st FU	0.0038(2)	10.28(2)	8.485
$(5/2^{-})$	$5/2_{2}^{-}$	3889.0(3)	1st FU	< 0.0017	>10.1	10.045
$(3/2^-, 5/2^-)$	$3/2_{3}^{-}$	3951.2(3)	1st FNU	0.010(5)	7.9(2) or 9.3(2)	9.896
(1/2, 3/2)	$1/2_{2}^{-}$	4453.1(4)	1st FNU	0.036(5)	6.99(6)	8.159
	$1/2_{2}^{+}$	4453.1(4)	Allowed	0.036(5)	6.99(6)	5.811
$3/2^+$	$3/2^+_2$	4528.3(3)	Allowed	0.38(1)	5.91(1)	5.454
$(5/2^+)$	$5/2_1^+$	4606.1(3)	2nd FNU	< 0.0027	>8.0	11.751
$3/2^+$	$3/2_{3}^{+}$	4989.5(3)	Allowed	0.246(6)	5.64(1)	5.233
$3/2^{+}$	$3/2_{4}^{+}$	5305.9(3)	Allowed	0.291(7)	5.20(1)	5.534
$3/2^{+}$	$3/2_{5}^{+}$	5456.1(3)	Allowed	0.38(1)	4.87(1)	5.668
3/2+	$3/2_{6}^{+}$	6064.2(4)	Allowed	0.0049(2)	5.56(2)	5.382



FIG. 4. Comparison of excitation energies of low-lying excited states in ⁴⁶Ca obtained from SDPF-MU interaction with previously obtained results in $sd_{3/2} + f_{7/2}p_{3/2}$, pf, and $pfg_{9/2}$ valence spaces using NN + 3N forces [30,45]. Experimental data are also shown in first column for comparison.

log ft values are 8.159, 5.811, 10.815, and 5.454 for $1/2^-$, $1/2^+$, $3/2^-$, and $3/2^+$ states, respectively. Also calculated excitation energies with SDPF-MU interaction for these states are 4.58, 6.202, 6.725, and 5.290 MeV, respectively. So, the log ft values favor this state as either $1/2^-$ or $1/2^+$. The experimental $(5/2)^+$ state is at 4.606 MeV, while the calculated value of log ft for this state is 11.751 (the experimental value is >8.0) and the calculated energy is 4.404 MeV. Thus, the shell-model results support this states as $5/2^+$.

In Figs. 4 and 5, we have shown a comparison of the energy levels obtained from our present calculations with those of previous works, where the level scheme was obtained in $sd_{3/2} + f_{7/2}p_{3/2}$ [30], pf [30] and $pfg_{9/2}$ [45] valence spaces using NN + 3N interactions. As can be seen from Fig. 4, although the lower excited states are well reproduced by previous calculation in $sd_{3/2} + f_{7/2}p_{3/2}$ model space [30], the higher states, however, are better reproduced by SDPF-MU interaction. For instance, our shell-model results with SDPF-MU interaction reported in this paper for the 3⁻ state of ⁴⁶Ca is in excellent agreement with the experimental value. Negative-parity states were not obtained below 5 MeV for $pfg_{9/2}$ shell-model space.

For ⁴⁷Ca, previous studies were performed in pf and $pfg_{9/2}$ valence spaces using NN + 3N forces [45], where only negative-parity states were calculated. In the present work, we have calculated both positive- and negative-parity states. From Fig. 5, it is seen, for instance, that previous work with pf and $pfg_{9/2}$ valence spaces give ≈ 1.8 MeV and ≈ 1 MeV energy difference between theory and experiment for the $3/2_1^-$ state in ⁴⁷Ca, respectively, while the difference is reduced to ≈ 600 keV in this work. This indicates that the



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FIG. 5. Comparison of excitation energies of low-lying excited states in ⁴⁷Ca obtained from SDPF-MU interaction with previously obtained results in *pf* and *pf*g_{9/2} valence spaces using NN + 3N forces [45]. Experimental data are also shown in first column for comparison.

sdpf-model space is a suitable valence space for ⁴⁷Ca. For other states also, we obtain improved results with the SDPF-MU interaction as compared with the previous study.

We have analyzed the configuration for low-lying positiveand negative-parity states of 46,47 Ca corresponding to 1p-1h excitation. For natural-parity states, there is no excitation from the *sd* shell to the *pf* shell. For 47 Ca, $7/2_1^-$ and $3/2_1^-$ states are generated from the configurations $v f_{7/2}^{-1}$ with probability of 94.41% and $\nu p_{3/2}^1$ with probability of 92.22%, respectively. These states correspond to single-particle states. In the case of unnatural parity states, either one proton or one neutron is excited into the *pf* shell. It is expected that, for calcium isotopes, which have a proton shell closure at Z = 20, protons might not be excited from the sd shell to the pf shell. But for these states, we have seen that not only neutrons but also protons are excited from the sd shell to the pf shell. In fact, a major contribution comes from proton excitation despite Z = 20being a magic number. The 3_1^- state in 46 Ca originated $2 - 20^-$ the configuration $\pi(d_{5/2}^6 s_{1/2}^1 d_{3/2}^4 f_{1/2}^1) \otimes \nu(d_{5/2}^6 s_{1/2}^2 d_{3/2}^4 f_{1/2}^6)$, which has a 22.45% contribution. The dominant configuration for $5/2_1^+$ in 47 Ca is $\pi(d_{5/2}^6s_{1/2}^2d_{3/2}^3f_{7/2}^1) \otimes \nu(d_{5/2}^6s_{1/2}^2d_{3/2}^4f_{7/2}^7)$ with a probability of 24.06%. So, protons are not treated as inert in ^{46,47}Ca. This effect is also seen in the case of 2p-2h excitations. Even for natural-parity states, protons are excited from the sd shell to the pf shell.

IV. CONCLUSION

In the present work, we have performed a systematic nuclear shell model calculation for recently available experimental data measured with the GRIFFIN spectrometer at the TRIUMF-ISAC facility from the β^- decay of 46 K and 47 K to

reproduce the level schemes of ⁴⁶Ca and ⁴⁷Ca. We have also calculated low-lying energy spectra for the parent nuclei ⁴⁶K and ⁴⁷K. In our shell-model calculations, the SDPF-MU interaction has been used to calculate the spectroscopic properties of ^{46,47}K and ^{46,47}Ca. For the first time, we have calculated the log ft values corresponding to new data for the β^- decay from 46,47 K to 46,47 Ca. The present shell-model study helps us to identify the spin-parity of unconfirmed states for which the log ft values are reported in these experimental works. Based on calculated $\log ft$ values, we have predicted a state with 3.984 MeV to be either 3^- or 2^+ with a log ft value of 6.009 and 9.080 for 46 Ca. A tentative state at 4.432 MeV is also assigned to be 3^- in 46 Ca. In the case of 47 Ca, we have also given spin confirmation to the tentative states at 2.850, 3.889, and 4.606 MeV. The states at 2.875, 3.951, and 4.453 MeV could be $1/2^{-}$, $3/2^{-}$, and $1/2^{-}$ or $1/2^{+}$ in 47 Ca, respectively. The agreement of our calculated $\log ft$ values

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with the experimental data is rather limited. In some cases, the calculated log ft values are close to the experimental ones; the difference in log ft is within 0.8 for about half of the states measured in ⁴⁶Ca and ⁴⁷Ca. The difference, however, amounts to 1.1–2.7 for other cases. The present nuclear-shell-model study has added more information to the recent experimental works [30,31].

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