$\Lambda_c N$ interaction in leading-order covariant chiral effective field theory

Jing Song,¹ Yang Xiao¹,^{1,2} Zhi-Wei Liu,¹ Chun-Xuan Wang,¹ Kai-Wen Li,^{3,1,*} and Li-Sheng Geng^{1,3,4,5,†}

¹School of Physics, Beihang University, Beijing 102206, China

²Université Paris-Saclay, CNRS/IN2P3, IJCLab, Orsay 91405, France

³Beijing Advanced Innovation Center for Big Data-Based Precision Medicine, School of Medicine and Engineering,

Beihang University, Key Laboratory of Big Data-Based Precision Medicine (Beihang University), Ministry of Industry and Information

Technology, Beijing 100191, China

⁴Beijing Key Laboratory of Advanced Nuclear Materials and Physics, Beihang University, Beijing 102206, China ⁵School of Physics and Microelectronics, Zhengzhou University, Zhengzhou, Henan 450001, China

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We study the $\Lambda_c N$ interaction in the covariant chiral effective field theory (ChEFT) at leading order. All the relevant low-energy constants are determined by fitting to the lattice QCD simulations from the HAL QCD Collaboration. Extrapolating the results to the physical point, we show that the $\Lambda_c N$ interaction is weakly attractive in the ${}^{1}S_{0}$ channel, but in the ${}^{3}S_{1}$ channel it is only attractive at extremely low energies and soon turns repulsive for larger laboratory energy. Furthermore, we show that the neglect of the ${}^{3}S_{1} - {}^{3}D_{1}$ coupling provided by the leading-order covariant ChEFT would result in an attractive interaction in the ${}^{3}S_{1}$ channel at the physical point, which coincides with the previous nonrelativistic ChEFT study. As a byproduct, we predict the ${}^{3}D_{1}$ phase shifts and the mixing angel ε_{1} , which can be checked by future lattice QCD simulations. In addition, we compare the $\Lambda_c N$ interaction with the ΛN and NN interactions to study how the baryon-nucleon (BN) interactions evolve as a function of the baryon mass with the replacement of a light quark by a strange or charm quark in the baryon (B).

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I. INTRODUCTION

Baryon-baryon (BB) interactions are one of the most important inputs in studies of hadronic matter. At present, the low energy nucleon-nucleon (NN) interaction has already been comprehensively studied both phenomenologically and model independently [1-5]. The investigation of the hyperonnucleon (YN) interaction has achieved significant success as well [6-11]. Hypernuclear spectroscopy provides one of the most important sources from which YN and hyperon-hyperon (YY) interactions can be derived. As a natural extension of NNand YN interactions, the charmed hyperon-nucleon (Y_cN) interaction has also been studied with growing interest [12-19]. High energy facilities such as BEPC in China [20,21], J-PARC in Japan [22], and FAIR in Germany [23] all have ongoing or proposed experiments on charm physics, for instance the production of Λ_c and Σ_c hyperons and their interactions with other hadrons [24].

Early theoretical studies, based on either meson-exchange models [12–17] or constituent quark models [18,19], indicated that the Y_cN ($Y_c = \Lambda_c, \Sigma_c$) interaction is fairly attractive. Particularly, compared with the ΛN interaction, the strange meson (K, K^*) exchanges are replaced by the charmed meson (D, D^*) exchanges in the $\Lambda_c N$ interaction [13,14,16] in meson-exchanged models. This would result in less (more) attraction in the *S* (*P*) partial waves in the $\Lambda_c N$ interaction than in the corresponding ΛN potential, because of the larger masses of exchanged mesons.

Recently, the HAL QCD Collaboration performed lattice QCD simulations for unphysical pion masses to study the $\Lambda_c N$ interaction [25]. They obtained the S-wave phase shifts for $m_{\pi} = 410$, 570, and 700 MeV. These results were subsequently studied in the next-to-leading-order nonrelativistic chiral effective field theory (ChEFT) and extrapolated to the physical point, and a moderately attractive $\Lambda_c N$ interaction was found for both the ${}^{1}S_{0}$ and ${}^{3}S_{1}$ channels [26]. In a later work, the S-wave $\Sigma_c N$ interaction with isospin 1/2 was studied by the HAL QCD Collaboration as well [27]. Taking these results as inputs, Meng *et al.* [28] calculated the $\Sigma_c N$ interaction to the next-to-leading order in the nonrelativistic ChEFT and found that the ${}^{3}S_{1}$ interaction for isospin 1/2 is weakly attractive, but the interaction for isospin 3/2 is strongly attractive, resulting in a $\Sigma_c N$ bound state. It should be stressed that the latter prediction depends on the quark model inputs adopted.

As all the lattice QCD simulations of the Y_cN system were still performed for unphysical light quark (pion) masses, a reliable extrapolation of these results to the physical point is essential to guide future experiments and to gain insights into the Y_cN interaction. In a series of recent works, we have shown that the recently proposed covariant ChEFT approach can be used for such a purpose. In Refs. [29–32], it was shown that the strangeness S = -1 lattice QCD YN interaction can be described reasonably well, and so can the strangeness

^{*}kaiwen.li@buaa.edu.cn

[†]lisheng.geng@buaa.edu.cn



FIG. 1. Leading-order Feynman diagrams for nonderivative fourbaryon contact terms and one-meson exchanges.

S = -2 YN/YY interaction. The extrapolated results are also consistent with limited experimental data. In a more recent work [33], we showed that the lattice QCD NN phase shifts for the ${}^{1}S_{0}$ and ${}^{3}S_{1} - {}^{3}D_{1}$ partial waves can be simultaneously described together with their physical counterparts by the leading-order (LO) covariant ChEFT, implying that a reliable chiral extrapolation of lattice QCD results for unphysical pions masses smaller than 500 MeV is possible. An interesting discovery of Ref. [33] is that the ${}^{3}S_{1} - {}^{3}D_{1}$ coupled channel is described by the same two low-energy constants (LECs), thus allowing one to make predictions for the ${}^{3}D_{1}$ phase shifts and the mixing angle ε_{1} using only the ${}^{3}S_{1}$ phase shifts as inputs.

In this work, we revisit the HAL QCD results [25] in the covariant ChEFT at leading order. Our purpose is threefold. First, we provide an independent extrapolation of the HAL QCD results, in addition to that of Ref. [26]. Second, we predict the ${}^{3}D_{1}$ phase shifts and the mixing angle ε_{1} , so that they can be checked by future lattice QCD simulations, which could also provide a nontrivial check of the covariant ChEFT. Third, we investigate the quark mass dependence of

baryon-nucleon interactions by comparing those of NN, ΛN , and $\Lambda_c N$.

This paper is organized as follows. In Sec. II, we briefly introduce the covariant ChEFT for the Y_cN system, including covariant chiral Lagrangians, potentials, and the scattering equation, as well as our strategy to determine the unknown LECs. In Sec. III we show the fitted results and extrapolations, and discuss coupled channel effects and quark mass dependence in the NN, ΛN , and $\Lambda_c N$ interactions. This is followed by a short summary and outlook in Sec. IV.

II. LEADING-ORDER COVARIANT CHIRAL EFFECTIVE FIELD THEORY

In this section, we briefly introduce the covariant ChEFT for the Y_cN interaction. At leading order, the Y_cN potentials consist of contributions from nonderivative four-baryon contact terms (CTs) and one-meson exchanges (OMEs), as shown in Fig. 1. The LO Lagrangian for the contact terms is

$$\mathcal{L}_{\mathrm{CT}}^{Y_c N \to Y_c N} = C_i \; (\bar{Y}_c \Gamma_i Y_c) (\bar{N} \Gamma_i N), \tag{1}$$

where C_i (i = 1, ..., 5) are the LECs that need to be determined by fitting to either experimental or lattice QCD data, and Γ_i (i = 1, ..., 5) are the elements of the Clifford algebra,

$$\Gamma_1 = 1, \quad \Gamma_2 = \gamma^{\mu}, \quad \Gamma_3 = \sigma^{\mu\nu}, \quad \Gamma_4 = \gamma^{\mu}\gamma_5, \quad \Gamma_5 = \gamma_5.$$

Then potentials are derived with the full baryon spinor,

$$u_B(p,s) = N_p \left(\frac{1}{\frac{\sigma \cdot p}{E_p + M_B}}\right) \chi_s, \qquad N_p = \sqrt{\frac{E_p + M_B}{2M_B}}, \qquad (2)$$

where $E_p = \sqrt{p^2 + M_B^2}$, and $M_B = M_{Y_c}$ or M_N is the mass of the charmed baryon or nucleon. By performing partial wave projection, the ¹S₀ and ³S₁ - ³D₁ CT potentials in the *LSJ* basis read

$$V_{150}^{Y_cN} = \xi_{Y_cN} \Big[C_{150} \Big(R_{p'}^N R_{p'}^{Y_c} + R_p^N R_p^{Y_c} \Big) + C_{150}' \Big(R_{p'}^N R_p^N R_{p'}^{Y_c} R_p^{Y_c} + 1 \Big) \Big], \tag{3}$$

$$V_{251}^{Y_cN} = \frac{1}{2} \xi_{Y_cN} \Big\{ 2(C_{150} - C_{150}') \Big(R_{p'}^{Y_c} R_p^{Y_c} - R_{p'}^N R_p^N \Big) + C_{351} \Big(-6R_{p'}^N R_p^N + 9R_{p'}^N R_{p'}^{Y_c} + 9R_p^N R_p^{Y_c} + 6R_{p'}^{Y_c} R_p^{Y_c} \Big) \Big\}$$

$$+9C'_{3S1} [R^{Y_c}_{p'}R^{Y_c}_p (R^N_{p'}R^N_p - 2) + 2R^N_{p'}R^N_p + 9]\},$$
(4)

$$V_{3D1-3S1}^{Y_cN} = \frac{\xi_{Y_cN}}{9\sqrt{2}} \{ (C_{1S0} - C_{1S0}') [R_p^N (R_{p'}^N + 3R_{p'}^{Y_c}) - R_p^{Y_c} (3R_{p'}^N + R_{p'}^{Y_c})] + C_{3S1} [9R_p^{Y_c} (R_{p'}^N + 4R_p^N) + 3R_{p'}^N R_p^N - 3R_{p'}^{Y_c} (3R_p^N + R_p^{Y_c})] + 9C_{3S1}' \{ R_{p'}^{Y_c} [R_p^N (4R_{p'}^N R_p^{Y_c} + 3) + R_p^{Y_c}] - R_{p'}^N (R_p^N + 3R_p^{Y_c}) \} \},$$
(5)

$$V_{3S1-3D1}^{Y_cN} = \frac{\xi_{Y_cN}}{9\sqrt{2}} \{ (C_{1S0} - C_{1S0}') [R_{p'}^N (R_p^N + 3R_p^{Y_c}) - R_{p'}^{Y_c} (3R_p^N + R_p^{Y_c})] + C_{3S1} [9R_{p'}^{Y_c} (R_p^N + 4R_{p'}^N) + 3R_p^N R_{p'}^N - 3R_p^{Y_c} (3R_{p'}^N + R_{p'}^{Y_c})] + 9C_{3S1}^{Y_c} [R_{p'}^N (4R_p^N R_{p'}^{Y_c} + 3) + R_{p'}^{Y_c}] - R_p^N (R_{p'}^N + 3R_{p'}^{Y_c}) \} \},$$
(6)

$$V_{3D1}^{Y_cN} = \frac{2}{9} \xi_{Y_cN} \{ (C_{1S0} - C_{1S0}' + 3C_{3S1}) \left(R_{p'}^N R_p^N - R_{p'}^{Y_c} R_p^{Y_c} \right) + 9C_{3S1}' \left[R_{p'}^N R_p^N \left(4R_{p'}^{Y_c} R_p^{Y_c} - 1 \right) + R_{p'}^{Y_c} R_p^{Y_c} \right] \},$$
(7)

where

$$\xi_{Y_cN} = 4\pi \frac{\sqrt{\left(E_{p'}^{Y_c} + M_{Y_c}\right)\left(E_p^{Y_c} + M_{Y_c}\right)\left(E_{p'}^N + M_N\right)\left(E_p^N + M_N\right)}}{4M_N M_{Y_c}} \quad \text{and} \quad R_{p(p')}^{Y_c,N} = \frac{p(p')}{E_{p(p')}^{Y_c,N} + M_{Y_c,N}}.$$
(8)

TABLE I. Baryon masses for different pion masses (in units of MeV) needed in this work [25].

m_{π}	m_N	m_{Λ_c}	m_{Σ_c}
138	939	2287	2455
412	1215	2434	2575
570	1399	2555	2674

Note that all the LECs are implicitly pion mass dependent as in Ref. [26] such that $C_{1S0} = \hat{C}_{1S0} + D_{1S0} m_{\pi}^2$. For M_{Y_c} , we used the average of Λ_c and Σ_c masses. On the other hand, because of the limited LQCD data, it is impossible to pin down all the LECs of the coupled $\Lambda_c N \cdot \Sigma_c N$ system. Therefore, following Ref. [34], we used an effective CT potential by only considering the $\Lambda_c N \to \Lambda_c N$ channel and assumed that the CT contributions from the $\Sigma_c N$ channel can be effectively absorbed into those from the $\Lambda_c N$ channel, thus in total only four LECs are needed in the present study, i.e., C_{1S0} , C'_{1S0} , C_{3S1} , and C'_{3S1} .

To construct the OME potentials, we need the following LO meson-baryon Lagrangian [35]:

$$\mathcal{L}_{MB} = \operatorname{tr}\left(\bar{B}(iD - M_B)B - \frac{D/F}{2}\bar{B}\gamma^{\mu}\gamma_5\{u_{\mu}, B\}_{\pm}\right) + \frac{1}{2}\operatorname{tr}[\bar{B}_{\bar{3}}(i\partial - M_{\bar{3}})B_{\bar{3}}] + \operatorname{tr}\frac{1}{8f_0^2}(i\bar{B}_{\bar{3}}\gamma^{\mu}\{[M, \partial_{\mu}M], B_{\bar{3}}\}) \\ + \operatorname{tr}[\bar{B}_6(i\partial - M_6)B_6] + \operatorname{tr}\frac{1}{4f_0^2}(i\bar{B}_6\gamma^{\mu}\{[M, \partial_{\mu}M], B_6\}) + \left(-\frac{1}{\sqrt{2}f_0}\right)g_1\operatorname{tr}(\bar{B}_6\gamma^{\mu}\gamma_5\partial_{\mu}MB_6) \\ + \left(-\frac{1}{\sqrt{2}f_0}\right)g_2\operatorname{tr}(\bar{B}_6\gamma^{\mu}\gamma_5\partial_{\mu}MB_{\bar{3}}) + \operatorname{H.c.} + \left(-\frac{1}{\sqrt{2}f_0}\right)g_6\operatorname{tr}(\bar{B}_{\bar{3}}\gamma^{\mu}\gamma_5\partial_{\mu}MB_{\bar{3}}), \tag{9}$$

where tr indicates trace in the corresponding flavor space, $D_{\mu}B = \partial_{\mu}B + [\Gamma_{\mu}, B]$, and Γ_{μ} and u_{μ} are the vector and axial-vector combinations of the meson fields and their derivatives,

$$\Gamma_{\mu} = \frac{1}{2} (u^{\dagger} \partial_{\mu} u + u \partial_{\mu} u^{\dagger}),$$
$$u_{\mu} = i (u^{\dagger} \partial_{\mu} u - u \partial_{\mu} u^{\dagger}).$$

In the Lagrangian \mathcal{L}_{MB} , M_B , $M_{\bar{3}}$, and M_6 are the ground-state masses of octet baryons, antitriplet baryons, and sextet baryons, respectively, and M, B, $B_{\bar{3}}$, and B_6 refer to the meson and baryon matrices, which are defined as

$$\begin{split} M &= \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & \frac{-\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{2\eta}{\sqrt{6}} \end{pmatrix}, \\ B &= \begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & \Sigma^+ & p \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & n \\ \Xi^- & \Xi^0 & -\frac{2\Lambda}{\sqrt{6}} \end{pmatrix}, \\ B_{\bar{3}} &= \begin{pmatrix} 0 & \Lambda_c^+ & \Xi_c^+ \\ -\Lambda_c^+ & 0 & \Xi_c^0 \\ -\Xi_c^+ & -\Xi_c^0 & 0 \end{pmatrix}, \\ B_6 &= \begin{pmatrix} \sum_{c}^{++} & \frac{\Sigma_c^+}{\sqrt{2}} & \frac{\Xi_c^{++}}{\sqrt{2}} \\ \frac{\Sigma_c^+}{\sqrt{2}} & \Sigma_c^0 & \frac{\Xi_c^0}{\sqrt{2}} \\ \frac{\Xi_c^{++}}{\sqrt{2}} & \frac{\Xi_c^0}{\sqrt{2}} & \Omega_0. \end{pmatrix}. \end{split}$$

The values of the coupling constants g_1 , g_2 , and g_6 and the meson decay constant f_0 will be specified below. Using \mathcal{L}_{MB} , one can straightforwardly obtain the OME potential,

$$V_{Y_cN \to Y_cN}^{\text{OME}} = -iN\bar{u}_{Y_c}(p') \left(\frac{\gamma^{\mu}\gamma_5 q_{\mu}}{2f_0}\right) u_{Y_c}(p) \frac{i}{\Delta E^2 - q^2 - m^2 + i\epsilon} \bar{u}_N(-p') \left(\frac{\gamma^{\nu}\gamma_5 q_{\nu}}{2f_0}\right) u_N(-p) \times \mathcal{I}_{Y_cN \to Y_cN},\tag{10}$$

where $Y_c = \Lambda_c$, Σ_c , q = p' - p is the transferred momentum, and *m* is the mass of the exchanged pseudoscalar meson. Note that we only consider light meson exchanges in the ChEFT. The coupling constant *N* is defined as

$$N = g_A^{Y_c Y'_c} g_A^{NN}.$$
 (11)

Following Ref. [26], $g_A^{Y_c Y'_c}$ and g_A^{NN} are assumed to be pion mass independent and are fixed to be $g_A^{NN} = 1.27$ [36], $g_A^{\Sigma_c \Sigma_c} = 0.71$ [37], and $g_A^{\Lambda_c \Sigma_c} = 0.74$ [37,38]. On the other hand, the meson decay constant f_0 varies with the pion mass, and the dependence has been deduced, e.g., in Ref. [39].



FIG. 2. Best fitted $\chi^2/d.o.f.$ as a function of the cutoff in the LO covariant ChEFT by fitting to the lattice QCD $\Lambda_c N$ S-wave phase shifts. The magenta circles denote the $\chi^2/d.o.f.$ for $m_{\pi} = 410$ MeV and the dark-blue dots refer to the $\chi^2/d.o.f.$ for $m_{\pi} = 570$ MeV, while their sum is shown in the right panel.

We use $f_0 = 93$ MeV for $m_{\pi} = 138$ MeV, $f_0 = 112$ MeV for $m_{\pi} = 410$ MeV, and $f_0 = 129$ MeV for $m_{\pi} = 570$ MeV. In Eq. (10), \mathcal{I} indicates the isospin factor, whose value can be found in, e.g., Refs. [40,41]. Note that OME does not contribute to $\Lambda_c N \to \Lambda_c N$ at tree level because of isospin conservation, but it contributes to the scattering amplitudes via the scattering equation.

In order to obtain the scattering amplitudes, we solved the coupled-channel Kadyshevsky equation [42],

$$T_{\rho\rho'}^{\nu\nu',J}(p',p;\sqrt{s}) = V_{\rho\rho'}^{\nu\nu',J}(p',p) + \sum_{\rho'',\nu''} \int_0^\infty \frac{dp''p''^2}{(2\pi)^3} \frac{M_{B_{1,\nu''}}M_{B_{2,\nu''}}}{E_{1,\nu''}E_{2,\nu''}} \frac{V_{\rho\rho''}^{\nu\nu'',J}(p',p'')}{E_{1,\nu''}E_{2,\nu''}} \frac{T_{\rho'',\nu'',J}^{\nu''\nu',J}(p'',p;\sqrt{s})}{E_{1,\nu''}E_{2,\nu''}},$$
(12)

where \sqrt{s} is the total energy of the two-baryon system in the center-of-mass frame and $E_{n,\nu''} = \sqrt{p''^2 + M_{B_{n,\nu''}}^2}$ (n = 1, 2). The labels ν, ν', ν'' denote the particle channels, and ρ, ρ', ρ'' denote the partial waves. In numerical calculations, the potentials in the scattering equation are regularized with an exponential form factor of the following form,

$$f_{\Lambda_F}(p, p') = \exp\left[-\left(\frac{p}{\Lambda_F}\right)^4 - \left(\frac{p'}{\Lambda_F}\right)^4\right].$$
 (13)

More details about the covariant ChEFT can be found in Refs. [5,29–33].

TABLE II. Values of the LECs from the best fits obtained with $\Lambda_F = 600-700$ MeV, where C'_{150} and C'_{351} are in units of 10^4 GeV⁻² and C_{150} and C_{351} are in units of 10^2 GeV⁻². The pion mass m_{π} and cutoff Λ_F are in units of MeV.

m_{π}	$\Lambda_{\rm F}$	C_{1S0}	C_{1S0}^{\prime}	C_{3S1}	C'_{3S1}
410	600	-1.2653	1.6882	0.2698	1.8966
	650	-0.9267	1.8736	0.1270	1.3170
	700	-0.2255	2.1488	-0.0130	0.8456
570	600	-0.7624	0.6540	-0.0520	0.1994
	650	-0.7168	0.6876	-0.0468	0.1608
	700	-0.6485	0.7274	-0.0414	0.1323

III. RESULTS AND DISCUSSION

A. Fitted results and extrapolations to the physical point

The four LECs in the CT potential are determined by fitting to the lattice QCD simulations from the HAL QCD Collaboration [25]. For this, we used the $\Lambda_c N$ S-wave phase shifts for $m_{\pi} = 410$ and 570 MeV with the center-of-mass energy



FIG. 3. $\Lambda_c N$ ¹S₀ phase shifts of the lattice QCD simulations in comparison with the ChEFT fits. The magenta open circles denote the LQCD data [25] for $m_{\pi} = 410$ MeV, while the dark-blue dots refer to the LQCD data [25] for $m_{\pi} = 570$ MeV. The lines and band denote the ChEFT fits. The band is generated from a variation of Λ_F from 600 to 700 MeV. The grey line and band refer to the predictions for $m_{\pi} = 138$ MeV. The vertical dashed line at $E_{c.m.} = 30$ MeV denotes that the $\Lambda_c N$ interaction is obtained by fitting to the lattice QCD data only up to this energy.



FIG. 4. Left: the same as Fig. 3 but for the ${}^{3}S_{1}$ phase shifts. Right: the same as the left panel, but with the *S*-*D* coupled channel effect turned off. The vertical dashed lines at $E_{c.m.} = 30$ MeV denote that the $\Lambda_{c}N$ interaction is obtained by fitting to the lattice QCD data only up to this energy.

 $E_{\rm c.m.}$ up to 30 MeV. Although the lattice QCD results for $m_{\pi} = 570$ MeV are probably already beyond the applicability of leading-order ChEFT, we included these results in order to pin down the pion mass dependence of the LECs so that we can extrapolate the lattice QCD results to the physical point. In Table I, we list the lattice QCD [25] and physical [36] baryon masses relevant to the present study. Similar to our previous study on the $\Lambda N \cdot \Sigma N$ system [29–31], the fits were first performed with cutoff values in the range of $\Lambda_F = 500-750$ MeV. The fitted χ^2 for lattice QCD simulations for different pion masses and the total χ^2 as a function of the cutoff Λ_F are shown in Fig. 2. For the ¹S₀ channel, within the cutoff range studied, the $\chi^2/d.o.f.$ for $m_{\pi} = 410$ MeV decreases with increasing Λ_F , while the $\chi^2/d.o.f.$ for $m_{\pi} = 570$ MeV stays almost constant. On the the other hand, for the ${}^{3}S_{1}$ channel, the $\chi^{2}/d.o.f.$ increases with increasing Λ_F for $m_{\pi} = 570$ MeV, but stabilizes in the range $\Lambda_F =$ 550–700 MeV for $m_{\pi} = 410$ MeV. From the right panel, one can see that a cutoff between 500 and 700 MeV yields the minimum χ^2 for all the lattice QCD data fitted. However, since the lattice QCD data for $m_{\pi} = 570$ MeV were used in our fits, in principle the cutoff value should be larger than the pion mass such that the inclusion of the OME potential is justified. As a result, we choose the range of $\Lambda_F = 600-700 \text{ MeV}$ in subsequent analyses, and the fitted LECs are shown in Table II.

The fitted S-wave $\Lambda_c N$ phase shifts are shown in Figs. 3 and 4. For the ¹S₀ partial wave, the covariant ChEFT phase shifts are in good agreement with the lattice QCD data. The $\Lambda_c N$ potential turns out to be moderately attractive when extrapolated to the physical point. It should be noted that the predicted 1S_0 phase shifts at the physical point are qualitatively similar to those of the nonrelativistic ChEFT of Ref. [26], but with slightly larger uncertainties.

On the other hand, for the ${}^{3}S_{1}$ partial wave shown in the left panel of Fig. 4, the covariant ChEFT phase shifts are in fair agreement with the lattice QCD data only for energies up to 30 MeV. The discrepancy then becomes larger as the energy increases. Extrapolated to the physical point, the $\Lambda_{c}N$ interaction is weakly attractive only in the very low energy region, then becomes repulsive as the kinetic energy increases. This results in a peculiar phenomenon that, although the scattering length of this channel is negative (see Table III) and therefore indicates a weakly attractive interaction, on the whole the ${}^{3}S_{1}$ interaction is repulsive. This is quite different from the results of the nonrelativistic ChEFT [26].

In order to understand this phenomenon, we set $V_{{}^{3}S_{1}}$ - ${}^{3}D_{1}$ and $V_{{}^{3}D_{1}}$ - ${}^{3}S_{1}$ in the CT potential to zero and redid the fits. The resulting phase shifts are shown in the right panel of Fig. 4. The covariant ChEFT phase shifts are in better agreement with the lattice QCD data for energies up to 40 MeV. In particular, the description of the $m_{\pi} = 570$ MeV data is much improved. Furthermore, when extrapolated to the physical point, an attractive interaction is obtained, which is similar not only to the ${}^{1}S_{0}$ interaction shown in Fig. 3, but also to the ${}^{3}S_{1}$ interaction of the nonrelativistic ChEFT. As a result, we conclude that the predicted ${}^{3}S_{1}$ interaction depends strongly on how the coupled channel *S-D* mixing is treated.

TABLE III. NN, ΛN , and $\Lambda_c N$ scattering lengths (in units of fm) obtained in the LO covariant ChEFT, NLO nonrelativistic ChEFT, and Nijmegen-D model. For guidance, we also show the experimental NN scattering lengths.

Channels		Cov. ChEFT (LO)	NR ChEFT (NLO)	Nijmegen-D	Expt.
NN	a_{150}^{NN}	-21.3	-23.0	-17.0 [15]	-23.7
	a_{3S1}^{NN}	5.75	5.48	5.42 [15]	5.42
ΛN	$a_{1S0}^{\Lambda N}$	-2.44 [29]	-2.91 [45]	-1.90 [46]	
	$a_{3S1}^{\Lambda N}$	-1.32 [29]	-1.54 [45]	-1.96 [46]	
$\Lambda_c N$	$a_{150}^{\tilde{\Lambda}_c N}$	-1.16	-1.00 [26]	-3.83 [15]	
	$a_{3S1}^{\Lambda_cN}$	-0.52	-0.98 [26]	-4.24 [15]	



FIG. 5. On-shell $\Lambda_c N$ potentials for the ${}^3S_1 - {}^3D_1$ coupled channel for different pion masses. The black solid lines denote potentials for $m_{\pi} = 138$ MeV, the magenta dashed lines refer to potentials for $m_{\pi} = 410$ MeV, and the dark-blue dotted lines are potentials for $m_{\pi} = 570$ MeV.

In the nonrelativistic ChEFT, there is no *S*-*D* mixing in the leading-order CT potential, while the same two LECs are responsible for the ${}^{3}S_{1} - {}^{3}D_{1}$ coupled channel in the LO covariant ChEFT. In the following, we further explore this coupled channel effect, which is due to relativistic corrections that are considered to be of higher order in the nonrelativistic ChEFT but already shows up at leading order in the covariant ChEFT.

For the sake of simplicity, we fixed the cutoff Λ_F at 600 MeV, but the general discussion remains unchanged for $\Lambda_F = 650$ and 700 MeV. The on-shell coupled channel potentials as a function of kinetic energy in the center-of-mass

frame are shown in Fig. 5. The ${}^{3}S_{1}$ potential increases slowly with $E_{c.m.}$, while the ${}^{3}D_{1}$ and ${}^{3}S_{1} - {}^{3}D_{1}$ potentials decrease with the energy. The ${}^{3}D_{1}$ potential is two order of magnitude smaller than the ${}^{3}S_{1}$ potential, while the ${}^{3}S_{1} - {}^{3}D_{1}$ mixing is even one more order of magnitude smaller. Such features of the triplet channel potentials are in qualitative agreement with the lattice QCD simulations [25]. Nonetheless, the small mixing seems to affect the ${}^{3}S_{1}$ phase shifts a lot, as we noted above. As a result, we strongly encourage lattice QCD collaborations to check whether the inclusion of the coupled channel effect in extrapolating the ${}^{3}S_{1}$ interaction can make a difference.



FIG. 6. $\Lambda_c N^3 S_1$, 3D_1 phase shifts and mixing angles ε_1 for different pion masses. The bands are generated from the variation of Λ_F from 600 to 700 MeV. The vertical dashed lines at $E_{c.m.} = 30$ MeV denote that the $\Lambda_c N$ interaction is obtained by fitting to the lattice QCD data only up to this energy.



FIG. 7. *NN*, ΛN , and $\Lambda_c N$ phase shifts in the 1S_0 and ${}^3S_1 - {}^3D_1$ coupled channels for physical pion masses. The green solid lines, red dashed lines, and blue dot-dashed lines denote the $\Lambda_c N$, ΛN , and *NN* interactions, respectively. The vertical dashed lines at $E_{c.m.} = 30$ MeV denote that the $\Lambda_c N$ interaction is obtained by fitting to the lattice QCD data only up to this energy.

In the following, we predict the ${}^{3}D_{1}$ phase shifts and the mixing angle ε_1 with the LECs determined by fitting to the lattice QCD ${}^{3}S_{1}$ phase shifts, which are shown in Fig. 6 together with their ${}^{3}S_{1}$ counterparts for three pion masses, $m_{\pi} = 138$, 410, and 570 MeV. As this is only a leading-order study and also demonstrated above, the results beyond $E_{c.m.} > 30$ MeV should be taken with caution. For the ${}^{3}S_{1}$ partial wave, the interaction changes from weakly attractive to moderately repulsive as the pion mass decreases from 570 to 138 MeV. As already stressed above, this transition is strongly related to the S-D coupling and should be checked by future lattice QCD simulations. For the ${}^{3}D_{1}$ partial wave, the interaction is weakly repulsive for $m_{\pi} = 570$ MeV, and becomes stronger as the pion mass decreases to $m_{\pi} = 410$ MeV. However, such a reduction does not extend to the physical point. As a matter of fact, the $\Lambda_c N$ interaction for the physical pion mass is almost the same as that for $m_{\pi} = 410$ MeV. As for the mixing angle ε_1 , it shows a strong dependence on the cutoff for $m_{\pi} = 570$ MeV, yet such a dependence becomes weaker as the pion mass decreases. In addition, for $m_{\pi} = 410$ MeV, the mixing angle has the largest magnitude.

B. Comparison of the *NN*, ΛN , and $\Lambda_c N$ interactions

It is instructive to compare the *NN*, ΛN , and $\Lambda_c N$ interactions, which not only allows for a better understanding of the evolution of the baryon-nucleon interactions as one

replaces one light quark in the baryon by one strange or charm quark, but also allows us to better assess the extrapolated $\Lambda_c N$ interaction from the lattice QCD simulations as both the *NN* and *YN* interactions are constrained by experimental data, particularly the former.

The ${}^{1}S_{0}$ and ${}^{3}S_{1} - {}^{3}D_{1}$ NN, ΛN , and $\Lambda_{c}N$ phase shifts with $\Lambda_F = 600$ MeV for the physical pion mass are shown in Fig. 7. In the ${}^{1}S_{0}$ channel, the NN interaction is strongly attractive (to the extent that there is a virtual bound state in this channel), while both the ΛN and $\Lambda_c N$ interactions become less attractive, but the latter two are of similar strength. In the ${}^{3}S_{1}$ channel, the NN interaction is strongly attractive (to the extent that the deuteron exists), the ΛN interaction becomes only weakly attractive, while the $\Lambda_c N$ interaction becomes weakly repulsive, as we discussed already. In the ${}^{3}D_{1}$ channel, both the NN and $\Lambda_c N$ interactions are weakly repulsive, while the ΛN interaction is quite small up to $E_{\rm c.m.} \approx 50$ MeV, and then increases quickly, corresponding to the opening of the ΣN channel. A similar phenomenon has been observed in the experimental data [43,44] and our previous studies [29,41] that a cusp appears in the $\Lambda p \to \Lambda p$ cross section at the opening of the $\Sigma^+ n$ channel. On the other hand, the *NN* and ΛN mixing angles are very similar up to $E_{\rm c.m.} \approx 50$ MeV but the $\Lambda_c N$ mixing angle is negative and smaller in magnitude.

In Table III, we list the corresponding scattering lengths. For comparison, we also show the results of the LO covariant ChEFT [29] for ΛN , next-to-leading-order nonrelativistic

ChEFT [26,45] for ΛN and $\Lambda_c N$, and the Nijmegen-D model [15,46]. The covariant ChEFT NN scattering lengths were obtained with the regulator of Eq. (13) with a cutoff of 600 MeV following the fitting strategy of Ref. [5], while those of the nonrelativistic ChEFT were obtained using the same regulator and cutoff following the fitting strategy of Ref. [47]. We note that the scattering lengths obtained in the covariant ChEFT are qualitatively similar to those obtained in the nonrelativistic ChEFT, while some of the predictions of the Nijmegen-D model are drastically different, e.g., those of the $\Lambda_c N$ and ${}^1S_0 NN$.

IV. CONCLUSION

In this work, we studied the lattice QCD simulations of the $\Lambda_c N$ interaction for $m_{\pi} = 410$, 570 MeV and extrapolated the results to the physical point. We found that the covariant ChEFT $\Lambda_c N$ phase shifts are in good agreement with the lattice QCD simulations in the 1S_0 partial wave for $E_{c.m.} \leq$ 40 MeV, while in the 3S_1 partial wave the ChEFT results are in good agreement with the lattice QCD data for $E_{c.m.} \leq$ 30 MeV. Different from the previous study of Ref. [26], we found an attractive $\Lambda_c N$ interaction in the 1S_0 partial wave, but a repulsive interaction in the 3S_1 partial wave, though it is slightly attractive at extremely low energies. We showed that such a repulsive $\Lambda_c N$ interaction originates from the coupling of 3S_1 and 3D_1 , and one ends up with an attractive interaction at the physical point once the coupling in the CT potential is neglected.

To understand how the baryon-nucleon (*BN*) interaction evolves if one replaces one of the light quarks in the baryon *B* with a strange or charm quark, we compared the so-obtained $\Lambda_c N$ interaction with those of ΛN and *NN*. We found that in general the strength of the *BN* interaction becomes weaker as one moves from *NN* to ΛN to $\Lambda_c N$.

We noted that although in good agreement with the lattice QCD simulations for unphysical pion masses, the covariant ChEFT results for the spin triplet channel seem to show strong dependence on the consideration of coupled channel effects. This needs to be checked by future and more refined lattice QCD simulations.

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