β decay of ¹³²In and spectroscopy of ¹³²Sn and ¹³¹Sb with the GRIFFIN spectrometer

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Spectroscopy of doubly magic ${}^{132}_{50}\mathrm{Sn_{82}}$ has been performed with the GRIFFIN spectrometer at TRIUMF-ISAC following the β decay of ${}^{132}_{49}\mathrm{In_{83}}$. The analysis has allowed for the placement of a total of 70 transitions and 29 excited states in ${}^{132}\mathrm{Sn}$. Detailed spectroscopy has also been performed on ${}^{131}\mathrm{Sh}$, resulting from the β decay of ${}^{131}\mathrm{Sn}$, produced from the β -delayed neutron decay of ${}^{132}\mathrm{In}$. Measurement of γ rays in both ${}^{131}\mathrm{Sn}$ and ${}^{131}\mathrm{Sh}$ has led to the determination of the β -delayed neutron emission probability P_n from ${}^{132}\mathrm{In}$. This is the first time that P_n has been measured for this nucleus by using γ spectroscopy, and the new value of 12.3(4)% is consistent with the most recent β -n counting experiment. Additionally, γ - γ angular correlations have been performed in ${}^{132}\mathrm{Sn}$, supporting the spin assignments of several excited states. Novel *ab initio* calculations are presented which describe several of the excited states, and these are compared with the experimental spectrum.

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I. INTRODUCTION

The tin isotopes have been the subject of many experimental studies because of the magic number of protons with Z=50. The known isotopes span more than a full shell closure and include both doubly magic $_{50}^{100}\mathrm{Sn}_{50}$ and $_{50}^{132}\mathrm{Sn}_{82}$. Very little is known about $_{100}^{100}\mathrm{Sn}$; no excited states have been identified, and only the mass, half-life, and some β -decay properties have been studied [1–3]. In contrast, many properties of $_{132}^{132}\mathrm{Sn}$ are known. With a first-excited state above 4 MeV, it has been described as the nucleus with the strongest shell closure

[4,5], and it serves as an important benchmark for theoretical calculations.

Several β -decay experiments have identified excited states in 132 Sn [5–7]. An early comprehensive β -decay study identified a total of 21 excited states and 44 transitions [5,7]. From the same experiment, conversion electron spectroscopy revealed the E1 nature of the 311-keV transition, providing a 3⁻ assignment for the 4352-keV level. A study of fission fragments from ²⁴⁸Cm identified a 9⁺ state at 5280 keV in delayed coincidence with the decay of the 8⁺ isomer and also confirmed other yrast states up to 4942 keV [8]. The first 2⁺ and 3⁻ excited states have been further characterized through Coulomb excitation experiments, both at the Holifield Radioactive Ion Beam Facility, which measured the $B(E2; 0^+ \rightarrow$ 2⁺) [9–12], and at the High Intensity and Energy Isotope Separator On-Line (HIE-ISOLDE) facility, which additionally measured the $B(E3; 0^+ \rightarrow 3^-)$ [13]. Another experiment at the ISOLDE Decay Station identified three new excited states from the β -delayed neutron (βn) decay of ¹³³In [14].

Despite the availability of experimental data, there has been relatively little theoretical work characterizing the structure of 132 Sn. Several quasiparticle random-phase approximation (QRPA) calculations have been able to reproduce the measured B(E2) and B(E3) values [15–18]. More recently, the first large-scale shell-model (LSSM) and Monte Carlo shell-model (MCSM) calculations have also reproduced the quadrupole and octupole transition strengths [13]. Most of

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these investigations have also calculated the energies of the first 2^+ and 3^- states, with generally good agreement with the measured values. However, the theoretical calculations have been limited to these two low-lying excited states. Additional work is therefore desired to examine the excited states beyond 5 MeV.

The region around 132 Sn is especially important in rapidneutron capture process (r-process) nucleosynthesis. The solar system abundance peak at $A \approx 130$ corresponds to nuclei along the N = 82 closed shell [19]. Sensitivity studies which determine the relative impact of nuclear properties on astrophysical element production reveal that β -decay properties, including half-lives and β -delayed neutron emission probabilities P_n , exert a strong influence over the final abundances in this region. The importance of determining neutron branching ratios, both for theoretical astrophysics and for heat production in reactors, has been highlighted by the International Atomic Energy Agency [20].

Several previous measurements of β -delayed neutron decay have been made by counting neutrons or β particles. More recently, however, several γ -spectroscopy experiments have provided updated and often more precise P_n values for various nuclei [14,21,22]. The first experiment to measure the β -delayed neutron decay from ¹³²In found a P_n of 4.2(9)% by using β/n coincidences [23]. Subsequent measurements using β -n counting resulted in values of 6.8(14)% and 10.7(33)% [24,25]. An investigation of the βn emission probability using the complimentary technique of γ spectroscopy, which has a higher resolution and selectivity than neutron detection, is therefore valuable.

The present work describes one of the most detailed analyses of 132 Sn, identifying 70 γ -ray transitions, along with 29 total excited states. The decay of 132 In has been characterized, including the half-life, β -feeding intensities, and the first measurement of P_n by using γ rays. For the first time, γ - γ angular correlations in 132 Sn have been performed, which support the spin assignments of several levels. While *ab initio* theory has progressed to the light tin isotopes for both energies and β -decay rates [26,27], it has been challenging to obtain converged calculations near 132 Sn [28,29]. Improved valence-space in-medium symmetry renormalization group (VS-IMSRG) calculations are presented, which are largely converged and are able to reproduce several low-lying levels in 132 Sn.

II. EXPERIMENT

The experiment was conducted at the Isotope Separator and Accelerator (ISAC) facility [30] at TRIUMF. A 9.8 μ A beam of protons was accelerated to 480 MeV in the main cyclotron and impinged onto a UC_x target, inducing spallation and fission reactions. The Ion Guide Laser Ion Source (IG-LIS) [31] was used to suppress surface-ionized elements. A beam of ¹³²In was selected by a high-resolution mass separator and sent to the experimental area in the ISAC-I hall at an energy of 28 keV.

The ¹³²In beam was delivered to the Gamma-Ray Infrastructure For Fundamental Investigations of Nuclei (GRIFFIN) [32,33]. Signals were read out and processed by the GRIFFIN

digital data-acquisition system [34]. GRIFFIN consists of 16 high-purity germanium clover detectors [35] arranged in a rhombicuboctahedral geometry. The clovers were placed at a distance of 11 cm from the beam implant position, leading to an absolute efficiency of about 14% at 1 MeV [33]. The high efficiency and energy resolution of GRIFFIN facilitated the observation of γ - γ coincidences that were used to build the level scheme in 132 Sn. To select γ rays originating from the decay of ¹³²In, the Scintillating Electron Positron Tagging Array (SCEPTAR) [33] was used to detect electrons emitted through β^- decay. SCEPTAR was located inside the vacuum chamber and consists of 20 plastic scintillators and covers approximately 80% of the solid angle around the beam implantation spot. Because of the large Q value of the 132 In $\beta^$ decay $[Q_{g.s.} = 14.140(60) \text{ MeV } [36]]$, a 2-cm-thick Delrin shield was placed around the vacuum chamber to prevent high-energy electrons from reaching the GRIFFIN detectors.

The beam was implanted onto a mylar tape system at the center of GRIFFIN and SCEPTAR. The tape was periodically moved to remove background events. The (7^-) ground state of ¹³²In has a half-life of 200(2) ms [37], and the activity on the tape saturated quickly. Tape cycles were chosen to maximize the implantation time and total decays of ¹³²In while reducing the activity from the subsequent decay of ¹³²Sn $[T_{1/2} = 39.7(8) \text{ s } [38]]$ as well as the build-up of ¹³²Cs contamination [$T_{1/2} = 6.480(6)$ d [38]]. A typical cycle consisted of tape moving and background measurement for 2 s, beam implantation for 30 s, and then 5 s of beam decay. During the background and decay portions of the cycle, the ¹³²In beam was deflected away from the GRIFFIN beamline by an electrostatic kicker. After cycling, the tape was moved into a lead-shielded box. During this experiment, ¹³²In was delivered at an average beam intensity of 70 pps over a period of 63 hours, providing a total of $5 \times 10^7 \beta$ -gated γ - γ coincidences.

Because of the short half-life of 132 In, only data taken during the beam implantation cycle were used for the spectroscopy. Contamination from 132 Cs was minimal and was almost completely eliminated by placing γ - γ coincidences on known transitions in 132 Sn. Several strong peaks in the β -decay granddaughter 132 Sb were observed, but these could also be eliminated from the analysis in the same way.

The relative efficiency of GRIFFIN was determined for the energy region up to 3.2 MeV by using standard sources of 133 Ba, 152 Eu, 60 Co, and 56 Co. Corrections to γ -ray intensities in the sources were made in order to account for real-coincidence summing. These were made by building a $180^{\circ} \gamma - \gamma$ coincidence matrix as described in Ref. [33].

In 132 Sn, there are three transitions above 4 MeV, where it was not possible to directly determine the efficiency using available sources. However, due to β -decay selection rules, the 2^+ state at 4.041 MeV is not directly populated by the β decay of the (7⁻) ground state in 132 In. Therefore, the relative efficiency above 4 MeV was tuned so that the intensity of the 4.041-MeV $2^+ \rightarrow 0^+$ transition matched the intensity of the 311- and 375-keV transitions which directly feed the 2^+ state. The intensities of these two low-energy transitions included the theoretical conversion coefficients calculated with the BrIcc code [39] with the frozen orbital approximation. The

relative efficiency curve determined from the sources was extrapolated out to 4.416 MeV, the highest-energy transition in the present analysis. Comparing the extrapolated efficiency curve with the tuned efficiency at 4.041 MeV gave a scale factor which was applied to the extrapolated efficiencies at 4.352 and 4.416 MeV.

Data from GRIFFIN was collected in addback mode, where hits from different germanium crystals within the same clover were combined into a single event. This method increased the photopeak signal while decreasing the Compton background. The time window for building addback coincidences was 300 ns. Summing corrections were also performed on the intensities of ¹³²Sn γ rays by using 180° coincidences. For weaker peaks which were only visible in gated spectra, summing corrections required more care. In these cases, corrections were made by requiring a γ - γ - γ triple coincidence condition in which the first hit was the strong y ray used to make the original gate. A second requirement that the remaining two ν rays be observed in detectors 180° apart provides a comparable analysis to the γ - γ coincidence method described in Ref. [33]. Signals from each crystal were linearly gain-matched by using two strong peaks in ¹³²Sn (375 and 4041 keV). Other relatively strong peaks were used to ensure that energies were well aligned among all the crystals.

III. RESULTS

A. β -delayed neutron spectroscopy

The Q_{β} value from the ground state of ^{132}In [14.140(60) MeV] is higher than the neutron separation energy in ^{132}Sn [7.353(4) MeV] [36], and ^{132}In has been observed to exhibit β -delayed neutron emission into the nucleus ^{131}Sn . The probability of one-neutron emission, P_n , has been measured previously by counting neutrons and β particles [23–25] with varied results. The current evaluated emission probability is 7.4(14)% [37], which is a weighted average of 6.8(14)% [24] and 10.7(33)% [25]. In the present experiment, it was possible to measure the P_n by counting γ rays in both ^{132}Sn and the A=131 daughters.

Allowed β decays from the (7^-) ground state in 132 In will populate states in 132 Sn with spin 6–8. Subsequent neutron emission from a highly excited state will populate states in 131 Sn with spin of at least 11/2. If either the β particle and antineutrino or the neutron carries away one unit of angular momentum from a unique first-forbidden β decay or l=1 neutron emission, then spins down to 9/2 are accessible. In 131 Sn, there is a low-spin $(3/2^+)$ ground state and high-spin $(11/2^-)$ isomer [40]. It is possible to populate this isomer with an allowed Gamow-Teller decay followed by the emission of an l=0 neutron. No other known levels in 131 Sn up to the $(15/2^-)$ level located 4102 keV above the isomer have high enough spin to be significantly populated in the βn decay, greatly reducing the energy available for neutron emission.

There are presently 19 γ -ray transitions listed in the ENSDF which feed either the $(3/2^+)$ ground state or $(11/2^-)$ isomer in ¹³¹Sn [40]. Of these, two transitions at 4220 and 4261 keV were identified in the current analysis. The 4220-

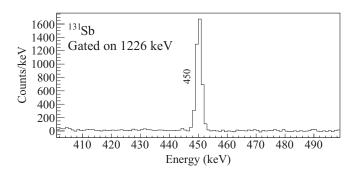


FIG. 1. A sample of the γ spectrum gated on the 1226-keV $(11/2^+) \rightarrow (7/2^+)$ transition in ¹³¹Sb, clearly demonstrating the sensitivity of the experiment to the β -delayed neutron decay of ¹³²In. The strong 450-keV transition feeds the 1226-keV level.

keV transition has been previously seen following the fission of 248 Cm and has been assigned to the decay of a $(13/2^+)$ level to the $(11/2^{-})$ isomer [8]. The transition at 4261 keV has been identified from the β decay of ¹³¹In [22,41]. It has been suggested to decay to the $(3/2^+)$ ground state [41]; however, the 4261-keV level has not been assigned any spin, and there are no coincident transitions. Based on the current observation, it is more likely that this level has a high spin and decays to the $(11/2^{-})$ isomer. The combined intensity of these two transitions yielded a total of $6.2(2) \times 10^{4}$ I31 Sn nuclei produced. The number of ¹³²Sn nuclei was calculated from the intensities of the three ground-state transitions (4041, 4352, and 4416 keV), giving $1.22(1) \times 10^7$ total nuclei. Comparing these numbers gives a P_n of 0.50(2)%. Although the statistical error is relatively small, there is a larger systematic uncertainty due to several effects. Most importantly, some of the transitions from high-spin levels, such as 4353 and 4423 keV, overlap with stronger transitions in ¹³²Sn, and there are not enough counts to identify $\gamma - \gamma$ coincidences. Additionally, there could be other unknown transitions which are not seen and would be difficult to assign to ¹³¹Sn without a full coincidence analysis. The measured 0.5% branch should be taken as a lower limit, because any decay directly to the $(11/2^{-})$ isomer would not be detected with the current setup. A βn decay to the isomer via an intermediate 6⁻ level was tentatively proposed in Ref. [6], although the proposed intermediate level is now known to lie below the neutron separation energy.

Although the tape cycling was used to remove contamination from the beam, including long-lived decay products, the 37-s cycle lasted long enough for much of the ¹³¹Sn daughter nuclei $[T_{1/2} = 56.0(5) \text{ s}, 58.4(5) \text{ s} [40]]$ to also β decay at the experimental station. Therefore, it was possible to perform limited spectroscopy on ¹³¹Sb. A sample γ -ray spectrum, gated on the 1226-keV $(11/2^+) \rightarrow (7/2^+)$ transition in ¹³¹Sb, is shown in Fig. 1. The peak at 450 keV clearly indicates the presence of ¹³¹Sb. A total of 19 γ -ray transitions belonging to ¹³¹Sb [40] were observed in the experiment. All of the transitions seen are displayed in the level scheme of Fig. 2. Relative γ -ray intensities and branching ratios are listed in Table I. Almost all of the spin assignments for the currently observed levels are in the range 9/2–15/2, indicating that

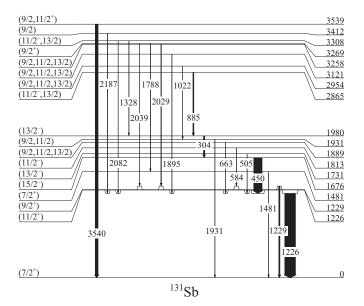


FIG. 2. A level scheme showing the transitions observed in 131 Sb following the β decay of the high-spin $11/2^-$ isomer in 131 Sn. The widths of the arrows are proportional to the observed γ -ray intensity. Energies are given in keV. Level energies are taken from the ENSDF [40].

these levels are much more likely to be fed from the $(11/2^-)$ isomer of $^{131}{\rm Sn}$, consistent with the expected βn feeding patterns from $^{132}{\rm In}$.

The number of ¹³¹Sb nuclei produced could be obtained from the observed intensities of the transitions. In particular, the intensities of four out of the five transitions which feed the ground state could be measured directly in the γ singles spectrum. Only the intensity of the 1481-keV transition could not be measured in singles. Direct β feeding to the $(7/2^+)$ 1481-keV level would constitute a unique first-forbidden transition, which is unlikely given the availability of higher-spin states. Therefore, it was assumed that this level had no direct β feeding, and the intensity of the 1481-keV transition was matched to the 1788-keV transition above it. Because the half-life of the isomer of ¹³¹Sn [58.4(5) s [40]] is longer than the decay portion of the tape cycle (5 s), it was necessary to make a correction to the observed intensities of those transitions to account for the fraction of nuclei which did not decay at the experimental station. The total number of ¹³¹Sb nuclei produced was determined to be $1.72(4) \times 10^6$, leading to a measured P_n of 12.3(4)%. This value is much larger than the one obtained from the γ -ray transitions in ¹³¹Sn and indicates that the βn decay of ¹³²In proceeds primarily through the $(11/2^-)$ isomer in ¹³¹Sn. This value is also larger than the current evaluated probability of 7.4(14)%, although it is in reasonable agreement with the most recent β -n counting experiment, which reported a value of 10.7(33)% [25]. In Ref. [25], the P_n values of several nuclei were tabulated. Among the tabulated results, many were consistent with previous results, but in the case of ¹³²In as well as a few others, the results were significantly larger. There was no general trend

TABLE I. A summary of the excited states and γ -ray transitions observed in ¹³¹Sb following the β decay of the high-spin 11/2⁻ isomer of ¹³¹Sn. For each transition, the initial and final levels, E_x and E_f , are listed along with the spins and parities $J_i^{\pi} \to J_f^{\pi}$ of the levels. Finally, the relative branching ratios BR $_{\gamma}$ are compared with the ENSDF [40], and relative intensities I_{γ} are compared with Ref. [42]. Level energies are taken from the ENSDF [40].

		$J_i^\pi o J_f^\pi$		BR_{γ} (rel.)		I_{γ} (rel.)	
E_x (keV)	E_{γ} (keV)		E_f (keV)	Present work	ENSDF	Present work	Ref. [42]
1226.04(3)	1226.5(3)	$(11/2^+) \to (7/2^+)$	0	100	100	100	100
1229.28(5)	1229.3(3)	$(9/2^+) \to (7/2^+)$	0	100	100(12)	11(5)	20.2
1481.15(3)	1481.5(5)	$(7/2^+) \rightarrow (7/2^+)$	0	100	100(4)	$1.6(5)^{a}$	
1676.06(6)	450.2(3)	$(15/2^-) \rightarrow (11/2^+)$	1226.04	100	100(11)	77(4)	72.6
1730.6(3)	504.6(3)	$(13/2^-) \rightarrow (11/2^+)$	1226.04	100	78(25)	3.3(6)	2.66
1812.93(13)	583.8(3)	$(11/2^-) \rightarrow (9/2^+)$	1229.28	100	100(19)	2.3(5)	4.9
1889.5(7)	663(1)	$(9/2, 11/2, 13/2) \rightarrow (11/2^+)$	1226.04	100		1.1(4)	2.6
1931.08(8)	1931(1)	$(9/2, 11/2) \rightarrow (7/2^+)$	0	100	100(22)	3(1)	8.1
1980.39(7)	304.4(5)	$(13/2^-) \rightarrow (15/2^-)$	1676.06	100	100(13)	$12(2)^{b}$	17.4
2865.47(10)	885.5(5)	$(11/2^-, 13/2) \rightarrow (13/2^-)$	1980.39	100	100(13)	8.6(7)	
2953.56(17)	1021.7(4)	$(9/2, 11/2, 13/2) \rightarrow (9/2, 11/2)$	1931.08	100	100(25)	1.8(3)	
3121.33(19)	1894.6(4)	$(9/2, 11/2, 13/2) \rightarrow (11/2^+)$	1226.04	100	88(20)	2.8(4)	
3258.58(18)	2029.2(3)	$(9/2, 11/2, 13/2) \rightarrow (9/2^+)$	1229.28	100	100(19)	4.8(6)	
3268.61(14)	1787.9(4)	$(9/2^+) \to (7/2^+)$	1481.15	52(15)	100(19)	1.6(5)	
	2039.0(4)	$(9/2^+) \to (9/2^+)$	1229.28	100	95(23)	3.1(5)	
3308.45(14)	1328.1(4)	$(11/2^-, 13/2) \rightarrow (13/2^-)$	1980.39	84(12)	70(13)	3.1(4)	
, ,	2082.4(5)	$(11/2^-, 13/2) \rightarrow (11/2^+)$	1226.04	100	100(26)	3.7(5)	
3411.91(20)	2186.9(5)	$(9/2) \to (11/2^+)$	1226.04	100	118(30)	3.1(4)	
3539.1(10)	3540.0(3)	$(9/2, 11/2^+) \rightarrow (7/2^+)$	0	100	100	26(3)	

^aCalculated from intensity of the 1788-keV transition.

^bCalculated from intensities of the 885- and 1328-keV transitions.

to measure larger values, and it is not clear why the previous measurements were smaller for the case of ¹³²In.

B. Spectroscopy of ¹³¹Sb

New spin and parity assignments have been determined for several known levels in ¹³¹Sb. In particular, the levels at 1889, 2865, 2954, 3121, 3258, 3269, and 3539 keV were assumed to be directly fed from the β decay of the $(11/2^{-})$ isomer of 131 Sn, limiting the spins to (9/2, 11/2, 13/2)for allowed or first-forbidden transitions. Several of these spins and parities can be restricted further based on γ -ray feeding patterns. The 2865-keV level was previously assigned a tentative spin of (11/2, 13/2, 15/2) based on γ -ray feeding patterns, including a weak transition to the 1676-keV $(15/2^{-})$ level. Thus, this level is assigned a tentative spin of (11/2⁻, 13/2). The 3269-keV level was previously assigned a tentative spin of (5/2, 7/2, 9/2) based on γ -ray feeding patterns. The current observation of direct β feeding of this level suggests a spin of $(9/2^+)$. The level at 3308 keV was observed to decay to the 1226-keV (11/2⁺) and 1980keV $(13/2^{-})$ levels. Previously, a weak transition to the 1916keV $(15/2^{-})$ level was also observed [40]. As a result, the 3308-keV level is assigned a tentative spin of $(11/2^-, 13/2)$. The 3539-keV state is observed to decay to the $(7/2^+)$ ground state, restricting this state to $(9/2, 11/2^+)$. Finally, the state at 1931 keV was previously given a tentative spin assignment of (7/2, 9/2, 11/2) based on γ -ray feeding patterns. The intensities of the 1931- and 1022-keV transitions indicate that there is a small amount of direct β feeding to this state, restricting the spin to (9/2, 11/2).

C. Spectroscopy of ¹³²Sn

A total of $5 \times 10^8 \ \gamma$ -addback events and $1.1 \times 10^8 \ \gamma$ - γ coincidence events were observed in the analysis. Based on the γ - γ statistics, a total of 70 transitions have been placed along with 29 excited states. A sample of the β -coincident spectrum gated on the 375-keV $4^+ \to 2^+$ transition is shown in Fig. 3. A total of 53 transitions were observed in coincidence with this gate, with relative intensities down to 0.14%. The γ - γ coincidence analysis was used to construct the level scheme which can be seen in Fig. 4.

A list of all observed excited states and γ -ray transitions with their measured intensities is shown in Table II. Intensities could be determined directly from the addback singles spectrum for 41 of the 70 transitions, while the intensities for the remaining 29 transitions were determined from gated spectra. The γ intensities are reported relative to the 4.041-MeV $2^+ \rightarrow 0^+$ transition. Because the efficiency at 4.041 MeV was tied to the efficiency in the 300-keV region, the relative uncertainty on the efficiency at this energy could be limited to 0.4%, even though the relative uncertainty on the extrapolated source efficiency curve was much larger above 4 MeV. Therefore, for strong peaks with a statistical uncertainty of $\leq 0.4\%$, the uncertainty on the relative intensity is less than 1%. In Table II, γ intensities and branching ratios are compared with the evaluated values. It is difficult to determine the level of agreement for many of the transitions, because the

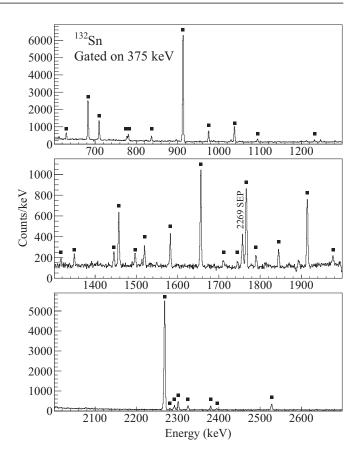


FIG. 3. A sample of the β - γ spectrum gated on the 375-keV $4^+ \rightarrow 2^+$ transition in 132 Sn. The black squares highlight some of the coincident peaks which could be identified and placed in the level scheme.

uncertainties in the intensities were not reported by Fogelberg *et al.* [5]. Instead, errors listed in the table were assigned by the evaluators. However, there is generally good agreement between the current and evaluated intensities.

Prior to the recent work by Benito *et al.* [43], the most comprehensive β -decay study performed placed 21 excited states and 44 transitions in the level scheme [5]. Of these, 20 excited states and 42 transitions have been confirmed in the current work. The 70-keV transition which feeds the 8^+ level at 4848 keV was not seen. Another transition at 774 keV and the level it depopulates at 6173 keV could not be confirmed. However, both the 1457- and 1038-keV transitions previously associated with this level were observed. The observation of a 355-keV transition in coincidence with the 1457-keV transition suggests a reordering of the 1457- and 1038-keV transitions and the placement of a level at 5754 keV. A possible 89-keV transition suggested by Björnstad *et al.* [6] to decay from the level at 4919 keV was seen neither by Fogelberg *et al.* [5] nor in the current work.

A 431-keV transition from a level at 5280 keV was reported to be in delayed coincidence with the 132-keV (8⁺) \rightarrow (6⁺) transition from a fission experiment [8]. This transition was assigned to be from a (9⁺) based on systematic comparisons with ²⁰⁸Pb. This level was observed in the current experiment, and the β feeding to this level was measured.

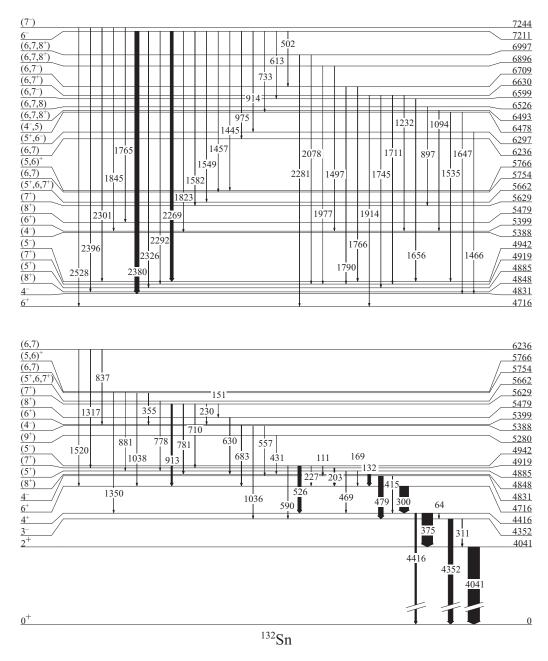


FIG. 4. A level scheme showing the transitions observed in 132 Sn following the β^- of 132 In. The widths of the arrows are proportional to the observed γ -ray intensity. Energies are given in keV. The two parts of the level scheme are not drawn to scale to each other.

A recent experiment on the βn decay of ¹³³In [14] also observed several new transitions at 1030, 1350, and 1374 keV. The 1350-keV transition and the 5766-keV level which it depopulates were confirmed in the present work. The placement of this level was supported by the additional observation of a 1445-keV transition which feeds it from the 7211-keV 6⁻ level, as well as an 881-keV transition which decays from this level to the 4885-keV (5⁺) level. Neither the 1030-keV transition nor the 1374-keV transition could be confirmed.

From the measured γ -ray intensities, the apparent direct β feeding to excited states in $^{132}{\rm Sn}$ could be calculated. The feeding calculations take into account theoretical conversion

coefficients, calculated using the BrIcc code [39] with the frozen orbital approximation. Direct feeding could be observed into 22 of the 30 levels, with upper limits placed on four additional levels. Based on the feeding intensities, $\log ft$ values could be calculated for the excited states. The feeding intensities and $\log ft$ values are listed in Table III. Intensities have been calculated with a 12.3% β -delayed neutron decay branch.

Spin and parity assignments for levels were primarily based on γ feeding patterns, as well as $\log ft$ values. The spins of several excited states with previous assignments have been restricted based on the observation of additional γ rays.

TABLE II. A summary of the excited states and γ -ray transitions observed in ¹³²Sn following the β decay of ¹³²In. For each transition, the initial and final levels, E_x and E_f , are listed along with the spins and parities $J_i^{\pi} \to J_f^{\pi}$ of the levels. Finally, the relative branching ratios BR $_{\gamma}$ and relative intensities I_{γ} are compared with the ENSDF [44].

				BR_{γ} (rel.)		I_{γ} (rel.)	
E_x (keV)	E_{γ} (keV)	$J_i^\pi o J_f^\pi$	E_f (keV)	Present work	ENSDF ^a	Present work	ENSDF ^a
4041.2(2)	4041.24(20)	$2^+ \rightarrow 0^+$	0	100	100	100	100(5)
4351.9(2)	310.74(20)	$3^- \rightarrow 2^+$	4041.1	11.7(3)	11(1)	4.9(1)	4.7(5)
	4351.88(21)	$3^- \rightarrow 0^+$	0	100	100	41.8(4)	42(2)
4416.3(2)	64.4(2)	$4^+ \rightarrow 3^-$	4351.9	0.8(4)	1.3(2)	0.8(4)	1.2(2)
	375.07(20)	$4^+ \rightarrow 2^+$	4041.1	100	100	93.4(8)	93(5)
	4416.22(20)	$4^+ \rightarrow 0^+$	0	15.8(2)	17(1)	14.7(2)	15.6(8)
4715.9(3)	299.59(20)	$6^+ \rightarrow 4^+$	4416.3	100	100	78.7(6)	73(4)
4830.9(3)	414.66(21)	$4^- \rightarrow 4^+$	4416.3	1.76(6)	2.1(5)	0.76(3)	0.8(2)
. ,	479.03(20)	$4^- \rightarrow 3^-$	4351.9	100	100	42.9(4)	40(2)
4848.4(4)	132.49(22)	$(8^+) \to 6^+$	4715.9	100	100	27.3(3)	22(1)
4885.4(3)	169.4(3)	$(5^+) \to 6^+$	4715.9	10(3)	20(7)	0.16(5)	0.28(9)
. ,	469.15(21)	$(5^+) \rightarrow 4^+$	4416.3	100	100	1.63(4)	1.4(2)
4919.0(3)	203.12(20)	$(7^+) \rightarrow 6^+$	4715.9	100	100	8.4(3)	7.0(7)
4942.4(3)	111.43(20)	$(5^-) \rightarrow 4^-$	4830.9	11.0(2)	9(1)	3.19(5)	2.7(3)
13 121 1(0)	226.64(21)	$(5^{-}) \to 6^{+}$	4715.9	2.7(2)	2.8(6)	0.78(4)	0.8(2)
	526.12(20)	$(5^-) \rightarrow 4^+$	4416.3	100	100	29.1(3)	30(2)
	590.45(21)	$(5^-) \rightarrow 3^-$	4351.9	4.5(1)	7(1)	1.31(4)	2.0(3)
5279.7(5)	431.3(3)	$(9^+) \to (8^+)$	4848.4	100	,(1)	0.4(1)	2.0(3)
5387.8(3)	556.8(3)	$(4^-) \rightarrow 4^-$	4830.9	12.4(6)		0.15(2)	
3307.0(3)	1035.71(22)	$(4^-) \rightarrow 3^-$	4351.9	100	100	1.18(6)	1.3(2)
5398.9(4)	682.96(21)	$(6^+) \rightarrow 6^+$	4715.9	100	100	4.60(8)	4.9(5)
5478.7(4)	630.24(20)	$(8^+) \rightarrow (8^+)$	4848.4	100	100	5.02(6)	6.4(7)
5628.9(3)	150.6(4)	$(7^+) \rightarrow (8^+)$	5478.7	1.9(1)	100	0.25(2)	0.4(7)
3020.9(3)	230.03(22)	$(7^+) \rightarrow (8^+)$ $(7^+) \rightarrow (6^+)$	5398.9	6.8(3)	7(2)	0.23(2)	0.9(2)
	709.95(21)	$(7^+) \rightarrow (0^-)$ $(7^+) \rightarrow (7^+)$	4919.0	18.1(4)	23(3)	2.45(4)	3.0(4)
	780.59(21)	$(7^+) \rightarrow (7^+)$ $(7^+) \rightarrow (8^+)$	4848.4				
		$(7^+) \rightarrow (8^+)$ $(7^+) \rightarrow 6^+$	4715.9	37.2(6)	29(4) 100	5.04(6)	3.8(4)
5660 4(4)¢	913.08(20)	$(5^+, 6, 7^+) \rightarrow (5^+)$		100 100	100	13.6(1)	13.1(9)
5662.4(4)°	777.96(21)		4885.4			0.17(1)	
5754.2(4) ^c	355.01(25)	$(6,7) \to (6^+)$	5398.9	18(2)		0.34(3)	1.4(2)
57.66 0(2)¢	1037.76(21) ^d	$(6,7) \to 6^+$	4715.9	100		1.84(4)	1.4(2)
5766.0(3) ^c	881.1(3)	$(5,6)^+ \to (5^+)$	4885.4	38(5)		0.095(8)	
(22(0/4))	1349.75(22)	$(5,6)^+ \to 4^+$	4416.3	100		0.25(3)	
6236.0(4) ^c	836.8(3)	$(6,7) \to (6^+)$	5398.9	59(4)		0.48(2)	
	1317.0(3)	$(6,7) \rightarrow (7^+)$	4919.0	17(3)	400	0.14(2)	0.74(0)
<	1520.0(3)	$(6,7) \rightarrow 6^+$	4715.9	100	100	0.81(4)	0.56(9)
6297.3(5) ^c	1466.4(4)	$(5^+, 6^-) \to 4^-$	4830.9	100		0.16(3)	
6477.7(5) ^c	1646.5(4)	$(4^-, 5) \to 4^-$	4830.9	100		0.25(3)	
	1535.1(5)	$(4^-, 5) \to (5^-)$	4942.4	22(7)		0.05(2)	
6492.6(5)	1093.7(3)	$(6,7,8^+) \rightarrow (6^+)$	5398.9	100		0.45(2)	
6526.1(5)	897.2(3)	$(6,7,8) \rightarrow (7^+)$	5628.9	100		0.26(2)	
6598.5(4)	1656.05(21)	$(6,7^-) \to (5^-)$	4942.4	100	100	3.88(6)	3.8(4)
6630.3(4) ^c	1231.8(3)	$(6,7^+) \to (6^+)$	5398.9	10.9(7)		0.24(1)	
	1711.4(3)	$(6,7^+) \to (7^+)$	4919.0	10.6(6)		0.24(1)	
	1745.1(3)	$(6,7^+) \to (5^+)$	4885.4	6.2(6)		0.14(1)	
	1914.45(21)	$(6,7^+) \rightarrow 6^+$	4715.9	100	100	2.22(8)	2.1(3)
6709.1(4)	1766.59(21)	$(6,7^-) \rightarrow (5^-)$	4942.4	100	100	3.01(7)	4.1(5)
	1789.9(3)	$(6,7^-) \to (7^+)$	4919.0	8.8(5)		0.26(1)	
6895.9(5) ^c	1497.2(3)	$(6, 7, 8^+) \rightarrow (6^+)$	5398.9	100		0.38(4)	
	1976.9(3)	$(6,7,8^+) \rightarrow (7^+)$	4919.0	94(18)	100	0.35(6)	0.37(9)
6997.2(4) ^c	2078.2(3)	$(6,7,8^+) \rightarrow (7^+)$	4919.0	45(8)		0.21(3)	
	2281.4(3)	$(6, 7, 8^+) \rightarrow 6^+$	4715.9	100		0.46(3)	
7211.1(4)	501.81(22)	$6^- \to (6, 7^-)$	6709.1	2.7(1)	2.9(5)	1.01(4)	1.1(2)
	612.7(3)	$6^- \to (6, 7^-)$	6598.5	0.92(5)		0.35(2)	. ,
	733.4(3)	$6^- \to (4^-, 5)$	6477.7	0.83(8)		0.32(3)	

TABLE II. (Continued.)

	E_{γ} (keV)	$J_i^\pi \! o \! J_f^\pi$	E_f (keV)	BR_{γ} (rel.)		I_{γ} (rel.)	
E_x (keV)				Present work	ENSDF ^a	Present work	ENSDF ^{ab}
	913.8(3)	$6^- \to (5^+, 6^-)$	6297.3	0.17(1)		0.063(6)	
	975.0(3)	$6^- \to (6,7)$	6236.0	2.11(7)		0.80(2)	
	1445.34(25)	$6^- \to (5,6)^+$	5766.0	0.61(4)		0.23(1)	
	$1457.24(22)^{d}$	$6^- \to (6,7)$	5754.2	3.7(1)		1.39(4)	1.4(2)
	1548.6(3)	$6^- \rightarrow (5^+, 6, 7^+)$	5662.4	0.28(1)		0.106(6)	
	1582.22(21)	$6^- \to (7^+)$	5628.9	3.2(1)	3.1(2)	1.21(4)	1.2(2)
	1823.1(3)	$6^- \to (4^-)$	5387.8	3.9(2)	3.1(5)	1.49(8)	1.2(2)
	2268.62(21)	$6^- \to (5^-)$	4942.4	71(1)	67(5)	27.2(4)	26(1)
	2292.1(3)	$6^- \to (7^+)$	4919.0	2.62(9)	3.1(5)	1.00(3)	1.2(2)
	2325.6(3)	$6^- \to (5^+)$	4885.4	2.35(8)	1.9(5)	0.90(3)	0.8(2)
	2380.24(20)	$6^- \rightarrow 4^-$	4830.9	100	100	38.1(5)	39(2)
7243.9(4)	1764.93(21)	$(7^{-}) \rightarrow (8^{+})$	5478.7	100	88(17)	2.51(4)	2.0(3)
	1844.7(3)	$(7^-) \to (6^+)$	5398.9	19.3(6)		0.48(1)	
	2301.33(21)	$(7^{-}) \rightarrow (5^{-})$	4942.4	92(5)	79(16)	2.3(1)	1.8(3)
	2395.6(3)	$(7^{-}) \rightarrow (8^{+})$	4848.4	88(2)	100	2.21(5)	2.2(3)
	2528.21(21)	$(7^-) \rightarrow 6^+$	4715.9	59(2)	75(16)	1.49(4)	1.7(3)

^aThe evaluator assigned 5% uncertainty for $I_{\nu} > 10$ values, 10% for $I_{\nu} = 3$ –10 and 15% for $I_{\nu} < 3$.

The level at 5766 keV was not previously assigned any spin. In the present work, the spin and parity of this level were determined to be $(5,6)^+$ based on the observation of γ -ray transitions to the 4885- (5⁺) and 4416-keV 4⁺ levels and a log ft value which is consistent with first-forbidden or unique first-forbidden decay. The level at 6236 keV was previously given a range of spins of $(6, 7, 8^+)$, based on γ -ray feeding patterns. The presently observed 975-keV transition feeds this level from the (6⁻) level at 7211 keV, which eliminates an 8⁺ assignment, so the reported spin is (6,7). The level at 6630 keV was also given a range of spins of (6, 7, 8⁺) based on γ -ray feeding patterns. Several transitions from this state have been observed, including a 1745-keV transition which connects this level to the (5⁺) level at 4885 keV. This rules out the possibility of an 8⁺ or 7⁻ spin, and the current reported spin is $(6, 7^+)$. The level at 6896 keV was assigned a range of (6,7,8) based on γ -ray feeding patterns. The presently observed 1497-keV transition to the (6⁺) level at 5398 keV restricts this level to $(6, 7, 8^+)$.

Spins and parities have also been tentatively assigned for other levels identified in the current work. The level at 5662 keV is fed from the 7211-keV 6^- level and decays to the 4885-keV (5^+) level. It also has a small amount of direct β feeding, and the $\log ft$ value is consistent with first-forbidden or unique first-forbidden decay. Therefore, this level is assigned a tentative spin of $(5^+, 6, 7^+)$. The level at 5754 keV is fed from the 7211-keV 6^- level and decays to two 6^+ levels; the $\log ft$ value is consistent with an allowed or first-forbidden transition. This level is therefore assigned a tentative spin of (6,7). The 6297-keV level is fed from the 7211-keV 6^- level and decays to the 4831-keV (4^-) level. The $\log ft$ value is consistent with either an allowed or unique first-forbidden transition, and this level is assigned

a tentative spin of $(5^+, 6^-)$. The level at 6478 keV is fed from the 7211-keV 6^- level and decays to the 4831-keV 4^- and 4942-keV (5^-) levels. It has a β feeding component with a two-sigma limit <0.04%, suggesting that it is not an allowed or first-forbidden transition. This level is assigned a tentative spin of $(4^-, 5)$. Three levels at 6493, 6526, and 6997 keV are directly fed from the β decay of 132 In. The log ft values for these levels are consistent with allowed or first-forbidden transitions, limiting the spins to (6,7,8). In addition, the 6493-and 6997-keV levels decay to known (6^+) levels, further restricting their spins to $(6,7,8^+)$.

D. Half-life of ¹³²In

The half-life of 132 In was measured by plotting the γ -ray counts as a function of time and placing gates on several of the strongest transitions in 132 Sn. Gates were placed on intense transitions at 300, 375, 2269, 2380, 4041, 4352, and 4416 keV, with background subtraction for each gate. The results are shown in Fig. 5. The decay was fit with a simple exponential function $f(t) = A + Be^{-\lambda t}$. The best-fit half-life based on the χ^2 of the fit is $T_{1/2} = 194(4)$ ms. A "chop-analysis" was performed by adjusting the range of the fit region to take into account possible rate-dependent effects. The result is a small increase in the systematic error. Therefore, the reported value of the half-life is 194(5) ms. This agrees with the evaluated value of 200(2) ms [37].

E. Angular correlations

It was possible to perform angular correlations by using the γ -ray cascades in ¹³²Sn. Angular correlations have the general

^bRelative intensities have been multiplied by 100/107.

^cSpins and parities determined in present work. See text for details.

^dTransition moved within the level scheme. See text for details.

TABLE III. Calculated β -feeding intensities and $\log ft$ values for the excited states in 132 Sn from the β decay of the (7⁻) ground state of 132 In. Feeding calculations take into account theoretical conversion coefficients, calculated using the BrIcc code [39] with the frozen orbital approximation. Values from the current work are calculated with a 12.3% β -delayed neutron decay branch. Limits for the current intensities are given at the two-sigma level. ENSDF values were calculated by the evaluators from the level scheme of Fogelberg $et\ al.$ [5] with a 7.4% β -delayed neutron branch and assuming 5%–15% errors on γ intensities. Where different $\log ft$ values are possible based on spin assignments, unique transitions are listed below nonunique transitions.

		I_{β} (%)		$\log ft$	
E_x (keV)	J^π	Present	ENSDF	Present	ENSDF
4041	2+	0	0		
4352	3-	0	0		
4416	4^{+}	0	0		
4716	6+	1.3(4)	5(3)	6.7(1)	6.1(3)
4831	4^{-}	<1.1	0	>11.5ª	
4848	(8^{+})	17.4(2)	13(2)	5.57(2)	5.7(1)
4885	(5^{+})	0.29(4)	0.6(2)	$9.65(7)^{b}$	9.3(2)
4919	(7^{+})	2.5(2)	2.0(5)	6.39(3)	6.5(1)
4942	(5^{-})	< 0.1		>7.8	
5280	(9^{+})	0.23(6)		$9.6(1)^{b}$	
5388	(4^{-})	< 0.02	0	>13ª	
5399	(6^{+})	0.70(6)	2.1(4)	6.84(4)	6.4(1)
5479	(8^{+})	1.24(4)	2.6(5)	6.57(2)	6.3(1)
5629	(7^{+})	11.7(1)	11.5(8)	5.57(2)	5.57(4)
5662	$(5^+, 6, 7^+)$	0.033(7)		8.1(1)	
				$10.4(1)^{b}$	
5754	(6,7)	0.45(4)		6.95(5)	
5766	$(5,6)^+$	0.07(2)		7.8(2)	
				$10.0(1)^{b}$	
6236	(6,7)	0.35(8)	0.33(6)	6.9(1)	7.0(1)
6297	$(5^+, 6^-)$	0.06(2)		7.7(1)	
				$9.9(1)^{b}$	
6478	$(4^-, 5)$	< 0.04		$> 10^{b}$	
				>12ª	
6493	$(6, 7, 8^+)$	0.25(1)		7.02(2)	
6526	(6,7,8)	0.148(9)		7.24(4)	
6599	$(6, 7^{-})$	1.98(4)	2.3(3)	6.10(2)	6.0(1)
6630	$(6, 7^+)$	1.59(5)	1.2(2)	6.19(2)	6.3(1)
6709	$(6, 7^{-})$	1.27(5)	1.8(3)	6.26(2)	6.1(1)
6896	$(6, 7, 8^+)$	0.41(4)	0.22(6)	6.71(5)	7.0(1)
6997	$(6, 7, 8^+)$	0.38(2)		6.71(3)	
7211	6^-	41.6(4)	42(2)	4.61(2)	4.61(3)
7244	(7-)	5.05(8)	4.5(4)	5.52(2)	5.57(5)

^aUnique second-forbidden transition.

form

$$W(\theta) = A_{00}[1 + a_2 P_2(\cos \theta) + a_4 P_4(\cos \theta)]. \tag{1}$$

Here, θ is the angle between successive γ rays emitted in cascade, A_{00} is a normalization factor, a_2 and a_4 are coefficients which depend on the multipolarities and mixing ratios of the γ -ray transitions, and $P_i(\cos \theta)$ are the Legendre polynomials.

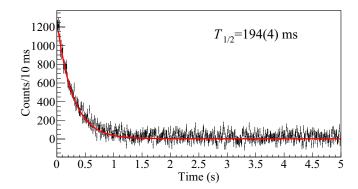


FIG. 5. The lifetime measurement for the decay of the (7^-) ground state in 132 In. Shown is a background-subtracted sum of gates on transitions at 300, 375, 2269, 2380, 4041, 4352, and 4416 keV in 132 Sn, plotted as a function of the time since the beam was blocked. The best-fit curve is shown in red, which gives a half-life of 194(4) ms.

Details about angular-correlation analysis with GRIFFIN can be found in Ref. [45]. A similar analysis obtaining angular correlations with the current experimental setup has been performed in Ref. [46] and with a different setup in Ref. [47]. For the angular correlations, clover addback was not used; instead, photopeaks were measured by using the 64 single crystals. The geometry of the HPGe detectors within GRIFFIN creates 51 distinct angles between pairs of detector crystals, ranging from 19° to 180°. In the present analysis, the 51 angles were grouped into 22 points in order to increase statistics for each data point. Angles used in the grouped analysis were calculated as a weighted average of the original angular pairs; each grouped angle had between one and five original angles. The data were also folded around 90° because of the symmetry of the correlations, resulting in 11 points.

To fit the experimental angular correlations to Eq. (1), it was necessary to take into account the finite-size effects of GRIFFIN, which tend to attenuate the a_2 and a_4 coefficients. Therefore, simulations were performed according to Method 2 of Ref. [45]. The simulations were based on the GEANT4 toolkit [48] with an additional extension to the radioactive decay classes to reproduce physical angular correlations [49]. For each cascade, three simulations were performed that match the following distributions:

$$\mathcal{Z}_0(\theta) = 1,\tag{2}$$

$$\mathcal{Z}_2(\theta) = 1 + P_2(\cos \theta),\tag{3}$$

$$\mathcal{Z}_4(\theta) = 1 + P_4(\cos \theta). \tag{4}$$

 \mathcal{Z}_2 and \mathcal{Z}_4 represent nearly pure Legendre polynomials and are simulated individually so that the attenuation effects can be separated. \mathcal{Z}_0 is a simulation with no angular-correlation effects and is used to normalize the outputs of the \mathcal{Z}_2 and \mathcal{Z}_4 simulations. A linear combination of these simulations was used to fit to the data:

$$\mathcal{Z}_{\text{sum}} = A_{00}[(1 - a_2 - a_4)\mathcal{Z}_0 + a_2\mathcal{Z}_2 + a_4\mathcal{Z}_4]. \tag{5}$$

The simulated data were grouped and folded in the same manner as the experimental data. A sample angular correlation

^bUnique first-forbidden transition.

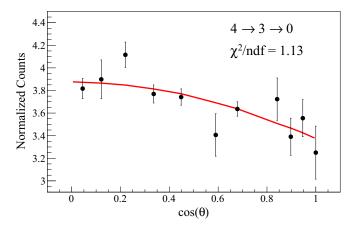


FIG. 6. The best-fit angular correlation for the 479–4352-keV $4^- \rightarrow 3^- \rightarrow 0^+$ cascade in ¹³²Sn. The experimental data points are shown in black, and the simulated curve is shown in red. The fit corresponds to an E2/M1 mixing ratio of 0.02(2) for the 479-keV $4^- \rightarrow 3^-$ transition.

is presented in Fig. 6, which shows a fit to the 479–4352-keV $4^- \rightarrow 3^- \rightarrow 0^+$ cascade in 132 Sn.

For many of the angular correlations described in Ref. [45], a mixing ratio is determined for a particular transition by performing a series of fits and varying the mixing ratio. By adjusting the mixing ratio of either γ -ray transition in a cascade, theoretical values for a_2 and a_4 can be calculated, which are input into Eq. (5). Then the simulated curve is fit to the experimental data with A_{00} as a free parameter, and the χ^2 of the fits can be determined as a function of δ . The minimum χ^2 then determines the best-fit mixing ratio. This process was performed for the 479–4352-keV $4^- \rightarrow 3^- \rightarrow 0^+$ cascade shown in Fig. 6. The 4352-keV transition is constrained by the 0^+ ground state to be a pure E3 transition. However, the 479-keV transition between the 4⁻ and 3⁻ states can have a mixed E2/M1 multipolarity. Therefore, the points were fit by varying the mixing ratio of the 479-keV transition. In the figure, the best-fit curve is shown along with the experimental data points, which corresponds to an E2/M1 mixing ratio of 0.02(2), consistent with a pure M1 transition.

Three other angular correlations were analyzed in the current work; these are listed along with the 479–4352-keV cascade in Table IV. In general, the procedure for cascades without pure transitions is complex because of the two free

TABLE IV. A summary of the γ -ray angular correlations for select cascades in $^{132}{\rm Sn}$. Listed are the first and second γ -ray transitions $E_{\gamma 1}$ and $E_{\gamma 2}$, the spin cascade used to calculate coefficients, and the reduced χ^2 resulting from the fit. The fits were made with the mixing ratios of both transitions set to zero, as discussed in the text.

$E_{\gamma 1}$ (keV)	$E_{\gamma 2}$ (keV)	Cascade	χ^2/ndf
375	4041	$4^+ \rightarrow 2^+ \rightarrow 0^+$	1.04
300	375	$6^+ \rightarrow 4^+ \rightarrow 2^+$	1.91
479	4352	$4^- ightarrow 3^- ightarrow 0^+$	1.29
2380	479	$6^- \rightarrow 4^- \rightarrow 3^-$	0.78

mixing ratios. The correlations in Table IV were approximated by looking at the χ^2 assuming zero mixing for both transitions in the cascades. Like the 4352-keV transition, the multipolarity of the 4041-keV transition was fixed by the 0⁺ ground state. The 375-, 300-, and 2380-keV transitions are E2, and E3 mixing is not expected to occur. Because the mixing ratio for the 479-keV transition determined from the E3 minimization was consistent with zero, this value was also used in the fit of the 479-4352-keV cascade. In all cases, the reduced E3 values are reasonable, confirming the spin and parity assignments of these states.

IV. THEORETICAL CONSIDERATIONS

Predictions for the excitation spectrum in 132Sn have been made using the ab initio VS-IMSRG. The VS-IMSRG [50–55] provides a prescription to generate approximately unitary transformations to decouple first a desired core energy followed by an appropriate valence-space Hamiltonian from the larger Hilbert space. Calculations began with the 1.8/2.0(EM) chiral interaction of Refs. [56–58], within a harmonic-oscillator basis of 15 major shells (i.e., e = 2n + $l \leqslant e_{\rm max} = 14$). This interaction has been found to successfully reproduce ground-state and excitation energies throughout the medium- to heavy-mass region, including dripline properties [26,58,59]. The interaction was transformed to the Hartree-Fock basis and capture effects of 3N forces among valence nucleons with the ensemble normal ordering described in Ref. [54]. Finally, for storage requirements, a cut of $e_1 + e_2 + e_3 \leqslant E_{3\text{Max}}$ was imposed for 3N matrix elements.

The IMSRG++ code [60], adopting the Magnus formulation of the IMSRG [52,61], was used to generate transformations to perform the above decouplings, where in the IMSRG(2) approximation, all induced operators are truncated at the two-body level. For the region near 132 Sn, a core of 92 Ni was used, and a valence-space Hamiltonian was decoupled for the $(0g_{7/2}, 1d_{5/2}, 1d_{3/2}, 2s_{1/2})$ proton orbits and $(1d_{3/2}, 2s_{1/2}, 0h_{11/2}, 1f_{7/2}, 2p_{3/2})$ neutron orbits. Finally, the resulting valence-space Hamiltonians were diagonalized with the KSHELL shell-model code [62] to obtain ground- and excited-state energies.

For heavier systems near 132 Sn, as mentioned earlier, achieving convergence with respect to $E_{3\text{Max}}$ has been the primary bottleneck to fully exploring the heavy region of nuclei. For example, in recent calculations near 132 Sn [28,29,63], energies were clearly not converged even at the $E_{3\text{Max}} = 18$ level, which was the previous computational limit. Very recently, however, significant advances in treatment of 3N matrix elements have been made which allow extension to at least $E_{3\text{Max}} = 28$ [64]. Here the ground-state energy is converged to better than 5 MeV (i.e., 0.5%), and excited states are converged to better than 100 keV with $E_{3\text{Max}} = 22$ [64].

The results of these calculations are shown in Fig. 7 alongside the experimental values. The calculated ground-state energy agrees quite well with the experimental value, at the level of approximately 1%. The theoretical spectra is shown up to 8 MeV, and the experimental spectrum is shown for the positive-parity states up to the 9^+ level at 5280 keV and for the negative-parity states up to the 5^- level at 4942 keV.

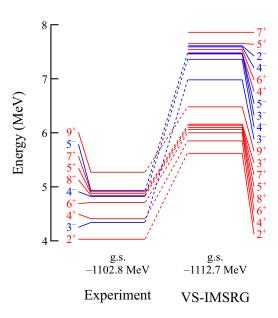


FIG. 7. A sample of the low-lying excited states in ¹³²Sn from experiment (left) and calculated with the VS-IMSRG (right). Positive-parity states are shown in red, and negative-parity states in blue. The calculated levels are shown up to 8 MeV and are connected to experimental levels by dashed lines where the levels can be directly matched. The experimental and calculated ground-state (g.s.) energies are also listed below the graph.

These levels can be most directly compared with the theoretical spectrum, and are connected to their theoretical counterparts in the figure. The lowest 1⁻ state is omitted from the figure, because it is highly sensitive to the center-ofmass correction discussed in recent cross-shell VS-IMSRG calculations [65]. The energy of the measured and calculated ground state is also listed in the figure. Comparing the spectra, there is a general ≈1.5-MeV shift for the positive-parity states, and a 2.5-MeV shift for the negative-parity states. This trend is a common feature of ab initio calculations truncated at the two-body level as is done in the IMSRG(2) approximation [65,66], and significant improvement in this respect is expected when calculations are eventually advanced to the IMSRG(3) level. Besides this shift, the ordering of positive-parity and negative-parity states are each individually well reproduced. Additionally, the spacing between levels of the same parity is well matched, within 100 keV for almost all levels, indicating the ab initio theory is well suited to describing energies in this region.

V. CONCLUSION

The analysis of the β and βn decay of ¹³²In using the GRIFFIN spectrometer is presented. The half-life of the decay has been confirmed, and the β -delayed neutron emission probability of 12.3(4)% has been measured for the first time with γ rays. Comparison of the γ rays in ¹³¹Sn and ¹³¹Sb indicates that the βn decay proceeds primarily through the high-spin $(11/2^-)$ isomer in ¹³¹Sn. Analysis of the γ rays in ¹³¹Sb following the decay of the isomer allowed for several new spin and parity assignments. This characterization of the decay will also provide valuable input to astrophysical r-process calculations. Within 132 Sn, 70 γ -ray transitions among 29 excited states have been identified with precise β -feeding and log ft values calculated for the excited states, and these have been used to provide more restricted spin and parity assignments for several levels. Angular correlations were able to confirm the spin assignments of a few of the strongly fed states. Finally, VS-IMSRG calculations were presented which reproduce the spacing of several of the excited states.

Note added. Recently, the authors learned of a similar article discussing additional results from ISOLDE [43] in which 68 new γ -ray transitions and 17 new levels were observed in $^{132}{\rm Sn}$ from both the β decay of $^{132}{\rm In}$ and βn decay of $^{133}{\rm In}$. Due to the timing of this publication, the results of this experiment are not discussed here.

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