Photoproduction of charged final states in ultraperipheral collisions and electroproduction at an electron-ion collider

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Ultraperipheral collisions (UPCs) of relativistic ions are an important tool for studying photoproduction at high energies. Vector-meson photoproduction is an important tool for nuclear structure measurements and other applications. A future electron-ion collider (EIC) will allow additional studies, using virtual photons with a wide range of Q^2 . We propose a significant expansion of the UPC and EIC photoproduction physics programs to include charged final states which may be produced via Reggeon exchange. We consider two examples: $a_2^+(1320)$, which is a conventional $q\bar{q}$ meson, and the exotic $Z_c^+(4430)$ state (modeled here as a tetraquark). The $Z_c^+(4430)$ cross section depends on its internal structure, so photoproduction can test whether the $Z_c^+(4430)$ is a tetraquark or other exotic object. We calculate the rates and kinematic distributions for $\gamma p \rightarrow X^+ n$ in pA UPCs and ep collisions at an EIC and in UPCs. The rates are large enough for detailed studies of these final states. Because the cross section for Reggeon exchange is largest near threshold, the final-state rapidity distribution depends on the beam energies. At high-energy colliders like the proposed LHeC or pA collisions at the Large Hadron Collider, the final states are produced at far forward rapidities. For lower energy colliders, the systems are produced closer to midrapidity, within reach of central detectors.

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I. INTRODUCTION

Ultraperipheral collisions (UPCs) are currently our main tool for studying photoproduction at high energies, above the reach of fixed-target experiments. UPCs are studied at both the Relativistic Heavy Ion Collider (RHIC) and the Large Hadron Collider (LHC) [1-3]. They have been used to probe both two-photon processes, such as lepton pair production and light-by-light scattering, and photonuclear interactions, such as vector-meson and dijet production in heavy-ion collisions [4]. Photoproduction has been studied for a variety of vector mesons, including the ρ , ρ' , ω , J/ψ , ψ' , and Υ , on both proton and ion targets. At the LHC, these reactions occur predominantly via photon-Pomeron fusion, while, for the ρ at RHIC, photon-Reggeon fusion also plays a role. A future electron-ion collider will allow studies of photoproduction using photons with significant Q^2 [5], and, by virtue of its high luminosity, expand the range of mesons that can be studied. At still lower energies, hadrons are produced via the decay of photoexcited baryon resonances. These processes are relevant very near threshold, but we do not consider them here.

In this paper, we discuss a new class of particles that can be studied with UPC and EIC photoproduction: electrically charged final states which are produced by the exchange of a charged Reggeon [6–8]. Regge trajectories allow the exchange of different spins, *J*, with either natural $[P = (-1)^J]$ or un-natural $[P = (-1)^{J+1}]$ parity. Because of this diversity of Reggeon trajectories, a wide range of final states can be produced. We consider two examples: the $a_2^+(1320)$, which is a conventional $q\bar{q}$ meson, which is produced via $\gamma p \rightarrow a_2^+(1320)n$, the manifestly exotic final state $Z_c^+(4430)$, which we model as a $u\bar{d}c\bar{c}$ tetraquark, produced by $\gamma p \rightarrow$ $Z_c^+(4430)n$. The $a_2^+(1320)$ is an attractive experimental target, since 70% of its decays involve three pions, leading to a good fraction of all-charged-particle final states. Photoproduction is an attractive reaction to search for exotic hadrons, since, compared to hadroproduction, production of exotics is enhanced [9].

Photoproduction of the a_2^+ in a Regge model was discussed in Ref. [10]. That paper used an effective Lagrangian approach, considering both π^+ exchange and a more general vector-meson dominance (VMD), determining the coupling constants based on the widths for the decays $a_2 \rightarrow \pi \gamma$ and $a_2 \rightarrow \pi \rho$. It considered dipole, monopole, and exponential form factors for the πNN and $a_2\pi\gamma$ vertices. The π^+ and VMD models predict cross sections that differ by about an order of magnitude but with a similar photon energy dependence. The paper notes that the absolute value of the cross sections can be tuned to match the experimental data by adjusting a parameter in the form factors.

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The Z_c^+ (4430) was discovered by the Belle collaboration [11]. It includes a $c\overline{c}$ pair but is also charged, so it cannot be a conventional $c\overline{c}$ meson. Different theoretical interpretations have treated it as a tetraquark ($u\overline{d}c\overline{c}$), a hadronic molecule or a hadroquarkonium state [12] or as due to a triangle singularity [13], with the tetraquark explanation attracting the most attention. A measurement of the photoproduction cross section would help differentiate between these models.

Photoproduction of the $Z_c^+(4430)$ was first discussed by Liu, Zhao, and Close [14], who used an effective Lagrangian. They considered *t*-channel π^+ and a_0^+ exchange to produce the charged Z_c , finding the $Z\gamma\pi$ coupling using VMD. They considered different spin-parity possibilities for the $Z_c^+(4430)$, finding a significant cross-section dependence, with $J^P = 1^-$ having a cross section of 70 nb at the peak photon energy of about 40 GeV. If the spin-parity is $J^P = 1^+$, the cross section is about 15% smaller, with a similar energy dependence, while $J^P = 0^-$ gives a larger peak cross section, about 170 nb.

Galata performed a Regge calculation, summing over multiple Regge trajectories, finding smaller cross sections than Liu *et al.*, with a peak of 13 nb for $J^P = 1^+$ for the π , ρ , and a_2 trajectories [15]. This cross section is about 20% of that found by Liu *et al.* but with a similar photon energy dependence. As Ref. [15] notes, the effect of using Regge trajectories leads to this reduction. We will adopt the Galata cross section in our calculation, focusing on the $J^P = 1^+$ possibility. A Reggeized treatment has also been applied to study photoproduction of the $Z_c^+(4200)$ [16].

The $Z_c^+(4430)$ decays to $J/\psi\pi^+$ or $\psi(2S)\pi^+$, so is also experimentally tractable, albeit with a lower branching ratio to easily reconstructible states like $e^+e^-\pi^+$ or $\mu^+\mu^-\pi^+$. A similar approach could be applied to other conventional and exotic hadrons. For example, the $Z_c^+(3900)$ is lighter than the $Z_c^+(4430)$, so if it is a similar class of hadron, it should have a higher production rate than the $Z_c^+(4430)$. Previously, Z_c^+ photoproduction was considered in *pp* collisions at the LHC [17].

Because these interactions involve charge exchange, we consider only proton targets: pA UPCs where the photon comes from the heavy nucleus, and ep collisions at an EIC. Nuclear targets are interesting, but there are theoretical uncertainties in extending these photoproduction calculations to nuclear targets. Photoproduction measurements are an important test of exotic hadron structure; heavy objects like the $Z_c^+(4430)$ are beyond the range of fixed-target photon beams, so UPCs and EICs are a unique probe of these heavy exotic states.

II. CROSS-SECTION CALCULATIONS

We extend two existing Monte Carlo codes to model the photoproduction of these objects. For UPCs, we use STARlight [18], which is widely used for photoproduction. For *ep* collisions, we use eSTARlight, which simulates vectormeson photoproduction and electroproduction [19,20]. Both codes make use of parameterized data. For the a_2^+ (1320), we added a parametrization of cross-section data from fixedtarget photoproduction experiments, while for the Z_c^+ (4430),

TABLE I. Parameters for the accelerators. For eRHIC and JLEIC, we use the integrated luminosity in Ref. [5]. For the LHeC and EicC, we assume a luminosity of 1.0×10^{33} cm⁻² s⁻¹ for 10^7 s of running. For RHIC, we assume a luminosity of 4.50×10^{29} cm⁻² s⁻¹ for 10^7 s of running while for the LHC, we use the integrated luminosity from Chapter 10 of Ref. [26].

Accelerator	AB	<i>e</i> / <i>p</i> Energy	<i>p/A</i> Energy	Integrated luminosity		
eRHIC [21]	ep	18 GeV	275 GeV	$10 {\rm ~fb}^{-1}$		
JLEIC [22]	ep	10 GeV	100 GeV	$10 {\rm ~fb^{-1}}$		
LHeC [23]	ep	60 GeV	7000 GeV	$10 {\rm ~fb^{-1}}$		
EicC [24]	ep	3.5 GeV	20 GeV	$10 {\rm ~fb^{-1}}$		
RHIC [25]	pĂu	100 GeV	100 GeV	4.5 pb^{-1}		
LHC [26]	<i>p</i> Pb	7000 GeV	2778 GeV	2 pb^{-1}		

we used the theoretical prediction in Ref. [15] for $J^P = 1^+$. The cross section is sensitive to the $Z_c^+(4430)$ spin and parity; $J^P = 1^-$ leads to a 40% larger cross section, while $J^P = 0^$ leads to a cross section about three times larger at the peak, with the ratio increasing at larger photon energies.

We consider the six accelerator configurations shown in Table I: *p*Au collisions at RHIC, *p*Pb collisions at the LHC, and *ep* collisions at four proposed accelerators: the U.S.-based eRHIC and JLEIC, CERN's proposed LHeC, and the proposed Chinese EIC, EicC.

For ep scattering, we follow the same approach that is in Ref. [19],

$$\sigma(ep \to eX^+n) = \int \frac{dk}{k} dQ^2 \frac{d^2 N_{\gamma}(k, Q^2)}{dk dQ^2} \times \sigma_{\gamma^* p \to X^+n}(W, Q^2), \tag{1}$$

where k is the photon energy in the target rest frame, W is the $\gamma^* p$ system center-of-mass energy, and Q^2 is the photon virtuality. The photon flux, $d^2N_{\gamma}(k, Q^2)/dkdQ^2$, is from Ref. [27], and $\sigma_{\gamma^* p \to X^+ n}(W, Q^2)$ is the X^+ photoproduction cross section. We model $\sigma_{\gamma^* p \to X^+ n}(W, Q^2)$ following [28]

$$\sigma_{\gamma^* p \to X^+ n}(W, Q^2) = \left(\frac{M_X^2}{M_X^2 + Q^2}\right)^n$$
$$\sigma_{\gamma p \to X^+ n}(W, Q^2 = 0)f(M_X), \tag{2}$$

where $f(M_X)$ is a relativistic Breit-Wigner function [29], with mass $M_X = 1318$ MeV and width $\Gamma = 105$ MeV for the $a_2^+(1320)$ and $M_X = 4478$ MeV and $\Gamma = 181$ MeV for the $Z_c^+(4430)$ [25]. We adopt the approach used in Ref. [30] to account for momentum-dependent broadening of the ρ^0 . The choice of momentum broadening approach does not significantly affect the total cross section [31].

The variable $\eta = c_1 + c_2(Q^2 + M_X^2)$ controls the Q^2 dependence of the flux. For vector mesons, c_1 and c_2 are determined from HERA data; they are unknown for the $a_2^+(1320)$, so we use $c_1 = 2.09$ and $c_2 = 0.0073/\text{GeV}^2$, as found for the ρ [32], while for the $Z_c^+(4430)$ we use $c_1 = 2.36$ and $c_2 = 0.0029/\text{GeV}^2$, determined for the J/ψ [19]. The errors on c_1 and c_2 dominantly systematic, because of the $a_2^+(1320) \rightarrow \rho$ and $Z_c^+ \rightarrow J/\psi$ substitutions. It is difficult to estimate the size of these uncertainties, but one hint can be seen by comparing η



FIG. 1. Total cross section of $a_{c}^{+}(1320)$ and $Z_{c}^{+}(4430)$ as a function of W. The experimental data are taken from Refs. [33–37].

for the two final states. This uncertainty does not have a major impact on the total cross section but is very important for (and easily measurable with) electroproduction.

We model $\sigma_{\gamma p \to a_2^+ n}(W, Q^2 = 0)$ with a parametrization of the fixed-target photoproduction data from Refs. [33–37], with four fitted parameters:

$$\sigma_{\gamma p \to a_2^+(1320)n}(W) \approx 5.42(W^2 - m_p)^{-0.82} - 5.80 \exp\left[-0.070\left(W^2 - m_p^2\right)^2\right], \quad (3)$$

where W is the energy of the γp system in GeV, m_p is the proton mass, and σ is in μ b. Figure 1 shows the data and fit. Near the peak in the cross section, at W = 2.9 GeV, the cross section to produce an a_2^+ is about 7% of that to photoproduce a ρ^0 [30]. This fit is very similar to that given in Ref. [10].

We model $Z_c^+(4430)$ photoproduction following the Reggeon-model calculation in Ref. [15]. Numerically, we use a four-parameter fit to the $J^P = 1^+$ curve in Ref. [15]:

$$\sigma_{\gamma p \to Z_c^+(4430)n}(W) \approx 0.0257 \exp(-0.0094W^2) - 0.0317 \exp\left[-0.00038 \left(W^2 - m_p^2\right)^2\right],$$
(4)

where W is in GeV and σ is in μ b. This gives a result within a few percentages of the published curve.

In UPCs, the cross section is [18]

$$\sigma(pA \to AX^+ n) = \int dk \frac{dN_{\gamma}(k)}{dk} \sigma_{\gamma p \to X^+ n}(W), \qquad (5)$$

where $dN_{\gamma}(k)/dk$ is the photon flux of the ions [2] and $\sigma_{\gamma p \to X^+n}(W)$ is the total cross section of photon-proton interaction. Because the photon flux is proportional to the square of the ion charge, the photon flux of heavy ions dominates over the photon flux of proton [2,26]. Therefore, we only consider the contributions of γp in photon flux emitted from heavy ions.

The p_T distribution of the photoproduced particles is an important in background rejection, particularly for UPCs. It includes contributions from the photon p_T and the Reggeon p_T , added in quadrature. The former is modeled based on the proton form factor [38], while, for the latter, we use a dipole form factor [39].

III. RESULTS

The cross sections and production rates for the six accelerators are shown in Table II. For the EIC's, we present rates for two Q^2 ranges, $Q^2 < 1 \text{ GeV}^2$, which we consider photoproduction, and 1 GeV² $< Q^2 < 5 \text{ GeV}^2$, which we consider electroproduction; the rate for $Q^2 > 5 \text{ GeV}^2$ is small. As with vector mesons, the rate for electroproduction is a few percent of that for photoproduction [19]. The electroproduction rates are quite sensitive to the η values in Eq. (2).

The rapidity distributions for photoproduction at an EIC are shown in Fig. 2, where the incoming electron comes from negative rapidity. The left plot is for the $a_2^+(1320)$, while the right is for the $Z_c^+(4430)$. The shapes of these distributions reflect the shape of cross sections presented in Fig. 1. The $a_2^+(1320)$ and $Z_c^+(4430)$ are produced in a relatively narrow rapidity regions because $\sigma(\gamma p \rightarrow X^+ n)$ for both is largest near threshold, due to the Reggeon exchange mechanism. This is very different from the Pomeron+ Reggeon exchange process which spreads ρ^0 over a wide rapidity range [19].

The pseudorapidity distribution of the final-state pions and leptons is somewhat broader than the rapidity distribution of their photoproduced parents. Reggeon exchange reactions can be easier to study at moderate energy EICs; the LHeC would be a difficult environment for these studies. Detailed observation will require detectors with good capabilities in the forward region. Alternately, an EIC could be run with a lowered proton/ion beam energy to shift production into a midrapidity detector. Still, other mesons, with masses between

TABLE II. Total cross section and event rates for $a_2^+(1320)$ and $Z_c^+(4430)$ photoproduction in proposed *ep* scattering and proton-nucleus UPCs. Here $B = 10^9$, $M = 10^6$, and $K = 10^3$. The integrated luminosities are taken from Table I.

	$\sigma \ (0 < Q^2 < 1.0 \ {\rm GeV}^2)$				$\sigma (1.0 \mathrm{GeV}^2 < Q^2 < 5.0 \mathrm{GeV}^2)$				$\sigma (Q^2 = 0.0)$	
	eRHIC	JLEIC	LHeC	EicC	eRHIC	JLEIC	LHeC	EicC	RHIC	LHC
$ \frac{a_2^+(1320)}{Z_c^+(4430)} $	79 nb 0.26 nb	69 nb 0.22 nb Event (0 < Q	$0.11 \mu b$ 0.36 nb $Q^2 < 1.0 \text{ GeV}$	47 nb 0.094 nb ⁷²)	0.51 nb 12 pb Even	0.50 nb 12 pb t (1.0 GeV ²	0.52 nb 12 pb $< Q^2 < 5.0 \text{ G}$	0.40 nb 6.8 pb GeV ²)	0.17 mb 0.31µb Events (9	0.56 mb $1.7\mu \text{b}$ $Q^2 = 0.0)$
	eRHIC	JLEIC	LHeC	EicC	eRHIC	JLEIC	LHeC	EicC	RHIC	LHC
$ \frac{a_2^+(1320)}{Z_c^+(4430)} $	0.79 B 2.6 M	0.69 B 2.2 M	1.1 B 3.6 M	0.47 B 0.94 M	5.1 M 0.12 M	5.0 M 0.12 M	5.2 M 0.12 M	4.0 M 68 K	0.77 B 1.4 M	1.1 B 3.4 M



FIG. 2. Rapidity distributions of $a_2^+(1320)$ and $Z_c^+(4430)$ in *ep* scattering at the planned EICs ($0 < Q^2 < 1.0 \text{ GeV}^2$). The electron is moving in the positive y direction.

 $a_2^+(1320)$ and Z_c^+ , should be produced at intermediate rapidities between the two.

Pseudorapidity acceptance is also an issue at RHIC and the LHC, where central detectors typically cover $|\eta| < 1$ to $|\eta| < 2.4$. Figure 3 (left) shows rapidity distributions for the $a_2^+(1320)$ in pAu UPCs at RHIC and pPb UPCs at the LHC, while Fig. 3 (middle) shows rapidity distributions for the $Z_c^+(4430)$ in pAu UPCs at RHIC and pPb UPCs at the LHC. Because the lower beam energy leads to more central production, At the LHC, the LHCb experiment covers $2 < \eta <$ 5 [40], so should have good acceptance for both the $a_2^+(1320)$ and the $Z_c^+(4430)$. At RHIC, a detector with moderately forward acceptance could also study the $a_2^+(1320)$.

Figure 3 (right) shows transverse-momentum distributions for $a_2^+(1320)$ and $Z_c^+(4430)$ in pAu UPCs at RHIC. These spectra are similar to those for vector mesons with similar masses and should be similarly easy to detect.

Even after accounting for detector acceptance and the branching ratios, the rates for the $a_2^+(1320)$ should be very high at the U.S. and Chinese EICs and at RHIC, enough for detailed studies of the energy dependence and (for the EIC) Q^2 dependence of the production cross section. Many other light-quark hadrons should also be accessible. The rates for the $Z_c^+(4430)$ are lower but still high enough for studies of the cross section to confirm (or refute) its nature as a tetraquark and shed light on its spin.

Studies with *pA* UPCs at RHIC could quickly lead to relatively precise measurements of the $a_2^+(1320)$ photopro-

duction cross section and establish a benchmark for Reggeonexchange photoproduction studies. Other lighter mesons should be accessible using the same approach. With enhanced forward detectors (or lower-energy collisions), the Z_c^+ (4430) and other $c\bar{c}$ -based exotic should also be within experimental reach.

IV. CONCLUSIONS

We have calculated the photoproduction cross sections, $d\sigma/dy$ and event rates for the $a_2^+(1320)$ and $Z_c^+(4430)$ at four EICs and two hadron accelerators. In all six cases, the total $a_2^+(1320)$ production rates are high (of order 1 billion events per year). The electroproduction rates are also high (millions of events per year). With a wide-acceptance detector, it will be possible to study photoproduction over a wide range of W and Q^2 and also study rare decays and the spin-structure of the production. At RHIC, it will also be possible to study photoproduction target.

The photoproduction rates for the Z_c^+ (4430) are lower of order 1 million events per year—but are still adequate for moderate precision studies, even after accounting for the lower branching ratios. Because the system is very clean, photoproduction will be a good place to search for different decay modes. Detection of the outgoing neutron in zerodegree calorimeters and, for the EIC, the scattered electron will allow for compete event reconstruction. At an EIC, it may be possible to search for final states with missing



FIG. 3. Rapidity distributions of $a_2^+(1320)$ and $Z_c^+(4430)$ in *pA* collisions at RHIC and the LHC and transverse-momentum distributions of $a_2^+(1320)$ and $Z_c^+(4430)$ in *p*Au UPCs at RHIC. The proton is moving in the positive *y* direction.

particles using missing-mass techniques; this would allow for branching-ratio independent measurements of production cross sections.

The major experimental challenge is that production is concentrated near the γp energy threshold, so, at high energies, production is in the far-forward region. However, they can be seen fairly readily in UPCs at RHIC and at lower energy EICs.

Although we have focused on proton targets, Reggeonexchange reactions should also occur for nuclear targets. Because the final nuclear state is altered, coherence may be lost, so the cross sections will be lower. Despite the low cross sections, Reggeons may be an interesting probe of sea quarks in heavy nuclei. Unlike Pomerons, which are mostly gluons,

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Reggeons represent meson exchange, so are composed mostly of quarks. They may thus be a way to probe the distribution of sea quarks and antiquarks in nuclei [31].

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