# Adsorption and ultrafast diffusion of lithium in bilayer graphene: *Ab initio* and kinetic Monte Carlo simulation study

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In this paper, we adopt first-principles calculations based on density functional theory and kinetic Monte Carlo simulations to investigate the adsorption and diffusion of lithium in bilayer graphene (BLG) as anodes in lithiumion batteries. Based on energy barriers directly obtained from first-principles calculations for single-Li and two-Li intercalated BLG, a new equation was deduced for predicting energy barriers considering Li's interactions for multi-Li intercalated BLG. Our calculated results indicate that Li energetically prefers to intercalate within rather than adsorb outside the BLG. Additionally, lithium exists in a cationic state in the BLG. More excitingly, ultrafast Li diffusion coefficient ( $\sim 10^{-5}$  cm<sup>2</sup> s<sup>-1</sup>) within AB-stacked BLG near room temperature was obtained, which reproduces the ultrafast Li diffusion coefficient measured in recent experiment. However, ultrafast Li diffusion was not found within AA-stacked BLG near room temperature. The analyses of potential distribution indicate that the stacking structure of BLG greatly affects its height of potential well within BLG, which directly leads to the large difference in Li diffusion. Furthermore, it is found that both the interaction among Li ions and the stacking structure cause Li diffusion within AB-stacked BLG to exhibit directional preference. Finally, the temperature dependence of Li diffusion is described by the Arrhenius law. These findings suggest that the stacking structure of BLG has an important influence on Li diffusion within BLG, and changing the stacking structure of BLG is one possible way to greatly improve Li diffusion rate within BLG. At last, it is suggested that AB-stacked BLG can be regarded as an excellent candidate for anode material in lithium-ion batteries.

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## I. INTRODUCTION

The performance of lithium-ion batteries (LIBs) relies predominantly on the material properties of the electrodes. Advanced electrodes not only require high storage capacity but also require ultrafast charge/discharge rates, which are characterized by lithium-ion diffusion coefficient. Carbonbased materials are at present the most commonly used negative electrode in LIBs. There are many studies on the structure of carbon atom layers [1-3] and lithium adsorption in carbon-based materials [4-8]. Experimental results have demonstrated that graphene nanosheets have a good cyclic performance and possess capacity up to 460 mA h g<sup>-1</sup> after 100 cycles [9]. Due to its high lithium storage capacity, high conductivity, and good mechanical flexibility, graphene has been regarded as a suitable candidate for electrodes in LIBs [10,11]. However, the reported experimental Li diffusion coefficients span a very wide range, for example, from  $10^{-16}$  cm<sup>2</sup> s<sup>-1</sup> to  $10^{-6}$  cm<sup>2</sup> s<sup>-1</sup> for a variety of compositegraphite electrode architectures [12-20]. What affects Li diffusion? How to accelerate Li diffusion? These issues are not currently addressed. Therefore, to optimize the performance of negative electrode for LIBs, understanding the changes

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of electronic properties induced by Li intercalation and the diffusion kinetics properties of Li within these intercalated structures is imperative.

Reducing dimensions of material to nanoscale can effectively improve energy and power capabilities [21-23]. Now advanced experimental techniques make it possible to build the structure composed of a few atomic layers as the anode materials for LIBs. Bilayer graphene (BLG), which is a gapless semiconductor similar to monolayer graphene, has been regarded as a good candidate for negative electrode of LIBs [24-26]. Recent experiments have reported intercalation of Li in BLGs [26,27]. Kühne et al. have successfully monitored the in-plane Li diffusion kinetics within the BLG and measured ultrafast Li diffusion coefficient of up to  $7 \times$  $10^{-5}$  cm<sup>2</sup> s<sup>-1</sup> at room temperature [27]. Theoretically, there have been some previous studies on Li diffusion in graphene or graphite [28-38]. Tachikawa calculated a Li diffusion coefficient ( $\sim 10^{-10}$  cm<sup>2</sup> s<sup>-1</sup>) on a fluorine terminated graphene surface at room temperature [28]. Persson et al. [12] found a fast intralayer Li diffusion coefficient ( $\sim 10^{-7} \text{ cm}^2 \text{ s}^{-1}$ ) in bulk graphite at room temperature. However, these theoretical studies of Li diffusion behavior do not consider the interaction between Li ions. In fact, the interaction between Li ions is always present, which must affect Li diffusion processes. Furthermore, ultrafast Li diffusion ( $\sim 10^{-5}$  cm<sup>2</sup> s<sup>-1</sup>) in BLG at room temperature has been measured in recent experiments [27]. However, the result of this ultrafast diffusion has not

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been explained well. This inspired us to study the adsorption and diffusion kinetics of lithium in BLG.

In the present paper, we study Li diffusion coefficient in Liadsorbed BLG systems by combining first-principles density functional theoretical (DFT) calculations with kinetic Monte Carlo (KMC) simulations, which is designed to effectively simulate the time evolution of a system. Li migration energy barriers obtained from DFT are used as input parameters in KMC simulations to assess Li diffusion coefficient. However, when considering the interaction between Li ions, it is hard to get the energy barriers momentarily from DFT because they are sensitive to ion arrangement, which might change at any time in Li migration process. Therefore, to consider the interactions between Li ions in multi-Li adsorbed systems, we deduce a new equation which is based on the energy barriers obtained from DFT for single-Li and two-Li adsorbed systems to evaluate the migration energy barriers. Using the evaluated energy barriers into KMC simulations, Li diffusion coefficients under specific temperature and concentration are studied. The interactions between Li and the BLG, the directional preference of Li diffusion, and the temperature dependence of Li diffusion are discussed. More importantly, the experimental ultrafast Li diffusion coefficient within the BLG near room temperature is reproduced, and the cause for Li ultrafast diffusion is analyzed in detail.

# **II. METHODS**

All first-principles calculations were implemented by using Vienna Ab initio Simulation Package (VASP) with projector augmented wave method [39–45]. The exchange-correlation energy was calculated based on Perdew-Burke-Ernzerhof (PBE) [46] formulation of generalized gradient approximation (GGA) [39]. The optimized PBE van der Waals [47,48] was used to consider the van der Waals forces between interlayer binding for BLG. The cutoff energy was chosen as 400 eV. The Monkhorst-Pack method is used to sample the k points in the Brillouin zone. Our calculated lattice constant for graphene was 2.47 Å, which is near the experimental value of 2.46 Å. The supercell consisting of a BLG and a vacuum separation was used to perform the convergence test of the layer size of graphene along xy plane. Here, we notate the x and y axes are parallel and the z axis perpendicular to the graphene plane. To avert the artificial coupling role between graphene layers in two adjacent periodic images along z axis, the vacuum separation of 35 Å was employed. After the test, the supercell consists of  $6 \times 6 \times 1$  graphene primitive cell was used to properly study lithium adsorption and diffusion in BLG. This is because in the  $1 \sim 3$  Liadsorbed BLG systems studied in our paper, the supercell consisting of  $6 \times 6$  graphene primitive cell is large enough to make the Li atoms in the neighboring supercells far apart, so that the overlap of their electronic states is very small and the Li-Li interaction among neighboring supercells in the xy plane can be neglected. The  $3 \times 3 \times 1$  Monkhorst-Pack k-meshes was adopted. The cutoff energy and the Monkhorst-Pack kmeshes were tested to ensure the accuracy of the results and they were consistent with previous studies [49]. The geometry optimizations were implemented until the force acting on each atom less than 0.02 eV/Å. To study the possible Li diffusion

pathways within BLG and their corresponding energy barriers, climbing image-nudged elastic band calculation (CI-NEB) [50] was performed. Based on previous research [50–52] and also according to the length of the pathways, three or five images were employed between two end points due to their simple pathways. Each image was relaxed until the forces on atom were less than 0.02 eV/Å. In all calculations, spin polarization was included. Then these diffusion energy barriers were applied into KMC simulations to estimate the macroscopic Li diffusion coefficient in BLG. The detailed KMC algorithm follows the conventional procedure [53,54]. In KMC simulation, the transition state theory (TST) is applied. According to TST, Li migrates from an initial site to its adjacent vacancy by experiencing a transition state, which has an energy barrier  $E_m$  separating the two corresponding states before and after migration. Li migration follows the general KMC procedures: (1) Determine all possible migration sites. (2) Identify a series of the transition rates  $(p_i)$  for all possible migration states according to the transition rate defined as [55,56]  $p_i = v^* \exp(-E_m/k_BT)$ , where  $v^*$  is the jump attempt frequency, which is taken to be  $1 \times 10^{13} s^{-1}$  [12,33,57].  $E_m$  is the migration energy barrier which can be obtained from the first-principles calculations.  $k_B$ , and T denote the Boltzmann constant and temperature (K), respectively. (3) Calculate a accumulation  $P_j = \sum_{i=1}^{j} p_i$ , with j = 1, ..., n. Here, *n* is the total number of the possible jumping sites. (4) Generate a uniform random number u in a range of [0-1]. Then the *j*th jumping direction is selected according to  $P_{i-1} < uP_n < uP_n$  $P_i$ . If the migration event occurs, then Li's distribution will be updated. The simulation moves into the next step. The simulation time t is incremented by  $\Delta t$  which is given by  $\Delta t = -P_n^{-1} \ln u$ . The diffusion coefficient can be decided by  $D = \lim_{t \to \infty} \frac{\langle r(t)^2 \rangle}{4t}$  [55,56], where  $\langle r(t)^2 \rangle$  is the mean-squared displacement of Li. Each KMC simulation step contains  $N_{\text{Li}}$ steps ( $N_{\text{Li}}$  is the total number of Li atoms).

BLG generally has AA and AB stacking structure, as shown in Fig. 1. The single graphene size with  $14 \times 14$  C atoms for BLG is used in the KMC simulations, using periodic boundary conditions for the simulation cell. The simulation temperature range is set to 263–333 K. For all simulations, 5000 MC steps are used. The first 3000 MC steps are disregarded to allow the system to relax to the equilibrium state. The diffusion coefficient is the average value of the last 2000 MC steps.

#### **III. RESULTS**

### A. Adsorption of Li in bilayer graphene

Our calculated total energies for BLG with AA (-9.206 eV/atom) and AB (-9.210 eV/atom) stacking structure indicate that the BLG is more stable in the AB stacking structure, which agrees with Refs. [58,59]. The average interlayer distances (the distance between average coordinates of carbon atoms in the upper layer and the lower layer) are 3.589 Å and 3.413 Å for AA-stacked and AB-stacked BLG, respectively. They are very close to the experimental values (3.7 Å for AA stacking and 3.35 Å for AB stacking [25]). As shown in Fig. 1, there are three high-symmetry sites considered for lithium adsorption within AA-stacked BLG: above two C

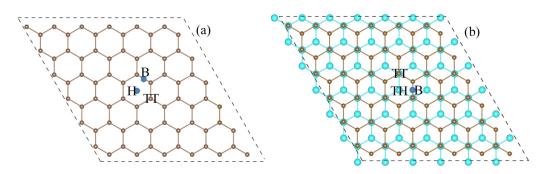


FIG. 1. Top view of bilayer graphene with AA (a) and AB (b) stacking structure.

atoms of both graphene layers, called top-top (TT) site; above the center of C hexagon or the C-C bond of two layers, called hollow (H) or bridge (B) sites. Similarly, there are also three high-symmetry sites within AB-stacked BLG: above two C atoms of both graphene layers, TT site; above the center of C hexagon in upper (or lower) layer, that is, the top of the C atom in the lower (or upper) layer, called top-hollow (TH) site; above the center of a C-C bond of upper (or lower) layer, B site. Moreover, when lithium adsorbs outside AB-stacked or AA-stacked BLG, lithium equivalently adsorbs on a graphene monolayer, in fact. Therefore, three high-symmetry sites have been considered: above C atom, the center of C hexagon, and C–C bond of graphene monolayer, called top (T), hollow (H), and bridge (B) sites, respectively. The stability of a Liadsorbed BLG system is generally described by the adsorption energy  $E_{ad}$  [31]:

$$E_{\rm ad} = E_{\rm Li+BLG} - E_{\rm Li} - E_{\rm BLG},\tag{1}$$

where  $E_{\text{Li}+\text{BLG}}$  represents the total energy for a Li-adsorbed BLG system with a Li atom adsorbed in BLG.  $E_{\text{Li}}$  and  $E_{\text{BLG}}$  represent the energies of an isolated Li atom and the isolated BLG, respectively. The calculated adsorption energies of various Li-adsorbed BLG systems show that the favorable site locates at the H one regardless of Li adsorbing within or outside BLG for AA stacking, and the TH or H one for AB stacking, as presented in Table I. Moreover, all adsorption energies for those systems with Li intercalating within BLG are more negative than that for Li adsorbing outside BLG. Therefore, Li energetically prefers to intercalate within BLG. This finding agrees with the experimental result [27] and the first-principles calculations result [25] that Li resides only in between pristine graphene sheets. Furthermore, our calculated results also indicate that Li is more inclined to intercalate within AA-stacked BLG than AB-stacked BLG, which is consistent with previous studies [58].

Due to a large difference in electronegativity between Li and C atoms, there is a charge transfer from Li to C atoms. The interaction between Li and C atoms can be visually explored by investigating the valence electron density distributions and the electron density difference, which are represented in Fig. 2. The electron density difference is usually defined as  $\Delta \rho = \rho_{\text{Li+BLG}} - \rho_{\text{Li}} - \rho_{\text{BLG}}$ , where  $\rho_{\text{Li+BLG}}$ ,  $\rho_{\text{Li}}$  and  $\rho_{\text{BLG}}$ denote the electron density distributions of the Li-adsorbed BLG system, the isolated Li atom and the isolated BLG, respectively. Our calculated results of electron distributions for Li adsorbing within (or outside) AA-stacked BLG or AB-stacked BLG are similar. All indicate that BLG is the major charge acceptor. For Li intercalating within AB-stacked BLG, as can be seen in Fig. 2(a), the electron distributions surrounding the Li atom are rare, indicating that charge depletion takes place in this region. It suggests that the Li atom donates its  $2S^1$  electron to the graphene layers and exists in a cationic state, which is consistent with previous reports [5,58]. Figures 2(b)-2(d) show that the charge transfers from the Li atom to its nearest-neighbor C atoms of BLG. The red and yellow isosurfaces denote the charge depletion and charge accumulation, respectively. Brown and turquoise balls are the C atoms located in the upper and lower layer, respectively. Green ball is Li atom. For Li intercalating within AA-stacked BLG [Figs. 2(g) and 2(h)], the behavior of the charge transfer is the same. But for the case of Li adsorbing outside AB-stacked BLG [Figs. 2(e) and 2(f)], the charge transfer

TABLE I. Adsorption energies  $E_{ad}$  for the systems with one Li atom adsorbing within AA-stacked and AB-stacked BLG ( $E_{ad,in}$ ) or outside AA-stacked and AB-stacked BLG ( $E_{ad,out}$ ) at various adsorbtion sites.

	Adsorption Site	Adsorption Energy $E_{ad}$ (meV/Å <sup>2</sup> )		Energy difference
		E <sub>ad,in</sub> for one Li within BLG	$E_{\rm ad,out}$ for one Li outside BLG	$\Delta E_{\rm ad} = E_{\rm ad,out} - E_{\rm ad,in}$ $({\rm meV/\AA}^2)$
	Н	-11.34	-6.45	4.89
AA	В	-9.55	-5.08	4.47
	TT	-8.91	-5.01	3.90
	TH(within)	-10.66	-6.47	4.19
AB	or H(outside)			
	В	-9.94	-5.17	4.77
	TT	-8.37	-5.09	3.28

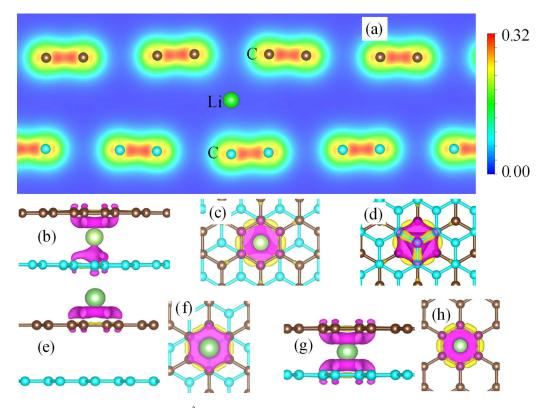


FIG. 2. (a) The valence electron density ( $e \cdot bohr^{-3}$ ) distributions for Li adsorbing at TH site within AB-stacked BLG. The electron density difference  $\Delta \rho$  (b) side view, (c) top view, and (d) bottom view for Li adsorbing within AB-stacked BLG, (e) side view, and (f) top view for Li adsorbing at H site outside AB-stacked BLG, (g) side view, and (h) top view for Li adsorbing at H site within AA-stacked BLG.

occurs between Li and C atoms only in Li's nearest-neighbor graphene layer, not in the layer far away. The case for Li adsorbing outside AA-stacked is the same, so its electron density difference isn't displayed repeatedly here. When Li intercalation content increases, it would appear Li atoms are close together. Figure 3 shows the valence electron density distributions and the electron density difference for two Li atoms intercalating closely within AB-stacked BLG. From the figure, it is clearly seen that the charge transfer only occurs rather locally, surrounding each Li atom, which is similar to the behavior of single Li atom. To quantify the amount of electron transfer, Bader charge analysis [60] was also carried out. Our Bader charge analysis for the system of Li adsorbing within AB-stacked BLG shows that about 0.85 e per Li atom is transferred from Li to the BLG, which agrees with previous reports [5,58]. Therefore, when Li atoms intercalate within BLG, we can reasonably think that they exist as Li ions.

## B. Migration energy barrier in single-Li and two-Li adsorbed BLG systems

The Li diffusion energy barrier is an important factor of kinetics linked to the Li diffusion in intercalation electrodes for LIBs. The charge/discharge rates of metal-ion batteries predominantly depend on Li diffusion in anode materials.

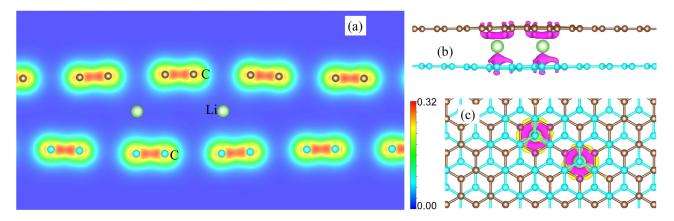


FIG. 3. (a) The valence electron density ( $e \cdot bohr^{-3}$ ) distributions for two adjacent Li atoms adsorbing at TH sites within AB-stacked BLG. The electron density difference  $\Delta \rho$  (b) side view and (c) top view.

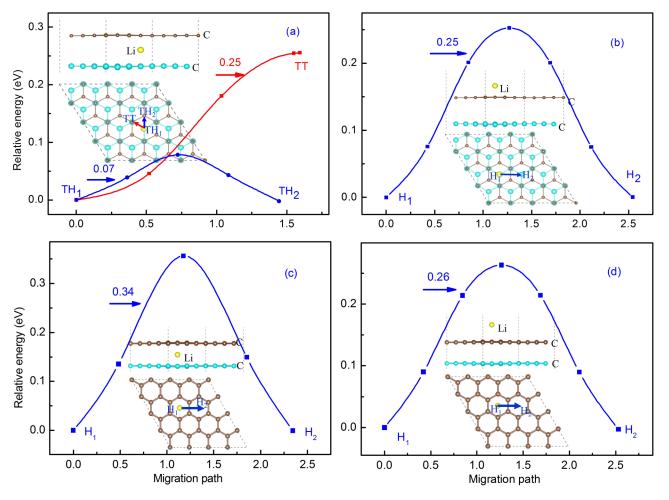


FIG. 4. The total energy profiles for a Li atom intercalated (a) within and (b) outside AB-stacked BLG, (c) within and (d) outside AA-stacked BLG.

Therefore, it is very important to study Li diffusion in BLG intercalation electrodes. The diffusion energy barriers of Li in BLG can be obtained from VASP with CI-NEB along diffusion pathways. For the system with a single Li atom intercalating within AB-stacked BLG, since the favorable site for Li locates at the TH site, the possible transition path that Li migrates via jumping between neighboring TH sites  $(TH_1 \leftrightarrow TH_2)$  was considered, as shown in Fig. 4(a). For the system with a single Li adsorbing outside AB-stacked BLG, actually the favorable site for Li locates at the H site of upper (or lower) monolayer graphene. Hence, Li migrates between the neighboring H sites  $(H_1 \leftrightarrow H_2)$ , as shown in Fig. 4(b). The total energy profiles along corresponding diffusion pathways were also shown in Fig. 4. From Fig. 4(a), a Li atom intercalated within AB-stacked BLG prefers to diffuse along the  $TH_1 \rightarrow TH_2$  pathway because of an obvious lower energy barrier ( $\Delta E$ ) merely of 0.07 eV, which indicates that Li could diffuse very fast within BLG between neighboring TH sites. However, the energy barrier for Li migrating between two neighboring H sites outside AB-stacked BLG reaches up to 0.25 eV, shown in Fig. 4(b). This clearly shows that Li diffusion within AB-stacked BLG is energetically favored compared with the case for Li diffusion outside BLG, which is consistent with the recent experimental finding that Li diffuses in between the graphene sheets but not on top of the BLG

that is the graphene/vacuum interface [27]. For the systems with a single Li atom intercalating within and adsorbing outside AA-stacked BLG, as shown in Figs. 4(c) and 4(d), respectively, Li also migrates between neighboring H sites  $(H_1 \leftrightarrow H_2)$ . The energy barrier for Li migrates between two neighboring H sites outside AA-stacked BLG is basically the same as that for AB-stacked BLG. Notably, however, it is obviously more difficult for Li to diffuse within AA-stacked BLG than outside AA-stacked BLG (energy barriers  $\Delta E =$ 0.34 eV and 0.26 eV for Li migrating within and outside BLG, respectively). Furthermore, the comparison between two energy barriers of 0.07 eV and 0.34 eV for Li diffusing within AB-stacked and AA-stacked BLG, interestingly, reveals that Li apparently rapidly migrates only within AB-stacked BLG but not AA-stacked BLG. Our results clearly indicate that the stacking sequence of two graphene layers can evidently impact the intercalation of Li and its diffusion in these BLG structures. Besides, it can also be found from Fig. 4(a) that along the  $TH_1 \rightarrow TT$  pathway, Li needs to overcome a large energy barrier of 0.25 eV, while it can easily jump from TH<sub>1</sub> site to TH<sub>2</sub> site, just getting over a small energy barrier of 0.07 eV. This obviously indicates that Li diffusion within AB-stacked BLG exhibits directional preference, and it may be attributed to its AB stacking structure of the BLG.

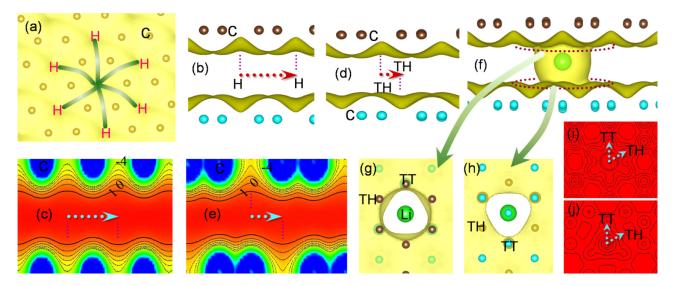


FIG. 5. The side view for the electrostatic potential (eV) isosurface for graphene monolayer (a) and within (b) AA-stacked BLG and (d) AB-stacked BLG. (c) and (e) Respective contour and profile maps of electrostatic potential along the directions of  $H \rightarrow H$  and  $TH \rightarrow TH$  paths for (b) and (d), respectively. The side view for the electrostatic potential isosurface of the system for Li-adsorbed within AB-stacked BLG (f), and the corresponding top view (g) and bottom view (h). The contour and profile maps between Li and upper graphene (i), between Li and lower graphene (j). The isosurface level is -0.23 eV.

To further understand the really large difference between two energy barriers for Li diffusing within AB-stacked and AA-stacked BLG and the directional preference of Li diffusion within AB-stacked BLG, the electrostatic potential distributions of the systems have been explored. For graphene monolayer, one observable feature of the electrostatic potential is its having potential well near the hollow region, as shown in Fig. 5(a). For AA-stacked or AB-stacked BLG, the electrostatic potential within them distributes periodically, attributing to their own periodic lattice structure, shown in Figs. 5(b) and 5(d). It can be considered that the underlying graphene layer provides a periodic potential for the upper layer. The difference is that for AA-stacked BLG, the potential wells generated by the upper and lower layers are the mirror images and just reside in the hollow regions of BLG, whereas for AB-stacked BLG the potential wells generated by both layers are staggered. As can be seen from Fig. 5(d), the potential wells for one layer deviate from the hollow regions of the other layer and face the C atoms of the other layer. This has resulted in that the potential wells within AA-stacked BLG are deeper than that within AB-stacked BLG, as can be observed in Figs. 5(c) and 5(e). This may explain why there is a large difference between two energy barriers for Li diffusion within AA-stacked and AB-stacked BLG. With intercalation of Li, the interaction between Li and C atoms greatly changes the electrostatic potential distribution near Li. Our previous finding has shown that Li diffusion within ABstacked BLG has directional preference, so here we explain this phenomenon qualitatively. As can be seen from Figs. 5(h)and 5(i), the potential distribution between Li and the upper layer is approximately the same in the TT and TH directions. However, in the region between Li and the lower layer, the potential distribution [Figs. 5(h) and 5(j)] is obviously different in the two directions. The potential distribution along the TH direction would help Li to more easily jump from the present potential well to another nearest potential well

along this direction. This corresponds to the previous result that the energy barriers of Li diffusion along the  $TH_1 \rightarrow TH_2$  pathway is lower than that along the  $TH_1 \rightarrow TT$  pathway within AB-stacked BLG.

According to the above findings, the Li atom becomes a Li ion when it intercalates into the BLG. Therefore, when two Li ions are close together, they would interact with each other. This interaction would have an important influence on the electronic structure and the related properties of the system, such as Li diffusion energy barrier in BLG. So, for rare Li intercalated into BLG, Li diffusion can be seen as the migration behavior for noninteracting particles. While Li content increases, ions being close together will lead to the inevitable interaction between Li ions. Moreover, Li energetically prefers to intercalate within BLG rather than adsorb outside BLG for both AA-stacked and AB-stacked BLG, hence only the cases for Li intercalating within BLG are considered in the following analyses of the interaction between Li ions. To study the interaction between Li ions, we calculated the total energy profiles along possible migration pathways for the two Li ion (named two-Li)-intercalated BLG systems that Li<sub>1</sub> is fixed while Li<sub>2</sub> is migrating, as shown in Fig. 6. For two-Li intercalated within AA-stacked BLG, as shown in Fig. 6(a), theoretically, when Li<sub>1</sub> already exists, the nearest-neighbor site for Li<sub>2</sub> should only locate at the H<sub>2</sub> site. It can also be confirmed in the total energy profile shown in Fig. 6(a). From the figure, the closer neighbor H site H<sub>4</sub> of Li<sub>1</sub> is the energetically unstable site for Li<sub>2</sub> due to its obviously higher energy than those of other H sites  $(H_1, H_2, H_3)$ . Thus, the  $H_4$  site acts as a transition state, and if  $Li_2$  locates at the H<sub>4</sub> site, it could easily hop into its neighbor lower-energy sites H<sub>2</sub> or H<sub>3</sub> via overcoming a lower energy barrier about 0.10 eV relative to the energy barrier of 0.40 eV for its reverse migration from the  $H_3$  site to  $H_4$  site. In Fig. 6(a), three possible migration pathways (labeled as  $H_1 \rightarrow H_2, H_3 \rightarrow$  $H_2, H_3 \rightarrow H_4$ ) for a Li<sub>2</sub> ion in its migration behavior were

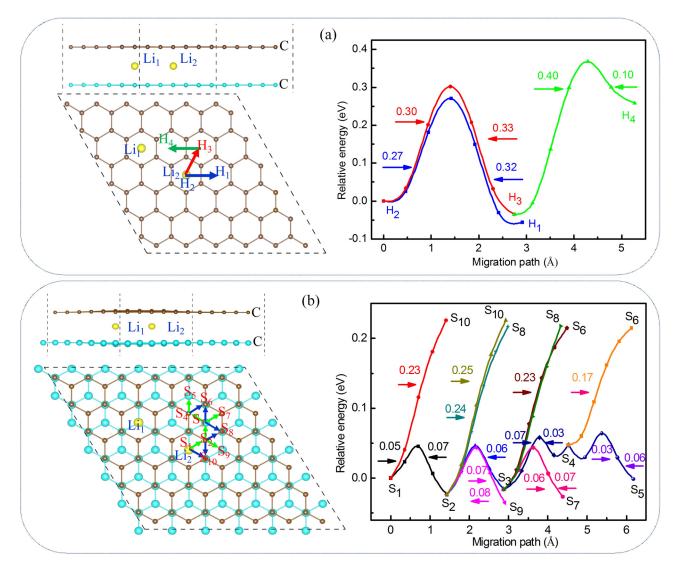


FIG. 6. The total energy profiles for two-Li intercalated within (a) AA-stacked BLG and (b) AB-stacked BLG.

investigated, assuming another Li<sub>1</sub> ion has already existed on Li2's theoretically nearest-neighbor site. In general, Li<sub>2</sub> demands relatively larger energy barriers to jump between  $H_2$  and  $H_1$  sites or  $H_3$  and  $H_2$  sites. According to our calculations, Li2 needs to get over energy barriers about 0.32 eV and 0.33 eV for pathways  $H_1 \rightarrow H_2$ and  $H_3 \rightarrow H_2$ , respectively. In the reverse migration processes, Li2's migration also requires overcoming large barriers of 0.27 eV and 0.30 eV for pathways  $H_2 \rightarrow H_1$  and  $H_2 \rightarrow H_3$ , respectively. Notwithstanding, Li<sub>2</sub>'s reverse migration processes still surpass the relatively lower barriers. Moreover, the differences of Li diffusion barriers along the paths  $H_2 \rightarrow H_1$  and  $H_2 \rightarrow H_3$  are observed. These may be attributed to the interaction between close Li ions. In other words, the interaction between Li ions causes Li diffusion within AA-stacked BLG to have directional preference.

For two-Li intercalated within an AB-stacked BLG system, as shown in Fig. 6(b), when Li<sub>1</sub> already exists, the theoretically nearest-neighbor site for Li<sub>2</sub> should locate at  $S_2$  (or  $S_5$ ) TH site. The closer neighbor TH-site  $S_4$  of Li<sub>1</sub>

is energetically more unstable for Li<sub>2</sub> than other TH sites  $(S_1, S_2, S_3, S_5, S_7, S_9)$ . Thus, the  $S_4$  site acts as a transition state. If Li<sub>2</sub> locates at S<sub>4</sub> site, it could easily jump into its adjacent lower energy sites  $S_3$  or  $S_5$  via overcoming a very lowenergy barrier about 0.03 eV. Furthermore, from the figure, the much higher energies of those TT sites once again prove their instability, and also confirm that Li is difficult to migrate along their corresponding pathways. That is, Li migrating from TH site to TH site is significantly easier than migrating from TH site to TT site. On the other hand, the barriers (0.07 eV, 0.07 eV, 0.08 eV, and 0.06 eV) along pathways  $S_2 \rightarrow$  $S_1, S_7 \rightarrow S_3, S_9 \rightarrow S_2$ , and  $S_5 \rightarrow S_4$  are slightly higher than those barriers (0.05 eV, 0.06 eV, 0.07 eV, and 0.03 eV) along their reverse migration pathways  $S_1 \rightarrow S_2, S_3 \rightarrow S_7, S_2 \rightarrow$  $S_9$ , and  $S_4 \rightarrow S_5$ . Just as in the case for AA-stacked BLG, the Li-Li repulsion leads Li diffusion to be have directional preference within AB-stacked BLG, although the impact is smaller than that induced by the AB stacking structure. Therefore, AB stacking structure and Li-Li repulsion are the main contributing factors that influence Li diffusion within ABstacked BLG to exhibit directional preference.

#### C. Li diffusion in multi-Li intercalated BLG

Macroscopic Li diffusion coefficient  $D_{Li}$  is an important physical quantity used to characterize the speed of Li diffusion and it can be estimated from the migration energy barriers. The previous paper has shown that Li may intercalate into BLG up to a stoichiometry of  $C_6LiC_6$  [26]. That is, the maximum Li content in  $Li_x C_{12}$  can only reach 1. For our studied AA-stacked and AB-stacked BLG systems with very low Li content x such as x = 0.03 and 0.11, since in such systems Li-Li interactions are hardly considered, we can estimate Li diffusion coefficients  $D_{Li}$  for these  $Li_xC_{12}$  BLG systems based on our previous migration energy barriers [as shown in Figs. 4(a), 4(c) and 6]. Our calculated Li diffusion coefficients  $D_{Li}$  for Li<sub>x</sub>C<sub>12</sub> with very low Li content x = 0.03 and 0.11 near room temperature (300 K) are about  $0.16 \times 10^{-6} \, \text{cm}^2 \, \text{s}^{-1}$ and  $0.3 \times 10^{-7}$  cm<sup>2</sup> s<sup>-1</sup> for AA-stacked BLG systems, while they are about  $0.94 \times 10^{-3}$  cm<sup>2</sup> s<sup>-1</sup> and  $0.16 \times 10^{-3}$  cm<sup>2</sup> s<sup>-1</sup> for AB-stacked BLG systems. It suggests that sparse Li atoms could ultrafast diffuse within AB-stacked BLG instead of AA-stacked BLG. The recent experiment has measured an ultrafast diffusion of Li within BLG at room temperature [27], so we only consider the systems of Li intercalated within AB-stacked BLG in the following study of the influence of Li-Li repulsion on Li's diffusion kinetics. Moreover, Sharmila et al. [58,59] found that for AB-stacked BLG with the Li/C ratio being more than 1/12, AB-stacked structure of layers would switch into AA-stacked structure. And for higher Li intercalation content (Li/C ratio being more than 1/12), the Li-adsorbed BLG became energetically unstable which was manifested by positive adsorption energies [58]. Similarly, our results for two-Li intercalated within AB-stacked BLG show that with the presence of Li1 the closest stable site for Li2 locates at  $S_1$  TH site. As Li intercalation content increases, when all such closest stable sites are filled, it corresponds that the maximum x for  $Li_x C_{12}$  is 1. Therefore, in the following study on the influence of interactions among Li ions on their diffusion kinetics, only those  $\text{Li}_x \text{C}_{12}$  systems with Li content x < 1for Li intercalated within AB-stacked BLG are considered.

For the systems of rare Li intercalated into AB-stacked BLG, Li ions are far away from each other. Therefore, Li-Li interactions through Coulomb repulsion are negligible. Li diffusion can be seen as the migration behavior for noninteracting particles. Thus Li diffusion coefficients may be easily estimated based on those migration barriers directly obtained from first-principles calculations combined with CI-NEB method. However, for multi-Li intercalated AB-stacked BLG with higher Li content, Li ions being close enough would interact with each other through Coulomb repulsion, and then play an important role on Li's migration energy barriers, ultimately affecting Li's diffusion process within BLG. Considering the interactions among many ions would have the problem become very complicated. Li's arrangements constantly change during the diffusion process, then Li's migration barriers change subsequently. Therefore, it is difficult to describe the influence of interaction between Li ions on the energy barrier using first-principles calculations. To further study the influence of Li's content on diffusion behavior, we have adopted an equation which has been developed to investigate the influence of Li's interactions on their migration energy barriers for multi-Li adsorbed graphene in our previous

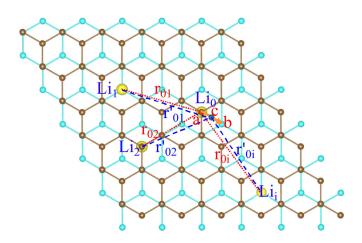


FIG. 7. A schematic diagram for multi-Li intercalated ABstacked BLG.

paper [61] to describe the interactions of Li ions intercalated within AB-stacked BLG. In the equation, the Li migration barrier of a multi-Li adsorbed system was simplified into a functional relation of the Li migration barriers of one-Li and two-Li adsorbed systems. These Li migration barriers for one-Li and two-Li adsorbed systems are directly calculated based on first-principles calculations combined with CI-NEB method. The equation is briefly derived in the next section.

A schematic diagram for multi-Li intercalated AB-stacked BLG is illustrated in Fig. 7. The energies for a and c sites on the migration path can be estimated as

$$E_{a} = K_{1} \left( \frac{1}{r_{0,1}} + \frac{1}{r_{0,2}} + \frac{1}{r_{0,3}} + \dots + \frac{1}{r_{0,i}} \right) + K_{2} E_{0,\text{BLG}} + H_{0},$$
(2)
$$E_{c} = K_{1} \left( \frac{1}{r_{0,1}} + \frac{1}{r_{0,2}} + \frac{1}{r_{0,3}} + \dots + \frac{1}{r_{0,i}} \right)$$

$$\mathcal{E}_{c} = K_{1} \Big( \frac{1}{r_{0,1}'} + \frac{1}{r_{0,2}'} + \frac{1}{r_{0,3}'} + \dots + \frac{1}{r_{0,i}'} \Big) + K_{2} E_{0,BLG}' + H_{0},$$
(3)

where  $E_a(E_c)$  denotes the total energy for multi-Li intercalated AB-stacked BLG with migrated Li (labeled as the zeroth Li<sub>0</sub>), locating at *a* (or *c*) site.  $E_{0,BLG}$  (or  $E'_{0,BLG}$ ) is the energy for the system which includes only the zeroth Li, locating at *a* (or *c*) site within BLG.  $H_0$  denotes the total energy for multi-Li intercalated AB-stacked BLG with the zeroth Li removed.  $K_1$ and  $K_2$  are proportionality coefficients.  $r_{0,i}$  and  $r'_{0,i}$  denote the distances between the zeroth and *i*th Li.

Subtracting Eq. (3) from Eq. (2), and eliminating the same  $H_0$  term in the two equations, the energy difference  $\Delta E_{ac}$  between *a* and *c* sites (corresponding to initial state and activated state, respectively) on the migration path  $a \rightarrow c \rightarrow b$  can be estimated as

$$\Delta E_{ac} = E_a - E_c = \left[ K_1 \left( \frac{1}{r_{0,1}} + \frac{1}{r_{0,2}} + \frac{1}{r_{0,3}} + \dots + \frac{1}{r_{0,i}} \right) + K_2 E_{0,\text{BLG}} \right] - \left[ K_1 \left( \frac{1}{r'_{0,1}} + \frac{1}{r'_{0,2}} + \frac{1}{r'_{0,3}} + \dots + \frac{1}{r'_{0,i}} \right) + K_2 E'_{0,\text{BLG}} \right].$$
(4)

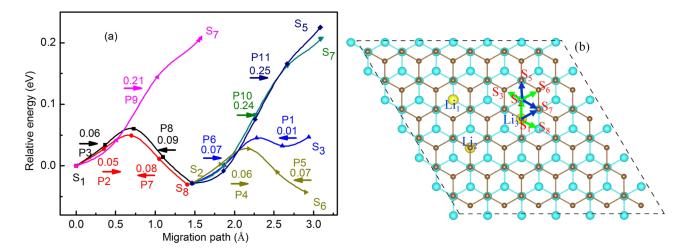


FIG. 8. (a) The total energy profiles and (b) the schematic diagram for three-Li intercalated AB-stacked BLG.

Subtracting the corresponding items of the two terms of Eq. (4), the energy difference  $\Delta E_{ac}$  can be rewritten as

$$\Delta E_{ac} = K_1 \left[ \left( \frac{1}{r_{0,1}} - \frac{1}{r'_{0,1}} \right) + \left( \frac{1}{r_{0,2}} - \frac{1}{r'_{0,2}} \right) + \cdots + \left( \frac{1}{r_{0,i}} - \frac{1}{r'_{0,i}} \right) \right] + K_2 (E_{0,\text{BLG}} - E'_{0,\text{BLG}}).$$
(5)

For a two-Li intercalated BLG system, such as the system with only two Li atoms (zeroth and *i*th) intercalating within BLG, the energies for the zeroth Li locating at *a* site  $E_{0,i}$  and for the zeroth Li locating at *c* sites  $E'_{0,i}$  can be estimated as

$$E_{0,i} = K_1 \frac{1}{r_{0,i}} + K_2 E_{0,\text{BLG}} + H_0', \tag{6}$$

$$E_{0,i}^{'} = K_1 \frac{1}{r_{0,i}^{'}} + K_2 E_{0,\text{BLG}}^{'} + H_0^{'}.$$
 (7)

Where  $H'_0$  denotes the total energy for the two-Li intercalated AB-stacked BLG with the zeroth Li removed. The energy difference  $\Delta E_{0,i}$  can be estimated as

$$\Delta E_{0,i} = E_{0,i} - E'_{0,i} = K_1 \left( \frac{1}{r_{0,i}} - \frac{1}{r'_{0,i}} \right) + K_2 (E_{0,\text{BLG}} - E'_{0,\text{BLG}}).$$
(8)

Combining Eq. (8) with Eq. (5), the energy difference for a multi-Li intercalated BLG system can be derived as

$$\Delta E_{ac} = (\Delta E_{0,1} + \Delta E_{0,2} + \dots + \Delta E_{0,i}) - (i-1) \times \Delta E_{0,\text{BLG}}.$$
(9)

Here,  $\Delta E_{0,BLG} = K_2(E_{0,BLG} - E_{0,BLG}')$  is the energy difference for the one-Li intercalated BLG system with single Li migrating from *a* to *c* site, which is the diffusion barrier for single-Li intercalated BLG system. In Eq. (9), the first term includes the energy differences corresponding to those two-Li intercalated BLG systems. The second term is merely related to the single-Li intercalated BLG system without interaction between Li ions. Therefore, the diffusion barriers of the multi-Li intercalated BLG system can be simplistically

estimated from diffusion barriers of the two-Li and single-Li intercalated BLG systems. To check again our method for energy barrier estimation, we used two methods to estimate the energy barriers along various possible migration pathways for three-Li intercalated BLG system. One is estimating the energy barriers from the total energy curves obtained by first-principles calculations combined with CI-NEB method. Figure 8(a) shows the total energy curves along migration pathways corresponding to Fig. 8(b) by CI-NEB method. The energy barriers of the migration pathways were also marked in the figure. The other method is to estimate the energy barriers directly by Eq. (9) based on the total energy curves of single-Li and two-Li intercalated BLG systems obtained from first-principles calculations. The results from the two methods are presented in Fig. 9. Just as the coincidence has already been obtained in our previous study for multi-Li adsorbed graphene system [61], it can be observed once again that the results from both methods are consistent. It can also be described by the mean deviation  $\Delta$  calculated as follows:

$$\Delta = \frac{1}{N} \sum_{i=1}^{N} \frac{|D_{i,ab} - D_{i,eq}|}{D_{i,eq}} \times 100\%.$$
(10)

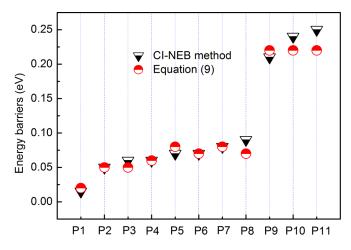


FIG. 9. The energy barriers obtained from CI-NEB method and from Eq. (9) for various Li's migration pathways shown in Fig. 8.

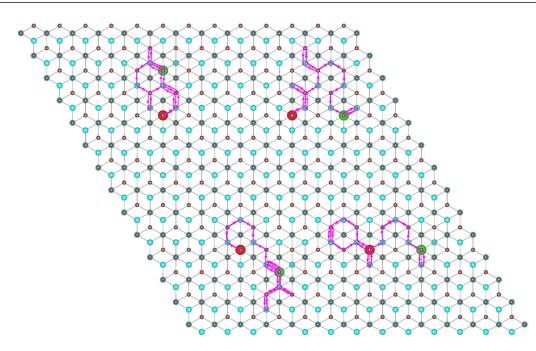


FIG. 10. Trajectories of Li atoms of the AB-stacked BLG with Li content x = 0.06 for T = 300 K, which show 20 steps. Li atoms start at the origin (red dot) and end at the green dot.

*N* represents the number of the samples.  $D_{i,ab}$  and  $D_{i,eq}$  are the results from first-principles calculations with CI-NEB method and Eq. (9), respectively. The calculated mean deviation  $\Delta$  is about 10.3%. Therefore, the method combining Eq. (9) with the total energy curves of single-Li and two-Li AB-stacked intercalated BLG systems from first-principles calculations is feasible in estimating the diffusion barriers for multi-Li intercalated AB-stacked BLG systems. Using the diffusion barriers obtained from Eq. (9), we have applied KMC to predict macroscopic diffusion coefficient  $D_{\text{Li}}$  of Li.

Figure 10 shows the trajectories of Li atoms in the ABstacked BLG with Li content x = 0.06 for T = 300 K. In the figure, Li diffuses along the TH  $\rightarrow$  TH pathway instead of the TH  $\rightarrow$  TT pathway, which is consistent with the result of Fig. 4(a)—that Li needs to overcome a much larger energy barrier along TH  $\rightarrow$  TT than along the TH  $\rightarrow$  TH pathway. It confirms the directional preference of Li diffusion more intuitively. The calculated Li diffusion coefficients  $D_{\text{Li}}$  for the Li<sub>x</sub>C<sub>12</sub> AB-stacked BLG systems with x < 0.7 in a temperature range from 263 K to 333 K are presented in Fig. 11(a). The values of  $D_{\text{Li}}$  are about  $0.3 \times 10^{-4} \sim 1.0 \times 10^{-4} \text{ cm}^2 \text{ s}^{-1}$ for the systems with Li content 0.15 < x < 0.61 near room temperature (300 K), which explains well the measured value up to  $0.7 \times 10^{-4} \text{ cm}^2 \text{ s}^{-1}$  of in-plane Li diffusion coefficient within BLG at room temperature [27]. This, in good agreement with measured experimental data, confirms again that our KMC simulations are reliable. As previously analyzed, the ultrafast diffusion of Li mainly attributes to the stacking

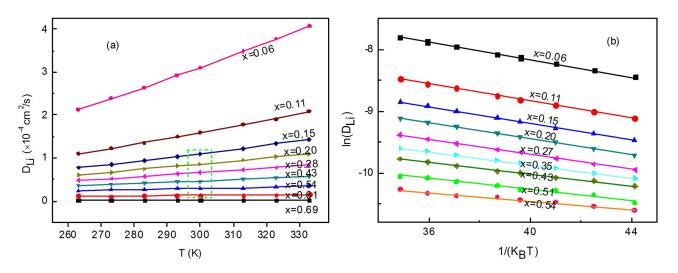


FIG. 11. (a) The diffusion coefficients  $D_{Li}$  as a function of temperature T, (b) the logarithms of  $D_{Li}$  as a function of  $1/(k_BT)$  and their fitting lines for various Li content x.

structure of AB-stacked BLG, which greatly affects its height of potential well within BLG. Furthermore, it is easily found from Fig. 11(a) that the diffusion coefficient  $D_{\text{Li}}$  decreases as Li content *x* increases. This accords with the general trend of experimental and theoretical studies on graphitic carbon [12,13]. Furthermore,  $D_{\text{Li}}$  increases with rising temperature, and the calculated results for Li-intercalated BLG with x <0.54 yield a better linear relationship between ln ( $D_{\text{Li}}$ ) and  $1/(k_BT)$ , as shown in Fig. 11(b). It indicates that the temperature dependence of  $D_{\text{Li}}$  could be described by the Arrhenius law [62,63],  $D_{\text{Li}}(T) = D_0 \exp [-E_A/(k_BT)]$ . Here,  $D_0$  is the pre-exponential factor,  $E_A$  represents macroscopic activation energy.

## **IV. CONCLUSION**

In summary, we have investigated the adsorption and diffusion of Li in BLG by combining first-principles calculations with KMC simulations. It is found that Li energetically prefers to intercalate within the BLG. Li atoms transfer electrons to the BLG so that they become Li ions when they have intercalated within the BLG. Interestingly, Li has an ultrafast diffusion within AB-stacked BLG but not within AAstacked BLG near room temperature. This may attribute to the stacking structure of AB-stacked BLG, which greatly

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affects its height of potential well within BLG. It implies that changing the stacking structure of BLG is one possible way to greatly improve Li diffusion rate within Li-intercalated BLG. Furthermore, both the stacking structure and the interaction among Li ions cause Li diffusion within AB-stacked BLG to exhibit directional preference. The temperature dependence of Li diffusion could be described by the Arrhenius law. These findings can help the rational design of the anode material in high charge–plx-sol-plxdischarge-rate LIBs, and also have practical significance for the application of electronic devices based on the Li-intercalated BLG structures.

#### ACKNOWLEDGMENTS

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