Magnetic structure and magnetoelastic coupling of GdNiSi₃ and TbNiSi₃

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The series of intermetallic compounds $RNiSi_3$ (R = rare earth) shows interesting magnetic properties evolving with R and metamagnetic transitions under applied magnetic field for some of the compounds. The microscopic magnetic structures must be determined to rationalize such rich behavior. Here, resonant x-ray magnetic diffraction experiments are performed on single crystals of GdNiSi3 and TbNiSi3 at zero field. The primitive magnetic unit cell matches the chemical cell below the Néel temperatures $T_N = 22.2$ and 33.2 K, respectively. The magnetic structure is determined to be the same for both compounds (magnetic space group Cmmm'). It features ferromagnetic ac planes that are stacked in an antiferromagnetic +-+- pattern, with the rare-earth magnetic moments pointing along the \vec{a} direction, which contrasts with the +--+ stacking and moment direction along the \dot{b} axis previously reported for YbNiSi₃. This indicates a sign reversal of the coupling constant between second-neighbor R planes as R is varied from Gd and Tb to Yb. The long b lattice parameter of GdNiSi₃ and TbNiSi₃ shows a magnetoelastic expansion upon cooling below T_N , pointing to the conclusion that the +-+- stacking is stabilized under lattice expansion. A competition between distinct magnetic stacking patterns with similar exchange energies tuned by the size of R sets the stage for the magnetic ground state instability observed along this series.

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I. INTRODUCTION

Rare-earth-based materials play a fundamental role in basic and applied condensed matter physics, offering a large amount of fascinating fundamental physical phenomena such as the Kondo effect [1,2], quantum criticality [3,4], unconventional superconductivity [5,6], and others. Combining rare-earth and transition-metal ions usually leads to remarkable magnetic properties such as those in Nd₂Fe₁₄B [7,8] and SmCo₅ [9], which are widely used as permanent magnets. In fact, such combinations often lead to high magnetic ordering temperatures, characteristic of 3d materials, combined to strong magnetic anisotropies, characteristic of the 4f moments. On the other hand, there are also cases of intermetallics where the 3d element becomes nonmagnetic and thus the magnetism is entirely dominated by the 4f electrons. One such family of materials is the recently synthesized $RNiSi_3$ series (R =Y, Gd-Lu) [10,11] with an intricate orthorhombic SmNiGe₃type crystal structure, space group Cmmm (see Fig. 1). The nonmagnetic nature of Ni in this structure is demonstrated by the absence of magnetic transitions and local moments in the specific heat and magnetic susceptibility data of YNiSi₃ and LuNiSi₃ [11].

The evolution of the magnetic properties within the RNiSi₃ series as R is varied from Gd to Yb is very interesting and deserves an individualized description. The temperatureand field-dependent anisotropic bulk magnetization of the compounds with R = Gd-Tm were studied in detail [11,12]. GdNiSi₃ ($T_N = 22.2$ K) is found to have an easy antiferromagnetic (AFM) axis along \vec{a} with a spin-flop transition

for a magnetic field along \vec{a} of $B_a = 2.7$ T; TbNiSi₃ ($T_N =$ 33.2 K) also shows an AFM axis along \vec{a} , displaying a series of steplike metamagnetic transitions with $B_a \gtrsim 4$ T and nearly reaching ferromagnetic saturation for $B_a \sim 6$ T. DyNiSi₃, also with an AFM axis along \vec{a} , shows two close magnetic transitions, at 22.7 and 23.7 K and metamagnetic transitions towards a ferromagnetic phase for $B_a \sim 2.2$ –2.7 T. Remarkably, HoNiSi₃ appears to show a component-separated magnetic transition, with two distinct ordering temperatures: one for the AFM axis along \vec{a} ($T_N^a = 10.0 \text{ K}$) and another for the AFM axis along \vec{c} ($T_N^c \sim 6$ K), also showing field induced metamagnetic transitions towards a partial (i.e., nonsaturated) ferromagnetic state for $B_a = B_c \sim 1.2\text{--}1.6$ T. ErNiSi₃ ($T_N =$ 3.5 K) shows a dominating AFM direction along b with another significant AFM component to the susceptibility along either \vec{a} or \vec{c} , displaying metamagnetic transitions towards a partial ferromagnetic state for $B \sim 1-2$ T. TmNiSi₃ ($T_N =$ 2.5 K) shows an AFM direction along \vec{b} and no clear sign of metamagnetic transitions with field at 2 K. Finally, the magnetic end member YbNiSi₃ ($T_N = 5.1 \text{ K}$) was thoroughly studied [10,13,14], with the AFM axis being along \vec{b} . The magnetic structure was solved by neutron diffraction and displays ferromagnetic ac planes of Yb moments that are stacked antiferromagnetically in a +--+ pattern [14] [see Fig. 1(left)]. Bulk measurements indicate a transition to a distinct ordered phase for $B_b = 1.6$ T that is suppressed for a higher field of $B_b \sim 8.5$ T.

In order to understand the intriguing evolution of the magnetic properties of the RNiSi3 series with R, it is necessary to

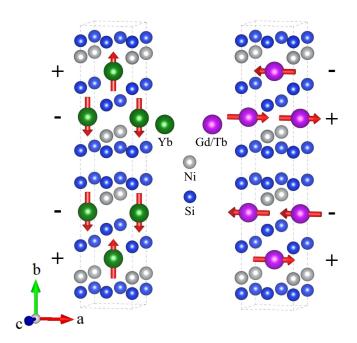


FIG. 1. Crystal and magnetic structures of YbNiSi₃ [14] (left), GdNiSi₃, and TbNiSi₃ (this work, right).

determine the corresponding magnetic structures beyond the already investigated R = Yb end member at zero field [14]. In this work, we take a step towards this direction by solving the zero-field magnetic structure of the known members with the largest R ionic radius, GdNiSi₃ and TbNiSi₃, which were found to have similar bulk magnetic properties at small magnetic fields (see above [11]). Due to the relatively small crystal sizes and the high neutron absorption coefficient of Gd, resonant x-ray magnetic diffraction was the technique of choice. We find that both the magnetic and chemical structures of these materials adopt the same primitive unit cell and the symmetry-allowed magnetic and charge reflections fall into the same points of the reciprocal space. Polarization analysis was employed to separate these contributions for selected reflections and to determine the magnetic structure of GdNiSi₃ and TbNiSi₃. It was found to be different to that of YbNiSi₃ and our results indicate that the magnetic properties of this family are impacted by an instability of the coupling between magnetic bilayers along the b direction.

II. EXPERIMENTAL DETAILS

Platelet-shaped single crystals of GdNiSi₃ and TbNiSi₃ were grown from the melt in Sn flux as described previously [11]. Sample dimensions for the measured GdNiSi₃ and TbNiSi₃ crystals are $1.80 \times 0.77 \times 0.08$ mm³ and $1.19 \times 0.75 \times 0.10$ mm³, respectively. The as-grown principal faces correspond the crystallographic *ac* plane and rocking curves revealed mosaic widths of 0.10° and 0.06° full width at half maximum (FWHM) for GdNiSi₃ and TbNiSi₃, respectively.

X-ray diffraction measurements were performed at the x-ray diffraction and spectroscopy (XDS) beamline of the Brazilian Synchrotron Light Laboratory in Campinas, which uses a 4 T superconducting multipolar wiggler source [15]. The sample was mounted at the cold finger of a closed-cycle

He cryostat (base temperature 10 K) with a cylindrical Be window. The cryostat was fixed onto the Eulerian cradle of a commercial 6 + 2 circle diffractometer, appropriate for single-crystal x-ray diffraction. The energy of the incident photons was selected by a double Si(111) crystal monochromator, with LN₂ cooling in the first crystal, while the second crystal was bent for sagittal focusing. The beam was vertically focused by a bent Rh-coated mirror placed before the monochromator, which also provided filtering of higher harmonics. Our experiments were performed in the vertical scattering plane, i.e., perpendicular to the linear polarization of the incident photons. A polarimeter stage was mounted downstream a scintillator detector, which enabled selecting either the $\sigma\sigma'$ or $\sigma\pi'$ polarization channels. For GdNiSi₃ data taken near the Gd L_{II} edge, the analyzer material was a highly ordered pyrolytic graphite, yielding $2\theta = 89.44^{\circ}$ for the 003 reflection at E = 7.924 keV. For TbNiSi₃, an Al(111) crystal was used, corresponding to $2\theta = 89.77^{\circ}$ for E = 7.516 keV (Tb L_{II} edge). The lattice parameters were obtained by analyzing the 2θ angles of the 2 14 0, 0 20 0, and 0 14 \(\bar{2}\) reflections for GdNiSi₃ and 1 19 0, 0 16 0, and 0 14 1 reflections for TbNiSi3.

III. RESULTS AND ANALYSIS

A. Magnetic diffraction

For Gd- and Tb-based magnetic materials, magnetic x-ray diffraction typically shows strong dipolar resonances at the $L_{2,3}$ edges, with maximum intensities at energies \sim 2 eV above the corresponding edge positions [16,17]. A preliminary x-ray fluorescence scan for GdNiSi $_3$ located the Gd L_{II} absorption edge at 7.922 keV (not shown), and the x-ray energy was subsequently fixed at 7.924 keV to search for magnetic reflections. An extensive search for either commensurate or incommensurate magnetic reflections was then performed, without immediate success. Particularly, no magnetic intensities were observed for integer hkl with h + k = 2n + 1, thereby excluding the magnetic structure of YbNiSi₃ [14] as a possibility for GdNiSi₃. From this initial survey, one could hypothesize at this point that GdNiSi₃ either displays (i) a very complex magnetic structure not covered by our survey scans, with a propagation vector $\vec{k} = [k_x, k_y, k_z]$ where neither of the components are integer or half-integer, or (ii) a particularly simple one (k = [0, 0, 0]) preserving the same C-centering symmetry element of the space group Cmmm of the chemical structure. In the latter case, the reflection conditions for the magnetic and chemical structures would be the same.

In order to test hypothesis (ii) above, the intensities of the selected reflections with particularly small structure factors for the chemical structure were collected for different polarizations, with the monochromator and analyzer being both fixed at either E=7.924 keV (on resonance) or E=7.885 keV (off resonance). Ideally, the charge sector is expected to show vanishing intensities at pure $\sigma\pi'$ polarization, while the magnetic sector would contribute strongly to this channel at dipolar resonances [18]. However, even small polarization leaks of the charge intensities, caused both by small deviations of $2\theta_{\rm analyzer}$ from 90° (see above) and by the horizontal divergence of the beam (\sim 6 mrad),

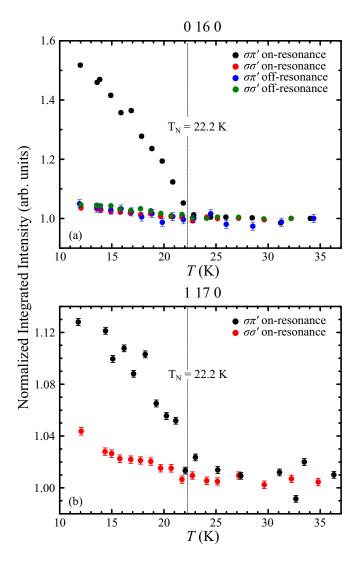


FIG. 2. (a) Temperature dependence of the integrated intensity of the 0 16 0 Bragg reflection of GdNiSi₃ at $\sigma\pi'$ and $\sigma\sigma'$ polarizations, with x-ray energy either on resonance at the Gd L_{II} edge (E=7.924 keV) or off resonance (E=7.885 keV). (b) Similar to (a) for the 1 17 0 reflection (on resonance only).

are sufficient to compete and in most cases dominate over the magnetic intensities even in $\sigma\pi'$ polarization. In fact, for $T \gg T_N$, where no magnetic Bragg peaks are present, nonvanishing intensities from polarization leak were observed at $\sigma \pi'$ for all investigated reflections in a typical level of $\sim 0.1\%$ with respect to the corresponding $\sigma \sigma'$ intensities (not shown). Figure 2(a) shows the temperature-dependence of the integrated intensities of the 0 16 0 reflection at $\sigma \pi'$ and $\sigma\sigma'$ polarizations and both on resonance and off resonance, normalized by the corresponding intensities at T = 34 K (>> T_N). The intensities show a smooth temperature-dependence within the studied temperature interval, except for those at $\sigma\pi'$ on resonance, which show a sharp increment below T_N . Crucially, these conditions for the appearance of extra intensities (polarization, energy and temperature) are exactly those expected for a resonant magnetic x-ray diffraction contribution, providing strong evidence for a simple magnetic structure for GdNiSi₃ with propagation vector $\vec{k} = [0, 0, 0]$.

The temperature-dependence of an additional reflection 1 17 0 was also studied on resonance, also showing an enhancement below T_N at $\sigma \pi'$ polarization [see Fig. 2(b)].

The crystal stucture of RNiSi₃ with Cmmm space group (Fig. 1) shows four R ions per conventional unit cell, i.e., two R ions per primitive cell. The presence of magnetic reflections at the same Bragg positions of the charge reflections is consistent with either a parallel or antiparallel alignment of the moments of the two R atoms of the primitive cell. A parallel alignment would lead to a ferromagnetic structure, which can be excluded by the macroscopic properties of GdNiSi₃ [11]. An antiparallel alignment of Gd spins in the primitive cell therefore remains as the only plausible solution for the magnetic structure of this material. This corresponds to ferromagnetic ac planes that are stacked in an antiferromagnetic +-+- pattern. Concerning the moment direction, a group-theoretical analysis indicated that the R moments must lie along one of the a, b, and c axes, without canting [14]. The moment direction can be experimentally determined by the magnetic intensities according to $I^{M}(\vec{Q}) \propto \left| \sum_{i} \vec{m}_{j} \cdot \vec{k}_{f} e^{i\vec{\tau} \cdot \vec{r}_{j}} \right|^{2}$ valid for dipolar resonances, where \vec{Q} is the reciprocal-lattice vector for the magnetic Bragg reflection, the sum is over the jth resonant magnetic ions in the magnet unit cell, \vec{m}_i is the magnetic moment at site j, and \vec{k}_f is the wave vector of the scattered light. In the conditions of our experiment for GdNiSi₃ and considering absorption corrections [19], this formula leads to the prediction that the magnetic intensity ratio between the 1 17 0 and 0 16 0 reflections would be $r \equiv$ $I^{1,17,0}/I^{0,16,0} = 0.38$ and 1.92 for $\vec{m}||\vec{a}|$ and $\vec{m}||\vec{b}|$, respectively, while zero magnetic intensity would be expected for both reflections for $\vec{m}||\vec{c}|$. The observed value r = 0.38(7), computed after subtracting the spurious polarization-leaked intensity from the total integrated intensity of each reflection, is thus consistent with $\vec{m}||\vec{a}$, in line with the AFM axis identified by magnetic susceptibility data [11]. A schematic representation of the magnetic structure identified for GdNiSi3 is displayed in Fig. 1 (right).

The magnetic structure of TbNiSi₃ is determined through the same procedure detailed above for GdNiSi3. A fluorescence scan located the Tb L_{II} absorption edge position at E =7.514 keV, and the monochromator energy was subsequently set at 7.516 keV. Magnetic intensities were then observed over the same hkl reflections allowed for the chemical crystal structure, revealing that the magnetic structure of TbNiSi₃ has the same +-+- stacking pattern of GdNiSi₃ (see above). Figure 3 shows the temperature dependence of the integrated intensity of the 0 14 1 reflection at $\sigma \pi'$ and $\sigma \sigma'$ polarizations, normalized by the corresponding values at $T = 44 \text{ K} \gg T_N$, showing the extra magnetic signal below T_N at $\sigma \pi'$. An analysis of the relative magnetic intensities of the 0 14 1, 0 16 1, 1 19 0, and 0 10 0 reflections (see Table I) show reasonable agreement between experimental and calculated data for $\vec{m}||\vec{a}$, also in line with the AFM axis identified by magnetic susceptibility data [11].

B. Magnetoelastic coupling

The temperature-dependence of the orthorhombic lattice parameters of GdNiSi₃ and TbNiSi₃ were investigated by

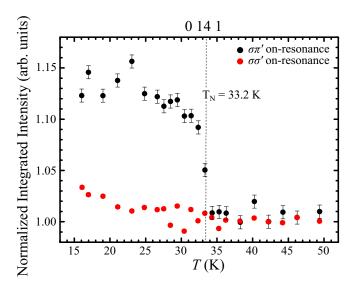


FIG. 3. Temperature dependence of the integrated intensity of the 0 14 1 Bragg reflection of TbNiSi₃ at $\sigma\pi'$ and $\sigma\sigma'$ polarizations, with x-ray energy on resonance at the Tb L_{II} edge (E=7.516 keV).

an analysis of the angular (2θ) positions of selected Bragg peaks measured with $\sigma\sigma'$ polarization. The results are given in Figs. 4(a)–4(d) for GdNiSi₃ and Figs. 5(a)–5(d) for TbNiSi₃. Both materials show a contraction of a and expansion of b below T_N , indicating a magnetoelastic coupling, while c remains approximately constant over the studied temperature interval.

IV. DISCUSSION

The zero-field magnetic structures of GdNiSi₃ and TbNiSi₃ determined in this work [see Fig. 1 (right)] are identical. Also, the continuous temperature dependence of the lattice parameters and magnetic intensities for both materials are indicative of second-order transitions, consistent with previous specific heat measurements [11]. A comparison of the observed magnetic structure with that of YbNiSi₃ [14] [see also Fig. 1 (left)] indicates that they have in common the ferromagnetic ac planes and the antiferromagnetic alignment between such nearest-neighbor planes, indicating that bilayers of R moments are the common magnetic units in this series, at least at zero field. On the other hand, these structures differ by the AFM axis (moment directions along $\pm \vec{a}$ for R = Gd

TABLE I. Observed and calculated intensities of magnetic Bragg reflections for TbNiSi₃, normalized by the most intense reflection, using a model with +-+- stacking of ferromagnetic ac planes and magnetic moments parallel either to \vec{a} , \vec{b} , or \vec{c} directions.

$(h \ k \ l)$	I_{obs}	+-+-		
		$\vec{m} \mid \mid \vec{a}$	$\vec{m} \mid\mid \vec{b}$	$\vec{m} \mid \mid \vec{c}$
(0 14 1)	86(7)	75	61	20
(0 16 1)	40(2)	93	100	25
(1 19 0)	98(12)	86	43	45
(0 10 0)	100	100	19	100

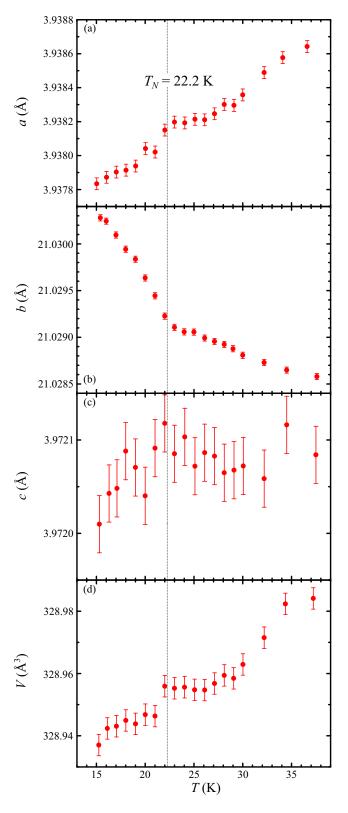


FIG. 4. Temperature-dependence of a, b, c orthorhombic lattice parameters and unit-cell volume V for GdNiSi₃ (a)–(d), respectively.

and Tb and $\pm \vec{b}$ for R = Yb), and also by the coupling between adjacent bilayers leading to the +-+- and +--+ stacking patterns, respectively. The change of the magnetic stacking pattern indicates a change of sign of the effective

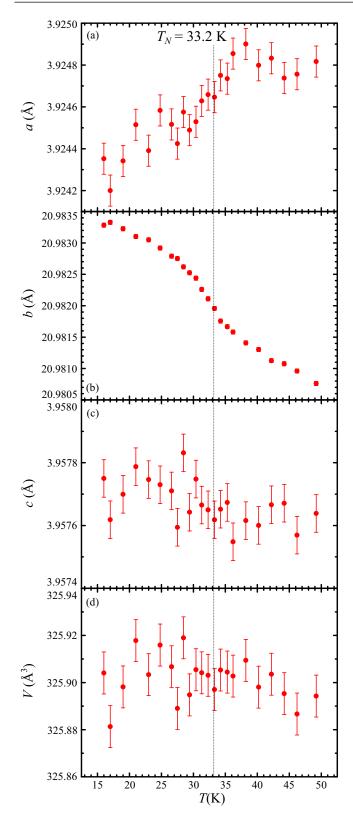


FIG. 5. Temperature-dependence of a, b, c orthorhombic lattice parameters and unit-cell volume V for TbNiSi₃ (a)–(d), respectively.

Ruderman-Kittel-Kasuya-Yosida (RKKY) exchange coupling between the second-neighbor R ac layers on reducing the R ionic radius from Gd and Tb to Yb, i.e., on reducing the

distance between such layers. In this way, above a certain critical value of b, the +-+- pattern is stabilized against the competing +--+ ground state of YbNiSi₃. We suggest that the intriguing evolution of the macroscopic magnetic properties of the intermediate members of this series [11] is at least in part due to a crossover between the two competing magnetic structures of GdNiSi₃ and YbNiSi₃. We should mention that both magnetic structures differ from the related material CeNiGe₃ with a similar crystal structure, where a single crystal neutron diffraction study revealed an incommensurate ground state with propagation vector $\vec{k}_2 = [0, 0.41, 1/2]$ below $T_N = 5$ K [20], while a powder neutron diffraction study showed the incommensurate phase coexisting with a commensurate magnetic structure with a ++-- stacking pattern [20].

The magnetoelastic coupling revealed in our investigation of the orthorhombic lattice parameters (see Figs. 4 and 5) also provide insight into the magnetism of this series. As mentioned above, the +-+- magnetic structure for R=Gd and Tb is stabilized by an expansion of b associated with the larger ionic radii of these ions with respect to Yb. The magnetic coupling energy for these compounds is further reduced by an additional expansion of b on cooling below T_N , characterizing an exchange striction effect that leads to the observed sign of the magnetoelastic coupling for R = Gdand Tb. It is expected that, for R = Yb, this effect would occur with the opposite sign, since its +--+ pattern seems to be stabilized by a contraction of b. A detailed thermal expansion investigation of YbNiSi3 is necessary to confirm this scenario. A stabilization of the magnetic structure under lattice expansion is unusual for direct exchange and superexchange coupling mechanisms in insulators; however, it is a relatively straightforward phenomenon for metals considering the oscillatory behavior of the exchange integral between local moments mediated by conduction electrons as a function of interatomic distances, such as in the RKKY mechanism.

V. CONCLUSIONS

In summary, resonant x-ray diffraction experiments were performed for GdNiSi₃ and TbNiSi₃. Both compounds have a commensurate magnetic structure with propagation vector $\vec{k} = [000]$ formed by a +-+- stacking pattern of ferromagnetic ac planes, where Gd and Tb magnetic moments are parallel to the \vec{a} axis. We also observe a magnetoelastic coupling in both compounds. The sign of this coupling along b is consistent with the stabilization of the +-+- stacking under increasing R ionic radius. A competition between distinct magnetic stacking patterns with similar exchange energies tuned by the size of R sets the stage for the magnetic ground state instability observed along this series.

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