## **Multigap nodeless superconductivity in CsCa2Fe4As4F2 probed by heat transport**

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Recently, a new family of iron-based superconductors called 12442 was discovered and the muon spin relaxation ( $\mu$ SR) measurements on KCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> and CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> polycrystals, two members of the family, indicated that both have a nodal superconducting gap structure with  $s + d$  pairing symmetry. Here we report the ultralow-temperature thermal conductivity measurements on  $\text{CsCa}_2\text{Fe}_4\text{As}_4\text{F}_2$  single crystals ( $T_c = 29.3 \text{ K}$ ). A negligible residual linear term *κ*0*/T* in zero field and the field dependence of *κ*0*/T* suggest multiple nodeless superconducting gaps in  $CSCa_2Fe_4As_4F_2$ . This gap structure is similar to  $CaKF_{4}As_{4}$  and moderately doped  $Ba_{1-x}K_xFe_2As_2$  but contrasts to the nodal gap structure indicated by the  $\mu$ SR measurements on CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> polycrystals.

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Since the discovery of superconductivity in layered iron arsenide  $La(O_{1-x}F_x)FeAs [1]$  $La(O_{1-x}F_x)FeAs [1]$ , many iron-based superconductors have come to the fore  $[2-8]$ . Up to now, iron-based superconductors have already developed into a diverse group of different structural families [\[9\]](#page-4-0), such as the so-called 1111, 122, 111, and 11 families [\[1–4\]](#page-4-0). Meanwhile, great efforts have also been made to understand their various unconventional superconducting properties, especially their superconducting gap structures and pairing symmetry [\[9,10\]](#page-4-0).

Of particular interest is the 122 family, in which the parent compound  $AeFe<sub>2</sub>As<sub>2</sub>$  ( $Ae = Ba$ , Ca, Sr) can be turned into a superconductor through either hole or electron doping [\[2,11\]](#page-4-0). For the typical hole-doped  $Ba_{1-x}K_xFe_2As_2$  with  $x \le 0.55$ , multiple full superconducting gaps have been demonstrated by many experimental studies [\[12–19\]](#page-4-0). In contrast, the extremely hole-doped KFe<sub>2</sub>As<sub>2</sub> ( $x = 1$ ) displays a clear nodal superconducting gap [\[20–23\]](#page-4-0). Such a change of the gap structure is attributed to the evolution of Fermi surface with K doping [\[24\]](#page-4-0), which has been revealed by angle-resolved photoemission spectroscopy (ARPES) measurements [\[25\]](#page-4-0). While the multiple nodeless gaps in the moderately doped regime of Ba1−*<sup>x</sup>*K*x*Fe2As2 are consistent with the *s*±-wave pairing [\[16,19,24\]](#page-4-0), it is still under debate whether the nodal gap in the heavily overdoped regime represents a fundamental change of the pairing symmetry. Some suggested that further doping causes the pairing symmetry to change into the *d*-wave pairing [\[22–24\]](#page-4-0), however others argued accidental gap nodes in heavily overdoped  $Ba_{1-x}K_xFe_2As_2$  [\[26,27\]](#page-4-0). Note that  $RbFe_2As_2$ and  $CsFe<sub>2</sub>As<sub>2</sub>$  also inherit the nodal superconducting gap structure of  $KF_{2}As_{2}$  [\[28,29\]](#page-4-0).

In order to avoid the substitutional disorder in Ba<sub>1−*x*</sub>K<sub>*x*</sub>Fe<sub>2</sub>As<sub>2</sub>, stoichiometric CaKFe<sub>4</sub>As<sub>4</sub> (1144) was first synthesized in 2016 [\[7\]](#page-4-0). Unlike the random occupation of Ba<sup>2+</sup> and K<sup>+</sup> ions in Ba<sub>1−*x*</sub>K<sub>*x*</sub>Fe<sub>2</sub>As<sub>2</sub>, the Ca<sup>2+</sup> and  $K^+$  ions in CaKFe<sub>4</sub>As<sub>4</sub> form alternating planes along the crystallographic *c* axis, separated by FeAs layers [\[7\]](#page-4-0). Soon afterwards, a variety of studies revealed the multiple nodeless superconducting gaps and  $s_{\pm}$ -wave pairing symmetry of  $CaKF_{4}As_{4}$  [\[30–36\]](#page-4-0), pretty like the moderately doped  $Ba_{1-x}K_xFe_2As_2.$ 

Recently, a new family of iron-based superconductor called 12442 was designed by replacement of the Ca layers in  $ACaFe<sub>4</sub>As<sub>4</sub>$  ( $A = K$ , Rb, Cs) with  $Ca<sub>2</sub>F<sub>2</sub>$  layers and synthesized successfully  $[8,37]$ . A series of  $\mu$ SR measurements on the polycrystalline 12442 compounds suggested the presence of line nodes in the superconducting gaps of  $KCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$ and  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  [\[38,39\]](#page-4-0). Since the replacement of Ca layers by  $Ca<sub>2</sub>F<sub>2</sub>$  layers does not introduce additional carriers, the 12442 compounds should have the same doping level as in 1144 compounds  $[8]$ . Thus, the nodal superconducting gap structure of 12442 compounds evidenced by *μ*SR measurements is very striking, which motivates us to investigate their gap structure by measuring the ultralow-temperature thermal conductivity of 12442 single crystals.

In this Rapid Communication, we grew and characterized  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> single crystals, then measured their ultralow$ temperature thermal conductivity. A negligible residual linear term  $\kappa_0/T$  in zero field is confirmed by two samples and a slow field dependence of  $\kappa_0/T$  at low field is also observed. These results suggest that  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  has multiple nodeless superconducting gaps, just as CaKFe<sub>4</sub>As<sub>4</sub> and Ba0*.*75K0*.*25Fe2As2.

High-quality platelike single crystals of  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$ were grown from CsAs flux [\[40\]](#page-4-0). The x-ray diffraction (XRD) measurement was performed by an x-ray diffractometer (D8 Advance, Bruker). The DC magnetization measurement was performed down to 1.8 K using a magnetic property measurement system (MPMS, Quantum Design). The specific heat was measured in a physical property measurement system

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FIG. 1. (a) Crystal structure of CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>. The Cs, As, Fe, Ca, and F atoms are presented as blue, orange, red, magenta, and green balls, respectively. (b) Room-temperature XRD pattern from the large natural surface of the  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  single crystal. Only (00*l*) Bragg peaks were found. Inset: A photo of the  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$ single crystal.

(PPMS, Quantum Design) via the relaxation method. Two samples, labeled as A and B, were cut to a rectangular shape with dimensions of  $\sim$ 2 × 1 mm<sup>2</sup> in the *ab* plane and a thickness of 50  $\mu$ m along the *c* axis for the transport measurements. The in-plane resistivity was measured from 273 to 1.5 K in a  ${}^4$ He cryostat. The in-plane thermal conductivity was measured in a dilution refrigerator by using a standard four-wire steady-state method with two  $RuO<sub>2</sub>$  chip thermometers, calibrated *in situ* against a reference RuO<sub>2</sub> thermometer. Magnetic fields were applied perpendicular to the *ab* plane.

Figure 1(a) displays the crystal structure of  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$ , whose Fe<sub>2</sub>As<sub>2</sub> layers are surrounded by Cs atoms on one side and  $Ca<sub>2</sub>F<sub>2</sub>$  layers on the other, leading to two distinct As sites above and below the Fe plane, similar to CaKFe4As4. The largest natural surface of the as-grown single crystals was determined as (001) plane by XRD, as illustrated in Fig. 1(b).

Figure  $2(a)$  shows the in-plane resistivity for two  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> single crystals labeled as sample A and sam$ ple B down to 1.5 K in zero field. The two samples both exhibit metallic behavior without any phase transition until the sharp superconducting transition occurs. The  $T_c$ s of both samples are identical, 29.3 K defined by  $\rho = 0$ . Previously, the polycrystalline  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  exhibits similar metallic behavior with a lower  $T_c = 28.2 \text{ K}$  [\[37\]](#page-4-0). In the inset of Fig. 2(a), the  $\rho(T)$  of sample B between 32 K and 45 K in the normal state can be described by Fermi liquid behavior  $\rho = \rho_0 + AT^2$ , and the fit gives the residual resistivity  $\rho_0 = 19.2 \mu \Omega$  cm. Thus the residual resistivity ratio RRR =  $\rho$ (273 K)/ $\rho$ <sup>0</sup> is 35.4, indicating the high quality of our single crystals.

Temperature dependence of the magnetic susceptibility from 2 to 50 K at 50 Oe in both zero-field and field cooling modes is plotted in Fig.  $2(b)$ . The diamagnetic transition occurs at 29.2 K, which is consistent with the resistivity measurement. Clear specific heat anomaly can also be seen at the superconducting transition of  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  single crystal, as displayed in Fig.  $2(c)$ . This behavior of the specific heat



FIG. 2. (a) Temperature dependence of in-plane resistivity for two  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  single crystals (labeled as sample A and sample B, respectively) in zero field. The two samples share the same critical temperature  $T_c = 29.3$  K, defined by  $\rho = 0$ . Inset: same data of sample B plotted as a function of  $T^2$ . The solid line is a fit to  $\rho = \rho_0 + AT^2$  between 32 K and 45 K, giving the residual resistivity  $\rho_0 = 19.2 \mu \Omega$  cm. (b) DC magnetization of CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> single crystal at  $H = 50$  Oe along the *c* axis, with zero-field and field cooling modes, respectively. The diamagnetic transition occurs at 29.2 K in both modes. (c) Temperature dependence of specific heat divided by temperature  $C/T$  for the  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  single crystal in zero field. Specific heat anomaly due to the superconducting transition is observed at 30.2 K.



FIG. 3. (a) Low-temperature resistivity of  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  sample B in magnetic fields up to 13 T. (b) Temperature dependence of the upper critical field  $H_{c2}(T)$ . For comparison, similar data of Ba<sub>0.55</sub>K<sub>0.45</sub>Fe<sub>2</sub>As<sub>2</sub> and CaKFe<sub>4</sub>As<sub>4</sub> are also shown and fitted to Ginzburg-Landau equation  $H_{c2}(T) = H_{c2}(0)[1 - (T/T_c)^2]/[1 +$  $(T/T_c)^2$  and empirical formula  $H_{c2}(T) = H_{c2}(0)[1 - (T/T_c)^2]$ , respectively  $[30,42,43]$  $[30,42,43]$ . The data of LaFeAsO<sub>0.89</sub>F<sub>0.11</sub> [\[44\]](#page-5-0) and our  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> show a concave tendency. The dashed line is a guide$ to the eye, from which we roughly estimate  $\mu_0 H_{c2}(0) \approx 50$  T for  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$ .

is very similar to those of  $CaKF_{4}As_{4}$  and  $Ba_{0.6}K_{0.4}Fe_{2}As_{2}$ [\[30,41\]](#page-4-0). Both susceptibility and specific heat results demonstrate the bulk superconductivity in our single crystals.

To determine the upper critical field  $H_{c2}(0)$  of  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$ , we measured the resistivity of sample B below 36 K in various magnetic fields up to 13 T, as shown in Fig.  $3(a)$ . The  $H_{c2}(T)$  obtained from Fig.  $3(a)$  is plotted in Fig. 3(b), compared with the  $H_{c2}(T)$  s of CaKFe<sub>4</sub>As<sub>4</sub>,  $Ba_{0.55}K_{0.45}Fe_2As_2$ , and LaFeAsO<sub>0.89</sub>F<sub>0.11</sub> [\[30,](#page-4-0)[42,44\]](#page-5-0). Note that the  $H_{c2}(T)$  of LaFeAsO<sub>0.89</sub>F<sub>0.11</sub> is defined by  $\rho =$  $10\% \rho_N$  [\[44\]](#page-5-0), while the others are defined by  $\rho = 0$  [\[30](#page-4-0)[,42\]](#page-5-0). The significant broadening of the superconducting transition in field and the concave  $H_{c2}(T)$  are attributed to the strong two-dimensionality of  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  [\[40\]](#page-4-0). Here we roughly estimate  $\mu_0 H_{c2}(0) \approx 50$  T for CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>, following the trend of the high-field data of LaFeAsO<sub>0.89</sub>F<sub>0.11</sub>. Note that a slightly different  $H_{c2}(0)$  does not affect our discussion on the field dependence of  $\kappa_0/T$  below.

The ultralow-temperature thermal conductivity measurement is a bulk technique to probe the superconducting gap structure  $[45]$ . Figure  $4(a)$  presents the in-plane thermal conductivity of the two  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  single crystals in zero field, plotted as  $\kappa/T$  vs T. The thermal conductivity at very low temperature usually can be fitted to  $\kappa/T = a + bT^{\alpha-1}$ . where the two terms  $aT$  and  $bT^{\alpha}$  represent contributions from electrons and phonons, respectively. For both samples, the fitting parameter  $\alpha$  in zero and magnetic fields is very close to 3 (e.g., in zero field  $\alpha = 3.07 \pm 0.05$  for sample A and  $3.06 \pm 0.04$  for sample B), so we fix it to 3. In order to obtain the residual linear term  $\kappa_0/T$  contributed by electrons, we extrapolate  $\kappa/T$  to  $T=0$ .

In Fig. [4\(a\),](#page-3-0) the fit to  $\kappa/T = a + bT^2$  below 0.6 K gives the residual linear terms  $(\kappa_0/T)_A = -7 \pm 2 \mu W K^{-2}$  cm<sup>-1</sup> and  $(\kappa_0/T)_B = 7 \pm 1 \mu W K^{-2}$  cm<sup>-1</sup> for sample A and B, respectively. The Wiedemann-Franz law can tell us the normalstate expectation  $\kappa_{N0}/T = L_0/\rho_0$ , where the Lorenz number  $L_0$  is 2.45 × 10<sup>−8</sup> W  $\Omega$  K<sup>−2</sup>. Here we take sample B for example and obtain  $\kappa_{N0}/T = 1.28$  mW K<sup>-2</sup> cm<sup>-1</sup> with  $\rho_0 =$ 19.2  $\mu\Omega$  cm. Considering this large value of  $\kappa_{N0}/T$  and our experimental uncertainty  $\pm 5 \mu W K^{-2}$  cm<sup>-1</sup>, the  $(\kappa_0/T)_A$ and  $(\kappa_0/T)_B$  in zero field are negligible. Generally, since all electrons form Cooper pairs and no fermionic quasiparticles conduct heat as  $T \to 0$ , there is no residual linear term  $\kappa_0/T$ in zero field for nodeless superconductors, as seen in the conventional *s*-wave superconductors Nb and InBi [\[46,47\]](#page-5-0). However, for nodal superconductors, the nodal quasiparticles will still contribute a finite  $\kappa_0/T$  in zero field. For example, the  $\kappa_0/T$  in zero field of the overdoped *d*-wave cuprate superconductor Tl<sub>2</sub>Ba<sub>2</sub>CuO<sub>6+</sub> $_{\delta}$  (Tl-2201) is 1.41 mW K<sup>-2</sup> cm<sup>-1</sup> [\[48\]](#page-5-0), and  $\kappa_0/T$  is 17 mW K<sup>-2</sup> cm<sup>-1</sup> in zero field for the *p*-wave superconductor  $Sr_2RuO_4$  [\[49\]](#page-5-0). Therefore, the negligible  $\kappa_0/T$ of  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  single crystal in zero field gives strong evidence for a fully-gapped superconducting state.

The field dependence of  $\kappa_0/T$  can provide more information on the superconducting gap structure [\[45\]](#page-5-0). The thermal conductivity in magnetic fields for sample B is shown in Fig. [4\(b\),](#page-3-0) which is also fitted to  $\kappa/T = a + bT^2$  below 0.6 K. The  $\kappa_0(H)/T$  obtained in Fig. [4\(b\)](#page-3-0) is normalized to  $\kappa_{N0}/T$ and plotted as a function of  $H/H_{c2}$  in Fig. [4\(c\)](#page-3-0) with the similar data of a clean *s*-wave superconductor Nb [\[46\]](#page-5-0), a dirty *s*-wave superconducting alloy InBi [\[47\]](#page-5-0), a multiband *s*-wave superconductor NbSe<sub>2</sub> [\[50\]](#page-5-0), an overdoped *d*-wave cuprate superconductor Tl-2201 [\[48\]](#page-5-0), and a moderately doped  $Ba_{0.75}K_{0.25}Fe_2As_2$  [\[18\]](#page-4-0).

In Fig.  $4(c)$ ,  $\kappa_0/T$  of the typical *d*-wave superconductor Tl-2201 starts with a finite value and shows a roughly  $\sqrt{H}$ in low fields due to the Volovik effect [\[48\]](#page-5-0). By contrast, in single-gap *s*-wave superconductors like clean Nb and dirty InBi,  $\kappa_0/T$  is zero at  $H = 0$  and rises rather slowly in low fields as it relies on the tunneling of quasiparticles between localized states inside adjacent vortex cores. Field dependence of  $\kappa_0/T$  of multigap *s*-wave superconductors like NbSe<sub>2</sub> and  $Ba_{0.75}K_{0.25}Fe_2As_2$  falls in between. A negligible  $\kappa_0/T$  at

<span id="page-3-0"></span>

FIG. 4. (a) Temperature dependence of thermal conductivity for two  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  single-crystalline samples (the same as that for resistivity measurements) in zero field. The solid curves represent a fit to  $\kappa/T = a + bT^2$  below 0.6 K, giving the residual terms  $(\kappa_0/T)_A = -7 \pm 2 \mu W K^{-2}$  cm<sup>-1</sup> and  $(\kappa_0/T)_B = 7 \pm 2 \mu W K^{-2}$  $1 \mu$ W K<sup>-2</sup> cm<sup>-1</sup>, respectively. (b) Low-temperature in-plane thermal conductivity of sample B in zero and magnetic fields applied along the *c* axis, plotted as  $\kappa/T$  vs  $T^2$ . The residual terms given by linear fit below 0.6 K are reproduced in (c). (c) Normalized residual linear term  $\kappa_0/T$  in (b) as a function of  $H/H_{c2}$ . For comparison, similar data are shown for a clean *s*-wave superconductor Nb [\[46\]](#page-5-0), a dirty *s*-wave superconducting alloy InBi [\[47\]](#page-5-0), a multiband *s*-wave super-conductor NbSe<sub>2</sub> [\[50\]](#page-5-0), an overdoped *d*-wave cuprate superconductor Tl-2201 [\[48\]](#page-5-0), and a moderately doped iron-arsenide superconductor  $Ba_{0.75}K_{0.25}Fe_2As_2$  [\[18\]](#page-4-0).

zero field and a rapid rise in low fields can be attributed to the fast suppression of the smaller gap by the applied field [\[50\]](#page-5-0). Because of the lack of the thermal conductivity data of 1144 superconductors, we take the moderately doped 122 superconductor Ba<sub>0.75</sub>K<sub>0.25</sub>Fe<sub>2</sub>As<sub>2</sub> for comparison. From Fig. 4(c), one can see that the normalized  $\kappa_0(H)/T$  of  $Ba<sub>0.75</sub>K<sub>0.25</sub>Fe<sub>2</sub>As<sub>2</sub>$  and  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  manifests very similar behavior, which suggests a multigap nodeless superconducting state in  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$ . The discrepancy between previous  $\mu$ SR measurements on CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> polycrystal in Ref. [\[39\]](#page-4-0) and our current work may come from the minor impure phase of  $CsFe<sub>2</sub>As<sub>2</sub>$  in the polycrystal, which is known as a nodal superconductor [\[28\]](#page-4-0).

For multigap superconductors, the field dependence of  $\kappa_0/T$  depends on the ratio between the large and small gaps [\[50\]](#page-5-0), therefore we examine the magnitudes of the gaps for  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  and  $Ba<sub>0.75</sub>K<sub>0.25</sub>Fe<sub>2</sub>As<sub>2</sub>$ . According to the charge homogenization, the 12442 and 1144 compounds should have similar doping level and Fermi surface topology to moderately doped Ba1−*<sup>x</sup>*K*x*Fe2As2 [\[8,30\]](#page-4-0). Previously, ARPES measurements on  $CaKF_{4}As_{4}$  single crystals observed three hole pockets  $(\alpha, \beta, \text{ and } \gamma)$  and one electron pocket  $(\delta)$  [\[31\]](#page-4-0). The superconducting gaps are nearly isotropic on each Fermi surface sheet but have different magnitudes. The larger gaps of 13 and 12 meV were obtained for the *β* hole and  $\delta$  electron sheets, while the  $\alpha$  and  $\gamma$  hole sheets have smaller magnitudes of 10.5 and 8 meV, respectively [\[31\]](#page-4-0). The ratio between the large and small gaps is roughly 1.6. For moderately doped  $Ba_{1-x}K_xFe_2As_2$ , taken  $x = 0.4$ for example, a large superconducting gap ( $\sim 12 \text{ meV}$ ) on one holelike  $(\alpha)$  and one electronlike  $(\gamma)$  Fermi surface sheet, and a small gap ( $\sim$  6 meV) on another holelike sheet ( $\beta$ ) [\[12\]](#page-4-0). The ratio between the large and small gaps is about 2. If  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> has similar superconducting gap structure$ and magnitudes to  $CaKF_{4}As_{4}$ , the above comparable gap ratio well explains the similar field dependence of  $\kappa_0/T$ between  $Ba_{0.75}K_{0.25}Fe_2As_2$  and  $CsCa_2Fe_4As_4F_2$ . We note that a more recent  $\mu$ SR measurement on RbCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> polycrystal suggested that an  $s + s$ -wave model explains better the temperature dependence of the superfluid density than an  $s + d$ -wave model [\[51\]](#page-5-0). However, their ratio between the large and small gaps  $(8.15/0.88 = 9.3)$  is much bigger than that of CaKFe4As4, which cannot explain the field dependence of  $\kappa_0/T$  for our CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub> single crystal.

In summary, we measure the ultralow-temperature thermal conductivity of  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$  single crystals to investigate its superconducting gap structure. A negligible residual linear term  $\kappa_0/T$  in zero field and the field dependence of  $\kappa_0/T$  mimic those of Ba<sub>0.75</sub>K<sub>0.25</sub>Fe<sub>2</sub>As<sub>2</sub>, suggesting multigap nodeless superconductivity in  $CsCa<sub>2</sub>Fe<sub>4</sub>As<sub>4</sub>F<sub>2</sub>$ . These results demonstrate that 12442 compounds, just as  $CaKF_{4}As_{4}$ , should have similar doping level and the superconducting gap structure to moderately doped Ba<sub>1−*x*</sub>K<sub>*x*</sub>Fe<sub>2</sub>As<sub>2</sub>, according to the charge homogenization.

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