Evolution of helimagnetic correlations in Mn1−*^x***Fe***x***Si with doping: A small-angle neutron scattering study**

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> \odot (Received 23 September 2018; published 28 November 2018)

We present a comprehensive small-angle neutron scattering study of the doping dependence of the helimagnetic correlations in Mn1−*^x*Fe*x*Si. The long-range helimagnetic order in Mn1−*^x*Fe*x*Si is suppressed with increasing Fe content and disappears for $x > x^* \approx 0.11$, i.e., well before $x_c \approx 0.17$ where the transition temperature vanishes. For *x>x*∗, only finite isotropic helimagnetic correlations persist which bear similarities with the magnetic correlations found in the precursor phase of MnSi. Magnetic fields gradually suppress and partly align these short-ranged helimagnetic correlations along their direction through a complex magnetization process.

DOI: [10.1103/PhysRevB.98.184431](https://doi.org/10.1103/PhysRevB.98.184431)

I. INTRODUCTION

Tuning the interactions in magnetic materials by pressure or chemical substitution is a well-visited route to discover new and exotic phases of condensed matter. In chiral magnetism, the most notable example is provided by the effect of hydrostatic pressure on the properties of the archetype chiral magnet MnSi. In this system, the helimagnetic order at ambient pressure results from the competition between the ferromagnetic exchange and the Dzyaloshinsky-Moriya (DM) [\[1,2\]](#page-9-0) interaction that arises from the noncentrosymmetric crystal structure of this B20 compound [\[3\]](#page-9-0). The helical order, of which the propagation vector is fixed to the $\langle 111 \rangle$ crystallographic directions by magnetic anisotropy, is suppressed under pressure at $p_C \approx 1.4 \text{ GPa}$. Above p_C , partial magnetic order persists in a non-Fermi liquid phase that emerges without quantum criticality [\[4–6\]](#page-9-0). Additionally, topological contributions to the Hall effect hint that magnetic correlations with nontrivial topology, similar to the skyrmion lattice phase at ambient pressure [\[7,8\]](#page-9-0), are stabilized in this region of the phase diagram [\[9\]](#page-9-0).

Another way of tuning the chiral magnetic order is by chemically substituting MnSi with iron. In Mn_{1−*x*}Fe_{*x*}Si, the helimagnetic order is suppressed with increasing Fe concentration, with the spontaneous magnetization [\[10,11\]](#page-9-0), Curie-Weiss $[11]$ and transition temperature T_C $[10,11]$ extrapolating to 0 at $x_c \approx 0.17$. Remarkably, a change of magnetic behavior is already observed at $x^* \approx 0.11$ by magnetization [\[11\]](#page-9-0), magnetic susceptibility [11], resistivity [\[12\]](#page-9-0), and electron spin resonance (ESR) measurements [\[13\]](#page-9-0). Based on these results, it has been suggested that *x*[∗] is a candidate for a quantum critical point (QCP), possibly associated with the suppression of the long-range helimagnetic order $[12,14-16]$. However, despite all these studies, the nature of x^* and of the magnetic correlations for $x^* < x < x_C$ remain unclear.

In the following we address these points and discuss the helimagnetic order in Mn1−*^x*Fe*x*Si around *x*∗. With smallangle neutron scattering (SANS), we systematically study the evolution of the helimagnetic correlations as a function of both temperature and magnetic field. In particular, we investigate the effect of dilution and compare the topology of the magnetic correlations for $x = 0, 0.03, 0.09, 0.10, i.e.,$ for $x < x^*$, with that for $x = 0.11, 0.14$, i.e., for $x > x^*$. All measurements were performed by systematically applying the magnetic field both perpendicular and parallel to the incoming neutron beam. In this way, we obtain an overview of the topology of the helimagnetic correlations, both perpendicular and parallel to the magnetic field, in a way that is not provided by previous studies.

The results show that with increasing Fe concentration, the helices at zero magnetic field first reorient from $\langle 111 \rangle$ to the $\langle 110 \rangle$ crystallographic directions and that the longrange helimagnetic order in Mn1−*^x*Fe*x*Si disappears at *x*∗. For *x* > *x*[∗] finite isotropic helimagnetic correlations set in which bear similarities to those seen in the precursor phase in MnSi [\[17–20\]](#page-9-0). Magnetic fields gradually suppress and only partly align the helices along their direction through a complex magnetization process.

II. EXPERIMENTAL

Single crystals of Mn_{1−*x*}Fe_{*x*}Si with nominal Fe concentration $x = 0.03, 0.09, 0.10, 0.11,$ and 0.14 were grown using the Bridgeman method. The composition of the single crystals, which are listed in Table [I,](#page-1-0) was checked with a PANalytical Axios x-ray fluorescence spectrometer and revealed Fe concentrations of 0.032, 0.089, 0.101, 0.112, and 0.140, respectively. The samples originate from exactly the same batches as the samples of our previous magnetization and susceptibility study [\[11\]](#page-9-0). They have irregular shapes and their dimensions vary from \sim 5 × 5 × 5 mm³ to \sim 10 × 10 × 15 mm³. The measurements on MnSi were performed on the same cubic single crystal with dimensions \sim 5 × 5 \times 5 mm³

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TABLE I. Overview of the Mn_{1−*x*}Fe_{*x*}Si compositions studied. The nominal composition, x_{nom} , was verified with x-ray fluorescence spectroscopy (x_{XRF}). The critical temperature T_C has been deter-mined from magnetic susceptibility [\[11\]](#page-9-0) and for $x \leq x^*$ from the inflection point of the temperature dependence of the total scattered intensity at zero magnetic field. The pitch of the helical modulation ℓ is tabulated for $T = 2.5$ K and $T = T_C$.

		x_{nom} x_{XRF} T_C (K) (SQUID) T_C (K) (SANS) $\ell_{2.5K}$ (nm) ℓ_{T_C} (nm)			
Ω		29.2	28.8	18.2	16.0
	0.03 0.032	19.2	19.2	13.8	13.2
	0.09 0.089	8.1	7.8	9.5	9.7
	0.10 0.101	5.4	5.5	8.9	9.0
	$0.11 \quad 0.112$	5.0		8.4	8.5
	0.14 0.140	2.4		7.0	7.0

used in previous experiments [\[20](#page-9-0)[–22\]](#page-10-0). The structure of all single crystals was checked with x-ray Laue diffraction and the $x = 0$, 0.03, 0.10, 0.11, and 0.14 samples were aligned with the [110] crystallographic direction vertical. The $x =$ 0*.*09 sample was aligned with the [001] direction vertical.

The SANS measurements were performed on the time-offlight instrument Larmor of the ISIS neutron spallation source using neutrons with wavelengths of $0.09 \le \lambda \le 1.25$ nm. The samples were placed at a distance of 4.4 m from the detector that consists of 80 3 He tubes, each 8 mm wide. The SANS patterns were normalized to standard monitor counts and background corrected using a high-temperature measurement. The magnetic field was applied by a three-dimensional vector cryomagnet either parallel $(H||k_i)$ or perpendicular $(H \perp)$ k_i) to the incoming neutron beam designated by its wave vector *ki*. All measurements were performed by first zero field cooling the sample to the lowest temperature of interest. Then a magnetic field was applied and the signal was recorded by stepwise increasing the temperature. The system was brought to thermal equilibrium before the measurement at each temperature commenced. The fitted values reported in this paper have been obtained using the nonlinear least-squares method and the error bars correspond to one standard deviation.

III. ZERO MAGNETIC FIELD

Figure [1](#page-2-0) depicts typical SANS patterns recorded at zero magnetic field and for different temperatures and compositions. The results for MnSi are displayed in Fig. $1(a)$ and are in good agreement with the literature [\[17,19,20](#page-9-0)[,23\]](#page-10-0): above T_c , a diffuse isotropic ring of scattering appears with radius $\tau = 2\pi/\ell$, where ℓ is the pitch of the helical modulation. This ring, which originates from isotropic, chiral, and fluctuating helimagnetic correlations, intensifies and narrows when approaching $T_C \sim 28.7$ K. This ring coexists in a temperature region of $\Delta T \approx 0.2 \text{ K}$ around T_C with two Bragg peaks. These Bragg peaks mark the onset of the long-range helical order oriented along the $\langle 111 \rangle$ directions. The patterns displayed in Fig. $1(b)$ for $x = 0.03$ show a qualitatively similar behavior, but with a lower transition temperature of $T_C \sim 19.2 \text{ K}.$

By further increasing the Fe concentration, the propagation direction of the helix below T_C changes from $\langle 111 \rangle$ to $\langle 110 \rangle$, as can be inferred from the alignment of the Bragg peaks along the $\langle 110 \rangle$ directions for $x = 0.09$ [Fig. [1\(c\)\]](#page-2-0).¹ This change of propagation direction is accompanied with a broadening of the Bragg peaks, which are no longer well-defined spots as for $x = 0$ and 0.03 [Figs. [1\(a\)](#page-2-0) and [1\(b\)\]](#page-2-0), but smeared on a ring with radius $\tau = 2\pi/\ell$.² A slight increase of the Fe concentration to $x = 0.10$ considerably enhances the broadening, indicating an ill-defined orientation of the helix and a weakening of the magnetic anisotropy, which is possibly due to the increased chemical disorder [\[24\]](#page-10-0).

The long-range helimagnetic order with a well-defined propagation direction disappears for $x > x^*$. For $x = 0.11$ and 0.14, broad isotropic rings of scattering instead of Bragg peaks are observed down to the lowest temperature measured, which are well below the respective transition temperatures inferred from susceptibility measurements (Table I). These rings of scattering intensify but remain broad with decreasing temperature, thus indicating finite helimagnetic correlations.

The effect of dilution on the zero-field helimagnetic order is further illustrated by Fig. $2(a)$, which displays the normalized scattering function *S*(*Q*) at μ_0 *H* = 0 T and below the transition temperature for several compositions. $S(Q)$ is obtained by radial averaging the SANS patterns of Fig. [1](#page-2-0) and is thus a one-dimensional representation of the two-dimensional scattering patterns. The line shape of $S(Q)$ is dramatically different for $x > x^*$ than for $x < x^*$. Indeed, for $x \le 0.10$, *S*(*Q*) has a Gaussian line shape with a constant FWHM of $\Delta Q/Q \approx 0.16$ that roughly corresponds to the resolution of the instrument. On the other hand, for $x = 0.11$ and especially for $x = 0.14$, $S(Q)$ is no longer resolution limited but broad, as indicated by the respective FWHM of $\Delta Q/Q \approx 0.23$ for $x = 0.11$ and $\Delta Q/Q \approx 0.65$ for $x = 0.14$. As further illustrated by Figs. $2(b)-2(d)$, which display $S(Q)$ at different temperatures for $x = 0.09, 0.11,$ and 0.14, $S(Q)$ remains for $x > x^*$ broad down to the lowest temperature measured (1.8 K), indicating that helimagnetic correlations with finite correlation lengths persist to the lowest temperatures.

We consider the Ornstein-Zernike relation to extract estimates for the correlation length *ξ* and the pitch of the helix *l*:

$$
S(Q) = C/[(Q - 2\pi/\ell)^2 + \xi^{-2}],
$$
 (1)

with *C* the Curie constant. The temperature dependence of both ℓ and ξ are displayed in Fig. [3.](#page-3-0) For the sake of clarity, the values of ℓ at $T = 2.5$ K and at T_C are also provided in Table I.

Figure $3(a)$ shows that ℓ decreases monotonously with increasing Fe concentration: at $T = 2.5$ K, it decreases from 18.2 nm for $x = 0$ to 6.2 nm for $x = 0.14$. As further addressed in the discussion, this indicates a strengthening of the DM interaction with respect to the ferromagnetic exchange interaction.

The correlation length follows a qualitatively similar behavior for all compositions with $x < x^*$: it increases monotonously with decreasing temperature and reaches approximately the pitch of the helix at T_C . On the other hand, for $x > x^*$, ξ increases monotonously down to the lowest

¹The change of the propagation direction of the helix for $x = 0.09$ is confirmed by triple-axis spectroscopy measurements.

²The rocking scans reveal a considerable broadening of the helical Bragg peaks on the surface of a sphere with radius $\tau = 2\pi/\ell$.

FIG. 1. SANS patterns recorded at zero magnetic field and different temperatures for Mn_{1 $-x$}Fe_xSi with (a) $x = 0$, (b) $x = 0.03$, (c) $x =$ 0.09, (d) $x = 0.10$, (e) $x = 0.11$, and (f) $x = 0.14$.

temperature. In particular for $x = 0.14$, ξ is significantly smaller than ℓ and reaches 5 nm \sim 2/3 ℓ at 1.8 K.

IV. MAGNETIC FIELD

A. Measurements at $T = 2K$

Figure [4](#page-4-0) displays SANS patterns recorded as a function of magnetic field for $Mn_{1-x}Fe_xSi$ with (a), (b) $x = 0.09$, (c), (d) $x = 0.11$ at $T = 2.5$ K and (e), (f) $x = 0.14$ at

 $T = 2$ K, i.e., for $T < T_C$. These patterns have been collected in two complementary experimental configurations: one with the magnetic field parallel to the incoming neutron beam $(H||k_i)$ and one with the field perpendicular to the incoming neutron beam $(H \perp k_i)$.

Figure [4\(a\)](#page-4-0) shows SANS patterns for $x = 0.09$ with $\vec{H} \parallel \vec{k}_i$, i.e., the configuration that is sensitive to helical modulations perpendicular to the magnetic field. At zero magnetic field, the pattern displays four smeared Bragg peaks oriented along

FIG. 2. Scattering function *S*(*Q*), deduced by radially averaging the scattered intensity, at zero field for $Mn_{1-r}Fe_rSi$. (a) *S*(*Q*) is determined for $T < T_c$ and the Fe concentrations indicated in the legend. *S*(*Q*) was measured at $T = 2.5$ K for $x \le 0.11$ and $T =$ 2.0 K for $x = 0.14$ and is normalized to its maximum value. (b)–(d) $S(Q)$ shown for the indicated temperatures and for (b) $x = 0.09$, (c) $x = 0.11$, and (d) $x = 0.14$. The solid lines in (a) indicate the best fits of the data to a Gaussian for $x < 0.11$ where the width of the Gaussian is fixed by the instrumental resolution. For $x \geq 0.11$ and in (b) –(d) the solid lines represent the best fits of Eq. (1) (convoluted with the instrumental resolution) to the data.

FIG. 3. Temperature dependence of (a) the pitch of the helical modulation ℓ and (b) the magnetic correlation length ξ at zero magnetic field and for the $Mn_{1-x}Fe_xSi$ compositions indicated in the legend. The values of ξ are obtained by fitting $S(Q)$ to Eq. [\(1\)](#page-1-0). For $x \leq 0.10$ and $T < T_c$, ℓ was obtained from fitting $S(Q)$ to a Gaussian centered at $\tau = 2\pi/\ell$. For $T < T_C$ and $x \leq 0.10$, the linewidth of $S(Q)$ is limited by the experimental resolution and ξ cannot be determined.

the $\langle 110 \rangle$ crystallographic directions that originate from the helical phase. For $\mu_0 H = 0.1$ T two of these peaks disappear completely, while the other two considerably weaken in intensity. For magnetic fields exceeding 0.1 T, the scattered intensity is negligible, as expected for the conical phase where all helices are oriented along the magnetic field.

A complementary picture is provided by the SANS patterns of Fig. [4\(b\)](#page-4-0) measured with $H \perp k_i$, an experimental configuration which probes helical modulations oriented along the magnetic field. In this configuration, spots of scattered intensity are found along the horizontal field direction for $\mu_0 H \gtrsim$ 0*.*05 T. Together with the disappearance of the Bragg peaks for $H||k_i$, this behavior marks the conical phase in which the propagation direction of the helices changes from along the (110) crystallographic direction to the direction of the magnetic field. These Bragg peaks disappear for $\mu_0 H \gtrsim 0.6$ T, marking the onset of the field polarized state (not shown).

The patterns for $x = 0.11$, which are displayed in Figs. $4(c)$ and [4\(d\),](#page-4-0) are qualitatively different from the ones for *x < x*∗. They show at zero field the isotropic ring of scattering discussed in the previous section. This isotropic scattering gradually disappears when the magnetic field is applied along k_i [Fig. [4\(c\)\]](#page-4-0). This is consistent with the patterns for $H \perp k_i$

FIG. 4. SANS patterns measured at $T < T_c$ as a function of the magnetic field for $Mn_{1-x}Fe_xSi$ with (a),(b) $x = 0.09$ at $T = 2.5$ K, (c),(d) $x = 0.11$ at $T = 2.5$ K, and (e),(f) $x = 0.14$ at $T = 2.0$ K. The magnetic field was applied (a),(c),(f) parallel to the incoming neutron beam $(\vec{H}||\vec{k}_i)$ and (b),(d),(e) perpendicular to it $(\vec{H} \perp \vec{k}_i)$. The two 30° red wedges in (d) and (f) indicate the section of the detector over which the radial integration was performed to obtain *S*(*Q*) for $\vec{H} \perp \vec{k}_i$.

[Fig. $4(d)$], which show that the scattering concentrates along the field direction, ultimately leading to intense spots at high magnetic fields. However, the alignment of the helices along the magnetic field is very gradual and the intense Bragg-like spots coexist with a weaker ring of scattering up to $\mu_0 H =$ 0.5 T. For $\mu_0 H \gtrsim 0.6$ T, the scattered intensity vanishes (not shown), indicating the onset of the field polarized state.

The alignment of the helimagnetic correlations by the magnetic field for $x = 0.14$ is considerably weaker than for $x = 0.11$. Although a slightly larger fraction of the helimag-

netic correlations is still oriented along the magnetic field for $\mu_0 H \ge 0.20$ T, this effect is much smaller than for $x = 0.11$. The effect of the magnetic field is also seen on the scattering function *S*(*Q*), displayed in Figs. [5\(a\)](#page-5-0) and [5\(b\)](#page-5-0) for $T = 2.0$ K. *S*(*Q*) is obtained by radial averaging over the entire detector for $H||k_i$ [Fig. [5\(a\)\]](#page-5-0), and over the two wedges of $\pm 15^\circ$ around the magnetic field direction, indicated in Fig. 4(d), for $\vec{H} \perp$ k_i [Fig. $5(b)$]. The results show that for both experimental configurations, $S(Q)$ broadens considerably with increasing magnetic fields and decreases in intensity.

FIG. 5. SANS results under magnetic field for $Mn_{0.89}Fe_{0.14}Si$ at $T = 2.0$ K. (a) Scattering function $S(Q)$ in arbitrary units obtained by radial averaging the scattered intensity over the entire detector with the magnetic field applied parallel to the incoming neutron beam $(H||k_i)$. (b) *S*(*Q*) in arbitrary units with the magnetic field applied perpendicular to the incoming neutron beam ($\hat{H} \perp \hat{k}_i$). In (b), *S*(*Q*) is deduced by radial averaging the scattered intensity over the two 30◦ wedges along the magnetic field direction indicated in Fig. [4\(f\).](#page-4-0) (c) Magnetic field dependence of the total scattered intensity obtained by summing the intensity over the entire detector for $\vec{H} || \vec{k_i}$ and over the two 30° wedges along the magnetic field for $H \perp k_i$. (d) Magnetic field dependence of the FWHM of *S*(*Q*); inset shows the field dependence of the pitch of the helix ℓ as obtained from fitting the data of (a) and (b) to Eq. [\(1\)](#page-1-0). These fits are indicated by the solid lines in (a) and (b).

The decrease of the scattered intensity of $S(Q)$ is also seen in the magnetic field dependence of the total scattered intensity displayed in Fig. $5(c)$, and is more pronounced for *H* || k_i than for *H* \perp k_i . This decrease can be the result of either the suppression of the helimagnetic correlations as a whole, and/or the orientation of the magnetic moments within the helices toward the magnetic field, as is also the case in the conical phase for $x < x^*$. In addition, $S(Q)$ broadens for $x = 0.14$ considerably with increasing magnetic field, as highlighted by the magnetic field dependence of the FWHM of *S*(*Q*) displayed in Fig. 5(d). This behavior is very different from that found for lower Fe dopings and shows that the characteristic correlation length decreases substantially with increasing magnetic field: from ∼5 nm at μ_0 *H* = 0 T to ξ ∼ 2 nm or approximately $1/4\ell$ at $\mu_0 H = 0.5$ T. This indicates a complex magnetization process in which the magnetic field first breaks the longer helical correlations, which are possibly those that encompass the lowest degree of disorder. On the other hand, the shorter helices appear to be more robust, as is is also the case for vortices in re-entrant spin glasses [\[25\]](#page-10-0).

B. Skyrmion lattice phase

The impact of Fe substitution on the skyrmion lattice correlations in Mn_{1−*x*}Fe_{*x*}Si is illustrated by Fig. [6](#page-6-0) which displays the total scattered intensity for four different Fe concentrations as a function of temperature at $\mu_0 H = 0.20$ T, i.e., in the heart of the skyrmion lattice phase. The magnetic field was applied both parallel $(H||k_i)$ and perpendicular $(H \perp k_i)$ to the incoming neutron beam.

For all compositions, the intensity above T_C is almost the same for both experimental configurations, as expected for isotropic correlations. In contrast, at low temperatures the intensity for $H \perp \vec{k}_i$ is significantly higher than the one for $H||k_i$, as expected for the conical phase. In the intermediate temperature region, the onset of skyrmion lattice correlations leads to a different and nonmonotonic evolution of the scattered intensity with temperature.

MnSi and $x = 0.09$ show basically the same behavior with a sharp maximum in intensity for $H||k_i$ occurring in a temperature region of about ± 1 K below T_c . Together with the characteristic six-fold symmetry of the scattering displayed in the insets of Figs. $6(a)$ and $6(b)$, this maximum marks the skyrmion lattice phase [\[7](#page-9-0)[,26,27\]](#page-10-0). We note that skyrmion lattice correlations coexist with conical correlations, as seen from the finite amount of scattering in the configuration where $\vec{H} \perp \vec{k}_i$.

With dilution, the skyrmion lattice scattering weakens considerably. In addition, for $x = 0.10$ an isotropic ring of scattering instead of six clear peaks is found. This is similar to Fe_{1−*x*}Co_{*x*}Si [\[28,29\]](#page-10-0), and the absence of clear peaks is likely related to a weakening of the fourth- and sixth-order cubic anisotropy terms responsible for the alignment of the skyrmion lattice with respect to the crystallographic one

FIG. 6. Temperature dependence of the total scattered intensity at $\mu_0 H = 0.20$ T for Mn_{1 $-x$}Fe_{*x*}Si with (a) $x = 0$, (b) $x = 0.09$, (c) $x =$ 0.10, and (d) $x = 0.11$. The field was applied both parallel $(H||\vec{k}_i)$ and perpendicular $(H \perp \vec{k}_i)$ to the incoming neutron beam. The insets show characteristics SANS patterns at the indicated temperatures for both field configurations.

[\[7,21](#page-9-0)[,28\]](#page-10-0). The disappearance of Bragg peaks in the skyrmion lattice phase is also consistent with the broadening of the helical Bragg peaks (Fig. [1\)](#page-2-0), which also indicates a weakening of the anisotropy with increasing Fe substitution.

A substantially different behavior unfolds for $x = 0.11$, where there are no clear indications for skyrmion lattice correlations [Fig. $6(d)$]. These results are consistent with magnetic susceptibility measurements [\[11\]](#page-9-0) which for $x > x^*$ do not show any indication of a skyrmion lattice phase. On the other hand, the sizable topological Hall effect reported for this composition [\[30\]](#page-10-0) possibly indicates the existence of individual skyrmions or clusters of skyrmions in this region of the magnetic phase diagram.

C. Phase diagrams

An overview of the effect of the Fe concentration on the magnetic field–temperature phase diagram of several $Mn_{1-x}Fe_xSi$ compositions is provided by Figs. [7](#page-7-0) and [8,](#page-7-0) which display contour plots of the scattered intensity as a function of temperature and magnetic field for both $H||\vec{k}_i$ and $\vec{H} \perp \vec{k}_i$. The contour plots are in excellent agreement with the phase diagrams published in [\[11\]](#page-9-0) which are derived from magnetic susceptibility measurements.

Figure $7(a)$ shows the contour plot of the scattered intensity of MnSi with *H*|| k_i . At low magnetic fields and below T_c ∼ 28*.*7 K, the high intensity originates from the helical phase. Magnetic fields beyond 0.05 T align the helices toward their direction, leading to almost zero scattered intensity in this configuration. On the other hand, the onset of the conical phase is accompanied by a strong increase in intensity in the complementary experimental configuration with $H \perp k_i$ [Fig. $8(a)$]. In this configuration, the scattered intensity of the conical phase is suppressed for $\mu_0 H \gtrsim 0.5$ T, i.e., in the field polarized state in which the magnetic field aligns the magnetic moments along its direction.

Just below T_C and in a magnetic field range of 0.14–0.22 T, a pocket of increased intensity shows up in the contour plot for $H||k_i$. As discussed in the previous section, the increased intensity in this pocket, also known as the A phase, originates from skyrmion lattice correlations that orient perpendicularly to the applied magnetic field. In the complementary configuration of Fig. $8(a)$, a clear decrease in intensity is seen in this region of the phase diagram, indicating a partial suppression of the conical correlations.

The magnetic-field–temperature contour plots of the scattered intensity for $x = 0.09$ and $x = 0.10$ look qualitatively similar to each other and to the ones for MnSi. However, some subtle differences are visible. Similar to Fe_{1−*x*}Co_{*x*}Si [\[28,29,31,32\]](#page-10-0), and consistent with susceptibility measurements [\[10,11\]](#page-9-0), the transition line from the helical to the conical phase is no longer horizontal, but shifts to higher magnetic fields with decreasing temperature. Furthermore, the increase of the scattered intensity for $\vec{H} \parallel \vec{k_i}$ in the A phase is less pronounced, representing a weakening of the skyrmion lattice correlations. This weakening is accompanied by a relative increase of the intensity originating from conical correlations that coexist with the skyrmion lattice correlations.

The contour plots for $x = 0.11$ bear some similarities to the ones for $x < x^*$ but also reveal substantial differences. The

FIG. 7. Contour plots showing the total scattered SANS intensity in arbitrary units in the configuration where the magnetic field was applied parallel to the incoming neutron beam $(\vec{H}||\vec{k})$ for $Mn_{1-x}Fe_xSi$ with (a) $x = 0$, (b) $x = 0.09$, (c) $x = 0.10$, and (d) $x = 0.11$. The black dots indicate the points at which the SANS measurements were performed.

FIG. 8. Same as Fig. 7, but with the magnetic field applied perpendicular to the incoming neutron beam $(H \perp \vec{k}_i)$.

scattered intensity for $\vec{H} \parallel \vec{k}_i$ [Fig. [7\(d\)\]](#page-7-0) persists until the lowest temperature measured and for magnetic fields up to 0.45 T. In the complementary configuration of Fig. [8\(d\)](#page-7-0) with $H \perp k_i$, the intensity is enhanced by the magnetic field for temperatures lower than $T_c \lesssim 5$ K. These results indicate that the helimagnetic correlations are only partly oriented along the magnetic field, even at relatively large fields. In addition, the contour plots provide no indication of a skyrmion lattice phase.

Above T_c , all contour plots show a similar gradual decrease of the scattered intensity with increasing temperature and for all magnetic fields up to $\mu_0 H \sim 0.3$ T. For higher fields, this intensity decreases gradually in the configuration with $H||k_i$, whereas it persists for the complementary one. This is not surprising, as sufficiently large magnetic fields suppress or align the helimagnetic correlations along their direction $[20]$. The intensive scattering above T_C defines the precursor region, which occurs over a temperature range that increases substantially with increasing Fe doping for $x < x^*$ [\[10,11](#page-9-0)[,24,33\]](#page-10-0).

V. DISCUSSION

The experimental results are summarized in the concentration dependence of the transition temperature, derived from previous susceptibility measurements [\[11\]](#page-9-0), and the pitch of the helix ℓ depicted in Fig. 9. These plots show that the transition temperature vanishes at $x_C \approx 0.17$ and that Fe substitution leads to a significant reduction of the helimagnetic pitch ℓ . In addition, a transition from long-ranged to shortranged helimagnetic correlations occurs already at $x^* \approx 0.11$.

In order to understand the evolution of the helimagnetic order with x , we consider the free energy per unit cell of a cubic chiral magnet such as Mn1−*^x*Fe*x*Si. This free energy is the sum of the ferromagnetic interaction, DM interaction, Zeeman, and magnetic anisotropy energies and is given by

$$
f = \frac{Ja^2}{2} \sum_{i=x,y,x} [\partial_i \hat{m} \cdot \partial_i \hat{m}] + aD\hat{m} \cdot \nabla \times \hat{m}
$$

$$
-a^3 \mu_0 M \hat{m} \cdot \vec{H} + f_a,
$$
 (2)

with a the lattice constant, \hat{m} the unit vector in the direction of the magnetization, *M* the magnetization value, *J* and *D* the strengths of the ferromagnetic exchange and DM interaction, respectively, and f_a the magnetic anisotropy contribution [\[26,27,34\]](#page-10-0). In this model, the transition temperature is proportional to *J*. By substituting the conical spiral ansatz, i.e., $\hat{m} =$ $\cos \theta \hat{e}_3 + \sin \left[\theta \cos(\vec{\tau} \cdot \vec{x})\hat{e}_1 + \sin(\vec{\tau} \cdot \vec{x})\hat{e}_2\right]$, with θ the cone angle, $\vec{\tau}$ the helical propagation vector, and $(\hat{e}_1, \hat{e}_2, \hat{e}_3)$ a set of orthogonal unit vectors, one can derive that the pitch of the helical modulation is, in the absence of Zeeman and magnetic anisotropy, given by $\ell = \frac{2\pi}{a} \frac{J}{D}$. Moreover, the field at which the conical-to-field polarized transition occurs at $T = 0$ K is $\mu_0 H_{C2}(0 \text{ K}) = \frac{D^2}{Ja^3M}$ [\[34\]](#page-10-0).

By comparing these expressions with the experimental results, we obtain that $J \to 0$ for $x \to x_c$. On the other hand, *l* is reduced from ∼18 nm for $x = 0.0$ to ∼6 nm at $x = 0.14$, i.e., by a factor of \approx 3, implying that D/J and thus the relative strength of the DM interaction increases with dilution. The DM interaction itself originates from the anisotropic

FIG. 9. Fe concentration dependence of (a) the critical temperature T_c and T' and (b) the pitch of the helix ℓ . The critical temperature T_c and T' , which mark the onset of the (short-ranged) helimagnetic correlations in the precursor phase, are adapted from [\[11\]](#page-9-0). LO indicates long-range helimagnetic correlations, SO shortrange helimagnetic correlations, P the precursor phase, and PM the paramagnetic phase.

exchange between the spins of the magnetic atoms and is thus a first-order correction to the Heisenberg exchange in spin-orbit coupling $\lambda : D \propto J_{\Delta}^{\lambda}$, with Δ the typical electron excitation energy on the site of the magnetic atom $[2,34]$ $[2,34]$. Thus, $D/J \propto \frac{\lambda}{\Delta} \propto \ell$, and although *J* vanishes at x_C , the ratio of *D/J* should remain finite, which is in good agreement with the experimental findings. Similar considerations explain why $\mu_0 H_{C2}(0 \text{ K})$ does not increase substantially as $x \to x_C$.

The helimagnetic order is already affected at dopings well below x_c . The helimagnetic spiral reorients at $x = 0.09$ from the $\langle 111 \rangle$ to the $\langle 110 \rangle$ crystallographic directions. Such a reorientation cannot be explained from the anisotropy term responsible for $\vec{\tau}$ || $\langle 111 \rangle$ at $x = 0$, $f_{a1} = K(m_x^4 + m_y^4 + m_z^4)$, as this term only has minima for $\vec{\tau}$ || $\langle 111 \rangle$ for $K < 0$ and $\vec{\tau}$ || $\langle 100 \rangle$ for $K > 0$ [\[3\]](#page-9-0). It therefore implies that other anisotropic terms become relevant. In fact, such a deviation from $\vec{\tau}$ || $\langle 100 \rangle$ or $\langle 111 \rangle$ is not unique to $Mn_{1-x}Fe_xSi$ but has been reported for the partially ordered state in MnSi under hydrostatic pressure [\[4](#page-9-0)[,35\]](#page-10-0).

As the helices do not align along a specific crystallographic lattice direction for $x > x^*$, we deduce that either the magnetic anisotropy is very weak or that disorder smears the effect of anisotropy. However, solely the differences in the anisotropy cannot explain the quantitatively different behavior for $x > x^*$. Indeed, the correlation length remains finite for these dopings down to the lowest temperature and magnetic fields do not raise the directional degeneracy as they do not align all helices along their direction. Differences between the magnetic behavior have also been reported based on measurements of bulk quantities $[11-13]$ and it has been suggested that the crossover at x^* is due to quantum fluctuations that destabilize the long-range helimagnetic order [12,14–16]. In this approach, *x*[∗] would be a quantum critical point. We conjecture that this is not necessarily the case because the disappearance of long-range helimagnetic correlations might be due to chemical disorder. This hypothesis is supported by the data obtained under magnetic field (Fig. [5\)](#page-5-0) that show a complex magnetization process. In this process, the magnetic field first breaks the longer helices, possibly those that encompass the lowest degree of disorder, whereas the shorter helices are more robust.

The isotropic zero magnetic field SANS patterns in combination with the finite helical correlations for $x > x^* \approx$ 0*.*11 indicate that *x*[∗] is associated with the disappearance of long-range periodic helimagnetic order and that the shortranged helimagnetic correlations for $x > x^*$ are completely degenerate in space. However, from these results it is not clear whether this helimagnetic state fluctuates, as in the precursor phase in MnSi above T_c [18,20], or not. The final answer can be given by additional inelastic neutron scattering or muon spin spectroscopy experiments.

VI. CONCLUSION

In conclusion, the results show that the helimagnetic order in Mn1−*^x*Fe*x*Si is suppressed with increasing Fe content. The

long-range helimagnetic correlations, which reorient at zero magnetic from $\langle 111 \rangle$ at low Fe concentrations toward $\langle 110 \rangle$ at $x = 0.09$, disappear completely for $x > x^*$. The helices have for $x > x^*$ finite lengths, are completely degenerate in space, and bear similarities to those found in the precursor phase of MnSi. Magnetic fields gradually suppress and partly align these helices along their direction trough a complex magnetization process.

ACKNOWLEDGMENTS

The authors thank the ISIS support staff for their assistance and are grateful for the kind help of G. Stenning and R. Perry with aligning the single crystals and B. Pedersen for testing our initial crystals with Neutron Laue Diffraction at FRMII. R.W.A. Hendrikx at the Department of Materials Science and Engineering of the Delft University of Technology is acknowledged for the XRF analysis. M. Mostovoy is acknowledged for fruitful discussions. D. Bosma is acknowledged for EDS/SEM analysis of the single crystals. Experiments at the ISIS Pulsed Neutron and Muon Source were supported by a beam-time allocation from the Science and Technology Facilities Council and The Netherlands Organization for Scientific Research (NWO). The work of L.B. and C.P. is financially supported by The Netherlands Organization for Scientific Research through Project 721.012.102 (Larmor). F.W. was supported by the Helmholtz Society under Contract No. VH-NG-840.

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