# Conductivity and transparency limits of Sb-doped SnO<sub>2</sub> grown by molecular beam epitaxy

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Ultraviolet (UV)/visible/infrared (IR) transmission spectroscopy, Hall effect measurements and synchrotron x-ray photoelectron spectroscopy were used to determine the limits of Sb doping on the electrical and optical properties of single crystal SnO<sub>2</sub> (101) films grown by molecular beam epitaxy. The resistivity ( $\rho$ ) and carrier density (n) of these Sb:SnO<sub>2</sub> films could be varied by more than seven orders of magnitude, covering the insulating, semiconducting, and semimetallic regimes, by adjusting the Sb fraction in the incident metal flux from 0 to 3.0 at. %, corresponding to a Sb incorporation of up to  $8 \times 10^{20}$  atoms/cm<sup>3</sup>. A maximum conductivity limit of  $\rho \approx 6 \times 10^{-4} \,\Omega$  cm and  $n \approx 4 \times 10^{20} \,\text{cm}^{-3}$  was determined at approximately  $3 \times 10^{20} \,\text{Sb}$  atoms/cm<sup>3</sup>, after which an increase in  $\rho$  (and decrease in n) with increasing Sb flux was observed, most likely due to charge compensation arising from the preferential formation of  $Sb^{3+}$  acceptors. The limits for the coexistence of transparency and electrical conductivity were found to be governed by a Burstein-Moss shift of the optical gap  $(E_{out})$  in the UV spectrum and a much larger blue shift of the free-carrier adsorption edge in the IR region due to an increasing plasma frequency ( $\omega_{\rm p}$ ), with both effects scaling with the carrier concentration of the Sb:SnO<sub>2</sub> films. Despite these effects, the transparency window in the visible region was almost unaffected, with more than 90% transmission in the 350–1500 nm range for 150-nm-thick Sb:SnO<sub>2</sub> films at the conductivity limit. The density of states reduced effective mass and the conductivity effective electron mass were determined from the variation of  $\omega_p$  and  $E_{opt}$  with *n*, resulting in values of  $(0.46 \pm 0.12) m_e$  and  $(0.31 \pm 0.10) m_e$ , with the difference consistent with a shrinkage of the fundamental gap due to many-body interactions. Finally, the correlation between the changes in  $E_{opt}$  and n with increasing Sb incorporation was used to provide an estimate for the charge neutrality level of  $SnO_2$  of +0.49 eV above the conduction band minimum.

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#### I. INTRODUCTION

Wide band gap transparent conducting oxides (TCOs) that combine both high transparency and strong electrical conductivity are the subject of significant research interest due to their increasing use in solar cell technology, touch screens, optical displays, and transparent electronic devices [1-4]. Among these, stannic oxide  $(SnO_2)$  is a promising earth-abundant transparent binary oxide, with an unusually high chemical stability and low toxicity, which is already found in solar cells and gas sensing devices [5,6]. SnO<sub>2</sub> crystallizes in the rutile structure with a tetragonal unit cell of the group P42/mnm and lattice constants a = b = 4.7374 Å and c = 3.1864 Å [7]. While insulating in its pure stoichiometric form, SnO<sub>2</sub> usually possesses a significant unintentional *n*-type conductivity [7] that is generally attributed to nonstoichiometric effects, although there is significant debate as to the identity of the defects responsible. Central to this debate is a disagreement over the nature of oxygen vacancies  $(V_0)$  as either deep or shallow donors in SnO<sub>2</sub>, due to the different band gap corrections used in the first principles calculation of defect level states [8-12]. It has been proposed that interstitial tin (Sn<sub>i</sub>) forms a spontaneously ionized donor level 203 meV above the conduction band minimum and directly promotes the formation of oxygen vacancies, an effect assisted by the multivalence nature of Sn (i.e., Sn<sup>4+</sup> and Sn<sup>2+</sup>). However, other theoretical studies have questioned the role of Sn<sub>i</sub> as a significant donor, due to its high formation energy and low migration barrier [9, 12, 13]. It has also been shown that hydrogen exclusively acts as a donor in SnO<sub>2</sub> (and many other TCOs), in particular forming a shallow donor level inside an oxygen vacancy (H<sub>0</sub>) where it is stabilized by multicentered bonding with the nearest-neighbor cations [9]. King et al. [13,14] have proposed that the unintentional *n*-type conductivity of  $SnO_2$  and other TCOs, such as ZnO,  $In_2O_3$ , and CdO can be explained by the fact that their charge neutrality level (CNL) are located above the conduction band minimum (CBM), which tends to favor the formation of donor-like native defect, localized impurity, and surface states. This is in contrast to most other semiconductors in which the CNL lies within the fundamental gap.

Transport measurements of unintentionally doped (UID) poly- and single-crystalline SnO<sub>2</sub> films typically show carrier concentrations (*n*), mobilities ( $\mu$ ), and resistivities ( $\rho$ ) in the range of  $10^{17}-10^{20}$  cm<sup>-3</sup>, 10-100 cm<sup>2</sup>/Vs and  $10^{-2}-10^{-3} \Omega$  cm, respectively [15–17]. Further increases in the conductivity of SnO<sub>2</sub> have usually been achieved by intentionally doping the host material with Sb and F in the 1% to 25% range [16–20]. Co, Mo, and Ni have also been

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used as donors but to a lesser extent [15,21,22]. Like all TCOs, ambipolar doping is problematic, although Al, Ga, and In have been investigated as potential acceptor candidates [4,23].

Theoretical calculations [24,25] are known to significantly underestimate the fundamental band gap of  $SnO_2$ , which is a posteriori corrected to a typical value of 3.6 eV [8,9,24,25]. Experimental studies on the optical properties of SnO<sub>2</sub> have reported direct optical band gaps in the range of 3.5–4.2 eV [21,26–29]. The wide range of reported values has been attributed to variations in crystalline quality, stoichiometry, and impurity content of different SnO<sub>2</sub> materials, and also to the diversity of experimental and analytical methods employed for its determination [26–29]. Sabino et al. [30] have recently shown that in oxides such as SnO<sub>2</sub>, in which selection rules prevent transitions from the valence band maximum to the conduction band minimum, intense illumination can promote weak transitions from near the top of the valence band, leading to optical band gap values close to the fundamental gap. However, under low and moderate illumination conditions only strong transitions are accessible, resulting in a widening of the optical band gap of up to  $\sim 0.7$  eV in the case of SnO<sub>2</sub> [30].

Despite its potential for transparent electronics and sensing applications [21,31-33], the study of the fundamental nature of SnO<sub>2</sub> has been hindered by the lack of commercially available single crystals and by the defective nature of UID material produced by most deposition techniques, which typically results in carrier concentrations in the  $10^{18}$ – $10^{20}$  cm<sup>-3</sup> range [7,17,34,35]. The reproducible growth of high structural quality, single crystal material is required to explore the optical and electrical limits of SnO<sub>2</sub>. Previous work [23,36] concerning the growth of single crystal SnO<sub>2</sub> films by plasma assisted molecular beam epitaxy (PAMBE) explored the conditions that produced single phase material, with a particular focus on maximizing the growth rate. These studies produced UID epitaxial SnO<sub>2</sub> (101) thick films (of up to 1500 nm) with *n* as low as  $3 \times 10^{17}$  cm<sup>-3</sup> and  $\mu$  up to 15 cm<sup>2</sup>/Vs (26 nm single layer) and  $100 \text{ cm}^2/\text{Vs}$  (1570 nm including a very thick buffer layer). While not electrically intrinsic in nature, these films allowed an exploration of the semiconducting regime of the material, a region not previously accessible. Subsequent Sb-doping during PAMBE growth produced a monotonic decrease in resistivity with doping level suggesting that all the Sb atoms were incorporated as ionized donors. Despite the high carrier concentrations obtained for Sb-doped SnO<sub>2</sub> films (up to  $2.8 \times 10^{20}$  cm<sup>-3</sup>), these studies did not establish the Sb:doping limit for PAMBE SnO<sub>2</sub> [17,37] or explore the effect of Sb doping on the transparency window of SnO<sub>2</sub>.

In this work, we have optimized the PAMBE growth of SnO<sub>2</sub> (101) films to obtain intrinsic, highly resistivity material with  $\rho > 1 \text{ k} \Omega$  cm and  $n < 10^{14} \text{ cm}^{-3}$ , with high bulk crystallinity and atomically abrupt step-terraced surfaces. These films represent the highest quality intrinsic, single crystalline SnO<sub>2</sub> (101) films reported so far and are therefore ideal springboards to explore the ultimate limits of the material. These intrinsic SnO<sub>2</sub> (101) films were used to investigate the effects of Sb doping on the electrical and optical properties of SnO<sub>2</sub> and explore the limits for the coexistence of high transparency and conductivity in this technologically important TCO.

### **II. EXPERIMENTAL METHODS**

Intrinsic SnO<sub>2</sub> films of thicknesses up to 600 nm were grown by PAMBE in a Thermionics ultrahigh vacuum chamber with a base pressure lower than  $4 \times 10^{-9}$  Torr. Doublesided polished r-plane sapphire substrates ([1–102], MTI corp.) were used to induce heteroepitaxial growth in the (101) direction with minimal lattice mismatch. A high temperature effusion cell (e-science Inc.) operated from 900 to 1200 °C was used to produce a metallic beam of Sn (99.999%, Lesker Company Ltd.), while an Oxford Applied Research HD25 RF plasma source operated at 200W was used to generate an oxygen plasma beam at  $3.5 \times 10^{-5}$  Torr that produced oxygen-rich conditions, as indicated by Sn/O flux calculations and previous literature reports [23]. At the limits of our xray diffraction (XRD) and x-ray photoelectron spectroscopy (XPS) studies, these conditions produced stoichiometric SnO<sub>2</sub> (101) films, with no other phases observed. An e-science LT Titan effusion cell was used as the Sb source (99.999%, Kamis Inc.) to explore the doping limits of Sb:SnO<sub>2</sub> films. Source and dopant atomic fluxes were calibrated with a MacVac quartz crystal microbalance that measured the Sn/Sb atomic flux ratio incident on the substrate. Sb atomic concentrations were determined by calibrated secondary ion mass spectroscopy (SIMS) measurements conducted in a Cameca IMS-6f ion microprobe system using a positive Caesium beam. A Staib RH20 reflection high energy electron diffraction (RHEED) system operating at 20 kV provided real-time assessment of the epitaxial growth mode, lattice matching, and surface crystallinity.

Substrate preparation involved sonication in trichloroethylene, acetone, and methanol followed by indium-bonding to a molybdenum mounting block that was then loaded into the molecular beam epitaxy (MBE) chamber. In situ preparation of the substrate surface involved a 30-min bake at 800 °C, followed by a 30-min oxygen plasma treatment at 800 °C. This produced a pristine, epi-ready surface, evidenced by sharp RHEED patterns with distinct Kikuchi lines. No further RHEED improvement was observed after an additional 800 °C annealing step, as used elsewhere [38–40], and atomic force microscopy (AFM) and XRD studies of films grown with and without this step were undistinguishable from each other. A total of 46 UID SnO2 films obtained at different substrate temperatures, cell temperatures, and film thicknesses were used to explore the growth modes involved, optimize film quality, and assess the origin of the electrical conductivity in UID SnO<sub>2</sub> films.

The surface morphology of the films was studied *ex situ* in a Raith 150 scanning electron microscope (SEM) at typical accelerating voltages of 10 kV and in a Veeco Dimension 3100 AFM operated in tapping mode. The thicknesses of the resulting SnO<sub>2</sub> films ranging from 20 to 600 nm were measured using a high resolution JEOL JSM-7000F SEM, while specular x-ray reflectivity (XRR) techniques were adopted for sub-20 nm films. A Bruker D8 diffractometer equipped with a Co radiation source was used to investigate the crystal orientation and the quality of the films, via  $\theta$ -2 $\theta$  and  $\omega$  scans in the Bragg-Brentano configuration, respectively. XPS studies conducted at the soft x-ray (SXR) beamline of the Australian Synchrotron confirmed the stoichiometry of the intrinsic SnO<sub>2</sub> films and the presence of Sb in the doped material. The optical properties of the  $SnO_2$  films were explored in the ultraviolet (UV), visible, near-infrared (IR) and mid-far IR parts of the spectrum with an Agilent Cary 6000i spectrophotometer, a Bruker Tensor 37 Fourier-transform infrared (FTIR) system and a Bruker Vertex 70 FTIR system, covering a wide spectral range from 200 to 16 000 nm.

The electrical properties of the films were investigated using an EGK HEM-2000 Hall effect measurement system and an Agilent B1500A semiconductor device analyzer. Resistivity measurements were performed in the van der Pauw configuration and the carrier type, carrier concentration, and mobility at room temperature were obtained through Hall measurements conducted under a 0.51 T magnetic field.

# **III. RESULTS AND DISCUSSION**

# A. Intrinsic UID SnO<sub>2</sub> (101) films

An extensive study of the effect of growth conditions on the structural, optical, and electrical properties of PAMBE SnO<sub>2</sub> was initially carried out to establish the optimal conditions for producing the highest quality intrinsic SnO<sub>2</sub> (101) films (as described in detail in the supplementary information [41]). These optimized conditions involved substrate and Sn cell temperatures of 800 and 1075 °C, respectively, and low growth rates of less than 1 nm/min, resulting in ~100-nm films characterized by streaky RHEED patterns both during and after growth, XRD  $\omega$ -FWHM of (0.6 ± 0.1)°, and atomically smooth surfaces with abrupt step-terraces (see Fig. 1).

Figure 2 presents the UV-visible transmission spectra of a typical 100-nm-thick UID SnO<sub>2</sub> (101) film grown using the optimized conditions, showing more than 93% transmission across the entire visible range. The inset shows the corresponding Tauc plot from which an optical band gap of  $(4.03 \pm$ 0.03 eV) was extracted. Synchrotron XPS was used to assess the near-surface stoichiometry of the intrinsic SnO<sub>2</sub> (101) films. While the Sn 3d emission has been used to distinguish SnO from SnO<sub>2</sub> [42], this analysis can be susceptible to misinterpretation because the relatively small difference in binding energy between  $\text{Sn}^{2+}$  and  $\text{Sn}^{4+}(\langle 0.7 \text{ eV} \rangle)$  can be obscured by screening effects that vary with the carrier concentration of the material [43,44]. Conventional analysis of O 1s and Sn 3d core level spectra is therefore not considered to be effective in distinguishing SnO<sub>2</sub> from SnO [45,46], and instead the valence band (VB) spectra was used to identify the predominant phase [45–49]. A well-established method for distinguishing SnO<sub>2</sub> from SnO involves studying the energetic separation between the Sn 4d 5/2 emission and the lowest binding energy (BE) peak in the VB region [7]. The energy difference between these features in SnO is known to be close to 23.7 eV, more than 2 eV larger than in SnO<sub>2</sub> (21.1 eV) [7,45,46,49]. In addition, a Sn<sup>2+</sup> related shoulder at BE between 2 and 3 eV is also associated with the presence of a SnO phase [46,49]. Conversely, the lack of this shoulder and the presence of a distinct emission with a BE close to 10 eV (assigned to Sn 5s-O 2*p* bonding states) is a spectral signature of  $SnO_2$  [46–49]. The 2-3 eV shoulder has also been attributed to Sn-Sn defects [42], although our studies show that the annealing of similar SnO<sub>2</sub> films removes surface oxygen, forming a SnO-like

surface that is accompanied by the emergence of this spectral feature. This shoulder also disappears upon reoxidation of the surface in ambient conditions. Our interpretation is also in agreement with previous studies on SnO films, which showed the appearance of the 2–3eV emission as the topmost  $SnO_2$  surface layer was removed [46].

Figure 3 shows a typical XPS spectrum of the intrinsic  $SnO_2$  (101) films in which the energy difference between the Sn 4*d* 5/2 emission and the lowest BE VB peak (~21.2 eV) is characteristic of SnO<sub>2</sub>. In addition, the absence of the 2–3 eV shoulder associated with SnO and the strong emission close to 10 eV indicates the presence of a pure SnO<sub>2</sub> phase.

The improvement in crystal quality and surface roughness achieved in the optimization of the intrinsic UID SnO<sub>2</sub> (101) PAMBE films (see supplementary information [41]) was accompanied by a significant increase in electrical resistivity, consistent with a defect origin (Sn<sub>i</sub> and  $V_{\Omega}$  or  $H_{\Omega}$ ) of the unintentional *n*-type conductivity of SnO<sub>2</sub>. Significantly, the resistivity of the fully-optimized UID  $SnO_2$  (101) films was beyond the measurements limit of  $\rho > 1 \text{ k}\Omega \text{ cm}$  regardless of thickness, indicating intrinsic-like material quality. In addition, the resistivity of the partially optimized UID  $SnO_2$  (101) films (grown at a Sn cell temperature of 1100 °C instead of 1075 °C) was found to increase with film thickness, as shown in Fig. 4. RHEED, AFM, and XRD/XRR studies comparing the coherent and the total thickness (see supplementary information [41]) indicated a high concentration of structural defects within the first five atomic layers of the film and a much lower concentration in subsequent layers once the lattice mismatch between the substrate and film had been accommodated and epitaxial growth established. The large increase in resistivity with film thickness is therefore a consequence of the highly localized nature of the defects responsible for the electrical conductivity in these films.

# B. Sb-doped SnO<sub>2</sub> (101) films-limit of conductivity

A wide range of 150-nm-thick, Sb-doped,  $SnO_2$  (101) PAMBE films (Sb:SnO<sub>2</sub>) were grown to investigate the electrical and transparency limits of Sb:SnO<sub>2</sub> as a TCO. The films were deposited using the previously established optimized growth conditions, i.e., a substrate temperature of 800 °C, Sn and Sb fluxes coevaporated at temperatures of 1075 °C and 180-360 °C, respectively, and a 200-W oxygen plasma beam at a partial pressure of  $3.5 \times 10^{-5}$  Torr. These conditions allowed the Sb fraction in the total incident metallic flux to be varied between 0 and 3.0 at. %, while maintaining the single phase growth of high quality Sb:SnO<sub>2</sub> (101) material as indicated by RHEED and XRD measurements. Figure 5(a)shows the effect of Sb doping on the resistivity at 300 K of the resulting Sb:SnO<sub>2</sub> films, where the efficient incorporation of Sb donors is evident by a more than four orders of magnitude decrease in resistivity for Sb concentrations of less than  $4 \times$  $10^{19}$  atoms/cm<sup>3</sup>.

Figure 5(a) also shows that as the Sb concentration increases beyond  $\sim 3 \times 10^{19}$  atoms/cm<sup>3</sup>, the rate of decrease in resistivity significantly slows and a turning point is reached at a Sb concentration of  $\sim 3 \times 10^{20}$  atoms/cm<sup>3</sup>, corresponding to a minimum resistivity of  $\rho \approx 6 \times 10^{-4} \Omega$  cm. Any further

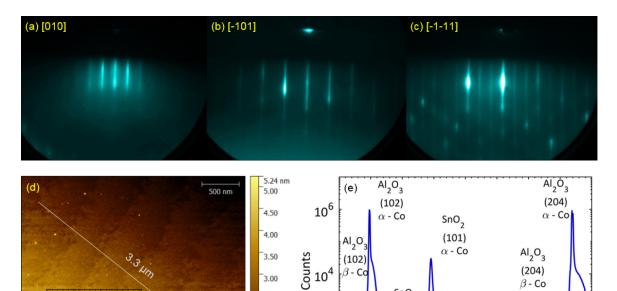
(204)

β-Co

55

65

60



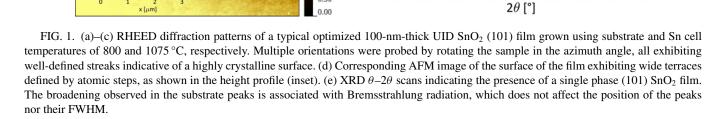
3.00

2.50

2.00

1.50 1.00

0.50



 $10^{2}$ 

25

30

SnO<sub>2</sub>

(101)

35

40

increase in the Sb fraction resulted in a gradual increase in resistivity, indicating that a maximum Sb doping limit for the increase of n-type conductivity in Sb:SnO<sub>2</sub> had been reached. This limit can also be seen in the dependence of carrier concentration on Sb fraction, shown in Fig. 5(b), where a maximum value of  $n \approx 4 \times 10^{20}$  cm<sup>-3</sup> occurs at the same

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 $\sim 3 \times 10^{20}$  atoms/cm<sup>3</sup> Sb concentration as for the resistivity minimum.

45

50

An almost unity relationship was observed between the carrier concentration and Sb atomic concentration in the  $3 \times 10^{19}$  to  $3 \times 10^{20}$  atoms/cm<sup>3</sup> range [Fig. 5(b)] that indicates a Sb<sup>5+</sup> donor efficiency of close to 100% over this

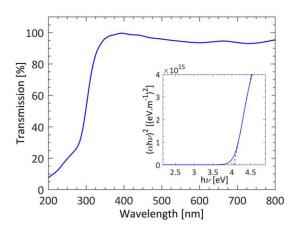


FIG. 2. UV-visible transmission spectra of a typical optimized 100-nm-thick UID SnO<sub>2</sub> (101) film with the inset showing the Tauc plot used to determine the optical band gap.

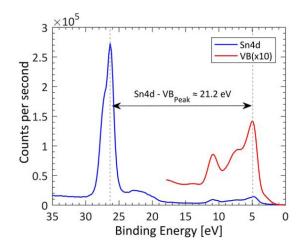


FIG. 3. Room temperature XPS spectra of the Sn 4d 5/2 (blue) and valence band (red) region of a typical intrinsic SnO<sub>2</sub> (101) film. The energy difference between the Sn 4d 5/2 peak and the VB lowest BE peak is in agreement with that reported for pure SnO<sub>2</sub>.

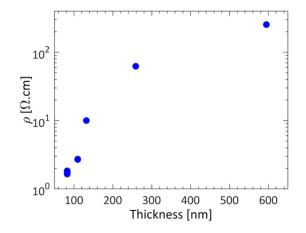


FIG. 4. Electrical resistivity of undoped SnO<sub>2</sub> (101) films as a function of film thickness measured using the Van der Pauw method at 300 K. Note: these films were only partially optimized, being grown at a Sn cell 1100 °C instead of 1075 °C. This was necessary because the resistivity of the fully optimized films at all thickness was above the  $\rho > 1 \,\mathrm{k\Omega}$  cm measurement limit of the semiconductor parameter analyzer.

range. This is in agreement with previous studies by White et al. [17] and Feneberg et al. [50] on Sb-doped SnO<sub>2</sub> films grown by PAMBE under similar conditions. However, these studies only explored a maximum Sb concentration of  $2.8 \times$  $10^{20}$  atoms/cm<sup>3</sup> and therefore the effects of Sb doping beyond this point cannot be compared. The significantly higher doping levels achieved in this work accessed an additional regime characterized by a significant decrease in donor efficiency resulting in a maximum conductivity limit. This indicates the emergence of a charge compensation mechanism, possibly due to the presence of Sb in the +3 valence state at higher doping levels. High-resolution XRD (HRXRD) and photoluminescence (PL) studies on epitaxial and polycrystalline films have reported Sb<sup>5+</sup>/Sb<sup>3+</sup> compensation occurring at doping levels in the 1-10% wt. range, which is consistent with the results obtained herein [27,34,51].

Our interpretation of the decrease in carrier concentration that limits the conductivity of Sb:SnO2 films is due to a competition between  $Sb^{5+}$  and  $Sb^{3+}$  as the substituting species. At lower Sb concentrations, the doping mechanism favors Sb<sup>5+</sup> ions substituting Sn<sup>4+</sup> ions in the SnO<sub>2</sub> lattice, donating electrons to the conduction band and thus increasing the carrier concentration and decreasing the resistivity of the material (i.e., the region up to  $\sim 3 \times 10^{20}$  Sb atoms/cm<sup>3</sup> in Fig. 5). As the Sb concentration increases, the formation energy for  $Sb^{3+}$ substitution of  $Sn^{4+}$  ions decreases [35,52,53]. In this valence state, Sb<sup>3+</sup> on Sn<sup>4+</sup> sites produces an acceptor concentration that reduces the number of carriers available for conduction and increases the resistivity of the sample (i.e., the  $3 \times 10^{20}$  to  $8 \times 10^{20}$  Sb atoms/cm<sup>3</sup> region in Fig. 5). While the presence of this charge compensation model has been proposed in SnO<sub>2</sub> polycrystalline films [27,34,51], the results presented here are evidence of the mechanism occurring in high quality single crystal SnO<sub>2</sub>.

Within this model, the observed conductivity limit at an Sb concentration of  $\sim 3 \times 10^{20}$  atoms/cm<sup>3</sup> corresponds to the position of the Fermi level for which the formation energy

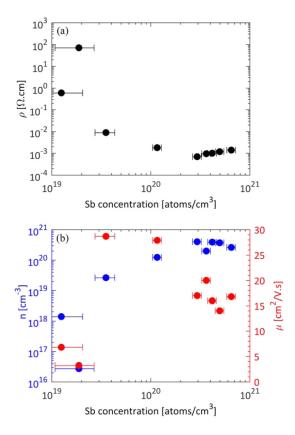


FIG. 5. (a) Resistivity (black), (b) carrier concentration (blue) and carrier mobility (red) of 150-nm-thick Sb:SnO<sub>2</sub> (101) films grown by PAMBE as a function of the atomic Sb concentration. Note: the carrier concentration of the intrinsic UID film at an Sb flux = 0% was less than  $10^{14}$  cm<sup>-3</sup>.

of donor-like Sb<sup>5+</sup> and acceptor-like Sb<sup>3+</sup> substituents are the same. The limiting *n* observed in this work is in close agreement with the maximum values reported for other Sbdoped epitaxial SnO<sub>2</sub> films (Table I), thus supporting the proposed model for the maximum limit for Sb doping in SnO<sub>2</sub>. Interestingly, the conductivity limit of  $n \approx 4 \times 10^{20}$  cm<sup>-3</sup> is the same as that observed by Swallow *et al.* [20] in a recent study of self-compensation in F-doped SnO<sub>2</sub>, suggesting that conductivity limit in SnO<sub>2</sub> films may be the same for different dopants.

Swallow et al. [20] used XPS analysis to explore a similar compensation mechanism in heavily doped F-SnO<sub>2</sub> films, with interstitial fluorine (F<sub>i</sub>) acting as single-charged acceptors that compensate substitutional fluorine ( $F_0$ ) donors, thus limiting the *n*-conductivity of the films. Unfortunately, such analysis was not possible in our Sb-doped films because the binding energies of Sb3d<sub>5/2</sub> emission associated with the Sb<sup>5+</sup> and Sb<sup>3+</sup> oxidation states are relatively close to each other and also directly overlap the O 1s spectral region, thus making any deconvolution of these states unreliable [54]. In addition, the O 1s emission also exhibits considerable spectral broadening due to adsorbed OH and H<sub>2</sub>O species which further complicates any attempt of deconvolution [54,55]. Analysis of other Sb-related XPS peaks (such as the  $Sb3d_{3/2}$ emission) was not possible due to their weak intensities and high signal-to-noise ratios, even with the use of Synchrotron

Method	Orientation	Dopant	$n \ [\times 10^{20} \mathrm{cm}^{-3}]$	$\mu$ [ cm <sup>2</sup> /Vs]	$\rho$ [×10 <sup>-3</sup> Ω cm]	Reference
MOCVD <sup>a</sup>	(101)	Sb	2.5	18	1.3	[52]
MBE	(101)	Sb	2.6	36	0.7	[17]
MBE	(101)	Sb	4.0	17	0.6	This work
MBE	(100)	Sb	4.1	4.5	3.4	[37]
MOCVD	(100)	Sb	5.3	12	0.9	[35]
APCVD <sup>b</sup>	-	F	4.0	40	0.4	[20]

TABLE I. Maximum *n* and corresponding  $\mu$  and  $\rho$  of epitaxial Sb:SnO<sub>2</sub> films.

<sup>a</sup>Metal-organic chemical vapor deposition.

<sup>b</sup>Atmospheric-pressure CVD.

radiation. However, Terrier *et al.* [56] were successful in deconvoluting the Sb<sup>3+</sup> and Sb<sup>5+</sup> contributions to the Sb3d<sub>3/2</sub> peak in highly doped SnO<sub>2</sub> films grown by sol-gel, and they showed the emergence of the Sb<sup>3+</sup> contribution as the Sb concentration increased beyond 4%, until it became the dominant component at 22%. This dominant Sb<sup>3+</sup>/Sn<sup>4+</sup> substitution at high Sb concentration was accompanied by a plateau in the (so far decreasing) resistivity, in agreement with the results presented here and with the compensation model proposed.

While no significant degradation in the structural quality of the 150-nm Sb:SnO<sub>2</sub> films with increasing Sb fraction was observed using *in situ* RHEED and *ex situ* XRD, the incorporation of Sb atoms had a significant effect on the carrier mobility, as shown in Fig. 5(b). Peak carrier mobilities of  $29 \text{ cm}^2/\text{V}$  s were obtained at Sb concentration of  $3.5 \times 10^{19} \text{ atoms/cm}^{-3}$ . As the incorporation of Sb increases (in both Sb<sup>5+</sup> and Sb<sup>3+</sup> forms), increased ionized impurity scattering reduces the mobility to the  $13-19 \text{ cm}^2/\text{V}$  s range. Higher mobilities approaching  $100 \text{ cm}^2/\text{V}$  s have been reported for much thicker (~1500 nm) Sb:SnO<sub>2</sub> PAMBE films that also involved a thick UID SnO<sub>2</sub> buffer layer whose contribution was analytically separated.

The highly resistive nature of the intrinsic PAMBE  $\text{SnO}_2$ material grown here allowed carrier concentration control via Sb doping (without the need for a buffer layer) over  $<10^{14}-10^{20} \text{ cm}^{-3}$  range encompassing the insulating, semiconducting, and semimetallic transport regimes.

### C. Sb-doped SnO<sub>2</sub> (101) films-limit of transparency

Figure 6 shows the effect of Sb doping on the UV-visible-IR transparency of the 150-nm-thick Sb:SnO<sub>2</sub> (101) PAMBE films. More than 95% transparency across the entire 350– 10 000 nm range was observed in films with carrier concentrations of up to  $10^{18}$  cm<sup>-3</sup> (corresponding to Sb concentration of up to  $2 \times 10^{19}$  atoms/cm<sup>-3</sup>). Further increase in carrier concentration significantly reduced the transparency of the films in the mid-IR region, with a more than tenfold reduction in the size of the IR transparency window for Sb:SnO<sub>2</sub> (101) films at the carrier concentration limit of  $n \approx 4 \times 10^{20}$  cm<sup>-3</sup>.

In the mid/far-IR region the transparency loss is associated with free-carrier oscillations, characterized by the plasma cut-off frequency  $\omega_p$ , and by its effect on the permittivity  $\boldsymbol{\varepsilon}$  of the medium. In the Drude model these effects are given by

$$\omega_{\rm p}^{\ 2} = \frac{e^2}{\varepsilon_0 \varepsilon_\infty m_{\rm c}^*} \, n, \tag{1}$$

$$\boldsymbol{\varepsilon} = \varepsilon_{\rm Re} + i\varepsilon_{\rm Im} = \left(1 - \frac{\omega_{\rm p}^2}{\omega^2}\right) + i\left(\frac{\varepsilon_{\infty}\omega_{\rm p}^2}{\omega^3\tau}\right), \qquad (2)$$

where *e* is the electron charge, *n* is the carrier concentration,  $\varepsilon_{\infty}$ ,  $\varepsilon_0$  are the high frequency and free space permittivity respectively,  $m_c^*$  is the conductivity effective mass,  $\omega$  is the incident wave frequency, and  $\tau$  is the relaxation time between collisions. As the carrier concentration increases, *e* becomes imaginary for progressively shorter wavelengths [Eq. (2)] producing a blue-shift of the IR adsorption edge. However, it is clear from Fig. 6 that while the shift of the plasma edge to lower wavelengths resulted in a significant reduction of the IR transparency window, it had little effect on the transparency of the Sb:SnO<sub>2</sub> films in the visible spectrum. Even at the carrier concentration limit of  $n \approx 4 \times 10^{20}$  cm<sup>-3</sup> the Sb:SnO<sub>2</sub> films maintained more than 90% transparency across the 350– 1500 nm range.

In the UV region (see Fig. 6) the band edge is noticeably blue shifted as n increases. This is due to the Burstein-Moss (BM) effect whereby the increasing carrier concentration leads to the filling of lowest conduction band states. This

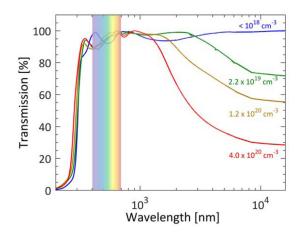


FIG. 6. UV-visible-IR spectra of 150-nm-thick  $Sb:SnO_2$  (101) films with increasing carrier concentration.

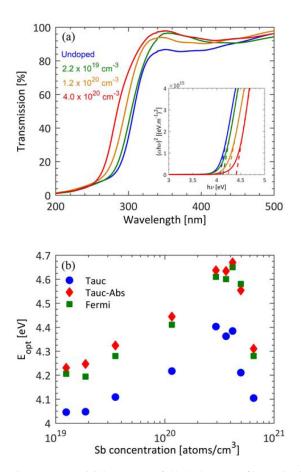


FIG. 7. (a) UV-visible spectra of Sb:SnO<sub>2</sub> (101) films with increasing doping level. Inset: Tauc plot used for extracting the optical band gap, exhibiting a strong BM shift. (b) Optical band gap obtained from UV-visible studies, indicating the filling of the conduction band as the Sb concentration increases and suggesting the emergence of the Sb<sup>5+</sup>/Sb<sup>3+</sup> charge compensation mechanism for Sb doping levels beyond  $3 \times 10^{20}$  atoms/cm<sup>3</sup>. Circles, diamond, and square markers correspond to the values extracted from Tauc plots, combined Tauc and absorption coefficient extrapolation, and Fermi-Dirac fits of the absorption edge.

raises the Fermi level into the conduction band, increasing the energy of the lowest energy band-to-band optical transitions due to Pauli blocking. Fig. 7(a) shows the transmission of typical Sb:SnO<sub>2</sub> films in the UV-visible region in greater detail, in which the BM shift with increasing *n* can be more clearly seen.

The corresponding Tauc plots used to extract  $E_{opt}$  are shown in the inset of Fig. 7(a). While obtaining the optical band gap using Tauc plots is only strictly valid in the case of nondegenerate semiconductors under the parabolic band approximation, this method has been widely used in the literature for a wide range of doping levels. We have, therefore, included Tauc plots in our analysis to allow a comparison of our results with previous studies. However, alternative methods for obtaining the optical gap from transmission or absorption spectra have been proposed by Dolgonos *et al.* [57] using time-dependent perturbation theory. These methods involve the use of combined Tauc and absorption coefficient spectra plots or direct Fermi-Dirac distribution fitting of the absorption spectra. Both methods were also used in this work with the results shown in Fig. 7(b). Although the absolute values of  $E_{opt}$  vary between methods (i.e., being ~150 meV higher using the two methods of Dolgonos *et al.*) the relative trends and BM shifts are almost identical. Figure 7(b) shows the dependence of  $E_{opt}$  with Sb concentration, which is characterized by a rapid increase of  $(0.49 \pm 0.08)$  eV as the Sb fraction is increased up to ~3 × 10<sup>20</sup> atoms/cm<sup>3</sup>, followed by a decrease in  $E_{opt}$  for Sb fractions beyond this value. This dependence mirrors the relationship between the carrier concentration and Sb fraction shown in Fig. 7(b) that also reaches a maximum at a Sb concentration of ~3 × 10<sup>20</sup> atoms/cm<sup>3</sup>.

As expected, the maximum BM shift in  $E_{opt}$  of 0.49 eV coincides with the maximum conductivity limit  $n \approx 4 \times$  $10^{20}$  cm<sup>-3</sup> of the Sb:SnO<sub>2</sub> films. Within the CNL model, this value can be used to provide an estimate for the CNL of SnO<sub>2</sub>, of  $E_{\text{CNL}} = E_{\text{CBM}} + (0.49 \pm 0.08) \text{eV}$ . Within the model, the CNL provides a guide to the position of  $E_{\rm F}$  at which the formation energies of donor-like and acceptor-like forms of certain localized impurity and native defects are likely to be the same [13,14]. This would be expected to occur near the conductivity limit assuming the formation energies of both the dopant and native defect states involved follow similar trends or if the concentration of native defects is negligible compared to that of the donor  $(Sb^{5+})$  and acceptor-like  $(Sb^{3+})$ states associated with Sb doping. The very good crystalline quality of both the undoped and Sb-doped films up to the conductivity limit as observed in both XRD and RHEED measurements suggest that the latter may indeed be the case in the films studied here. Despite these assumptions, the experimentally derived CNL value for SnO<sub>2</sub> is very close to the theoretical value of  $E_{\rm C} + 0.5$  eV reported by Falabretti and Robertson [58,59]. The discrepancy may be in part due to many-body effects caused by the high free electron density at the conductivity limit, which can result in band-gap narrowing and cause the energetic separation between the CNL and the CBM to be underestimated [60,61]. Vasheghani Farahani explored the surface-state charge density and surface band bending in Sb-doped PAMBE SnO<sub>2</sub> (101) films as a function of carrier concentration showing that both decreased as  $E_{\rm F}$ increases towards the CNL [62]. However, the maximum Sb-doping level (carrier concentration) of their films was  $3.5 \times 10^{19}$  atoms/cm<sup>3</sup> ( $2.6 \times 10^{19}$  cm<sup>-3</sup>) and consequently they still exhibited significant downward surface band bending consistent with  $E_{\rm F} < E_{\rm CNL}$ .

Using a free-electron-like parabolic dispersion for the conduction band minimum of  $SnO_2$ , the dependence of BM shift on carrier concentration can be expressed as [19,63]

$$E_{\rm opt} = E_{\rm g} + \frac{\hbar^2 (3\pi^2)^{\frac{2}{3}}}{2m_{\rm d}^*} n^{\frac{2}{3}}.$$
 (3)

Equations (1) and (3) were used to fit the observed variations of the plasma frequency and the optical band gap of the Sb:SnO<sub>2</sub> films with *n*, respectively, and thereby determine values for the conductivity effective mass  $m_c^*$  and the density of states reduced effective mass  $m_d^*$ . Figure 8 presents the results of these fits, from which values of  $m_c^*$  (0.31 ± 0.10)  $m_e$ and  $m_d^*$  (0.46 ± 0.12)  $m_e$  were obtained.

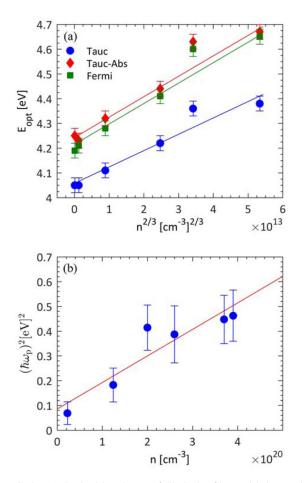


FIG. 8. (a) Optical band gap of  $Sb:SnO_2$  films with increasing carrier concentration obtained using Tauc plots, combined Taucabsorption coefficient plots, and Fermi-Dirac fits of the absorption edge, and the corresponding fits to Eq. (3). (b) Plasma frequency versus carrier concentration and the corresponding fit to Eq. (1).

The value of  $m_c^*$  obtained from the variation in plasma frequency with *n* is close to that reported in previous computational [7,25,64] (0.26–0.31)  $m_e$  and experimental [7,16,65] (0.1–0.39)  $m_e$  studies, whereas the higher value of  $m_d^*$  is in agreement with previous values reported for chemical vapor deposition (CVD) [61], spray pyrolysis [16], and radiofrequency (RF) reactive sputtered [66] SnO<sub>2</sub> films (of 0.59, 0.73, and 0.46)  $m_e$ , respectively. The physical origin of this higher value of  $m_d^*$  may be due to many body electron-electron interactions that become more significant as *n* increases and that have been shown to influence the dispersion of the conduction and valence bands [60,61].

### **IV. SUMMARY AND CONCLUSIONS**

The PAMBE growth of epitaxial (101)  $SnO_2$  films on *r*-plane sapphire was optimized to produce insulating material

 $(\rho > 1 \,\mathrm{k}\Omega \,\mathrm{cm}, n < 10^{14} \,\mathrm{cm}^{-3})$  with an intrinsic optical band gap of  $(4.03 \pm 0.03)$  eV at 300 K, that was characterized by highly crystalline, atomically abrupt surfaces with the majority of electrically active intrinsic defects contained in the first five atomic layers adjacent to the substrate. This intrinsic-quality material was then used to explore the conductivity and transparency limits of Sb doped SnO<sub>2</sub>. The electrical conductivity could be controlled over at least seven orders of magnitude by Sb-doping, covering the insulating, semiconducting, and semimetallic regimes, with a maximum conductivity limit observed at  $\rho \approx 6 \times 10^{-4} \,\Omega\,{\rm cm}$  and  $n \approx$  $4 \times 10^{20} \,\mathrm{cm}^{-3}$ , corresponding to a Sb concentration of  $3 \times$  $10^{20}$  atoms/cm<sup>3</sup>. Any further increase in Sb flux past this limit resulted in a decrease in conductivity, most likely due to charge compensation resulting from the preferential formation of Sb<sup>3+</sup> acceptors. No significant deterioration of the crystalline quality of the Sb:SnO<sub>2</sub> films with increasing Sb incorporation was observed in either RHEED or XRD analysis, indicating that the conductivity limit is likely to be determined by changes in the electronic nature of incorporated Sb species. The observed conductivity limit therefore coincides with the Fermi level position at which the donor-

of SnO<sub>2</sub>. The limits for the coexistence of high transparency and electrical conductivity were found to be determined by a BM shift of up to 0.49 eV in the optical band gap in the UV region (from 310 to 280 nm) and by a much larger blue shift (from beyond 14 to less than 2  $\mu$ m) in the free-carrier adsorption edge in the IR region, due to an increased plasma frequency. Both these effects scaled with the carrier concentration of the material, reaching a maximum at the conductivity limit of  $n \approx 4 \times 10^{20} \,\mathrm{cm}^{-3}$ . This correlation allowed an estimated experimental value of  $E_{\rm C} + (0.49 \pm 0.08) \, {\rm eV}$  to be proposed for the charge neutrality level of SnO<sub>2</sub>, which is very close to the predicted theoretical value from first principles calculations. Remarkably, the transparency in the visible region was almost unchanged, with more than 90% transmission in the 300-1500 nm range for 150-nm-thick Sb:SnO<sub>2</sub> films at the conductivity limit, suggesting considerable promise for the use of Sb:SnO<sub>2</sub> materials in transparent electronics.

like  $(Sb^{5+})$  and acceptor-like  $(Sb^{3+})$  states of antimony have the same formation energy, i.e., the charge neutrality level

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