Double pair breaking peak in Raman scattering spectra of the triple-layer cuprate $Bi₂Sr₂Ca₂Cu₃O_{10+z}$

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We report the Raman scattering measurements on the triple-layer $Bi_2Sr_2Ca_2Cu_3O_{10+z}$ (Bi2223) crystals of four different doping levels from slightly overdoped to strongly underdoped regimes. We observed a double pair breaking peak in the antinodal B_{1g} configuration that we attribute to the two antinodal gaps opening on the outer and inner CuO₂ plane (OP and IP) band, respectively. The doping dependence of the pair breaking peak energy was investigated. Considering the difference in doping level between the IP and OP, all the B_{1g} pair breaking peak energies for OP and IP were found to align on a single line as a function of doping, which is consistent with the previous results on the double and monolayer cuprates. Within our experimental accuracy the IP and OP peaks start to appear almost at the same temperature. These findings suggest some sort of interaction between the layers. The observed gap energy is very large, not scaling with T_c .

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I. INTRODUCTION

One of the long-standing issues in the research of cuprates superconductors is the doping dependence of the superconducting gap. While in the overdoped regime the gap size is proportional to the critical temperature T_c , in the underdoped regime the antinodal and nodal gaps show different doping dependence, indicating that the gap function deviates from a simple *d*-wave type [\[1–3\]](#page-4-0). With further reduction of the doping level the antinodal gap keeps on increasing although *T*^c decreases [\[4\]](#page-4-0). This unusual behavior is connected to the pseudogap coexisting with superconductivity at low temperature, for which many theoretical models have been proposed [\[5\]](#page-4-0).

Another interesting topic of the field is the study of multilayer component, firstly and mainly because the T_c of the cuprates strongly depends on the number of Cu-O planes per unit cell *n*. T_c increases when *n* increases from $n = 1$ to $n = 3$, where it reaches its maximum, and then decreases for $n \geq 4$ [\[6\]](#page-4-0). To date the cause of this T_c enhancement is not clear, with several possible factors being proposed, such as the tunneling of Cooper pairs between different layers [\[7\]](#page-4-0), the increased next-nearest-neighbor hopping parameter *t*['] [\[8\]](#page-5-0), and the disorder protection of the inner $Cu - O_2$ plane (IP) by the outer Cu – O₂ planes (OP) [\[9\]](#page-5-0). Additionally for $n \ge 3$ an interesting situation arises, namely that Cu-O planes with different doping levels coexist in the same sample, where the OP is more doped than the IP due to its proximity to the charge reservoir layer [\[10\]](#page-5-0). How these layers interact with each other, and how this affects T_c is an open problem.

In the present work $Bi_2Sr_2Ca_2Cu_3O_{10+z}$ (Bi2223), the triple-layer ($n = 3$) member of the BSCCO family ($Bi₂Sr₂$) $Ca_{n-1}Cu_nO_{2n+4}$, is examined. Bi2223 features the highest

 $T_c(T_{c,max} = 110 \text{ K})$ in the BSCCO family. The OPs and IPs are chemically inequivalent in Bi2223 because the two OPs are in the pyramidal configuration with the apical oxygen and the IP is in the planar configuration with no apical oxygen. For Bi2223 we can study the electronic state at two doping levels simultaneously using one sample. Nuclear magnetic resonance (NMR) uncovered a large doping imbalance between the IP and OP of Bi2223 $[p(OP) \approx 0.203]$ and $p(\text{IP}) \approx 0.127$) [\[11\]](#page-5-0). The angle-resolved photoemission spectroscopy (ARPES) also revealed band splitting where one band was assigned to the IP and the other to the OP [\[12\]](#page-5-0). Furthermore these two bands originating from the IP and OP were found to have a different value of the superconducting gap. The multilayer effects enhancing T_c is another interest to study this material.

Electronic Raman scattering (ERS) is a powerful technique which is bulk sensitive, momentum resolved, and sensible to occupied and unoccupied states alike [\[13\]](#page-5-0). Using this technique, we investigated Bi2223 samples with four different doping levels, ranging from slightly overdoped to strongly underdoped. A double pair breaking peak, signature of the double superconducting gap was observed, and its doping and temperature dependence was investigated.

II. EXPERIMENT

Bi2223 single crystals were grown by a traveling solvent floating zone method at Hirosaki [\[14,15\]](#page-5-0), and annealed in oxygen atmosphere to control the doping levels [\[16\]](#page-5-0). The Raman spectra were corrected to account for the Bose-Einstein factor and are therefore proportional to the imaginary part of the Raman response function $\chi''(\omega, T)$. B_{2g} and B_{1g} configurations probe the nodal and antinodal region, respectively, where the incident and scattered light perpendicular to each other are

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FIG. 1. Normalized magnetic susceptibility of the four samples. The T_c of all the samples were defined by the onset temperature of the Meissner signal as 109, 109, 105, and 88 K.

along and at 45° with the Cu–O bonds, respectively $[13]$ [see the inset in Figs. $2(h)$ and $2(g)$, respectively].

Figure 1 shows the magnetic susceptibility of the samples investigated. The T_c was determined from the onset temperature of the Meissner signal as 109 K for the slightly overdoped and optimally doped samples, 105 K for the slightly underdoped sample, and 88 K for the strongly underdoped sample. These will be referred to as OvD109, OpD109, UnD105, and UnD88, respectively, from now on. The systematic change of T_c indicates that our tuning of the oxygen content was successful. Although the T_c values are nearly the same in the overdoped and optimally doped samples, the lattice parameters are different in these two samples as described later. The difference of their ERS spectra also supports the difference in doping level of these samples.

III. RESULTS

The ERS spectra for the optimally doped sample are shown in Figs. $2(c)$ and $2(d)$. For the antinodal B_{1g} configuration in Fig. $2(c)$ two signatures were observed when the temperature decreases from room temperature to 10 K. These are the suppression of spectral weight at low frequency below [≈]600 cm−¹ and the two peaks appearing at higher frequency (\approx 560 cm⁻¹ and \approx 800 cm⁻¹). As to the former, going from room temperature (RT) to 115 K, we have the loss of spectral weight between 200 and 600 cm−¹ that is to be attributed to the pseudogap opening [\[17–20\]](#page-5-0). Experimentally the pseudogap opening gives no peak in the Raman spectra, but only this kind of weak suppression of spectral weight is observed below T^* . At $T < T_c (= 109 \text{ K})$, a more dramatic suppression is observed below 500 cm^{-1} , which is due to the superconducting gap opening.

The two peaks are associated with the Cooper pair breaking into two Bogoliubov quasiparticles. The unexpected observation is that two pair breaking peaks are visible, and we attribute this to the double superconducting (SC) gap of Bi2223. Following the ARPES [\[12\]](#page-5-0) and NMR [\[11\]](#page-5-0) studies, the peak at lower energy is assigned to the OP and the one at higher energy is assigned to the IP. Here we report a double peak structure in Raman spectra which is in clear contrast with

the single peak shown by the double-layered $Bi₂Sr₂CaCu₂O₈$ (Bi2212) [\[20–24\]](#page-5-0), and the other double or single-layered compounds $[25-27]$. Note that in some recent data on the triple-layer $HgBa₂Sr₂Cu₃O_z$ (Hg1223) a double pair breaking peak could be visible, although it was not identified by the authors [\[28\]](#page-5-0).

Here we note that an oxygen phonon is present at \approx 590 cm⁻¹, which may mislead us to think that the OP pair breaking peak does not disappear above T_c , even though this is not the case. We have carefully measured the temperature dependence of the spectra to check whether the two peaks start to develop at different temperatures or not [see Fig. [2\(c\)\]](#page-2-0). However, within our measurement resolution, no clear difference was observed in the onset temperature for the peak development. This indicates that the two superconducting gaps open simultaneously, although the T_c values are different in the IP and the OP. The energy values found here for the B_{1g} peak positions are in good agreement with the ARPES data from Ref. [\[12\]](#page-5-0).

In the B_{2g} spectrum at 10 K in Fig. [2\(d\)](#page-2-0) a double pair breaking peak is not visible. Instead a single, very broad peak appears. It is expected that due to the smaller values of the SC gaps in the nodal region and the originally broad feature for B_{2g} , the two peaks, even if they exist, overlap with each other, forming a single broad peak.

When the doping level slightly increases, the double B_{1g} peaks are also clearly observed but at slightly lower energies [see Fig. $2(a)$]. By contrast, the B_{2g} peak appears at almost the same energy or a slightly lower energy as shown in Fig. [2\(b\).](#page-2-0) A small but evident difference between the spectra of OpD109 and OvD109 proves that the doping levels of these two samples are different although the T_c values are almost the same.

Next, in Figs. $2(e)$ and $2(f)$, the spectra for the slightly underdoped sample (UnD105) are shown. In the lowtemperature B_{1g} spectrum in Fig. [2\(e\),](#page-2-0) the double peak feature is still visible, even though not as clearly as in the optimally and overdoped sample. Again the pseudogap opening is visible as a suppression of spectral weight between 200 and 500 cm⁻¹, going from RT to 115 K. In the B_{2g} configuration in Fig. [2\(f\),](#page-2-0) a strong but broad single peak is visible at 10 K.

Figures $2(g)$ and $2(h)$ show the spectra for the strongly underdoped sample (UnD88). Here in the B_{1g} configuration in Fig. $2(g)$ no pair breaking peak seems visible. This suppression of the B_{1g} Raman peak in the underdoped region is consistent with the previous reports for Bi2212 [\[21,22,24,25\]](#page-5-0). It can be explained by the picture of the confinement of Cooper pairs in the antinodal region with underdoping [\[29\]](#page-5-0) and is consistent with the tunneling [\[30,31\]](#page-5-0) and the ARPES data [\[32–34\]](#page-5-0). Here the pseudogap opening is clearly visible when the temperature decreases. Contrary to B_{1g} , the pair breaking peak in nodal B_{2g} configuration is clear and intense, as it can be seen in Fig. [2\(h\).](#page-2-0)

To better view the redistribution of spectral weight due to superconductivity, we subtract the spectra just above T_c from the 10 K spectra. This is demonstrated in Figs. $3(a)$ and $3(b)$ for the B_{1g} and B_{2g} configuration, respectively. In Fig. [3\(a\)](#page-3-0) for the B_{1g} spectra the double peak structure can be seen for most samples. For the slightly underdoped sample the double peak structure, which was not so clear from the raw spectra in Fig. [2\(e\),](#page-2-0) becomes evident. For the strongly underdoped

FIG. 2. B_{1g} and B_{2g} Raman spectra of Bi2223 for (a), (b) OvD109; (c), (d) OpD109; (e), (f) UnD105; and (g), (h) UnD88 samples. The OP and IP peak positions are indicated by blue and red dashed lines, respectively, in panels (a), (c), and (e). The single peak observed in the B_{2g} configuration is indicated by a green dashed line in panels (b), (d), (f), and (h). The precise peak positions have been extracted by the subtracted intensity plot in Fig. [3.](#page-3-0)

sample although a peak was too weak to be seen in the raw data, it becomes visible in Fig. $3(a)$. We attribute this to the pair breaking peak of the OP. Considering that the IP should be more underdoped than the OP and therefore suppressed more, it is reasonable that the IP pair breaking peak does not appear. From this figure we can extract the precise peak position indicated by the dashed lines. For the B_{1g} configuration the maximum of the subtracted spectra was taken as the peak position, whereas for B_{2g} configuration this approach would lead to large uncertainty due to the broad peak. Therefore for B_{2g} configuration we defined the peak position as the middle point between the two frequencies where the intensity is half the maximum value. While the B_{1g} peak shifts to higher energy and loses intensity with underdoping, both for IP and OP, the B_{2g} peak shifts to lower energy when going from the optimal to the underdoped samples. This opposite doping dependence of the peak position in the underdoped regime is consistent with the previous reports for the double and single-layer cuprates and is commonly referred to as two energy scale [\[21,22,25,26\]](#page-5-0).

In order to visualize the doping dependence of the two energy gaps, we need to estimate the doping level of the IP and OP for all the samples. Although the average doping

value *p* of the sample can be obtained from the T_c value, assuming the parabolic T_c dependence of p [\[35\]](#page-5-0), this is a crude approximation, especially for a triple-layer compound. To account for the different doping levels of the IP and OP, an alternative approach is needed. For the optimally doped sample, the IP and OP doping levels were estimated from the NMR measurement as $p(OP) = 0.203$ and $p(IP) = 0.127$, respectively [\[11\]](#page-5-0). For the two underdoped samples, however, such data are currently not available. Therefore, as a first approximation, we assume that the amount of imbalance of the doping level of the OP and IP does not change with doping. Then, the doping levels for the IP and OP can be determined from the base values for OpD109 plus the shift of the average doping level Δp from the optimum value $(p = 0.16)$, where Δp can be estimated from the T_c value, assuming the parabolic T_c -*p* relation $T_c/T_{c,\text{max}} = 1-82.6 \Delta p^2$. Namely, $p_{\text{UnD}}(\text{OP or IP}) = \Delta p_{\text{Average, UnD}} + p_{\text{OpD}}(\text{OP or IP}).$

For the slightly overdoped sample, since the T_c is the same as the optimum value, we cannot use this method to estimate the doping level. As an alternative way, we used the *c*-axis lattice parameter determined by x-ray diffraction measurement. Assuming that the *c*-axis lattice parameter is linearly proportional to the doping level (oxygen content),

FIG. 3. Low-temperature Raman spectra of all samples after the subtraction of the spectra just above T_c . (a) Antinodal B_{1g} high-*T* subtracted spectra. The double peak structure becomes clear for the OvD109, OpD109, and UnD105 samples. The peak of the OP becomes visible for the UnD88 sample. (b) Nodal B_{2g} high-*T* subtracted spectra. The peak positions are extracted from this figure and indicated by the dashed lines.

we extrapolate the c -axis- $\Delta p_{\text{AVERAGE}}$ relation, obtained from the other three samples, to the overdoped side. From the *c*-axis value of the OvD109 sample, we roughly estimated $\Delta p_{\text{AVERAGE}}$ (\approx 0.0097), and calculated each layer doping of this sample as described above. The estimated average and layer doping for the IP and OP for all the samples are summarized in Table I.

We use these p values to plot the B_{1g} pair breaking peak energy as a function of the Cu-O layer doping in Fig. 4. Both IP and OP *B*1g peak energies increase with decreasing *p*. The striking result is that, when the difference in doping between the two layers is taken into account, the B_{1g} peak energies of

TABLE I. Summary of the samples name, T_c , average and layer doping for the OP and IP.

Sample name	T_c (K)	P AVERAGE	p(OP)	$p(\text{IP})$
OvD109	109	0.170	0.213	0.137
OpD109	109	0.160	0.203	0.127
UnD105	105	0.139	0.182	0.106
UnD88	88	0.112	0.155	0.079

FIG. 4. Doping dependence of the pair breaking peak energy. The antinodal B_{1g} energy is plotted using the estimated OP and IP doping. The B_{2g} peak energy is plotted as a function of the estimated average doping. The dashed line and curve are the doping dependence curves taken from Fig. 2 in Ref. [\[25\]](#page-5-0) where the peak energy of single and double-layer cuprates collapse when divided by $T_{c, max}$.

the IP and OP align on a single line, giving a unifying picture of the behavior of both layers.

The B_{2g} peak energy seems to be following the superconducting dome, but it is not clear whether this is a real behavior or not. Firstly, since the double peak structure is not resolved, we cannot separate the IP and OP peak energies. It is possible that two different doping dependences for OP and IP are overlapped, giving an artifact doping dependence. Additionally the originally broad B_{2g} peak gives strong uncertainty on the peak position determination, and this can be seen in the large error bars in Fig. 4. Finally it must be considered that we did not examine a large doping window with our four samples, to reveal a clear dome shape as in the case of other single and double-layer cuprates. For all the above reasons we believe that we cannot draw strong conclusions on the doping dependence of the B_{2g} peak energy. One aspect of the B_{2g} spectra that seems to show a clear doping dependence is how far on the high-energy side does the peak tail extend. This seems to be maximum in the optimally doped sample, while the peak tail moves at lower frequency with decreasing or increasing doping. This is especially evident with decreasing doping, suggesting a signature of the Fermi arc shrinking.

IV. DISCUSSION

The doping dependence found here is qualitatively consistent with the reports on the single and double-layer cuprates $[21,22,25,26]$. Namely, the two energy scale behavior has been confirmed also in the triple-layer compound. The unusual increase of B_{1g} peak energy with underdoping does not necessarily imply the increase of *d*-wave gap but possibly indicates the deviation from *d* wave, due to the strong effect of the pseudogap in the antinodal region of the *k* space, as indicated by ARPES [\[36,37\]](#page-5-0). The latter idea comes from the assumption of some interaction between the pseudogap and the superconducting gap. This interaction enhances the pair breaking energy in the antinodal region which does not contribute to the superconducting condensate, whereas it suppresses T_c . These opposite effects of the pseudogap on the gap energy and on T_c seem to hint at the superconductivity mechanism in the high- T_c cuprates.

Here we also introduce another scale in the right axis of Fig. [4,](#page-3-0) the peak energy (PE) divided by $PE/k_B T_{c,max}$, which should be 4.2 at the optimal doping in a *d*-wave BCS superconductor in the weak coupling limit, if the PE corresponds to a double of the gap energy Δ . In Ref. [\[25\]](#page-5-0), it was demonstrated that this ratio of various single and doublelayer compounds collapses on a universal doping dependence (see Fig. 2 in Ref. [\[25\]](#page-5-0)) that is plotted by dashed lines in Fig. [4.](#page-3-0) It is clear that for both B_{1g} and B_{2g} the PE/ $k_B T_{c,max}$ ratios are larger in Bi2223 than the case for the single or double-layered cuprates. This suggests a larger energy scale of the pair breaking peak, compared with T_c in Bi2223.

The characteristic feature of Bi2223 is the coexistence of different doping layers in a unit cell, where the lower doping CuO layer (IP) is sandwiched by the higher doping CuO layers (OP). Experimentally we observe only a single superconductivity transition, but not a double step transition. It means that the IP and OP are not completely independent but interact with each other. The interaction between the layers is also supported by the result in Fig. [4,](#page-3-0) where, despite the chemical inequivalence between the two layers, the B_{1g} peak energies of the two layers align on a single line, indicating that the gap value is only controlled by doping. The interlayer coupling or a proximity effect can enhance the lower energy gap [\[38\]](#page-5-0), in turn reducing the higher energy gap. This averaging of the two gaps gives the peak position alignment observed here.

The origin of the large pair breaking energy of Bi2223 cannot be concluded in the present study. However, the interlayer coupling is one of the candidates to explain it in terms of the multilayer effect. As previously described, multiple effects have been proposed to explain the high T_c of the triple-layer component; one or many of these can explain the gap enhancement in the two layers. These include: protection from the blocking layer disorders [\[9\]](#page-5-0), appropriately high nextnearest-neighbor hopping parameter t' [\[8\]](#page-5-0), and tunneling of Cooper pairs between the layers [7]. Another possible gap enhancement mechanism is some degree of positive interaction between superconductivity and the pseudogap. With decreasing doping the superconducting gap is enhanced by the interaction with the increasing pseudogap. Therefore, the lower doping IP has a larger gap value due to its larger pseudogap. In this case the OP gap enhancement is expected from the proximity effects [\[38\]](#page-5-0).

In addition to these positive effects, we need to consider a negative effect of the pseudogap on superconductivity to explain the large ratio of $PE/k_B T_{c,max}$. Since the T_c is suppressed by the pseudogap in general, it is likely that the bulk T_c of Bi2223 is lowered by the pseudogapped IP. The enhanced gap energy together with the suppressed T_c must result in a large ratio of $PE/k_B T_{c,max}$ in Bi2223, which suggests the potential of this triple-layer compound to exhibit superconductivity at a higher T_c .

In conclusion we performed Raman scattering measurements on Bi2223 crystals with four different doping levels, and successfully resolved a double pair breaking peak structure in the B_{1g} spectra which was attributed to the superconducting gaps for the IP and OP. Both of the IP and OP peaks show clear doping dependences. Taking into account the difference in doping level of the IP and OP, all the B_{1g} peak energies can be plotted on a single line, while the B_{2g} spectra show only a broad single pair breaking peak. The present results of doping-dependent pair breaking peaks on the triple layer cuprates are consistent with the B_{1g}/B_{2g} gap behavior reported for various double and single-layer cuprates. The IP and OP peaks were found to appear at the same temperature within our experimental resolution, and this, together with the alignment of the IP and OP layer B_{1g} peak energy on a single line, hints at an interaction between the two layers. A large energy scale of the pair breaking peaks was found in both nodal (B_{2g}) and antinodal (B_{1g}) gaps. Even though we cannot conclude its origin from the present result, it is likely that the multilayer structure with the underdoped IP causes this large gap energy scale, PE/k_BT_c , through enhancement of the gap and/or suppression of T_c due to the effect of the pseudogap on IP.

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