Independence of spin-orbit torques from the exchange bias direction in Ni81Fe19*/***IrMn bilayers**

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We investigated a possible correlation between spin Hall angles and exchange bias in Ni₈₁Fe₁₉/IrMn samples by performing spin-torque ferromagnetic resonance measurements. This correlation is probed by patterning of Ni₈₁Fe₁₉/IrMn bilayers in different relative orientations with respect to the exchange bias direction. The measured voltage spectra allow a quantitative determination of spin Hall angles, which are independent of the exchange bias orientation around $2.8 \pm 0.3\%$.

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Recently, antiferromagnetic materials have received increased interest in spintronics devices beyond their traditional use in exchange bias based applications $[1-3]$. Antiferromagnets are magnetically ordered with zero net magnetization, which makes them insensitive to external magnetic fields. For the same reason, they do not produce any magnetic stray fields, which avoids cross-coupling between different devices in close proximity. Furthermore, they have very high characteristic frequencies in the terahertz regime; hence they can operate at high speeds. The discovery of several magnetotransport effects in antiferromagnets such as spin-orbit torques [\[4\]](#page-3-0), anisotropic magnetoresistance [\[5,6\]](#page-3-0), spin Seebeck effects [\[7,8\]](#page-3-0), inverse spin Hall effects [\[9](#page-3-0)[,10\]](#page-4-0), galvanic effects [\[4\]](#page-3-0), and efficient spin current transmission $[11-13]$ shows the feasibility of using them as active components for spintronic devices. In particular, the discovery of electrical switching and readout of an antiferromagnet by spin-orbit torque shows that antiferromagnets can be controlled electrically in similar ways as their ferromagnetic counterparts [\[14\]](#page-4-0).

Of particular interest is the possibility to drive the magnetization dynamics of a ferromagnet using the spin Hall effect [\[15–18\]](#page-4-0), which generates a spin accumulation on the lateral surface of a charge carrying material. The efficiency of the spin Hall effect is described by the spin Hall angle [\[19\]](#page-4-0), $\Theta_{\text{SH}} = \frac{2e}{\hbar} (J_s/J_c)$. Using the spin-torque ferromagnetic resonance technique [\[20\]](#page-4-0), spin Hall effects in metallic CuAu-I-type antiferromagnets (IrMn, FeMn, PtMn, and PdMn) have been investigated and spin Hall angles have been reported between 0.02 and 0.08 [\[9,](#page-3-0)[10\]](#page-4-0). Furthermore, it was shown that spin Hall effects in antiferromagnets can be very anisotropic and depend on crystalline orientation [\[21\]](#page-4-0). It has been also demonstrated that spin-orbit torques in PtMn are sufficiently strong for switching the magnetization of an adjacent Co/Pt layer [\[22\]](#page-4-0). Theoretically, it is expected that the spin current injection from an antiferromagnet to a normal metal varies as

the antiferromagnets' spin texture changes [\[23\]](#page-4-0). These studies indicate that the interface plays an important role for the spin current injection and transmission.

Another interfacial effect is exchange bias, and its origin is understood to be due to exchange coupling between a ferromagnet and an antiferromagnet at the interface [\[24\]](#page-4-0). When an antiferromagnet and a ferromagnet are in direct contact with each other and field cooled in a particular magnetic field direction, some fraction of the antiferromagnetically ordered spins at the interface aligns in a way that minimizes the interaction with the magnetization in the ferromagnet, the direction of which is determined by the applied field. Subsequently, when the magnetic field and hence the magnetization in the ferromagnet are changed, these antiferromagnetic spins are locked in their position, which leads to a shift in the hysteresis loop known as exchange bias shift [\[25\]](#page-4-0). This interfacial interaction has been extensively used in many spintronics devices such as spin valves and magnetic tunnel junctions, where it provides a reference magnetization orientation [\[26,27\]](#page-4-0). By using exchange bias, the direction of antiferromagnetic order at the interface can be manipulated at a microscopic level. Thus, the natural question to ask is whether there is a direct correlation between exchange bias and spin-orbit torques as the ferromagnetic/antiferromagnetic interface is crucial for both phenomena.

Previous studies intentionally avoided the exchange bias by adding a Cu layer between the ferromagnetic and antiferromagnetic layer $[9,10]$ $[9,10]$. While this Cu layer eliminates direct magnetic interfacial coupling, it is highly transparent for spin currents. Here, we removed the Cu layer sandwiched between the ferromagnet and the antiferromagnet and performed spin-torque ferromagnetic resonance measurements on Ni81Fe19*/*IrMn bilayers with different relative orientations of applied fields and exchange bias. As it will be discussed below, these measurements revealed no significant dependence of spin-orbit torques on the exchange bias field directions.

Multiple patterned samples with lateral dimension of 20 \times 90 μ m² of the same Ni₈₁Fe₁₉/IrMn bilayer were fabricated on

FIG. 1. (a) Schematic representation of the spin-torque ferromagnetic resonance experimental setup. (b) Relative orientations between exchange bias and external field during spin-torque ferromagnetic resonance measurement. (c) Illustrative picture of a Ni₈₁Fe₁₉/IrMn showing the spin-transfer torques τ_F and τ_D , magnetization *M*, and external field H_{ext} .

SiO2 substrate using magnetron sputtering, photolithography, and ion milling $[28]$. Ni₈₁Fe₁₉ and IrMn were kept at 6 and 8 nm in thickness, respectively. Subsequently, contact pads [Ti (3 nm)/Au (150 nm)] were deposited on the samples for electrical measurements [see Fig. $1(a)$]. In order to establish exchange bias, the patterned antiferromagnet/ferromagnet samples were annealed at 250 °C in vacuum and subsequently cooled down to room temperature in the presence of 600-Oe magnetic field. Note that all the devices with different relative orientations were fabricated on the same chip and annealed simultaneously.

Spin-torque ferromagnetic resonance measurements were performed for all the samples with various relative orientations between exchange bias and external field [Fig. 1(b)]. A schematic of the measurement setup is illustrated in Fig. 1(a). An oscillating charge current was driven through rf probes in contact with the contact pads. This oscillating charge current generates a transverse spin current, which exerts a torque on the magnetization of $Ni_{81}Fe_{19}$. The rf current flowing through the $Ni₈₁Fe₁₉$ layer mixes with the time-dependent resistivity of the $Ni₈₁Fe₁₉$ due to anisotropic magnetoresistance in response to the oscillating magnetization, which results in a rectified dc voltage that was measured as a function of applied magnetic field. During the measurements, a 10-mW fixed microwave current was applied with frequencies varied from 8 to 15 GHz and the external magnetic field was kept constant at 45° with respect to the rf current direction [Fig. 1(c)]. Note that all the measurements have been performed at room temperature, which is below the blocking temperature of Ni81Fe19*/*IrMn [\[29\]](#page-4-0).

Figure $2(a)$ shows typical measured spin-torque ferromagnetic resonance signals for a Ni₈₁Fe₁₉/IrMn sample at frequencies of 8, 10, 12, and 14 GHz and $\theta = 0^\circ$. As the microwave frequency increases, the resonance field shifts towards higher fields, which is in agreement with the Kittel model [\[30\]](#page-4-0), and the magnitude of measured dc voltage (V) decreases. Here, the measured dc voltages are sums of symmetric and antisymmetric Lorentzian components, which can be attributed to dampinglike and fieldlike torques, respectively. Figure $2(b)$ shows a spin-torque ferromagnetic resonance spectrum, which was measured at 8 GHz and decomposed into its symmetric (V_s) and antisymmetric (V_a) Lorentzian voltage contributions. In order to illustrate the angular dependence of exchange bias on spin-orbit torques, we examine the ratio of symmetric to antisymmetric voltage contributions, as well as associated effective spin Hall angles [\[31\]](#page-4-0) for both negative and positive external fields. We extracted the symmetric and antisymmetric voltage contributions by fitting the spin-torque ferromagnetic resonance curves [\[20\]](#page-4-0):

$$
V = \left[V_s \frac{\Delta H^2}{\Delta H^2 + (H_{\text{ext}} - H_{\text{res}})^2} + V_a \frac{\Delta H (H_{\text{ext}} - H_{\text{res}})}{\Delta H^2 + (H_{\text{ext}} - H_{\text{res}})^2} \right],
$$
(1)

where ΔH is the resonance linewidth, H_{ext} is the applied field, and *H*res is the resonance field for ferromagnetic resonance at a given frequency. The effective spin Hall angles can be quantified via the ratio of symmetric and antisymmetric voltage

FIG. 2. (a) Measured spin-torque ferromagnetic resonance signals at 8, 10, 12, and 14 GHz with the angle $\theta = 0$ ° between the applied field and the exchange bias direction. (b) Single spin-torque ferromagnetic resonance spectrum measured at 8 GHz. The red solid line represents the fit to the Lorentzian function. The green dashed and blue dash-dotted lines represent symmetric and antisymmetric voltage components, respectively.

FIG. 3. (a) Spin-torque ferromagnetic resonance spectra obtained at 12 GHz illustrate the resonance field shift due to exchange (for $\theta = 0^{\circ}$). Blue and red curves depict positive and negative field sweeps, respectively. (b) Magnetic hysteresis loop for $N_i{}_{81}Fe_{19}(6)$ thin film (red circles) and $\text{Ni}_{81}\text{Fe}_{19}(6)/\text{IrMn}(8)$ bilayer (black squares). (c) Measured in-plane exchange bias field H_B , which represents the relative orientation of exchange bias anisotropy with respect to the measurement field *H*ext.

contributions [\[20\]](#page-4-0):

$$
\Theta_{\text{SH}}^{\text{eff}} = \frac{V_s}{V_a} \frac{e\mu_0 M_s t_{\text{AF}} t_{\text{FM}}}{\hbar} \left[1 + \frac{4\pi M_s}{H_{\text{ext}}} \right]^{1/2},\tag{2}
$$

where μ_0 is the permeability in vacuum, t_{AF} and t_{FM} are the thicknesses of the ferromagnetic and antiferromagnetic layers, respectively, and M_s is the saturation magnetization of $Ni₈₁Fe₁₉$, which can be extracted by fitting the resonance frequency as a function of H_{res} by the Kittel equation [\[30\]](#page-4-0):

$$
f_{\rm res} = \frac{\gamma}{2\pi} [(H_{\rm res} + H_B)(H_{\rm res} + H_B + 4\pi M_s)]^{1/2}, \quad (3)
$$

where H_B is the effective exchange bias field.

In exchange biased ferromagnetic/antiferromagnetic bilayers, the exchange anisotropy gives rise to a resonance shift and enhanced linewidth broadening compared to unbiased films [\[32\]](#page-4-0). Patterning samples in four different directions with respect to the unidirectional exchange bias anisotropy, i.e., $\theta = 0$, 45, 90, and 135[°], enables us to control the shift in resonance field during measurements $[33,34]$. Figure $3(a)$ shows the measured dc voltage as a function of field at 12 GHz for $\theta = 0$. When the measurement field and exchange bias field are parallel (perpendicular) to each other, we measured the maximum (minimum) resonance field shift of 60 Oe. This exchange bias shift can also be seen in the magnetization versus

field curve for the Ni₈₁Fe₁₉/IrMn bilayer [see Fig. 3(b)]. The summary of electrically measured exchange bias fields for all angles ($\theta = 0$, 45, 90, and 180[°]) is shown in Fig. 3(c).

We also measure effective damping (Δa) due to the exchange bias, which can be extracted from the frequency dependence of the linewidth broadening $[35] (\Delta H)$ $[35] (\Delta H)$ [Fig. 4(a)]. Almost identical Δa values were observed for all directions [see Fig. $4(b)$]. If we consider that at least part of the effective damping is related to spin pumping into the adjacent IrMn, then this suggests that the efficiency of spin current transmission at the interface is approximately identical for all directions, i.e., independent from the exchange bias direction. Furthermore, the additional effective damping for our Ni81Fe19*/*IrMn sample is larger than the measured value in the previous study $[10]$, where exchange coupling at the interface is eliminated by inserting a thin Cu layer. This can be attributed to magnetic losses in the antiferromagnetic spin lattice, which is also directly exchange coupled to the ferromagnetic magnetization in the $Ni₈₁Fe₁₉$ and therefore can provide additional damping.

Figure $5(a)$ shows the ratio of symmetric and antisymmetric voltages for frequencies ranging from 8 to 15 GHz. No angular dependence of V_s/V_a was observed, which is consistent with the effective damping data. These findings suggest that both

FIG. 4. (a) Frequency dependence of the linewidth broadening ΔH , for varying θ (for positive field sweeping). (b) Effective damping $\Delta \alpha$ as a function of *θ* for positive and negative fields.

FIG. 5. (a) Ratio of symmetric voltage to antisymmetric voltage for varying frequencies from 8 to 15 GHz. Open and closed circles represent negative and positive field sweeping, respectively. (b) Effective spin Hall angles Θ_{SH}^{eff} as a function of frequency for different θ .

dampinglike (given by *Vs*) and Oersted-fieldlike torques (given by *Va*) are independent of the local spin structure at the Ni81Fe19*/*IrMn interface. However, we observed that *Vs/Va* values for positive and negative fields differ slightly. A possible explanation for this difference could be a resonant heating of the samples. Together with the asymmetric structure of the sample layout [see Fig. $1(a)$], this may result in a lateral temperature difference. Ultimately, this difference may generate additional Seebeck voltage across the sample, which is due to the fact that the resonant heating should have a symmetric Lorentzian line shape.

Ignoring this offset, the averaged effective spin Hall angles for positive and negative fields for varying microwave excitation frequencies from 8 to 15 GHz are shown in Fig. $5(b)$. The effective spin Hall angles for different relative orientations between exchange anisotropy and external field show very small variation, and we estimate $\Theta_{\text{SH}}^{\text{eff}} = (2.8 \pm 0.3)\%$. We observed slightly smaller spin Hall angles compared to previous measurements [\[10\]](#page-4-0) in the presence of a Cu interlayer between IrMn and $Ni₈₁Fe₁₉$. Furthermore, measurements with thicker IrMn (15 nm) show qualitatively the same behavior, i.e., we observe no dependence of spin Hall angles on relative orientations between exchange bias and current flow, and the effective damping is almost identical for all directions. Our observations are inconsistent with previous spin-orbit ferromagnetic measurement experiments on the NiFe/IrMn system, where a large enhancement of dampinglike torques was measured arising from the antiferromagnetic order at the interface [\[18\]](#page-4-0).

We conclude that there is no dependence of the effective spin Hall angles on the relative orientation of the in-plane exchange bias with respect to current flow and thus the polarization direction of the concomitant spin currents and accumulations. However, there are still strong spin-orbit torques even when the antiferromagnet is directly exchange coupled to the ferromagnet. We also observe a similar trend in ferromagnetic resonance data, where the angular dependence of effective damping is almost identical for all directions, which may suggest that the spin current transmission through the Ni81Fe19*/*IrMn interface is not affected by the local magnetic structure.

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