

Unconventional planar Hall effect in exchange-coupled topological insulator–ferromagnetic insulator heterostructures

David Rakhmievich,^{1,2} Fei Wang,³ Weiwei Zhao,³ Moses H. W. Chan,³ Jagadeesh S. Moodera,^{1,4} Chaoxing Liu,³ and Cui-Zu Chang^{1,3,*}

¹*Francis Bitter Magnet Laboratory, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA*

²*School of Engineering and Applied Sciences, Harvard University, Cambridge, Massachusetts 02139, USA*

³*Department of Physics, The Pennsylvania State University, University Park, Pennsylvania 16802, USA*

⁴*Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA*



(Received 13 September 2017; revised manuscript received 20 August 2018; published 6 September 2018)

The Dirac electrons occupying the surface states (SSs) of topological insulators (TIs) have been predicted to exhibit many exciting magnetotransport phenomena. Here we report the experimental observation of an unconventional planar Hall effect (PHE) and a gate-tunable hysteretic planar magnetoresistance in EuS/TI heterostructures, in which EuS is a ferromagnetic insulator (FMI) with an in-plane magnetization. In such exchange-coupled FMI/TI heterostructures, we find a significant (suppressed) PHE when the in-plane magnetic field is parallel (perpendicular) to the electric current. This behavior differs from previous observations of the PHE in ferromagnets and semiconductors. Furthermore, as the thickness of the 3D TI films is reduced into the 2D limit, in which the Dirac SSs develop a hybridization gap, we find a suppression of the PHE around the charge-neutral point indicating the vital role of Dirac SSs in this phenomenon. To explain our findings, we outline a symmetry argument that excludes linear Hall mechanisms and suggest two possible nonlinear Hall mechanisms that can account for all the essential qualitative features in our observations.

DOI: [10.1103/PhysRevB.98.094404](https://doi.org/10.1103/PhysRevB.98.094404)

I. INTRODUCTION

The Hall effect or the appearance of a voltage transverse to an electric current for electric conductors placed in an external magnetic field is among the most well-known magnetotransport phenomena [1]. The ordinary Hall effect, arising from the Lorentz force experienced by current carriers, requires the magnetic field to be perpendicular to both the electric current direction and the sample plane. However, a transverse voltage can also emerge in certain systems when the magnetic field is in the plane of the sample and electric current, a phenomenon known as the planar Hall effect (PHE). The PHE was experimentally observed in bulk ferromagnets [2], nanocrystalline $\text{Co}_{60}\text{Fe}_{20}\text{B}_{20}$ [3], magnetic semiconductors such as (Ga, Mn)As [4], and nonmagnetic semiconductors like germanium [5] and topological insulator (TI) films [6]. The PHE cannot be induced by the Lorentz force, and various microscopic mechanisms have been proposed for this phenomenon, including anisotropic scattering by impurities [2,6], a nonspherical Fermi surface [5], spin Hall magnetoresistance [7], and chiral anomaly [8–10]. In particular, it has been shown that the PHE is usually related to anisotropic magnetoresistance (AMR) and in the absence of spontaneous resistivity anisotropy in the crystal, both effects could be described by the following phenomenological

equations [11,12]:

$$\rho_{\text{PHR}} = (\rho_{//} - \rho_{\perp}) \sin \Phi \cos \Phi, \quad (1)$$

$$\rho_{\text{AMR}} = \rho_{\perp} \left(1 + \frac{\rho_{//} - \rho_{\perp}}{\rho_{\perp}} \cos^2 \Phi \right), \quad (2)$$

where ρ_{PHR} and ρ_{AMR} are the transverse and longitudinal magnetoresistances, respectively, Φ is the angle between the current I and the in-plane magnetic field B , while $\rho_{//}$ (ρ_{\perp}) is the resistance of the sample when I is parallel (perpendicular) to B . The above angular dependence was shown to be consistent with recent experimental studies on metallic and semiconducting ferromagnets [3,4] as well as on nonmagnetic TIs under high magnetic fields [6]. Specifically, according to Eq. (1) the planar Hall resistance (PHR) is zero when B is parallel ($\Phi = 0^\circ$) or perpendicular ($\Phi = 90^\circ$) to I while it is maximized when $\Phi = 45^\circ$.

In this paper, we present in-plane magnetotransport measurements in $\text{EuS}/(\text{Bi}_{0.22}\text{Sb}_{0.78})_2\text{Te}_3$ heterostructures, as a prototype of ferromagnetic insulator (FMI)/TI heterostructures. Our measurements demonstrate the observation of a PHE and tunable planar magnetoresistance (PMR) in FMI/TI heterostructures. The gate voltage (V_g) dependence of the PHE shows a peak of PHR when the chemical potential is near the Dirac point. Moreover, as the TI film thickness in the heterostructures is reduced from 4 quintuple layers ($QL \sim 1$ nm) to 3 QL, in which the Dirac surface states (SSs) develop a hybridization gap [13–15], the PHE and PMR properties change dramatically indicating the vital role of Dirac SSs in magnetotransport. Interestingly, we observed a significant

*Corresponding author: cxc955@psu.edu

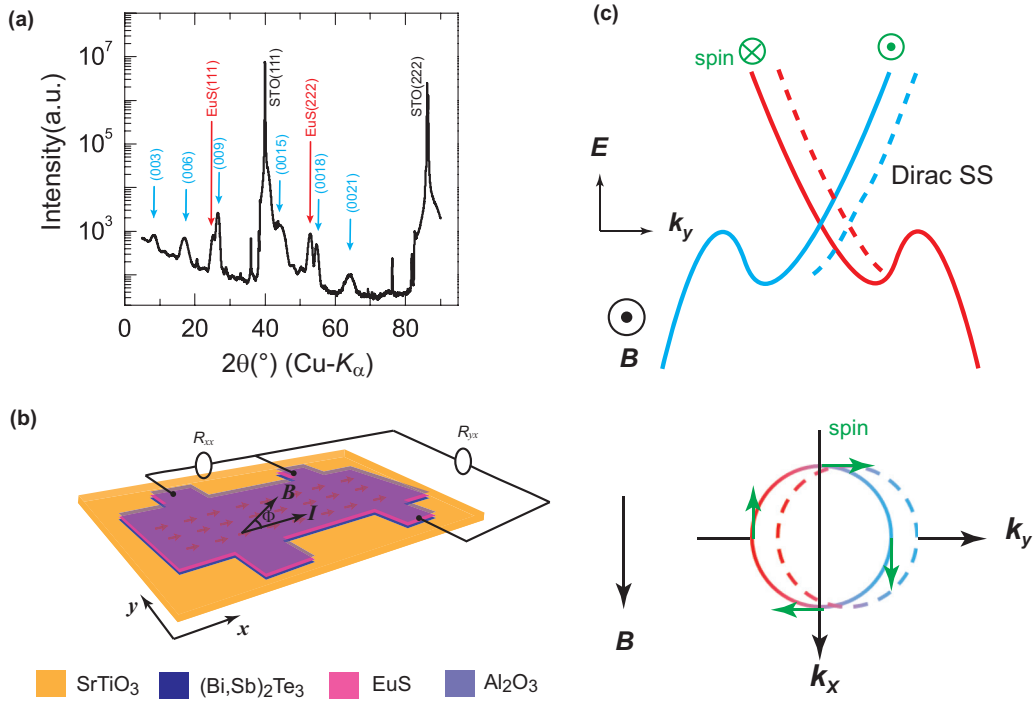


FIG. 1. The EuS/(Bi_{0.22}Sb_{0.78})₂Te₃ heterostructures. (a) X-ray diffraction spectrum of a 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ heterostructure, with the peaks of the epitaxial (Bi_{0.22}Sb_{0.78})₂Te₃ film and EuS film identified by blue and red arrows, respectively. (b) Schematic drawing of the sample structure and the Hall bar configuration. An image of the real Hall bar is shown in Ref. [22]. (c) Schematic diagrams showing the shift of the Dirac SSs in the presence of the in-plane magnetization. The linear surface bands are a bit tilted due to the quadratic term Dk^2 included in the Hamiltonian of the Dirac surface states. The green arrows denote the spin of the Dirac electrons.

PHR for in-plane magnetic field B parallel to the current I while it was suppressed for B perpendicular to I , in contrast to the conventional PHE as described by Eq. (1). Based on these findings and a simple symmetry argument, we exclude linear Hall mechanisms and suggest two possible nonlinear Hall mechanisms, which capture all the essential qualitative features in our observations.

II. SAMPLE GROWTH AND EXPERIMENTAL PROCEDURES

The EuS/(Bi_{0.22}Sb_{0.78})₂Te₃ heterostructures were grown on 0.25-mm-thick heat-treated SrTiO₃ (111) substrates in a custom-built molecular-beam epitaxy (MBE) chamber [16,17]. The Bi:Sb ratio was controlled to locate the chemical potential close to the Dirac point in order to enhance the contribution of the SSs in magnetotransport [16,18–20]. The growth was monitored using *in situ* reflective high-energy electron diffraction. A 5-nm EuS (111) layer was deposited over the TI film at room temperature followed by a 4-nm-thick Al₂O₃ capping layer. A representative x-ray diffraction pattern of the 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ heterostructure is shown in Fig. 1(a). We have previously demonstrated that EuS forms a continuous film when grown on top of Sb₂Te₃ films with no interdiffusion and exhibits a well-defined in-plane magnetization [21]. The EuS/(Bi_{0.22}Sb_{0.78})₂Te₃ heterostructures were patterned into Hall bar geometries with an aspect ratio of ~ 2 (Fig. 1(b) and Supplemental Material Fig. S1(a) [22]). The in-plane magnetotransport measurements were carried out using conventional

direct-current techniques in a homemade glass cryostat with a base temperature of $T = 1$ K. The out-of-plane magnetotransport measurements were done in a commercial Physical Properties Measurement System with a base temperature of $T = 2$ K.

III. RESULTS

A. Magnetotransport measurements of 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ films

A major challenge in transport studies of TIs is to distinguish between the contributions of bulk carriers and SSs. In order to respond to this challenge, we focus on 4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ films. At such a thickness, the bulk carrier contribution is minimized while preserving the gapless Dirac SSs on the surface [13–15]. In addition, the large dielectric constant of SrTiO₃ (111) substrates at low temperatures makes it possible to efficiently tune the chemical potential of the TI films by changing V_g [16,17]. The sheet longitudinal resistance R_{xx} of a 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ heterostructure exhibits a sharp peak at $V_g = -13$ V when the chemical potential is swept across the Dirac point, with a maximum of ~ 19.6 k Ω due to the ambipolar carrier contributions [Fig. 2(a)]. This indicates the conduction of the 4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ film is indeed dominated by the Dirac SSs. The corresponding current-voltage (I_{sd} - V_{sd}) curves exhibit a linear relation throughout the shifting of the chemical potential which indicates the absence of activation energy for transport and is consistent with gapless Dirac SSs on the surface [Fig. 2(b)].

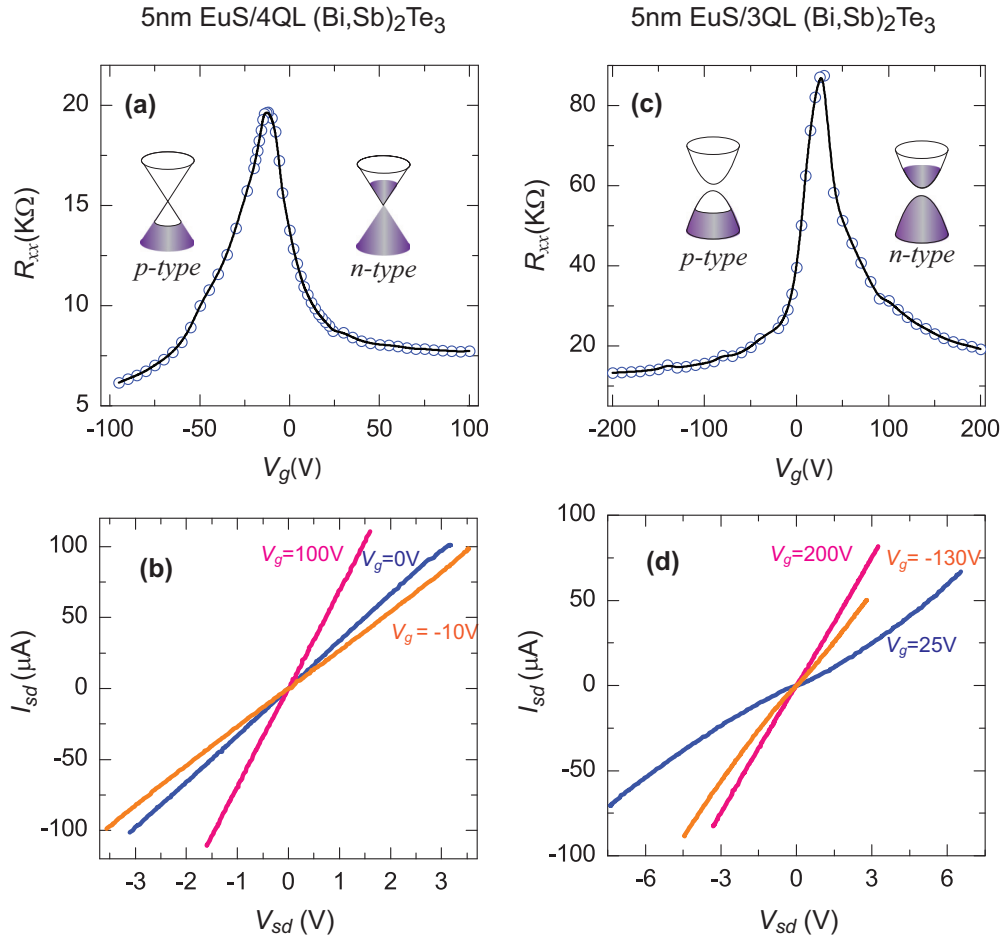


FIG. 2. Gate-dependent measurements on EuS/(Bi_{0.22}Sb_{0.78})₂Te₃ heterostructures measured at $T = 1$ K. The gate (V_g) dependence of the sheet longitudinal sheet resistance (R_{xx}) of 4-QL (with Dirac SSs) and 3-QL (with a hybridization gap) heterostructures is shown in (a) and (c), respectively. The corresponding I_{sd} - V_{sd} curves for several V_g s are shown in (b) and (d).

The in-plane magnetized 3D TI preserves the gapless character of the Dirac SSs while shifting the Dirac cone in momentum space [Fig. 1(c)]. To isolate the spin-related effects of the Dirac SSs, we applied in-plane magnetic fields in the range of ± 650 Oe [x axis in Fig. 1(c)]. Figure 3(a) summarizes the PMR and PHR of a 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ heterostructure with representative curves at several V_g s. The PMR and PHR are defined as $\text{PMR}(\%) = \{R_{xx}(B) - \min[R_{xx}(B)]\} / \min[R_{xx}(B)] \times 100$ and $\text{PHR} = [V_y(B)] / I_x$. The PMR shows a butterfly-shaped hysteresis loop and can be tuned by the V_g to a maximum amplitude of over 0.4%. Interestingly, the maximum of PMR occurs at $V_g = 0$ V [Fig. 3(b)], slightly different from the peak of the R_{xx} at $V_g = -13$ V, which corresponds to the Dirac point [Fig. 2(a)]. Since V_g serves to filter out bulk conduction, this observation suggests that in addition to Dirac SSs, the bulk conduction may also contribute toward the PMR. We note that there is more than an order-of-magnitude enhancement of PMR in the 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ heterostructures with Dirac-SSs-dominated conduction observed here as compared to EuS/20-QL Bi₂Se₃ heterostructures with bulk-carriers-dominated conduction ($\text{PMR} \sim 0.02\%$) [23,26], indicating the vital role of the SS in PMR. While obtaining appreciable hysteretic PMR changes in novel materials is of

importance for future development of spintronic applications, it can arise from a variety of mechanisms such as AMR [27,28], domain-wall scattering [29], and spin Hall magnetoresistance [7,30]. Furthermore, a prior experiment attributed the hysteretic PMR in EuS/TI heterostructures to magnetic domain-wall-trapped 1D conduction channels [23].

As compared with PMR, PHE measurements provide more insight into the underlying transport processes. The upper panel in Fig. 3(a) shows clear hysteresis loops, demonstrating the observation of PHE in an exchange-coupled FMI/TI heterostructure. Interestingly, the PHE amplitude (i.e., PHR) can also be tuned by the V_g , with a maximum at the position of the Dirac point ($V_g = -13$ V) showing a direct correlation with the peak of R_{xx} . We note that while the observed PHR of several Ω is orders of magnitude larger than the PHR in 2D metallic ferromagnets (typically on the order of a few m Ω) [3,4,31,32], the Hall angle in both systems is comparable due to the large R_{xx} in the TI/EuS system. In addition, we point out that the absence of symmetry outside the hysteretic PHR loop is attributed to noise and background reduction, which can play a role when modest resistance changes are recorded over a substantial sweep time.

To explore the physical origin of the large PHR signal in EuS/TI heterostructures, transport measurements were

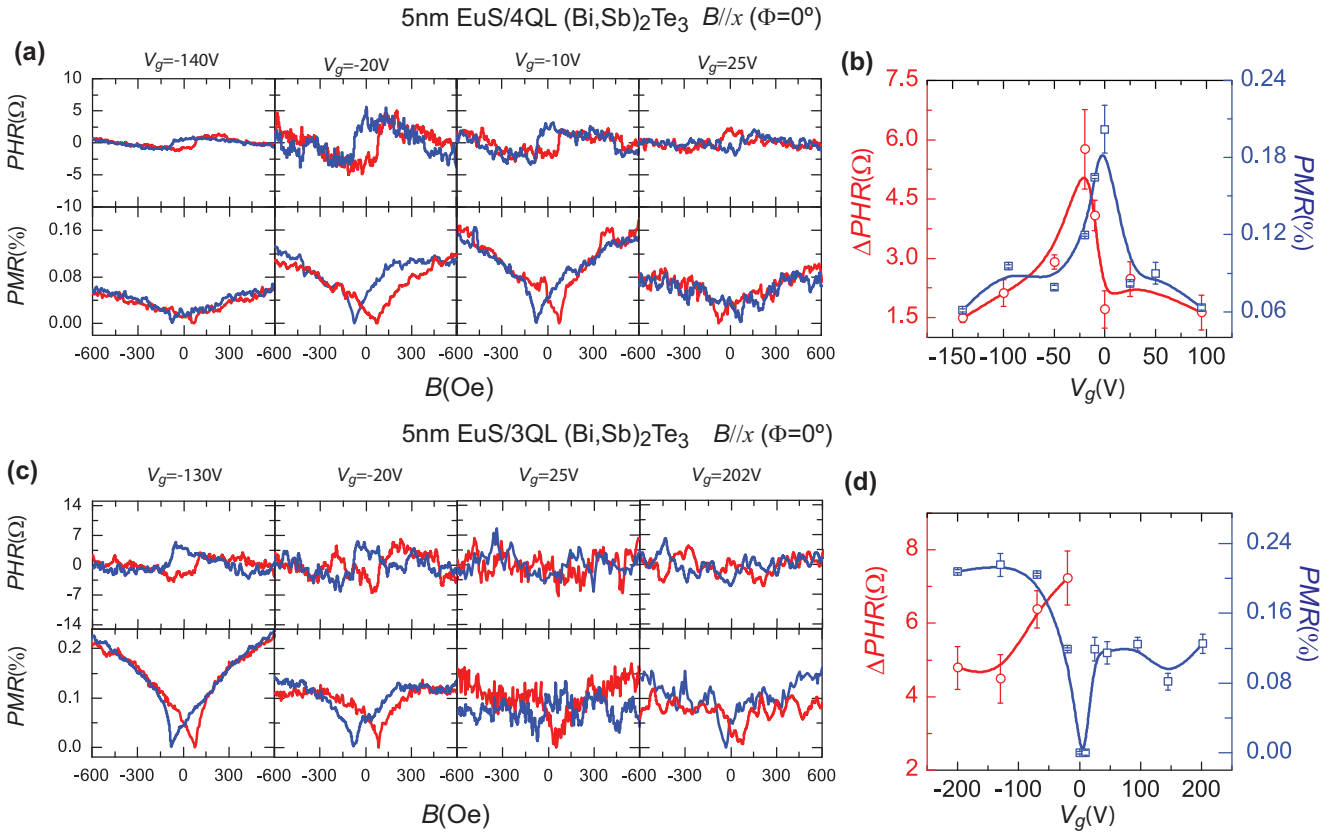


FIG. 3. In-plane magnetotransport in EuS/(Bi_{0.22}Sb_{0.78})₂Te₃ heterostructures. (a), (c) Representative PHE and PMR measurements for several V_g s taken on 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ (with Dirac SSs) (a) and 5-nm EuS/3-QL (Bi_{0.22}Sb_{0.78})₂Te₃ (with a hybridization gap) (c) heterostructures, respectively. (b), (d) Summary of the V_g dependence of PHE and PMR for 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ (b) and 5-nm EuS/3-QL (Bi_{0.22}Sb_{0.78})₂Te₃ (d) heterostructures, respectively. The error bars for the PHE quantify the deviations in the signal around the limits of the transition, while the error bars in PMR quantify the deviations around 600 Oe. The zero PMR value in (d) was assigned due to the inability to observe a clear MR dependence while the error bar quantifies the fluctuations in the signal.

performed on another 5-nm EuS/4-QL (Bi_{0.22}Sb_{0.78})₂Te₃ sample with the measuring current aligned at three different angles Φ with respect to the external in-plane magnetic field B [Figs. 4(a)–4(c)]. The pronounced PHE signal around $\Phi = 0^\circ$ shows a small decrease at $\Phi = 30^\circ$ and is completely suppressed at $\Phi = 90^\circ$ [Fig. 4(d)]. This phenomenon is in stark contrast to the PHE observed in ferromagnets and semiconductors, where the suppression of the signal was observed both around $\Phi = 0^\circ$ and 90° [2–6]. Similar angular dependence was also found in a 5-QL (Bi_{0.22}Sb_{0.78})₂Te₃ film (Supplemental Material [22]), with both 4- and 5-QL (Bi_{0.22}Sb_{0.78})₂Te₃ films being in the 3D TI regime with gapless Dirac SSs [13–15]. In addition, we note that the PMR does not depend strongly on the angle between I and B [the bottom panels of Figs. 4(a) to 4(c)], suggesting that AMR does not play a large role in our system and that the PHE arises from a different mechanism. The latter is also supported by the different V_g s at which maximum PMR ($V_g = 0$ V) and maximum PHR ($V_g = -13$ V) are attained [Fig. 3(b)]. This is in contrast with conventional AMR and PHE, which are both governed by the scaling of Eqs. (1) and (2) with $(\rho_{//} - \rho_{\perp})$. Specifically, the maximum PHR is correlated with the peak in R_{xx} ($V_g = -13$ V) corresponding to the Dirac point and suggesting the unusual PHE observed here is very likely related to the Dirac SSs of TI films. We note that the similar PMR

values obtained in the measurements and the reproducibility of the data exclude the degradation of the exchange-induced magnetization of the EuS/TI heterostructure.

B. Magnetotransport measurements of EuS/3-QL (Bi_{0.22}Sb_{0.78})₂Te₃ films

To shed more light on the role of the Dirac SSs in the magnetotransport of EuS/TI heterostructures, we reduced the thickness of the (Bi_{0.22}Sb_{0.78})₂Te₃ films. It is established both theoretically and experimentally that in the 2D limit of a 3D TI film (<4 QLs in Sb₂Te₃ and <6 QL in Bi₂Se₃), hybridization between the bottom and top Dirac SSs can occur, resulting in a hybridization gap [13–15,33–36]. The gap opening in our 3-QL TI heterostructures is confirmed by the much larger response to V_g , as shown in Fig. 2(c). Additional support comes from the nonlinear I_{sd} - V_{sd} characteristics near the charge-neutral point (CNP) [Fig. 2(d)]. This I_{sd} - V_{sd} nonlinearity could be attributed to the presence of a gap [37,38] or shallow traps [39] in the narrow-gap semiconductors, both of which suggest the absence of a gapless Dirac SS. We note that the I_{sd} - V_{sd} curves of 3-QL TI heterostructure are linear in the n - and p -doped regimes [Fig. 2(d)], thus excluding film discontinuity and nonuniformity as the source of the observed nonlinearity.

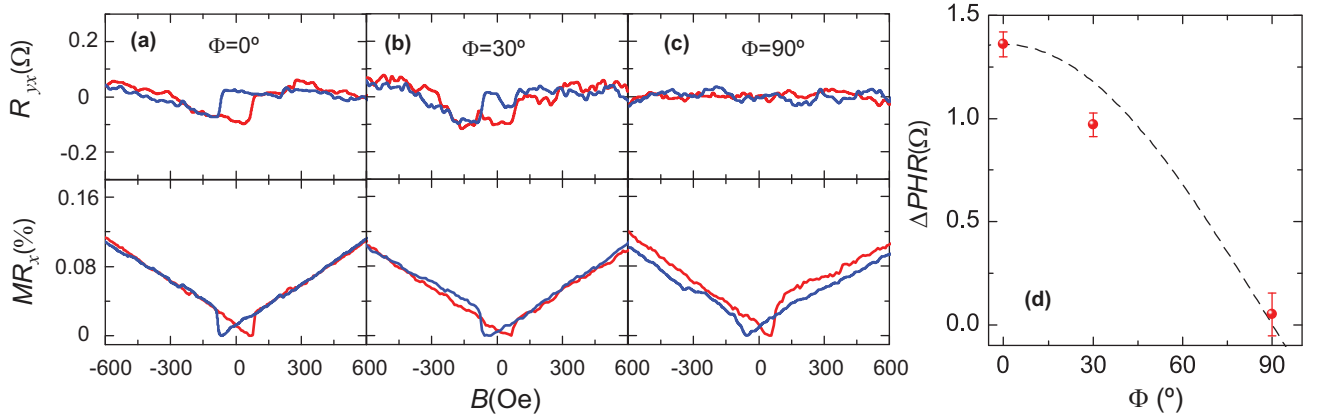


FIG. 4. Angle-dependent PHE and PMR measurements in another 5-nm EuS/4-QL $(\text{Bi}_{0.22}\text{Sb}_{0.78})_2\text{Te}_3$ heterostructure. (a)–(c) PHE (top panels) and PMR (bottom panels) taken on another 5-nm EuS/4-QL $(\text{Bi}_{0.22}\text{Sb}_{0.78})_2\text{Te}_3$ (with Dirac SSs) heterostructure with $\Phi = 0^\circ$ (a), $\Phi = 30^\circ$ (b), and $\Phi = 90^\circ$ (c), respectively. Φ is the angle between the current I and the in-plane magnetic field B . (d) Summary of the PHR as a function of Φ . The dashed line is a fit to $A \cdot \cos\Phi$ (A is the amplitude).

The 5-nm EuS/3-QL $(\text{Bi}_{0.22}\text{Sb}_{0.78})_2\text{Te}_3$ heterostructure exhibited different magnetotransport properties [Figs. 3(c) and 3(d)]. The PHR signal is observed only in the p -doped region and vanishes in the CNP region. The noticeable suppression of both the PMR and PHE around the CNP is consistent with a gap formation at the Dirac point. This emphasizes the role of the gapless Dirac SSs on magnetotransport. We note that in the p -doped region, the observed PHR signal in this heterostructure was also suppressed when the magnetic field was rotated from the x direction ($\Phi = 0^\circ$) to the y direction ($\Phi = 90^\circ$) [22]. The similar angular dependence observed in the p -doped region of 3-QL $(\text{Bi}_{0.22}\text{Sb}_{0.78})_2\text{Te}_3$ films is likely due to the contribution of the Rashba-type bands in the hybridized SSs and/or bulk valence bands [14].

IV. DISCUSSION

Below we will explore possible existing mechanisms for PHE in relation with our two major findings: (1) the PHR shows a peak at the Dirac point, as revealed by the gate dependence; (2) the PHR is maximized when the in-plane magnetic field B is parallel to the current I ($\Phi = 0^\circ$) but it is suppressed for B perpendicular to I ($\Phi = 90^\circ$). It has been found that an out-of-plane ferromagnetic order exists at the interface between EuS and highly n -doped Bi_2Se_3 and can persist up to room temperature [40]. Out-of-plane magnetization can induce a large anomalous Hall (AH) response for chemical potentials in the vicinity of the CNP. However, no hysteresis loops or nonlinear features were observed in our Hall measurements on a 5-nm EuS/4-QL $(\text{Bi}_{0.22}\text{Sb}_{0.78})_2\text{Te}_3$ heterostructure with an out-of-plane magnetic field [Fig. 5(a)], thus excluding the possibility that the observed PHE comes from a weak out-of-plane ferromagnetism due to the misalignment of magnetic fields. In addition, the out-of-plane magnetoresistance shows a weak antilocalization with a steeper increase of the MR in the vicinity of the charge-neutral point, which is consistent with previous studies on intrinsic TI films [Fig. 5(b)] [41]. This further excludes the presence of out-of-plane magnetization in our heterostructures. The emergence of a PHE was previously explained by a

variety of mechanisms, including anisotropic scattering by magnetic impurities [2], a nonspherical Fermi surface [5], spin Hall magnetoresistance [7], and chiral anomaly [8–10]. However, these mechanisms satisfy the relationship described by Eqs. (1) and (2) and although they might play some role in our observations, they cannot explain the observed large PHR at $\Phi = 0^\circ$ as well as the different scaling of the PHE and PMR. We note that deviations from Eq. (1) due to anisotropic resistivity in single crystals [42,43], such as in SrRuO_3 films [44–46], are also unlikely since the Hall bars used in our experiments were patterned by hand, and therefore repeated alignment with specific crystal axis is unlikely. Furthermore, no such deviations were found in high magnetic-field measurements of TIs [6]. Additional deviations were attributed to strong magnetic anisotropy, similar to (Ga, Mn)As films [4] and $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ films [43], but such an anisotropy is absent in the epitaxial EuS films [47]. Therefore, the unconventional PHE observed in EuS/ $(\text{Bi}_{0.22}\text{Sb}_{0.78})_2\text{Te}_3$ heterostructures cannot be explained satisfactorily by the microscopic mechanisms discussed above.

To understand our observation of PHE, we next present a symmetry argument of the Hall response. The standard

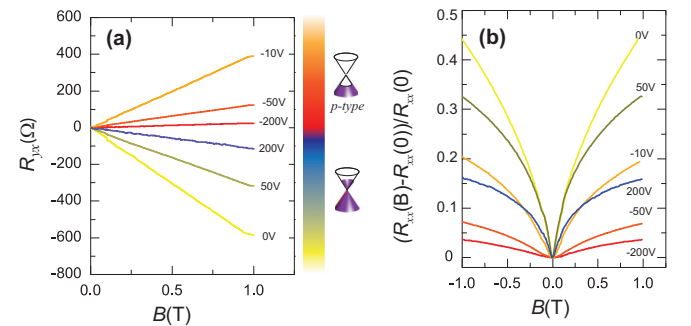


FIG. 5. Out-of-plane magnetotransport in a 5-nm EuS/4-QL $(\text{Bi}_{0.22}\text{Sb}_{0.78})_2\text{Te}_3$ heterostructure. (a) Out-of-plane Hall resistance R_{yx} at different V_g s and $T = 2\text{ K}$. (b) MR curves at different V_g s and $T = 2\text{ K}$.

(linear) Hall response is described by $j_y = \sigma_{yx} E_x$, where j_y is the Hall current, E_x is the driving electric field, and σ_{yx} is the Hall conductivity. Without loss of generality, we may consider the magnetization of our system to be along the x direction ($\Phi = 0^\circ$) which implies the symmetry of the system with respect to in-plane mirror operation $m_x (x \rightarrow -x, y \rightarrow y)$. As a result, the Hall conductivity σ_{yx} must be zero since $E_x \rightarrow -E_x$, $J_y \rightarrow J_y$ under this symmetry operation. This symmetry argument is consistent with the vanishing PHR for $\Phi = 0^\circ$ according to Eq. (1), and thus any linear Hall response mechanism cannot explain the observed nonzero PHE for $\Phi = 0^\circ$ in our experiment. This motivates us to consider the nonlinear Hall response, defined as $j_y = \sigma_{yxx} E_x^2$. Since E_x^2 is invariant under the mirror operation m_x , the above symmetry argument cannot exclude a nonzero nonlinear Hall conductivity σ_{yxx} . Thus, our experimental observation should have nonlinear Hall mechanism origin. Below, we will discuss two possible scenarios for the observed PHE in our experiment.

The first scenario is attributed to spin-orbit torque, which has been previously demonstrated in a magnetic TI film with an in-plane magnetic field parallel to the current [48,49]. According to this scenario, a current in the x direction will be accompanied by an effective magnetic field $B_{SO} = -I\lambda_{SO}\hat{y} \times \mathbf{m}$, with \mathbf{m} being the magnetization vector, I is the current, and λ_{SO} is the spin-orbit coupling strength of surface states. When the external magnetic field is in parallel to the current (x direction), the effective magnetic field B_{SO} is expected to possess an out-of-plane component, which can induce an out-of-plane magnetization component at equilibrium through the additional spin-orbit torque term $\tau_{SO} = -\gamma \mathbf{M} \times B_{SO}$ in the Landau-Lifshitz-Gilbert equation. The resulting out-of-plane magnetization can in turn give rise to an AH resistance, which is proportional to the current. Thus, this AH response induced by external in-plane magnetic fields is nonlinear. On the other hand, when the external magnetic field is perpendicular to the current (y direction), the effective magnetic field B_{SO} vanishes and no spin-orbit torque term appears. This is consistent with our observation that PHR is maximized for $\Phi = 0^\circ$ but suppressed for $\Phi = 90^\circ$. Previous studies on magnetic TI films [48,49] have shown the spin-orbit torque term will maximize at the charge-neutral point of the top surface state, which agrees with our observation. However, we need to point out that while both surface states in magnetic TI films can contribute to spin-orbit torque [48,49], only the top surface state can couple to magnetic moments in the EuS layer in our EuS/TI heterostructure. Therefore, to confirm this scenario additional experimental techniques which are beyond the scope of the present work, such as spin pumping [50–52], spin torque ferromagnetic resonance [53–55], and spin Seebeck effect [56] are required to directly probe spin torque in EuS/TI heterostructures.

The second scenario is related to the nonlinear response of Dirac fermions to the in-plane magnetic field. In fact, recent findings have demonstrated that asymmetric scattering of electrons by magnons in magnetic TIs with perpendicular anisotropy can lead to stronger PHR than the above-mentioned SOT mechanism in the in-plane magnetic field [57] accompanied with pronounced unidirectional magnetoresistance [58]. The limited experimental data of angular dependent measurements on our EuS/TI heterostructure prevents us

to examine this scenario. Below we will describe an additional mechanism for non-linear Hall response. We examine the effective Hamiltonian of the Dirac SS of TI with an in-plane magnetization [59],

$$H_0 = Dk^2 + \hbar v_f (k_x \sigma_y - k_y \sigma_x) + M \cos \Phi \sigma_x + M \sin \Phi \sigma_y. \quad (3)$$

Here the kinetic energy term is expanded up to the second order in momentum (Dk^2) and the exchange-induced magnetization is described by M and the angle Φ . One can easily show that the Berry curvature for H_0 is always zero except at one gapless point $k_x = -[M \sin \Phi / \hbar v_f]$, $k_y = M \cos \Phi / \hbar v_f$, which indicates a vanishing linear Hall contribution. The nonlinear Hall conductivity σ_{yxx} can be evaluated through the perturbation theory and is given by

$$\sigma_{yxx} = \frac{3e^2}{2\pi} \sum_{k, \eta \neq \xi} \left\langle \phi_{k\eta} \left| \frac{\partial \phi_{k\xi}}{\partial k_y} \right\rangle \left\langle \phi_{k\xi} \left| \frac{\partial \phi_{k\eta}}{\partial k_x} \right\rangle \right. \\ \times ((J_x)_{\eta\eta}(k) - (J_x)_{\xi\xi}(k)) \frac{(\rho_{0,\xi\xi}(k) - \rho_{0,\eta\eta}(k))}{(E_{k\eta} - E_{k\xi})^2}, \quad (4)$$

where $E_{k\eta(\xi)}$ and $\phi_{k\eta(\xi)}$ are eigenenergy and eigenstate with the index $\eta(\xi)$, $(J_x)_{\eta\eta} = (1/\hbar)(\partial E_\eta / \partial k_x)$ is the current operator and $\rho_{0,\eta\eta}(k)$ is the equilibrium distribution function (see Ref. [22] for a detailed derivation). For the Hamiltonian H_0 , Eq. (4) suggests that the nonlinear σ_{yxx} mainly arises from the interband transition between the two branches of Dirac SSs with the same momentum but opposite velocities. Direct calculations in the clean limit (the relaxation time $T_2 \rightarrow \infty$) give rise to the nonlinear $\sigma_{yxx} = (3De^3M)/(4\hbar^2 v_f \varepsilon_F^2) \cos \Phi$, where ε_F is the Fermi energy. The $\sigma_{yxx} \propto 1/\varepsilon_F^2$ dependence is consistent with the observation of PHE enhancement around the Dirac point, as revealed by the gate-dependence measurement. It should be pointed out that the divergence of σ_{yxx} at $\varepsilon_F \rightarrow 0$ should be rounded off by disorder scattering. Furthermore, this nonlinear Hall mechanism can also explain the absence of PHE in the CNP region of the 5-nm EuS/3-QL ($\text{Bi}_{0.22}\text{Sb}_{0.78}$)₂Te₃ heterostructures, since the hybridization gap formed by quantum confinement in thinner TI film will lead to an enhancement of energy denominator in Eq. (4) and thus suppress the nonlinear σ_{yxx} , in particular for chemical potentials near the CNP. Finally, although we cannot fully support the $\cos \Phi$ dependence, the above analysis indicates that the nonlinear σ_{yxx} is maximized for $\Phi = 0^\circ$, but suppressed for $\Phi = 90^\circ$, in agreement with our observations [Fig. 4(d)]. We note that the presence of a PHE signal in the p -doped region can be explained by the existence of Rashba-type bands in the hybridized SSs and/or bulk valence bands [14] since the relative position of the CNP is close to the maximum of the bulk valence bands [18,60,61]. In our experiment, the PHE is not observed in the n -type region of 3-QL heterostructures. This is not surprising since the band structure of TI in the n - and p -type regions are usually not symmetric [14].

V. CONCLUSION

To summarize, our studies reveal the observation of a significant PHE signal in FMI/TI heterostructures,

demonstrating a unique dependence on TI film thickness, chemical potential, and the angle between the in-plane magnetic field and the current. Based on a simple symmetry argument, we explain why linear Hall contributions cannot account for our observations and suggest two alternative non-linear contributions, with more experiments required to clarify the exact contribution of each mechanism. Our work will pave the way for the investigations of the topological magnetization dynamics and promote FMI/TI heterostructures as a platform for potential topological spintronic and electronic applications.

ACKNOWLEDGMENTS

The authors would like to thank N. Samarth and J. Shi for the helpful discussions. D.R., J.S.M., and C.-Z.C. acknowledge support from NSF Grant No. DMR-1207469, ONR Grant No. N00014-13-1-0301, and the STC Center for Integrated Quantum Materials under NSF Grant No. DMR-1231319. C.L. acknowledges the support from the Office of Naval Research (Grant No. N00014-15-1-2675). C.-Z.C. acknowledges the support from the Alfred P. Sloan Research Fellowship and ARO Young Investigator Program Award No. W911NF1810198.

- [1] E. H. Hall, *Am. J. Math.* **2**, 287 (1879).
- [2] V. D. Ky, *Sov. Phys. JETP-USSR* **23**, 809 (1966).
- [3] K. M. Seemann, F. Freimuth, H. Zhang, S. Blugel, Y. Mokrousov, D. E. Burgler, and C. M. Schneider, *Phys. Rev. Lett.* **107**, 086603 (2011).
- [4] H. X. Tang, R. K. Kawakami, D. D. Awschalom, and M. L. Roukes, *Phys. Rev. Lett.* **90**, 107201 (2003).
- [5] C. Goldberg and R. E. Davis, *Phys. Rev.* **94**, 1121 (1954).
- [6] A. A. Taskin, H. F. Legg, F. Yang, S. Sasaki, Y. Kanai, K. Matsumoto, A. Rosch, and Y. Ando, *Nat. Commun.* **8**, 1340 (2017).
- [7] Y. T. Chen, S. Takahashi, H. Nakayama, M. Althammer, S. T. B. Goennenwein, E. Saitoh, and G. E. W. Bauer, *Phys. Rev. B* **87**, 144411 (2013).
- [8] S. Nandy, G. Sharma, A. Taraphder, and S. Tewari, *Phys. Rev. Lett.* **119**, 176804 (2017).
- [9] A. A. Burkov, *Phys. Rev. B* **96**, 041110 (2017).
- [10] S. Nandy, A. Taraphder, and S. Tewari, *arXiv:1707.06262* (2017).
- [11] D. A. Thompson, L. T. Romankiw, and A. F. Mayadas, *IEEE T. Magn.* **11**, 1039 (1975).
- [12] *Solid State Physics*, edited by F. Seitz and D. Turnbull (Academic Press, New York, 1955), p. 1.
- [13] Y. P. Jiang, Y. L. Wang, M. Chen, Z. Li, C. L. Song, K. He, L. L. Wang, X. Chen, X. C. Ma, and Q. K. Xue, *Phys. Rev. Lett.* **108**, 016401 (2012).
- [14] Y. Zhang, K. He, C. Z. Chang, C. L. Song, L. L. Wang, X. Chen, J. F. Jia, Z. Fang, X. Dai, W. Y. Shan, S. Q. Shen, Q. Niu, X. L. Qi, S. C. Zhang, X. C. Ma, and Q. K. Xue, *Nat. Phys.* **6**, 584 (2010).
- [15] T. Zhang, J. Ha, N. Levy, Y. Kuk, and J. Strosio, *Phys. Rev. Lett.* **111**, 056803 (2013).
- [16] C. Z. Chang, J. S. Zhang, X. Feng, J. Shen, Z. C. Zhang, M. H. Guo, K. Li, Y. B. Ou, P. Wei, L. L. Wang, Z. Q. Ji, Y. Feng, S. H. Ji, X. Chen, J. F. Jia, X. Dai, Z. Fang, S. C. Zhang, K. He, Y. Y. Wang, L. Lu, X. C. Ma, and Q. K. Xue, *Science* **340**, 167 (2013).
- [17] C. Z. Chang, W. W. Zhao, D. Y. Kim, H. J. Zhang, B. A. Assaf, D. Heiman, S. C. Zhang, C. X. Liu, M. H. W. Chan, and J. S. Moodera, *Nat. Mater.* **14**, 473 (2015).
- [18] J. S. Zhang, C. Z. Chang, Z. C. Zhang, J. Wen, X. Feng, K. Li, M. H. Liu, K. He, L. L. Wang, X. Chen, Q. K. Xue, X. C. Ma, and Y. Y. Wang, *Nat. Commun.* **2**, 574 (2011).
- [19] D. S. Kong, Y. L. Chen, J. J. Cha, Q. F. Zhang, J. G. Analytis, K. J. Lai, Z. K. Liu, S. S. Hong, K. J. Koski, S. K. Mo, Z. Hussain, I. R. Fisher, Z. X. Shen, and Y. Cui, *Nat. Nanotechnol.* **6**, 705 (2011).
- [20] R. Yoshimi, A. Tsukazaki, Y. Kozuka, J. Falson, K. S. Takahashi, J. G. Checkelsky, N. Nagaosa, M. Kawasaki, and Y. Tokura, *Nat. Commun.* **6**, 6627 (2015).
- [21] M. D. Li, C. Z. Chang, B. J. Kirby, M. E. Jamer, W. P. Cui, L. J. Wu, P. Wei, Y. M. Zhu, D. Heiman, J. Li, and J. S. Moodera, *Phys. Rev. Lett.* **115**, 087201 (2015).
- [22] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevB.98.094404> for MBE growth of EuS/TI heterostructures, device fabrications, additional transport results, theoretical calculations, and other supporting data, which includes Refs. [2–6,23–25].
- [23] P. Wei, F. Katmis, B. A. Assaf, H. Steinberg, P. Jarillo-Herrero, D. Heiman, and J. S. Moodera, *Phys. Rev. Lett.* **110**, 186807 (2013).
- [24] H. Haug and S. W. Koch, *Quantum Theory of the Optical and Electronic Properties of Semiconductors* (World Scientific, Singapore, 2004).
- [25] D. J. Thouless, M. Kohmoto, M. P. Nightingale, and M. den Nijs, *Phys. Rev. Lett.* **49**, 405 (1982).
- [26] M. Li, Q. Song, W. Zhao, J. A. Garlow, T.-H. Liu, L. Wu, Y. Zhu, J. S. Moodera, M. H. W. Chan, G. Chen, and C.-Z. Chang, *Phys. Rev. B* **96**, 201301 (2017).
- [27] J. Smit, *Physica* **17**, 612 (1951).
- [28] T. R. McGuire and R. I. Potter, *IEEE Trans. Magn.* **11**, 1018 (1975).
- [29] P. M. Levy and S. F. Zhang, *Phys. Rev. Lett.* **79**, 5110 (1997).
- [30] H. Nakayama, M. Althammer, Y. T. Chen, K. Uchida, Y. Kajiwara, D. Kikuchi, T. Ohtani, S. Geprags, M. Opel, S. Takahashi, R. Gross, G. E. W. Bauer, S. T. B. Goennenwein, and E. Saitoh, *Phys. Rev. Lett.* **110**, 206601 (2013).
- [31] K. Hong and N. Giordano, *Phys. Rev. B* **51**, 9855 (1995).
- [32] Y. Bason, L. Klein, J. B. Yau, X. Hong, and C. H. Ahn, *Appl. Phys. Lett.* **84**, 2593 (2004).
- [33] H. Z. Lu, W. Y. Shan, W. Yao, Q. Niu, and S. Q. Shen, *Phys. Rev. B* **81**, 115407 (2010).
- [34] C.-X. Liu, H. J. Zhang, B. Yan, X.-L. Qi, T. Frauenheim, X. Dai, Z. Fang, and S.-C. Zhang, *Phys. Rev. B* **81**, 041307 (2010).
- [35] J. Linder, T. Yokoyama, and A. Sudbo, *Phys. Rev. B* **80**, 205401 (2009).
- [36] G. Landolt, S. Schreyeck, S. V. Eremeev, B. Slomski, S. Muff, J. Osterwalder, E. V. Chulkov, C. Gould, G. Karczewski, K. Brunner, H. Buhmann, L. W. Molenkamp, and J. H. Dil, *Phys. Rev. Lett.* **112**, 057601 (2014).

- [37] C. W. Zhou, J. Kong, and H. J. Dai, *Phys. Rev. Lett.* **84**, 5604 (2000).
- [38] A. N. Akimov, V. G. Erkov, A. E. Klimov, E. L. Molodtsova, S. P. Suprun, and V. N. Shumsky, *Semiconductors* **39**, 533 (2005).
- [39] M. A. Lampert, *Phys. Rev.* **103**, 1648 (1956).
- [40] F. Katmis, V. Lauter, F. S. Nogueira, B. A. Assaf, M. E. Jamer, P. Wei, B. Satpati, J. W. Freeland, I. Eremin, D. Heiman, P. Jarillo-Herrero, and J. S. Moodera, *Nature (London)* **533**, 513 (2016).
- [41] J. Chen, H. J. Qin, F. Yang, J. Liu, T. Guan, F. M. Qu, G. H. Zhang, J. R. Shi, X. C. Xie, C. L. Yang, K. H. Wu, Y. Q. Li, and L. Lu, *Phys. Rev. Lett.* **105**, 176602 (2010).
- [42] N. Naftalis, Y. Bason, J. Hoffman, X. Hong, C. H. Ahn, and L. Klein, *J. Appl. Phys.* **106**, 023916 (2009).
- [43] W. Y. Cui, P. Li, and H. L. Bai, *J. Appl. Phys.* **117**, 133904 (2015).
- [44] I. Genish, L. Klein, J. W. Reiner, and M. R. Beasley, *Phys. Rev. B* **75**, 125108 (2007).
- [45] N. Haham, Y. Shperber, J. W. Reiner, and L. Klein, *Phys. Rev. B* **87**, 144407 (2013).
- [46] M. Ziese and I. Vrejoiu, *Phys. Rev. B* **84**, 104413 (2011).
- [47] B. Saftic, N. Rasula, W. Zinn, and J. Chevallier, *J. Magn. Magn. Mater.* **28**, 305 (1982).
- [48] Y. B. Fan, X. Kou, P. Upadhyaya, Q. Shao, L. Pan, M. Lang, X. Che, J. Tang, M. Montazeri, K. Murata, L. T. Chang, M. Akyol, G. Yu, T. Nie, K. L. Wong, J. Liu, Y. Wang, Y. Tserkovnyak, and K. L. Wang, *Nat. Nanotechnol.* **11**, 352 (2016).
- [49] Y. B. Fan, P. Upadhyaya, X. F. Kou, M. R. Lang, S. Takei, Z. X. Wang, J. S. Tang, L. He, L. T. Chang, M. Montazeri, G. Q. Yu, W. J. Jiang, T. X. Nie, R. N. Schwartz, Y. Tserkovnyak, and K. L. Wang, *Nat. Mater.* **13**, 699 (2014).
- [50] Y. Shiomi, K. Nomura, Y. Kajiwar, K. Eto, M. Novak, K. Segawa, Y. Ando, and E. Saitoh, *Phys. Rev. Lett.* **113**, 196601 (2014).
- [51] H. L. Wang, J. Kally, J. S. Lee, T. Liu, H. C. Chang, D. R. Hickey, K. A. Mkhoyan, M. Z. Wu, A. Richardella, and N. Samarth, *Phys. Rev. Lett.* **117**, 076601 (2016).
- [52] M. Jamali, J. S. Lee, J. S. Jeong, F. Mahfouzi, Y. Lv, Z. Y. Zhao, B. K. Nikolic, K. A. Mkhoyan, N. Samarth, and J. P. Wang, *Nano Lett.* **15**, 7126 (2015).
- [53] A. R. Mellnik, J. S. Lee, A. Richardella, J. L. Grab, P. J. Mintun, M. H. Fischer, A. Vaezi, A. Manchon, E. A. Kim, N. Samarth, and D. C. Ralph, *Nature (London)* **511**, 449 (2014).
- [54] K. Kondou, R. Yoshimi, A. Tsukazaki, Y. Fukuma, J. Matsuno, K. S. Takahashi, M. Kawasaki, Y. Tokura, and Y. Otani, *Nat. Phys.* **12**, 1027 (2016).
- [55] Y. Wang, P. Deorani, K. Banerjee, N. Koirala, M. Brahlek, S. Oh, and H. Yang, *Phys. Rev. Lett.* **114**, 257202 (2015).
- [56] Z. L. Jiang, C. Z. Chang, M. R. Masir, C. Tang, Y. D. Xu, J. S. Moodera, A. H. MacDonald, and J. Shi, *Nat. Commun.* **7**, 11458 (2016).
- [57] K. Yasuda, A. Tsukazaki, R. Yoshimi, K. Kondou, K. S. Takahashi, Y. Otani, M. Kawasaki, and Y. Tokura, *Phys. Rev. Lett.* **119**, 137204 (2017).
- [58] K. Yasuda, A. Tsukazaki, R. Yoshimi, K. S. Takahashi, M. Kawasaki, and Y. Tokura, *Phys. Rev. Lett.* **117**, 127202 (2016).
- [59] C. X. Liu, X. L. Qi, H. J. Zhang, X. Dai, Z. Fang, and S. C. Zhang, *Phys. Rev. B* **82**, 045122 (2010).
- [60] G. Wang, X. G. Zhu, J. Wen, X. Chen, K. He, L. L. Wang, X. C. Ma, Y. Liu, X. Dai, Z. Fang, J. F. Jia, and Q. K. Xue, *Nano Res.* **3**, 874 (2010).
- [61] C. Z. Chang, W. W. Zhao, D. Y. Kim, P. Wei, J. K. Jain, C. X. Liu, M. H. W. Chan, and J. S. Moodera, *Phys. Rev. Lett.* **115**, 057206 (2015).