Multiple topologically nontrivial bands in noncentrosymmetric YSn₂

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The square lattices formed by main-group elements such as Bi, Sb, Sn, and Si in layered materials have attracted a lot of interest, since they can create rich topological phases. In this paper, we report the slightly distorted square lattice of Sn in a noncentrosymmetric compound YSn_2 generates multiple topologically nontrivial bands, one of which likely hosts a nodal line and tunable Weyl semimetal state induced by the Rashba spin-orbit coupling and proper external magnetic field. The quasiparticles described as relativistic fermions from these bands are manifested by nearly zero mass and nontrivial Berry phases probed in de Haas-van Alphen (dHvA) oscillations. The dHvA study also reveals YSn_2 has a complicated Fermi surface, consisting of several three-dimensional (3D) and one 2D pocket. Our first-principles calculations show the pointlike 3D pocket at Y point on the Brillouin zone boundary hosts the possible Weyl state. Our findings establish YSn_2 as a new interesting platform for observing novel topological phases and studying their underlying physics.

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I. INTRODUCTION

Three-dimensional (3D) topological Dirac and Weyl semimetals are characterized by linear band crossings near the Fermi level. The low-energy excitation around the Dirac or Weyl nodal points are viewed as quasiparticles or emergent relativistic fermions, which can be described by the Dirac/Weyl equation. These relativistic fermions result in exotic properties of the host materials, such as large magnetoresistance [1], high carrier mobility [1,2], and chiral anomaly [3]. The 3D Dirac semimetals (DSMs) were first predicted and then discovered in Na₃Bi [4,5] and Cd₃As₂ [6-8], which show fourfold degenerate Dirac nodes. When the spin degeneracy is lifted by breaking time-reversal symmetry or inversion symmetry, a Dirac semimetal is expected to evolve into a Weyl semimetal (WSM), with each Dirac cone splitting into a pair of Weyl cones with opposite chirality [9,10]. The inversion symmetry breaking WSM state was first realized in transition-metal monopnictides (Ta/Nb)(P/As) [9-16] and photonic crystal [17], and even extended to phononic crystal [18]. The time-reversal symmetry breaking Weyl state has been predicted in many material systems such as Y₂Ir₂O₇ [19], HgCr₂Se₄ [20], YbMnBi₂ [21], and Heusler compounds $Co_2 XZ$ (X = IVB or VB, Z = IVA or IIIA) [22,23] and

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most of these predictions are still waiting for experimental verifications. Additionally, a new type (type-II) of Weyl nodes violating the Lorentz symmetry has recently been reported in several material systems including WTe₂ [24,25], MoTe₂ [26,27], LaAlGe [28], and TaIrTe4 [29–32]; such a type-II Weyl state features strongly tilted Weyl cones, which lead to the touching of the electron and hole Fermi pockets at Weyl points.

Recently, there has been growing interest in relativistic fermions generated by 2D square lattices. Several material families with square lattices have been found to harbor relativistic fermions, including $AMnBi_2$ - (A = Ca, Sr, Ba, or rare-earth element) [21,33–36], $AMnSb_2$ - (A = Ca, Sr, Ba, or rare-earthelement) [37-42], and WHM-type (W = Zr, Hf, or rare-earth elements; H = Si, Ge, Sn, Sb; and M = S, Se, Te) [43–52] compounds. The 2D square lattices consisting of group IV or V elements such as Si, Sn, Ge, Bi, and Sb play a critical role in generating relativistic fermions in these materials. Such a 2D square lattice effectively forms checkerboardlike complex lattice due to its chemical environment. This might result in band folding and nonsymmorphic symmetric operation, which are closely related with band topology. A rich variety of topological phases have been observed or predicted in these materials, e.g., the anisotropic Dirac cone state [33], the nodal-line state [44,46,53], the 2D nonsymmorphic Dirac state [44], time-reversal symmetry breaking Weyl state [21,38], quantum spin Hall insulator in ZrSiO monolayer [43], etc. This suggests that layered compounds with the square lattices formed by group IV/V elements are fertile ground for the search of new topological phases. Here, we report the discovery

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FIG. 1. (a) Crystal structure of YSn_2 . (b) Top view of Sn plane. (c) Distorted Sn layer of YSn_2 . (d) Single-crystal x-ray diffraction spectra of YSn_2 . Inset is an optical image of single-crystal YSn_2 .

of a new layered topological semimetal YSn_2 with a noncentrosymmetric crystal structure and lightly distorted Sn square lattice. We find this material possesses multiple topologically nontrivial bands, one of which hosts a new type of tunable Weyl state induced by Rashba spin-orbit coupling (SOC) and tunable by magnetic field.

II. METHODS

A. Experiment

The YSn₂ single crystals used in this study were synthesized using a flux method. The Y pieces and Sn lumps with molar ratio of 1:4 were loaded in an Al₂O₃ crucible and sealed in a quartz tube under high vacuum. The mixtures were then heated to 1050°C and held at this temperature for 48 hours for homogeneously melting, followed by a slow cooling down to 750°C at rate of 2°C per hour and then a quick cooling down (4°C/h) from 750°C to 350°C. Excessive Sn flux was removed by centrifugation. The excellent crystallization of the single crystals was confirmed by the sharp (0 K 0) x-ray diffraction (XRD) peaks, as shown in Fig. 1(d). The inset in Fig. 1(d) displays an optical image of a typical YSn₂ crystal. We have also measured the composition of the synthesized crystals using an energy dispersive x-ray spectrometer (EDS) and the measured composition is YSn_{1.95}, slightly deviated from the expected stoichiometric composition YSn₂. The Sn deficiency implies that there are possible vacancies at Sn sites. The magnetization was measured using a SQUID magnetometer (Quantum Design) and the magnetic torque measurements were carried out at the NHMFL in Tallahassee using a cantilever torque magnetometer.

We have studied the structure of YSn₂ using both singlecrystal neutron and x-ray diffractions. Neutron diffraction measurements were performed at room temperature using the HB-3A four-circle diffractometer ($\lambda = 1.003$ Å) at High Flux Isotope Reactor in Oak Ridge National Laboratory. The crystal structure of YSn₂ was obtained via Rietveld refinement of a collection of nuclear Bragg peaks using the FULLPROF program, as described in Table S1 in the Supplemental Material [54]. For the x-ray diffraction (XRD) measurements, the YSn₂ single-crystal sample was mounted on the tips of Kapton loop. Room temperature (293 K) intensity data were collected on a Bruker Apex II x-ray diffractometer with Mo radiation K $\alpha_1(\lambda = 0.71073$ Å) using a completely identical sequence. Data were collected over a full sphere of reciprocal space with 0.5° scans in ω with an exposure time of 10 s per frame. The 2θ range extended from 4°–75°. The SMART software was used for data acquisition. Intensities were extracted and corrected for Lorentz and polarization effects with the SAINT program. Numerical absorption corrections were accomplished with XPREP, which is based on face-indexed absorption [55]. The twin unit cell was tested. With the SHELXTL package, the crystal structures were solved using direct methods and refined by full-matrix least-squares on F² [56].

B. Computation

The first-principles calculation for YSn_2 is based on density functional theory (DFT) [57,58] within the Perdew-Burke-Ernzerhof (PBE) exchange correlation [59,60] implemented in the Vienna *ab initio* simulation package [61,62]. The planewave cutoff energy is 520 eV with a $8 \times 8 \times 12 k$ mesh in the Brillouin zone (BZ) [63]. We employ maximally localized Wannier functions [64,65] to obtain the tight-binding model of the bulk YSn_2 and use it for the Fermi surface (FS) calculation.

III. RESULTS AND DISCUSSIONS

A. Structure determination of YSn₂

Previous powder XRD studies show YSn₂ possesses an orthorhombic structure with space group Cmcm [66,67]. Although our neutron scattering spectra can be refined by the reported centrosymmetric Cmcm crystal structure, we found that two slightly different noncentrosymmetric orthorhombic structures with space groups C2cm and $Cmc2_1$ can also yield good refinements. As shown in Table S1 in the Supplemental Material, the agreement factors are comparable among these three refinements, which prevent us from determining the exact structure of YSn₂. Since these three different space groups correspond to the same powder diffraction pattern, it is difficult to determine whether the structure has inversion symmetry or not through powder diffraction spectra refinements. This inspired us to determine if our synthesized YSn₂ has broken inversion symmetry through single-crystal XRD measurements. We conducted careful single-crystal XRD measurements on YSn₂ and refined the structure with different space groups. We find that the best refinement is obtained with the space group $Cmc2_1$. The detailed structural parameters obtained

TABLE I. Structural parameters of YSn₂ determined by singlecrystal XRD measurements at 293(2) K. Space group: $Cmc2_1$ (No. 36). Lattice parameters: a = 4.332(1) Å, b = 16.052(3) Å, c = 4.235(1) Å, $\alpha = \beta = \gamma = 90^{\circ}$. $R_1 = 0.0611$; $wR_2 = 0.1291$; Goodness of fit = 0.936. U_{eq} is defined as one-third of the trace of the orthogonalized U_{ij} tensor (Å²).

Atom	Wyckoff.	Occupancy.	x	У	z	U_{eq}
Y	4 <i>a</i>	0.94(2)	0	0.0999(4)	0.240(4)	0.016(2)
Sn1	4a	1	0	0.4372(3)	0.237(3)	0.024(1)
Sn2	4 <i>a</i>	1	0	0.7490(3)	0.238(3)	0.023(1)

from the refinement are shown in Table I. The flack factor obtained in this refinement is 0.3(2), which confirms the noncentrosymmetric structure. Supplemental Tables S2 and S3 present the comparison of crystallographic data between $Cmc2_1$ and Cmcm. The $Cmc2_1$ structure of YSn₂ is also supported by our first-principles calculations, which show that only the band structure calculated with the space group of $Cmc2_1$ matches with the experimentally probed bands (see below).

Figure 1(a) depicts the crystal structure of YSn_2 determined by our XRD experiment, which can be viewed as the alternative stacking of the Sn staggered layers and the Sn planes, with Y ions located in between. As shown in Fig. 1(b), the Sn planar layer is a distorted square net with the bonding angles slightly deviating from 90°. It is worth noting that the two bonding angles shown in Fig. 1(b) are not supplementary (i.e., not adding up to 180°), indicating that this plane is not exactly 2D. That is, the Sn layers are slightly corrugated along the *a* or *c* axis, as shown in Fig. 1(c).

B. Relativistic fermion behavior probed by dHvA oscillations in YSn₂

Signatures of topological relativistic fermions in YSn₂, including light effective mass, high mobility, and nontrivial Berry phase, have been found from our quantum oscillation studies on YSn2 single-crystal samples. We have observed clear dHvA oscillations in the isothermal magnetization measured using a SQUID magnetometer. As shown in Fig. 2(a), when the magnetic field was applied along the out-of-plane direction (i.e., B//b axis), the magnetization at 1.8 K starts to oscillate for B > 3.2 T and the oscillations remain observable up to 21 K. The oscillations look more striking after removing the background, as shown in Fig. 2(b). The fast Fourier transform (FFT) analyses show such dHvA oscillations consist of a single oscillation frequency of $F_{\beta} = 78$ T, as shown in the inset to Fig. 2(c). For the in-plane magnetic field, no oscillations were probed up to 7 T (the highest field of the SQUID). However, as will be presented later, we observed multifrequency dHvA oscillations for both out-of-plane and in-plane magnetic fields in high-field magnetic torque measurements. The observation of low-field dHvA oscillations in the magnetization measured using a SOUID is rare and its presence usually implies high carrier mobility.

The relativistic fermion properties of YSn_2 were found from the analyses of the observed dHvA oscillations. In general, the dHvA oscillations of a topological material can be described



FIG. 2. (a) Isothermal out-of plane (B//b axis) magnetization M for YSn₂ at various temperatures (T = 1.8 K-21 K). (b) Oscillatory magnetization after subtracting the background for B//b in the 1.8–21 K temperature range. (c) The fits of the FFT amplitudes of the dHvA oscillations to the temperature damping factor R_T in the LK formula. Inset shows the FFT spectra of the oscillatory magnetization for B//b. (d) The fit of the dHvA oscillation pattern at 1.8 K by the LK formula, with the solid line representing the fitted curve.

by the Lifshitz-Kosevich (LK) formula [68,69] with a Berry phase being taken into account [70]:

$$\Delta M \propto -B^{1/2} R_T R_D R_S \sin\left[2\pi \left(\frac{F}{B} + \gamma - \delta\right)\right], \quad (1)$$

where $R_T = \alpha T m^* / [Bm_0 \sinh(\alpha T m^* / Bm_0)]$, $R_D = \exp(-\alpha T_D m^* / Bm_0)$, and $R_S = \cos(\pi g m^* / 2m_0)$. T_D is the Dingle temperature, and $\alpha = (2\pi^2 k_B m_0) / (\hbar e)$. The oscillation of ΔM is described by the sine term with a phase factor $\gamma - \delta$, in which $\gamma = \frac{1}{2} - \frac{\phi_B}{2\pi}$ and ϕ_B is Berry phase. The phase shift δ , which is determined by the dimensionality of the FS, is 0 and $\pm 1/8$ respectively for 2D and 3D cases. For the 3D case, the sign of δ depends on whether the probed extreme cross-section area of the FS is maximal or minimal. $\delta = -1/8 (1/8)$ for maximal (minimal) cross section for a 3D electron pocket and vice versa for a 3D hole pocket [69].

From the LK formula, the effective mass m^* can be obtained through the fit of the temperature dependence of the oscillation amplitude to the thermal damping factor R_T . As shown in Fig. 2(c), the effective masses we obtained from this type of fit for the observed dHvA oscillation of magnetization is $(0.082 \pm 0.002)m_0$ where m_0 is the free-electron mass. Since the FFT amplitude (FFTA) is used as the oscillation amplitude for the fit in Fig. 2(c), the inverse field 1/B in R_T should be replaced by the average inverse field $1/\overline{B}$, defined as $1/\overline{B} = (1/B_{\text{max}} + 1/B_{\text{min}})/2$, where B_{max} and B_{min} define the magnetic field range used for the FFT. With the effective masses and the oscillation frequency being the known parameters, we have further fitted the dHvA oscillation pattern at 1.8 K by the LK formula [Eq. (1)], as shown in Fig. 2(d). Such an oscillation pattern fit yields the Dingle temperature of 10 K,



FIG. 3. (a) and (d) The field dependence of magnetic torque τ for YSn₂ at different temperatures from 1.7 K–50 K, which show strong dHvA oscillations. The magnetic field is applied nearly along the *b* axis (a) and *ac* plane (d). (b) and (e) show the FFT spectra of the oscillatory magnetization $\Delta \tau$ for B//b' and B//ac', respectively. (c) and (f) show the fits of the FFT amplitudes by the temperature damping term R_T of the LK formula.

from which the quantum mobility $\mu_q [=e\hbar/(m^*2\pi k_B T_D)]$ is estimated to be 2609 cm² V⁻¹ s⁻¹.

The relativistic nature of carriers in YSn₂ is supported by the nontrivial Berry phases. The phase factors of the oscillations extracted from the above LK-fit [Fig. 2(d)] is $\gamma - \delta = 0.01$, from which the Berry phase of $(0.49-\delta) \times 2\pi$ can be derived. As will be shown below, the Fermi pocket associated with the $F_{\beta} = 78$ T frequency displays 2D characteristics, implying that δ should be taken as 0 for the F_{β} band. Thus, the Berry phase is 0.98π , close to the ideal value of π for Dirac-like energy band crossings.

The observation of single-frequency dHvA oscillation in the low-field range does not necessarily imply YSn₂ is a singleband system. In order to gain more insights into its electronic band structure, we have further extended the dHvA studies to high fields up to 31 T, through the magnetic torque measurements [which were performed at the National High Magnetic Field Lab (NHMFL), Tallahassee]. We observed multiple oscillation frequencies in these measurements, implying that YSn_2 has a complicated Fermi surface. In Fig. 3(a), we present the torque oscillation pattern measured with the field applied nearly along the out-of-plane direction (denoted as B//b'). We chose such a field orientation because the torque signal vanishes when the field is perfectly aligned normal or parallel to the surface of the cantilever tip [47]. The dHvA oscillations under high magnetic fields show multiple frequencies. As shown in Fig. 3(b), three major frequencies can be resolved in the FFT spectrum, i.e., $F_{\alpha} = 23$ T, $F_{\gamma} = 301$ T, and $F_{\theta} =$ 433 T. These frequencies originate from three different 3D Fermi pockets according to the first-principles calculations (see below). Surprisingly, the oscillation frequency of $F_{\beta} = 78 \text{ T}$ seen in the low-field magnetization measurements [Fig. 2(c),

inset] is not probed in torque. This is possibly due to the fact that the torque signal is the weakest for the out-of-plane or in-plane field. This conjecture is verified by the observation that the F_{β} oscillation component appears when the field is tilted away from the out-of-plane direction. The effective quasiparticle masses m^* corresponding to F_{α} , F_{γ} , and F_{θ} probed in torque are estimated to be $(0.029 \pm 0.002)m_0 (m_{\alpha}^*)$, $(0.023 \pm 0.002)m_0 (m_{\gamma}^*)$, and $(0.038 \pm 0.004)m_0 (m_{\theta}^*)$. The fits of the temperature dependences of the FFT amplitudes from which m^* is derived are shown in Fig. 3(c).

Although $m_{\alpha}^{*}, m_{\gamma}^{*}$, and m_{θ}^{*} are comparable and F_{α} is one order of magnitude smaller than F_{γ} or F_{θ} , the FFT amplitude of F_{α} is about 16 times stronger than that of F_{γ} or F_{θ} , as shown in Fig. 3(b), which implies that the quasiparticles hosted by the F_{α} pocket must have much longer life time (i.e., higher quantum mobility) compared with the F_{γ} or F_{θ} pocket. To further evaluate the quasiparticle properties of the F_{α} pocket, we have performed the LK fit for the T = 1.7 K oscillatory torque obtained by subtracting the nonoscillating background. To minimize fitting parameters, we have filtered the F_{γ} and F_{θ} components and the fit is made for the single F_{α} component, as shown in Fig. 4(a). This LK fit yields a quantum mobility of $776 \text{ cm}^2/\text{Vs}$ and a Berry phase of $(0.309 - \delta) \times 2\pi = 0.968\pi$, suggesting nontrivial band topology. Here we take $\delta = -1/8$, since the F_{α} pocket is a 3D spherelike electron pocket as discussed below and the probed F_{α} oscillation should correspond to a maximal cross section of the F_{α} pocket for B//b'. The first-principles calculations find that around the F_{α} pocket the related two bands can host nodal line and such a nodal line decays into a Weyl semimetal state caused by Rashba spin-orbit coupling and proper external magnetic field, which will be discussed in great detail below. On considering the very



FIG. 4. (a) and (b) show the low-frequency (F_{α}) dHvA oscillations probed in magnetic torque for B//b' and B//ac', respectively, obtained after filtering the high-frequency components. (c) shows the high-frequency $(F_{\gamma} \text{ and } F_{\theta})$ oscillatory components of magnetic torque for B//ac', obtained after filtering the low-frequency components. The solid curves in (a), (b), and (c) represent the fits of the T = 1.7 K oscillation patterns by the single-/two-band LK formula.

small mass, high mobility, and closeness to both nodal line and WSM state, the F_{α} pocket is most probably topologically nontrivial. For the high-frequency oscillation components F_{γ} and F_{θ} , however, their LK fits are difficult since their dHvA oscillations show a low signal-to-noise ratio.

In order to further characterize the properties of the quasiparticles hosted by the F_{α} , F_{γ} , and F_{θ} pockets, we have also performed high-field magnetic torque measurements with the field applied nearly along the in-plane direction (denoted as B/(ac'). Strong dHvA oscillations have also been observed in these measurements, as shown in Fig. 3(d). The FFT analyses of these data [Fig. 3(e)] reveal four major fundamental frequencies, i.e., 21 T, 386 T, 465 T, and 655 T. The first three frequencies correspond, respectively, to F_{α} , F_{γ} , and F_{θ} probed with B//b' and such a correspondence is manifested by the angular dependences of the oscillation frequencies, which will be presented below. However, the highest frequency 655 T (denoted by F_{ϕ}) is an additional component, which is not probed for B//b'. From the fit of temperature dependence of FFT amplitude, we have also estimated m^* for each oscillation frequency probed for B//ac' [Fig. 3(f)] and found m^* is also very small for all probed frequencies and within the range of $(0.022-0.065)m_0$, consistent with the small values of $m^*[\sim(0.023-0.038)m_0]$ probed with B//b'. Table II lists m^* for all frequencies probed in both field orientations for comparison. The errors of the fitted m^* are also given in this table. As will be shown later, these experimentally measured m^* agree well with the first-principles calculated mass (Table III).

For the dHvA oscillations shown in Fig. 3(d), we have also conducted Berry phase analyses. In general, for multiplefrequency quantum oscillations, the Berry phase for each band can be extracted via fitting the oscillation pattern by a multiband LK model, which can be generalized from Eq. (1) [71,72]. In order to achieve more accurate fits, we have separated the low- ($F_{\alpha} = 21 \text{ T}$) and high-frequency ($F_{\gamma} = 386 \text{ T}$ and $F_{\theta} = 465 \,\mathrm{T}$) oscillation components and fit them individually, as shown in Figs. 4(b) and 4(c). The F_{ϕ} component has been filtered out, since this component exhibits very few oscillation peaks in the measured field range, which hinders a meaningful fit. As shown in Fig. 4(b), for the F_{α} component, the oscillation becomes aperiodic above 14 T, which is most likely due to Zeeman effect and cannot be fitted by the simple LK formula with only the fundamental frequency [Eq. (1)]. Therefore, our fit for this component is performed within the <14 T field range. For the high-frequency components (F_{ν} and F_{θ}) shown in Fig. 4(c), the two-band LK model can well reproduce the oscillation pattern at T = 1.7 K. From these LK fits, we also obtained nontrivial Berry phases not only for the F_{α} pocket, but also for the F_{γ} , and F_{θ} pockets, as listed in Table II. [Note that δ should be taken as 1/8 for the F_{α} pocket for B//ac', since the Rashba effect splits this Fermi surface, leading to a minimum cross section for B//ac' (see below).] This indicates that all the F_{α} , F_{γ} , and F_{θ} pockets host relativistic fermions. Other signatures of relativistic fermions such as high quantum mobility and small effective mass are also revealed from the above LK fits, as summarized in Table II. The LK mass fits for F_{α} , F_{γ} , F_{θ} , and F_{ϕ} for B//ac' are shown in Fig. 3(f). The F_{α} pocket, while being the smallest, hosts relativistic fermions with much higher quantum mobility ($\sim 1621 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ for B//ac', almost twice of those of the F_{γ} , and F_{θ} pockets). High quantum mobility generally means low back-scattering rate in cyclotron motions. This might be the reason why the FFT amplitude of the F_{α} pocket is much stronger than those of the F_{γ} , and F_{θ} pockets [Figs. 3(b) and 3(e)]. These facts imply that the relativistic fermions of the F_{α} pocket may have better topological protection against back scattering than those of the F_{γ} , and F_{θ} pockets. As will be shown below, the F_{α} pocket is

TABLE II. Parameters derived from the analyses of dHvA oscillations for YSn₂. *F*, oscillation frequency; T_D , Dingle temperature; m^* , effective mass; μ_q , quantum mobility; ϕ_B , Berry phase; δ , the phase shift factor in quantum oscillations; $\delta = 0$ for a 2D FS, but $\pm 1/8$ for a 3D FS (see text).

Field Direction	$F(\mathbf{T})$	Notation	$T_D(\mathbf{K})$	m^*/m_0	$\mu_q (\mathrm{cm}^2/\mathrm{Vs})$	ϕ_B
	23	F_{α}	95	0.029 ± 0.002	776	$(0.968 \pm 0.003)\pi \ (\delta = -1/8)$
B//b'	301	F_{γ}	١	0.023 ± 0.002	١	λ
	433	$\dot{F_{ heta}}$	١	0.038 ± 0.004	١	١
B//b (Magnetization)	78	F_{eta}	10	0.082 ± 0.002	2609	$(0.98 \pm 0.012)\pi \ (\delta = 0)$
	21	F_{lpha}	60	0.022 ± 0.002	1621	$(0.87 \pm 0.069)\pi \ (\delta = 1/8)$
B//ac'	386	F_{γ}	82	0.034 ± 0.003	767	$(0.49 \pm 0.032)\pi \ (\delta = -1/8)$
	465	$F_{ heta}$	60	0.065 ± 0.008	891	$(0.66 \pm 0.019)\pi$ ($\delta = 1/8$) or (1.16 ± 0.019) π ($\delta = -1/8$)
	655	F_{ϕ}	١	0.040 ± 0.003	١	

Pocket Name	dHvA frequencies (T) for $B//b'$	$k_F (\text{\AA}^{-1})$ estimated from the dHvA	DFT-calculated $k_F(\text{\AA}^{-1})$	Effective mass estimated from the dHvA (m_0)	DFT-calculated effective mass (m_0)
α	23	0.0264	0.025	0.029 ± 0.002	0.0118
β	78	0.0478	١	0.082 ± 0.002	١
γ	301	0.0955	0.09	0.023 ± 0.002	0.0121
θ	433	0.115	0.111	0.038 ± 0.004	0.0625

TABLE III. Fermi wave vector and effective mass obtained from the first-principles calculations and dHvA experiments for the α , β , γ , and θ pockets.

at the Y point on the Brillouin zone boundary and hosts a Weyl state driven by Rashba spin-orbital coupling.

In addition to the quantum oscillation studies for B//b'and B//ac', we have also measured the angular dependence of the dHvA oscillations to reveal the information on the Fermi surface morphology. With the field being rotated from the out-of-plane (B//b), defined as $\theta = 0^{\circ}$) to the in-plane $(B//ac, \theta = 90^{\circ})$ direction [see the inset of Fig. 5(c) for the experiment setup], the dHvA oscillations probed in both the low-field magnetization [Fig. 5(a)] and the high-field torque [Fig. 5(b)] display clear evolutions. The backgrounds have been subtracted for the dHvA oscillation data presented in Figs. 5(a) and 5(b). The dHvA oscillations in magnetization show only a single-frequency F_{β} in the low angle range of $<30^{\circ}$, but double frequencies for $30^{\circ} < \theta < 45^{\circ}$, i.e., F_{β} and an additional low frequency. The low additional frequency component [displayed by white open circles in Fig. 5(c)] is actually the F_{α} component detected in the torque measurements. As noted above, the oscillation frequency of F_{β} is absent in the torque measurements for the field exactly along the b axis, but it appears when the field is tilted away from the b axis. In both the magnetization and torque measurements, the F_{β} oscillation component was found to disappear when θ is increased above 45°. As seen in Fig. 5(c), F_{α} as well as F_{β} probed by both techniques are consistent. The fact that F_{β} is present only for $\theta < 45^{\circ}$ and its angular dependence F_{β} (θ) follows the $1/\cos\theta$ dependence [see the red fit curve in Fig. 5(c)] suggests the existence of a small 2D Fermi pocket, which is expected for a layered material such as YSn₂. For other frequencies, F_{α} , F_{γ} , F_{θ} , and F_{ϕ} , their angular dependences all display 3D

characters. Particularly, F_{α} is almost independent of angle, suggesting a very small, spherelike Fermi surface, which is consistent with the calculated Fermi surface as shown in the next section.

It is interesting to note that although the F_{α} band hosts a Weyl state as discussed below, the quantum mobility of the relativistic fermions hosted by this band $(776 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1} \text{ for})$ B//b') is smaller than that of the F_{β} band (2609 cm² V⁻¹ s⁻¹). This may be associated with the fact that the F_{α} and F_{β} bands form two different Fermi surfaces with different morphology, dimensionality, and Fermi velocity. Given that quantum oscillations originate from cyclotron motions, the scattering process could be very different between the F_{α} and F_{β} pockets due to their different Fermi surface properties. Unlike transport mobility, which is only sensitive to large angle scattering, the quantum mobility depends sensitively on both small and large angle scattering. As a result, it is not surprising to see different quantum mobility between two nontrivial pockets with different Fermi surfaces. The other possibility is that the F_{β} band may host a new topological state, which may have better topological protection against scattering than the F_{α} band. Clarification of this matter requires further studies.

C. Electronic band structure of YSn₂

In order to understand the relativistic fermion behavior revealed through the dHvA studies on YSn₂, we performed first-principles calculations for both the $Cmc2_1$ and Cmcmcrystal structures and found that the band structure calculated with the space group of $Cmc2_1$ is nearly consistent with



FIG. 5. (a) dHvA oscillations of isothermal magnetization (*M*) for YSn₂ at T = 1.8 K under different magnetic field orientations. (b) dHvA oscillations of magnetic torque of YSn₂ at T = 1.8 K under different magnetic field orientations. The data of different θ have been shifted for clarity and the nonoscillating background has been subtracted. (c) The angular dependences of oscillation frequencies for YSn₂. Inset: the experimental setup.



FIG. 6. (a) Crystal structure for YSn₂ with the space group of $Cmc2_1$. There is a distorted Sn lattice every two layers and a glide mirror $\overline{M}_{y}\{\frac{1}{2},\frac{1}{2},0\}$ for YSn₂. (b) Band dispersions for YSn₂. The radius of red dots represents atomic projections from Sn in the Sn lattice. (c), (d) Magnified band dispersion of the α pocket along different directions. The two bands are nondegenerated along Γ -Y and Y-U directions and form a nodal line along the Y-T direction.

the bands probed by the dHvA experiments, while the band structure of *Cmcm* does not match with the experimentally probed bands at all. Figures 6 and 7 display the calculated band structure and FS respectively for the $Cmc2_1$ structure (the band structure and FS calculated with the space group of *Cmcm* is shown in Fig. S1). These calculated results clearly show



FIG. 7. (a)–(c) shows the Fermi surface formed by the three pairs of bands around Fermi level. (d)–(e) shows the Fermi surfaces for YSn₂ at $k_y = 0$ and $k_y = \pi$ plane, respectively. (f) is the BZ for YSn₂ and the green dashed line indicates the momenta of nodal line. (g) shows the magnification of the α pocket where the two red points are two crossing points along the T-Y direction. (i), (ii), (ii), and (iv) in (g) depict four possible paths of cyclotron orbitals for the Fermi pocket α for B//b.

YSn₂ is a multiple band system. Its Fermi surface consists of multiple sheets as shown in Figs. 7(a)-7(c). The energy bands probed in the dHvA calculations mostly agree with calculated ones. Specifically, three calculated small pockets, i.e., the α , γ , and θ pockets [see Figs. 7(b) and 7(c) for the α and γ pockets] all have been probed in the dHvA oscillations. As shown in Table III, the calculated Fermi wave vectors k_F as well as the effective quasiparticle mass for these three pockets are in good agreement with those derived from the F_{α} , F_{γ} , and F_{θ} oscillation components. Figures 7(d) and 7(e) show the FS at $k_v = 0$ and π respectively, from which we can see the α pocket is at the highly symmetric momentum point, i.e., the Y point on the BZ boundary, while the γ and θ pockets are at accidental momentum points [see Figs. 6(b)-6(d)]. The calculated α , γ , and θ pockets all exhibit 3D characters, consistent with the angular dependences of F_{α} , F_{γ} , and F_{θ} shown in Fig. 5(c). The estimated k_F given in Table III for the α , γ , and θ pockets are based on the cross sections of these pockets at the $k_v = 0$ and π planes [Figs. 7(d) and 7(e)]. The calculations also reveal several other bigger Fermi pockets shown in Figs. 7(a)-7(c). However, these pockets were not clearly resolved in the dHvA oscillations possibly due to the lower mobility of quasiparticles hosted by these pockets. Since these pockets have very complex morphologies, it is hard to tell whether the F_{ϕ} band is associated with them. As indicated above, in the dHvA oscillations, we have also probed a 2D band hosting relativistic fermions in the dHvA oscillations, i.e., the F_{β} band, but this band is not clearly reflected in the calculated band structure.

Next, we will show the α pocket hosts a Weyl semimetal state driven by the Rashba SOC coupling and external magnetic field. Glide mirror $\bar{M}_y\{\frac{1}{2},\frac{1}{2},0\}$ [Fig. 6(a)] and time-reversal symmetry τ play import roles in YSn₂. Here, we define an antiunitary symmetry Θ as their composition. $\Theta = \bar{M}_y * \tau$. Importantly, $\Theta^2 = \bar{M}_y^2 * \tau^2 = T110 = e^{-i(k_x a + k_y b)}$, where k_x and k_y are reciprocal lattice vectors, a and b are crystal constants, and T_{110} is the unit lattice translation along the (110) direction. Specially, we will get Kramers degeneracy $\Theta^2 = -1$ at the BZ boundary where $k_x = 0$, $k_y = \pi/b$. Thus, the green dashed lines (T-Y) in Fig. 7(f) will be double degenerate, forming a nodal line in the BZ. However, since the space group $Cmc2_1$ has no inversion symmetry and a polar axis is allowed along the z direction, the Rashba-type spin-orbit coupling will break the degeneracy along the directions other than T-Y on the $k_y = \pi/b$ plane. So the α pocket is spin splitting other than the two red dots shown in Fig. 7(g) where it intersects with the nodal line along T-Y. The Rashba-like effective Hamiltonian at the $k_y = \pi/b$ plane is $H_R = \sigma_z k_x - \sigma_x k_z$ without considering other symmetries in YSn₂. Once an external magnetic field, e.g., B_z , is applied in the *ac* plane to the system, such Rashba term will become to $H'_{R} = \sigma_{z}(k_{x} + B_{z}) - \sigma_{x}k_{z}$ and time-reversal symmetry will be broken. Therefore, on one hand, the twofold degenerate nodal line along T-Y will decay into Weyl points due to the Θ symmetry breaking; on the other hand, such Weyl points will move along the direction perpendicular to the magnetic field to $(-Bz, \pi/b, 0)$. Once the Weyl points are achieved around the Fermi energy, they can lead to a π Berry phase for electrons making cyclotron motion on the α pocket, as demonstrated in the dHvA experiments discussed above. For an external magnetic field along the b'direction, Zeeman splitting introduces tiny band gap around Y and along the nodal line T-Y, which leads to small deviation of Berry phase from π proportional to the size of gap [73]. Insets (i), (ii), (ii), and (iv) in Fig. 7(g) depict four possible paths of cyclotron motion for electrons in the α pocket. However, the slight difference in the cyclotron frequency is not resolved in present dHvA experiments due to the quite small Rashba splitting and limited experimental resolution.

As seen in Fig. 6(c), the Rashba spin splitting (RSS) energy for YSn_2 is about 3.6 meV, which is much smaller than that of a typical Rashba semiconductor BiTeI whose RSS reaches 400 meV [74]. However, as long as the RSS energy is larger than the Zeeman energy, a nontrivial Berry phase is expected for the Weyl node induced by the RSS as discussed above, but a deal Berry phase of π is expected only when the RSS energy is much larger than the Zeeman energy. The dHvA oscillations probed in torque measurements indeed suggest that the RSS energy of the α pocket is much greater or greater than the Zeeman energy. For B//ac', we find that the dHvA oscillations of the α pocket start to deviate from the LK fit from 14 T, which is most likely caused by the Zeeman effect [Fig. 4(b)]. The Zeeman energy at 14 T is ~ 0.8 meV, indicating the Zeeman energy in the field range of < 14 T is smaller than the RSS energy. For B//b', the Zeeman effect is much weaker, we do not observe a clear trace of Zeeman splitting and the dHvA oscillation pattern can be fitted by the LK formula in the whole field range [see Fig. 4(a)]. The experimental observation of nontrivial Berry phase for both field configurations for the α pocket (i.e., $\phi_B = 0.968\pi$ for B//b' and 0.87π for B//ac') provides a strong support for our prediction that weak Rashba effect can create a Weyl node at Y point in YSn₂.

IV. CONCLUSION

In summary, we have synthesized single crystals of YSn₂ and characterized its crystal structure using neutron scattering and single-crystal XRD. Although previous work suggested YSn₂ has an orthorhombic centrosymmetric structure with space group of Cmcm, we find our YSn₂ single crystals possess a noncentrosymmetric $Cmc2_1$ structure. We also performed quantum oscillation studies on this compound through magnetization and magnetic torque measurements, from which we have demonstrated that it has multiple bands hosting relativistic fermions, including several 3D bands and one 2D band. From first-principles calculations, we found one of the 3D bands hosts a new type of Weyl state caused by Rashba spin-orbital coupling. This band forms a pointlike FS at Y point on the BZ boundary. Other 3D bands probed in the dHvA oscillations have also been predicted in the band structure calculations. However, the 2D band seen in the experiment was not revealed in the calculations, which is yet to be studied. Our findings show YSn2 is an interesting playground for observing and understanding novel topological phases. In addition, given that YSn₂ belongs to a large family of material $RESn_2(RE = rare - earth)$, our results may motivate further studies on other isostructural RESn₂ compounds, which show magnetic orders. If they also harbor relativistic fermions, they may provide opportunities to study the interplay between relativistic fermions and magnetism.

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