Magnetoresistance in LuBi and YBi semimetals due to nearly perfect carrier compensation

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Monobismuthides of lutetium and yttrium are shown as representatives of materials which exhibit extreme magnetoresistance and magnetic-field-induced resistivity plateaus. At low temperatures and in magnetic fields of 9 T, the magnetoresistance attains orders of magnitude of 10^4 % and 10^3 %, on YBi and LuBi, respectively. Our thorough examination of electron-transport properties of both compounds shows that observed features are the consequence of nearly perfect carrier compensation rather than of possible nontrivial topology of electronic states. The field-induced plateau of electrical resistivity can be explained with Kohler scaling. An anisotropic multiband model of electronic transport describes very well the magnetic field dependence of electrical resistivity and Hall resistivity. Data obtained from the Shubnikov–de Haas oscillation analysis also confirm that the Fermi surface of each compound contains almost equal amounts of holes and electrons. First-principle calculations of electronic band structure are in a very good agreement with the experimental data.

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Materials with extremely magnetic-field-dependent resistivity attract massive attention because of their possible applications in sensors and spintronic devices. Rare-earth-metal monopnictides with the NaCl-type crystal structure form a group of materials that possess relevant extraordinary properties. The very first observation of extreme magnetoresistance (XMR) in lanthanum monopnictides was reported by Kasuya et al. in 1996 [1]. Two decades later, it was proposed that lanthanum monopnictides could be topologically nontrivial materials [2], and magnetotransport properties of LaSb and LaBi have been found to resemble those of topological semimetals [3,4]. It was the starting point of an intensive revival of interest in rare-earth-metal monopnictides. Up to now, the question of the nontrivial topology of their electronic structures has remained open. Reports on the angle-resolved photoemission spectroscopy (ARPES) investigations of rareearth-metal monopnictides differ in their conclusions. Some describe these materials as having Dirac-like features in their electronic structure [5–9], while others show that nontrivial topology is absent [10-13].

Nonsaturating (in magnetic field) XMR has earlier been reported for Dirac semimetals Cd₃As₂ and ZrSiS, and Weyl semimetals NbP and TaAs [14–17]. However, their XMR could be often understood without invoking nontrivial topology. In nonmagnetic materials, charge carrier compensation [18], field-induced metal-insulator transition [19] (all unrelated to nontrivial topology), or field-induced lifting of topological protection from backscattering [14] could be responsible for XMR.

This work on YBi and LuBi is a continuation of our previous investigations of NaCl-type monoantimonides with high magnetoresistance [20,21]. These two compounds have been barely

studied previously. The first report on YBi crystal structure appeared in Ref. [22], and then binary phase diagrams Y-Bi and Lu-Bi, including YBi and LuBi, have been determined [23–25]. Several theoretical papers on lutetium monopnictides and YBi also appeared in the past few years [26–28]. There has been hitherto no information about magnetotransport properties of yttrium and lutetium monobismuthides. Here we report on electronic transport properties of high-quality single crystals of YBi and LuBi studied in magnetic fields up to 9 T. Experimental data are compared with results of electronic structure calculations.

We grew high-quality single crystals from Bi flux with the starting atomic composition RE:Bi of 1:19 (RE = Yor Lu). They had shapes of cubes with dimensions up to $4 \times 4 \times 4$ mm³. Microanalysis of the crystals with a scanning electron microscope equipped with energy-dispersive x-ray spectrometer (FEI SEM with an EDAX Genesis XM4 spectrometer) yielded equiatomic chemical composition of both compounds. Electrical resistivity and Hall effect measurements were carried out in a temperature range from 2 to 300K and in applied magnetic fields up to 9 T on a Quantum Design PPMS platform. The standard four-probe method was used for all measurements. Bar-shaped specimens with all edges along (100) crystallographic directions were cut from single crystals and then polished. Electrical contacts were made from 50- μ m-thick silver wires attached to the samples by spot welding and strengthened with silver epoxy. The electric current was always flowing along the [100] crystallographic direction and the magnetic field was applied along the [001] crystallographic direction.

Electronic structure calculations were carried out using both the WIEN2K code [29] with the full-potential linearized augmented plane wave (FLAPW) method and the full-potential Korringa-Kohn-Rostoker (KKR) Green's function method [30]. The exchange and correlation effects were treated using

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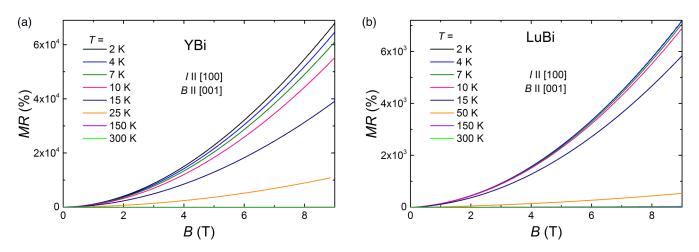


FIG. 1. Magnetoresistance isotherms of YBi (a) and LuBi (b) measured in magnetic field applied along [001] direction, transverse to electrical current.

the generalized gradient approximation (GGA) [31]. Spin-orbit coupling was included as a second variational step, using scalar-relativistic eigenfunctions as the basis, after the initial calculation was converged to self-consistency. The Monkhorst-Pack special *k*-point scheme with $44 \times 44 \times 44$ mesh was used in the first Brillouin zone sampling, and the cutoff parameter ($R_{mt}K_{max}$) was set to 8. For the Fermi surface, the irreducible Brillouin zone was sampled by 20225 *k* points to ensure accurate determination of the Fermi level [32]. Shubnikov–de Haas (SdH) frequencies were calculated using the Supercell *k*-space Extremal Area Finder tool [33].

I. MAGNETORESISTANCE, ELECTRICAL RESISTIVITY, AND HALL RESISTIVITY

Figure 1 shows magnetoresistance, $MR = 100\% \times [\rho(B) - \rho(B=0)]/\rho(B=0)$, of YBi and LuBi as a function of magnetic field, *B*, measured at several temperatures, *T*, in the range from 2 to 300K. For both compounds, *MR* has extreme values at low temperatures (for YBi, $MR = 6.8 \times 10^4$ % and for LuBi, $MR = 7.2 \times 10^3$ % at T = 2 K in B = 9 T). Up to T = 10 K, magnitudes of *MR* change only slightly, a pattern which corresponds to the

resistivity plateaus in $\rho(T)$ (see Fig. 3). We suppose that such big *MR* of our samples could be due to nearly perfect carrier compensation, as it has been reported for other rare-earth-metal monopnictides [5,10,20,21,34–38].

The difference between MR values of LuBi and YBi seems to reflect the difference in sample quality, rather than difference in electronic structures (see the next subsection). On the example of compensated semimetal WTe₂ and lanthanum monopnictides, it has been shown that magnitude of MRstrongly depends on sample quality [4,39]. On heating above 10K, MR of both compounds decreases strongly, and at 300K reaches 6% and 7% (in 9 T) for LuBi and YBi, respectively.

Figure 2 shows the results of Kohler scaling of MR for both compounds. All MR isotherms measured at different temperatures collapse on a single curve. According to the Kohler rule,

$$MR \propto (B/\rho_0)^m,$$
 (1)

where *m* is a sample-dependent constant that depends on the level of compensation (for perfectly carrier compensated systems m = 2). From the fitting of Eq. (1) (red solid lines in Fig. 2) to experimental data, we obtained m = 1.81 and

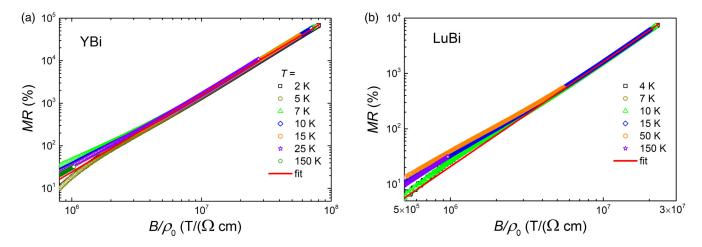


FIG. 2. Kohler scaling of transverse magnetoresistance, with $MR \propto (B/\rho_0)^m$ fitted to the data from temperature range 2–300K yielding m = 1.81 for YBi (a) and m = 1.89 for LuBi (b).

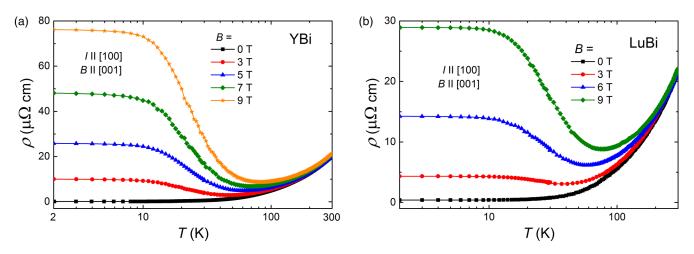


FIG. 3. Temperature variations of electrical resistivity of YBi (a) and LuBi (b) in various magnetic fields applied perpendicular to the current direction.

m = 1.89 for YBi and LuBi, respectively. These values of m are larger than previously reported for rare-earth-metal monoantimonides [20,21,37]. Our m values are close to that determined for LaBi [35], but still smaller than 1.92 reported for WTe₂ in Ref. [40]. They show that the carrier compensation in LuBi is slightly better than in YBi.

Figure 3 presents the results of electrical resistivity, ρ , measurements for YBi and LuBi in varying temperature in zero and in finite magnetic fields. When B = 0, both compounds demonstrate metallic behavior of $\rho(T)$, ρ gradually decreases with T lowering, from the values 20.0 and 21.6 $\mu\Omega$ cm at T = 300K to the values 0.1 and 0.4 $\mu\Omega$ cm at T = 2K for YBi and LuBi, respectively. It means that residual resistivity ratios [$\rho(300$ K)/ $\rho(2$ K)] are quite large and equal to 180 and 55 for YBi and LuBi, respectively.

Applying a magnetic field drastically changes the $\rho(T)$ behavior. Already in 3 T, ρ of each compound decreases upon cooling only to certain temperature where it has a minimum. Further decreasing of temperature leads to increase of ρ and its saturation below $T \approx 10$ K. Higher fields increase the values of resistivity in plateau region in accordance with $MR \propto B^m$ behavior depicted in Fig. 1. Such magnetic-field-induced resistivity plateau is a characteristic feature of topological

semimetals [15,19,41] and has also been observed in several rare-earth-metal monopnictides [4,20,21,34,36,42].

The authors of Ref. [40] argued that analogous turn-on behavior of $\rho(T)$ in WTe₂ could be understood in the scope of Kohler scaling. We used this approach to describe electrical resistivity of both studied monopnictides (see Fig. 4). Previously, it has also been used by Han *et al.* to explain magnetotransport properties of LaSb [37]. According to Wang *et al.*, $\rho(T)$ measured in magnetic field can be described by the following equation [40]:

$$\rho(T,B) = \rho_0(T,0) + \Delta \rho(T,B), \qquad (2)$$

where the first term corresponds to the temperature dependence of resistivity in zero magnetic field and the second term describes magnetic-field-induced resistivity. Assuming that $\rho_0(T,0)$ can be well approximated with the Bloch-Grüneisen law,

$$\rho(T) = \rho_0 + A \left(\frac{T}{\Theta_D}\right)^k \int_0^{\frac{\Theta_D}{T}} \frac{x^k}{(e^x - 1)(1 - e^{-x})} dx \quad (3)$$

and

$$\Delta \rho(T,B) = \gamma B^m / [\rho_0(T,0)]^{m-1},$$
(4)

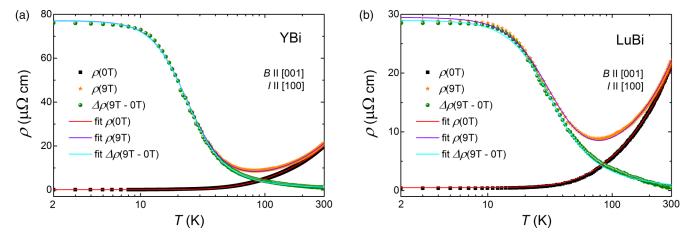


FIG. 4. Temperature variations of electrical resistivity measured in magnetic fields of 9 and 0 T and their difference for YBi (a) and LuBi (b). The solid lines correspond to fits of Eqs. (2) and (3).

TABLE I. Parameters obtained from the fitting of Eqs. (2) and (3) to the $\rho(T)$ data, as shown in Fig. 4.

	$ ho_0$ ($\mu\Omega$ cm)	$A \\ (\mu\Omega \mathrm{cm})$	Θ_D (K)	k	т	γ $(\Omega \text{ cm})^m$
YBi LuBi	0.12 0.5	42.3 34	295 307	3.08 2.55		

we simultaneously fitted $\rho(T)$ in zero field with Eq. (3) and $\rho(T)$ measured in B = 9 T with Eq. (2) using shared parameters. Fits to these model with ρ_0 , A, k, Θ_D , and γ as free parameters, and parameter m fixed at its value obtained from Kohler scaling are shown as red and purple solid lines in Fig. 4. The obtained parameters for both compounds are rather similar and listed in Table I. Values of k are close to that previously determined for LuSb [21] and several Lu- and La-containing intermetallics [43]. The Debye temperatures are smaller than $\Theta_D = 408$ and 420K reported for LuSb and LuAs, respectively [21,44].

Additionally, we show in the Fig. 4 magnetic-field-induced resistivity versus temperature as a green circles. This data were obtained by subtraction of data measured in zero magnetic field from those measured in 9 T. Cyan solid lines in Fig. 4 represent Eq. (4) with parameters yielded by the fitting of Eq. (2). In order to get more insight in carrier concentration, we measured Hall resistivity (ρ_{xy}) at the temperature of 2K, where MR attains its maximum. The $\rho_{xy}(B)$ plots for both compounds are shown in insets to Figs. 9(a) and 9(b). Their curved shapes indicate multiband character of conductivity. Since $\rho_{xy} << \rho_{xx}$ for both compounds, in further analysis (see Sec. III) we use Hall

conductivity σ_{xy} and longitudinal conductivity σ_{xx} , calculated using Eq. (6).

II. ELECTRONIC STRUCTURE CALCULATIONS AND SHUBNIKOV-DE HAAS EFFECT

Figure 5 presents calculated bulk electronic band structures of YBi and LuBi. The results of our calculations are consistent with scalar-relativistic data obtained for YBi [28]. Both compounds have very similar electronic structures. Due to spin-orbit interaction, threefold degeneracy of Bi-6*p* states is modified at the Γ point; i.e., one of the *p* bands dips deeply below E_F , whereas two other *p* bands remain degenerated and stay above E_F . Furthermore, the twofold degeneracy of these two bands is gradually lifted along Γ -L and Γ -X lines, and they become well separated at points L and X. The corresponding shifts of *p* bands are noticeably smaller in analogous monoantimonides [20,21], and eventually become just noticeable in arsenides (data not shown), reflecting decreasing spin-orbit coupling strength.

Fermi level crosses two holelike bands near the Γ point of Brillouin zone and one electronlike band around the X point. Besides, at ≈ 0.5 eV below the Fermi level, there is a tiny gap between the bands and the band inversion occurs. This is where the Dirac cones potentially may form. Analogous gaps have previously been reported in lanthanum monopnictides [2,45] and YSb [20], calculated using the GGA with Perdew-Burke-Ernzerhof exchange-correlation potential. Our electronic structure calculations reveals also some d - p mixed orbital texture near the X point of the Brillouin zone (visualized with red and blue colors in Fig. 5). This finding resembles those for PtSn₄, NbSb₂, LaBi, and WTe₂ [4,46]. The Fermi surface

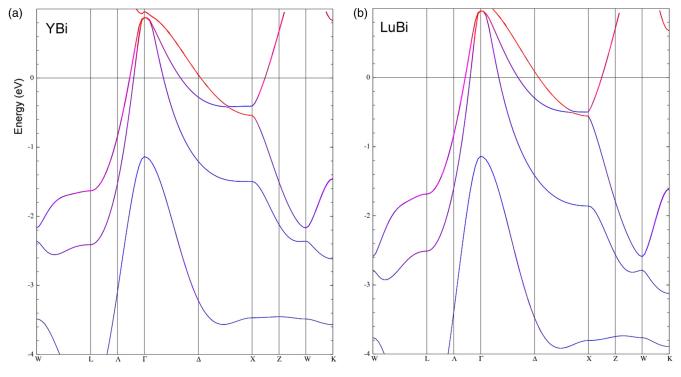


FIG. 5. Electronic band structure of YBi (a) and LuBi (b). Horizontal line marks the Fermi level. Red and blue colors denote contributions from d electrons of Y or Lu, and p electrons of Bi, respectively.

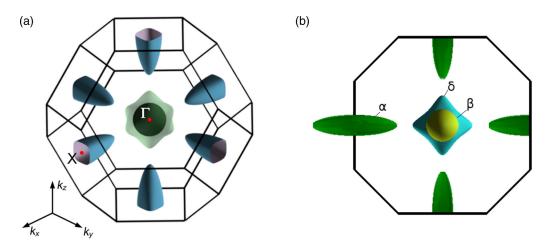


FIG. 6. (a) Fermi surface of YBi and LuBi. It consists of a triplicate electron pocket α and two hole pockets δ and β . (b) Projection of the Fermi surface on the (001) plane. Proportions between the Brillouin zone and Fermi pockets sizes were not preserved.

is very similar in both compounds and thus schematically depicted, together with its projection on (001) plane, in a common Fig. 6. It consists of a triplicate electron pocket centered at the X points (denoted as α) and two hole pockets (β and δ) nested in the center of the Brillouin zone. The calculations of electronic structure brought also the carrier concentrations, n_p^{calc} , cyclotron frequencies for maximal cross sections of Fermi pockets by planes perpendicular to [001] direction, f_p^{calc} , and corresponding cyclotron masses, m_p^{*calc} . Their values are collected in Table II. Comparing the ratios of the concentrations of electrons and holes $n_{\alpha}^{calc}/(n_{\beta}^{calc} + n_{\delta}^{calc})$, being 1.003 in YBi and 1.002 in LuBi, suggests that carrier compensation is nearly perfect in both compounds.

Good quality of our samples allowed us to observe quantum oscillations of electrical resistivity in magnetic field, i.e., the Shubnikov–de Haas (SdH) effect. The subtraction of the third-order polynomial background from the $\rho(1/B)$ data resulted in experimental curves presented in Fig. 7. Strong SdH oscillations were clearly observed at temperatures up to at least 10 and 15K for YBi and LuBi, respectively. The shape of $\Delta \rho(1/B)$ suggests multifrequency character of the oscillations. Indeed, their fast Fourier transform (FFT) analysis

shows for each of two compounds, six pronounced maxima (see Fig. 8). Corresponding SdH frequencies f_p^{FFT} are listed in Table II. These, denoted with f_{α}^{FFT} and $f_{\alpha'}^{FFT}$, we ascribe to the electrons on orbits being maximal cross sections of ellipsoid-like Fermi pocket α , perpendicular to its long and short axes, respectively. $f_{2\alpha}^{FFT}$ and $f_{3\alpha}^{FFT}$ are the second and the third harmonics of f_{α}^{FFT} . Frequencies f_{β}^{FFT} and f_{δ}^{FFT} are due to the hole pockets. We obtained very similar FFT spectra, matching very well the results of our electron structure calculations, for both compounds. According to the Onsager relation $f_{SdH} = hS/e$, where S is the area of Fermi surface cross section [47]. Assuming perfect ellipsoidal shape of the α subpockets and the spherical one of pocket β , we calculated the Fermi wave vectors and than carrier concentrations using the formula $n_p = V_{F,p}/(4\pi^3)$, where $V_{F,p}$ is the volume of Fermi pocket *p*. The n_e/n_h ratios resulting from analysis of SdH oscillations are 0.97 and 0.95 for YBi and LuBi, respectively. This shows that the electron-hole compensation is very close to perfect in both compounds, as hinted above by Kohler scaling and DFT calculations.

Effective masses (m^*) of the carriers of α Fermi pocket were calculated from the temperature dependence of FFT amplitude,

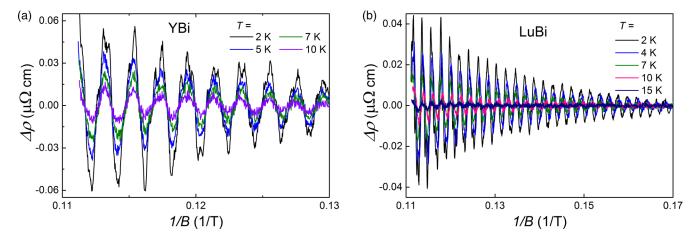


FIG. 7. Oscillating part of electrical resistivity as a function of inverted magnetic field for YBi (a) and LuBi (b), measured at several different temperatures.

TABLE II. Parameter	s obtained from ana	alysis of SdH oscillation	s measured at $T = 2K$ and	l from electronic ban	d structure calculations.
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Compound		$p = \alpha$	lpha'	2α	3α	eta	δ	n_e/n_h
YBi	f_p^{FFT} (T)	490	1766	966	1478	900	2069	
	$k_F \qquad (\text{\AA}^{-1})$	0.122	0.439			0.165	0.251	
	n_p (10 ²⁰ cm ⁻³)	6.0	53			1.53	5.33	0.97
	f_p^{calc} (T)	544	1853			1018	2492	
	n_{p}^{calc} (10 ²⁰ cm ⁻³)	7.5	52			1.80	5.70	1.003
	m_p^{*calc} (m ₀)	0.24	0.60			0.20	0.61	
LuBi	f_p^{FFT} (T)	477	1784	953	1535	884	2112	
	k_F (Å ⁻¹)	0.120	0.451			0.164	0.253	
	n_p (10 ²⁰ cm ⁻³)	6.0	51			1.49	5.50	0.95
	f_p^{calc} (T)	680	1868			980	2738	
	n_p^{calc} (10 ²⁰ cm ⁻³)	8.3	39			1.73	6.64	1.002
	m_p^{*calc} (m ₀)	0.29	0.56			0.18	0.59	

 R_{α} , at f_{α}^{FFT} frequency, obtained from the field window 7–9 T, using the following relation [47]:

$$R_{\alpha}(T) \propto (\lambda m^* T / B_{\text{eff}}) / \sinh(\lambda m^* T / B_{\text{eff}}), \qquad (5)$$

with $B_{\text{eff}} = 7.875$ T being the the reciprocal of average inverse field from the window where FFT was performed: $B_{\text{eff}} = 2/(1/B_1 + 1/B_2)$ (with $B_1 = 7$ T and $B_2 = 9$ T), and the constant $\lambda = 2\pi^2 k_B m_0/e\hbar$ (≈ 14.7 T/K), we obtained $m^* = 0.22 m_0$ for both compounds. This value of effective mass is close to those reported previously for other rare-earth-metal monopnictides [3,20,21,34,42,48] and also to effective masses $m_{\alpha}^{*\text{calc}} = 0.24 m_0$ and 0.29 m_0 , obtained from our electronic structure calculations for YBi and LuBi, respectively.

Observing good agreement of SdH analysis, the calculations and multiband fitting of magnetotransport (described in next section), all revealing or taking into account strong anisotropy of electron pocket, we decided not to pursue angle-dependent SdH measurements as we expect that they would yield results very similar to those presented in other papers on similar monopnictides [20,21,34,49].

III. MULTIBAND MODEL OF MAGNETOTRANSPORT

After establishing the presence of three distinct Fermi pockets, we proceeded to analyze how their form determines the field dependence of transverse magnetoresistivity, ρ_{xx} , and Hall resistivity, ρ_{xy} .

Cubic crystal symmetry of YBi and LuBi allows us to define components of conductivity tensor as follows:

$$\sigma_{xx} = \rho_{xx} / [(\rho_{xx})^2 + (\rho_{xy})^2],$$

$$\sigma_{xy} = -\rho_{xy} / [(\rho_{xx})^2 + (\rho_{xy})^2].$$
(6)

In semiclassical Drude model, conductivities of individual electron and hole pockets (indexed with p) are summed up to obtain total transverse and longitudinal components of conductivity tensor as follows:

$$\sigma_{xx} = \sum_{p} e n_{p} \mu_{p} / [1 + (\mu_{p} B)^{2}],$$

$$\sigma_{xy} = \sum_{p} e n_{p} \mu_{p}^{2} B / [1 + (\mu_{p} B)^{2}].$$
 (7)

Following the idea of Xu et al. [38] and stressing the inadequacy of an isotropic multiband model for the transport

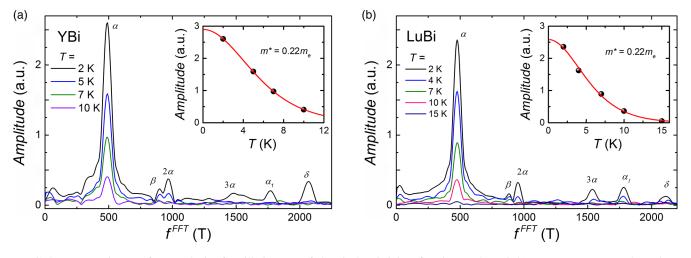


FIG. 8. Fast Fourier transform analysis of oscillating part of electrical resistivity of YBi (a) and LuBi (b). Insets: temperature dependence of the amplitude of the highest peak in the FFT spectra. Red solid line represents fits of Eq. (5) to the experimental data.

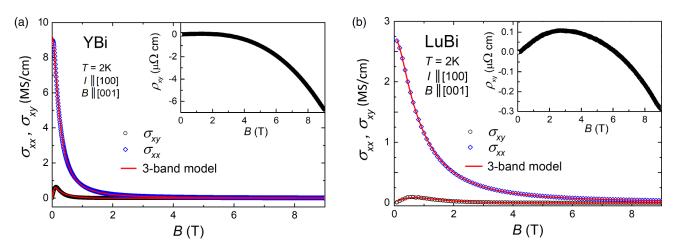


FIG. 9. Electrical conductivity and Hall conductivity versus magnetic field measured at T = 2K of (a) YBi and (b) LuBi. Red lines correspond to the fits with Eqs. (7).

properties of a system with anisotropic Fermi pockets, we used the same analysis as those authors, namely an anisotropic threeband model, taking into account pronounced anisotropy of the electron band α by using separate conductivities for pockets elongated parallel and transverse to the current direction, distinguished by two mobilities μ_{\parallel} and μ_{\perp} .

Since in the case of LaBi several authors used the effective two-band model, neglecting the anisotropy of electron pocket [3,34,35], we also tested that model for YBi and LuBi. However, the fittings with the three-band model were clearly better (see the Supplemental Material, [50]).

We fitted simultaneously both σ_{xx} and σ_{xy} of Eq. (7) to $\sigma_{xx}(B)$ and $\sigma_{xy}(B)$ data recorded at T = 2K, with shared parameters [using as $\rho_{xx}(B)$ the data shown in Fig. 1 plots of *MR* for 2K] as shown in Fig. 9. Resulting n_{α} , n_{β} , and $\kappa (\equiv \mu_{\perp}/\mu_{\parallel})$, together with μ_{\perp} , μ_{β} , n_{δ} , and μ_{δ} obtained from the fitting of Eq. (7), are listed in Table III.

These parameters allow us to estimate again the level of compensation of electrons and holes, expressed by the ratio $n_{\alpha}/(n_{\beta} + n_{\delta})$ being equal to 0.95 for YBi and 0.97 for LuBi. Comparing them to analogous values from analysis of SdH oscillations (0.97 for YBi and 0.95 for LuBi), we conclude that electron-hole compensation is nearly perfect in both compounds. Small discrepancies between compensation values derived by different methods are most likely due to the approximations of Fermi pocket's shapes we made in our analyzes.

IV. CONCLUSIONS

We investigated electron transport properties of highquality single crystals of two compounds, YBi and LuBi. The electronic structure that emerges from our results is almost identical for both compounds and points to their semimetallic character with nearly perfect compensation of electron and hole carriers. We found that low-temperature field-induced resistivity plateau could be interpreted in terms of Kohler scaling with the main parameter confirming good compensation. This outcome is strengthened by our electronic structure calculations and analysis of Shubnikov-de Haas oscillations, revealing Fermi surfaces that consist of two hole pockets and a triplicate electron pocket. The multiband anisotropic model of electronic transport describes very well the experimental results of $\sigma_{xx}(B)$ and $\sigma_{xy}(B)$ for both compounds. Therefore, our experimental results confirmed that prominent magnetotransport properties of YBi and LuBi could be explained without invoking nontrivial topology of electronic bands.

Electronic structure calculations showed that band inversion exists in both compounds, but plausible Dirac points could appear about 0.5 eV below the Fermi level (that is about twice as deep as in LaSb or LaBi [4]). There is also considerable (d - p)-orbital mixing of electron states visible in the same region. How such structures would influence magnetotransport of a semimetal remains an open question.

The mobilities, of both electrons and holes, are considerably larger in YBi than in LuBi (Table III), which is reflected in almost four times smaller residual resistivity of the former compound, and consequently leads to its three times larger magnetoresistance. But the band structure region where important orbital mixing occurs differs very little between YBi and LuBi (cf. Fig. 5). This suggests that (d - p)-orbital mixing is

TABLE III. Parameters obtained from the analysis of magnetic field dependences of electrical conductivity and Hall conductivity with anisotropic multiband model.

Compound	n_{α} (cm ⁻³)	$(m^2 V^{-1} s^{-1})$	n_{eta} (cm ⁻³)	$\mu_{\beta} \ (m^2 V^{-1} s^{-1})$	n_{δ} (cm ⁻³)	$\mu_{\delta} \ ({ m m}^2 { m V}^{-1} { m s}^{-1})$	К	n_e/n_h
YBi LuBi	$\begin{array}{c} 6.88 \times 10^{20} \\ 6.91 \times 10^{20} \end{array}$	6.92 1.91	$\begin{array}{c} 2.37 \times 10^{20} \\ 2.31 \times 10^{20} \end{array}$	1.37 1.85	$\begin{array}{c} 4.81 \times 10^{20} \\ 4.80 \times 10^{20} \end{array}$	4.10 0.65	5.33 5.33	0.95 0.97

not the predominant mechanism in magnetoresistance of these two compounds.

A scenario of mobility mismatch between electron and hole bands, proposed recently to explain reduced *MR* in LaAs [49], does not seem appropriate for LuBi because its mobilities of holes and electrons differ very little, and the Hall coefficient is over two orders of magnitude smaller than in LaAs (for which the large Hall coefficient reflected strong mismatch of mobilities) [49]. In the Supplemental Material, we show also how YBi and LuBi follow $MR \propto RRR^2$ behavior, in common with several other monopnictide samples, in contrast to LaAs [50].

Future research with the ARPES technique would be very helpful in making the final conclusion on the hypothetical presence of topologically nontrivial electronic states in YBi and LuBi.

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