# Magnetism and the phase diagram of  $MnSb<sub>2</sub>O<sub>6</sub>$

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Static and dynamic magnetic properties of  $\overline{P}31m$ -phase MnSb<sub>2</sub>O<sub>6</sub> have been studied by means of muon-spin relaxation (*μ*SR), high-frequency electron-spin resonance (HF-ESR), specific heat, and magnetization studies in magnetic fields up to 25 T. The data imply onset of long-range antiferromagnetic order at  $T_N = 8$  K and a spin-flop-like transition at  $B_{\text{SF}} \approx 0.7$ –1 T. Below  $T_N$ , muon asymmetry exhibits well-defined oscillations indicating a narrow distribution of the local fields. A competing antiferromagnetic phase appearing below  $T_{N2} = 5.3$  K is evidenced by a step in the magnetization and a slight kink of the relaxation rate. Above  $T_N$ , both  $\mu$ SR and HF-ESR data suggest short-range spin order. HF-ESR data show that local magnetic fields persist up to at least  $12T_N \approx 100$  K. Analysis of the antiferromagnetic resonance modes and the thermodynamic spin-flop field suggest zero-field splitting of  $\Delta \approx 18$  GHz which implies small but finite magnetic anisotropy.

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## **I. INTRODUCTION**

Frustrated spin systems provide the access needed to study the emergence of novel ground states and unusual excitations. Triangular Heisenberg antiferromagnets are generic for frustrated magnetism and may possess rich magnetic phase diagrams and unusual ground states  $[1-3]$ . Even in the classical case, i.e., for large spin values, the ground state exhibits a hidden symmetry and unusual excitations [\[4\]](#page-6-0). While the tendency toward static magnetic order increases upon partial lifting of frustration, competing interactions still yield unusual ground states and short-range spin fluctuations evolve far above  $T_N$ . A further ingredient determining the ground states in addition to the spin size and the degree of geometrical frustration is magnetic anisotropy as frustration is more severe when spin alignment is restricted [\[1,5\]](#page-6-0).

The honeycomb structure in  $MnAs<sub>2</sub>O<sub>6</sub>$  with  $P\overline{3}1m$  structure exhibits a trigonal arrangement of  $Mn^{2+}$  ions and is an example of a frustrated spin system as it exhibits a network of  $S = 5/2$ triangles with competing antiferromagnetic exchange interactions [\[6\]](#page-6-0). Indeed, the layered and frustrated magnetic structure gives rise to an incommensurate spin order below 12 K [\[7\]](#page-6-0). The recently synthesized P31 $m$  phase of MnSb<sub>2</sub>O<sub>6</sub> is isostructural

and isoelectronic to  $MnAs<sub>2</sub>O<sub>6</sub>$  [\[8\]](#page-6-0). Note that this phase differs from the trigonal, structurally and magnetically chiral polymorph of  $MnSb<sub>2</sub>O<sub>6</sub>$  [\[9–11\]](#page-6-0). Density functional theory (DFT) calculations on the  $P31m$  phase suggest that the exchange in-

## **II. EXPERIMENTAL**

Layered trigonal ( $P\bar{3}1m$ ) MnSb<sub>2</sub>O<sub>6</sub> was prepared by ion exchange reaction as reported elsewhere [\[8\]](#page-6-0). Static magnetization was studied in static magnetic fields up to 15 T by means of a home-built vibrating sample magnetometer [\[12\]](#page-6-0) (VSM)

teractions are very similar to those of its counterpart  $MnAs<sub>2</sub>O<sub>6</sub>$ and that the long-range antiferromagnetically ordered ground state appearing below  $\sim$ 8 K is of incommensurate nature [\[6\]](#page-6-0). In addition, weak ferromagnetism was suggested from static susceptibility data to be present below  $T = 41$  K. Here, we report the magnetic phase diagram and a detailed study of the magnetic properties of  $MnSb<sub>2</sub>O<sub>6</sub>$  by means of zero-field muonspin resonance  $(\mu$ SR), high-frequency electron-spin resonance (HF-ESR), and static magnetization measurements. Our data imply long-range antiferromagnetic order of most presumingly commensurate nature. In addition, there is thermodynamic evidence for a competing AFM phase below  $T_{N2} = 5.3$  K. While weak ferromagnetism is ruled out by our experiments, there is clear evidence for short-range magnetic order well above  $T_N$ , i.e., up to about 100 K, which corresponds to the frustrated nature of magnetism in the  $P\overline{3}1m$  polymorph of MnSb<sub>2</sub>O<sub>6</sub>. Observed zero-field splitting of  $\Delta \approx 18$  GHz implies small but finite magnetic anisotropy.

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FIG. 1. Static magnetic susceptibility  $\chi = M/B$  of MnSb<sub>2</sub>O<sub>6</sub> at low temperatures and at various magnetic fields  $B \leq 1$  T. The inset displays  $\chi$  and its derivative  $\partial \chi / \partial T$ , at  $B = 0.5$  T, in order to highlight the anomaly at  $T_{N2}$ . The dashed lines and the double arrow indicate the jump size of the associated anomaly.

and in fields up to 5 T in a Quantum Design MPMS-XL5 SQUID magnetometer. Pulsed field studies up to 25 T were done in a home-built device utilizing magnetic pulses of about 8 ms. Specific heat has been measured in magnetic fields up to 7 T by means of a relaxation method in a Quantum Design PPMS. Transmission HF-ESR measurements were carried out using a phase-sensitive millimeter-wave vector network analyzer (MVNA) from AB Millimetré [\[13\]](#page-6-0). Experiments on a  $MnSb<sub>2</sub>O<sub>6</sub>$  powder sample which was fixed with eicosane were performed in the frequency range from 30 to 350 GHz in a 16 T superconducting magnet from Oxford instruments.  $ZF-\mu SR$  experiments were performed at the Paul Scherrer Institute using the DOLLY instrument with a  $He<sup>4</sup>$ -flow cryostat in the temperature range from 2 to 250 K on a pressed powder sample ( $m \sim 100$  mg). A veto-logic was used to detect only the decay positrons from muons stopped in the sample. The *μ*SR data were analyzed with the software package MUSRFIT [\[14\]](#page-6-0).

#### **III. STATIC MAGNETIZATION AND SPECIFIC HEAT**

The static magnetic susceptibility  $\chi = M/B$  at low temperatures shown in Fig. 1 illustrates the evolution of magnetic order in MnSb<sub>2</sub>O<sub>6</sub>. While there is a broad maximum in  $\chi$  vs *T* centered around  $T = 9$  K, we infer  $T_N = 8.0(4)$  K from the maximum in  $\partial(\chi T)/\partial T$ . The negative Weiss temperature  $\Theta = -20(5)$  K derived from a Curie-Weiss approximation to the high-temperature data (not shown) implies a moderate frustration parameter, i.e.,  $f = |\Theta|/T_N \approx 2.6$ .

While application of magnetic fields up to  $B = 1$  T does not significantly affect the onset of magnetic order at  $T_N$ , there are two notable features: (1) There is a general strong increase of the low-temperature susceptibility as a function of magnetic field. As will be discussed in detail below, this is associated with the spin-flop transition. (2) There is an additional anomaly, i.e., a step-like increase of the susceptibility



FIG. 2. Magnetization *M* and magnetic susceptibility *∂M/∂B* vs magnetic field at (a)  $T = 2$  K and (b) various temperatures up to 9 K. The inset in (a) enlarges the field range where the spin-flop occurs. The vertical dashed line indicates  $B_{\rm SF}$  and the straight line in the inset linearly extrapolates  $M$  to  $B = 0$  T.

below  $T_N$  at finite magnetic fields. The associated increase in the static magnetization is illustrated in the inset of Fig. 1. For example, at  $B = 0.5$  T, there is a increase in the magnetization of  $\Delta M_{\text{N2}} = 6.1(2) \times 10^{-3} \mu_{\text{B}}/\text{Mn}$  at  $T_{\text{N2}} = 5.5(2) \text{ K. As}$ the applied magnetic field increases, the step-like anomaly emerges and correspondingly shifts to higher temperatures.

The field dependence of the magnetization shown in Fig. 2 displays additional features. At  $T < T<sub>N</sub>$ , there is a small feature in *M*(*B*) which is associated with a pronounced maximum in the magnetic susceptibility. This anomaly is attributed to the spin-flop transition. At 2 K, the spin-flop transition appears at  $B_{\rm SF} = 0.72$  T and there is a small magnetic field hysteresis of about 0.1 T. The corresponding jump in the magnetization data amounts to  $\Delta M_{\rm SF} \approx 0.04 \mu_{\rm B} / \text{Mn}$ . Upon heating, the anomaly at  $B_{\rm SF}$  is suppressed and finally vanishes above  $T_{\rm N}$ [see Fig. 2(b)]. This scenario of spin reorientation is supported by the static susceptibility data in Fig. 1 where magnetic anisotropy is evidently overcome by a magnetic field of less than 1 T. The high-field behavior shown in Fig. [3](#page-2-0) displays a linear field dependence of the magnetization saturating at  $B_{\text{sat}}(T = 2.4 \text{ K}) = 17.9 \pm 0.1 \text{ T}$ . The saturation magnetization amounts to  $4.9 \pm 0.2 \mu_B/Mn$  which agrees with the expected high-spin value of  $Mn^{2+}$  ions.

The effects of magnetic fields on the long-range antiferromagnetically ordered phase as well as the associated magnetic entropy changes are demonstrated by the specific heat data in Fig. [4.](#page-2-0) At  $T_N$ ,  $c_p$  displays a rounded peak-like anomaly which we interpret to be a remnant from a *λ*-shaped one. In general, the actual transition temperature might be

<span id="page-2-0"></span>

FIG. 3. Pulsed field magnetization obtained at *T* = 2*.*4 K and  $T = 4.2$  K. Arrows indicate the saturation fields.

alternatively associated with the midpoint of the specific heat jump at ∼8*.*6K[\[15\]](#page-6-0). While all our conclusions do not change with either assignment of  $T_N$ , the  $\mu$ SR data presented in Fig. 5 are compatible with  $T_N \approx 8.0$  K. Upon application of magnetic fields, the anomaly is shifted to lower temperatures. To estimate the magnetic entropy changes, the specific heat of the isostructural nonmagnetic analog,  $\text{ZnSb}_2\text{O}_6$ , was subtracted from the data  $[15]$ . Integrating the resulting magnetic specific heat  $c_p^{\text{magn}}/T$  yields the magnetic entropy changes displayed in Fig. 4. At  $T_N$ , about  $2/3$  of the total magnetic entropy  $R \ln(2S + 1)$  is found to be released.

In contrast to the clear anomaly at  $T_N$ , at  $T_{N2}$  there is no clear feature in the specific heat data. The measured field dependence  $T_{N2}(B)$  enables assessing the associated entropy or specific heat changes from the slope of the phase boundary. This procedure requires knowledge of the nature of the phase transition. Interpreting the magnetization anomaly as a step  $\Delta M$  and exploiting a Clausius-Clapeyron relation, i.e., assuming a (very weak) first-order character yields associated entropy changes  $\Delta S_{N2} = -\Delta M_{N2}(dT_{N2}/dB)^{-1}$  =



FIG. 4. Specific heat of  $MnSb<sub>2</sub>O<sub>6</sub>$  at low temperatures and at various magnetic fields and of  $ZnSb<sub>2</sub>O<sub>6</sub>$ . Arrows indicate  $T<sub>N</sub>(B)$ . Inset: Magnetic entropy changes (see text).



FIG. 5. ZF- $\mu$ SR spectra of MnSb<sub>2</sub>O<sub>6</sub> at (a) representative temperatures  $\geq T_N$  and (b) early decay times below the magnetic ordering temperature  $T_N$ . The symbols and the lines represent the experimental data and the corresponding model description (for details see the main text), respectively. For clarity, the spectrum at  $T = 7.5$  K in (b) is vertically shifted by 0.25, while no offset is applied to the spectra in (a).

70(10) mJ*/*(mol K). For a continuous transition where the anomaly is analyzed as a step in *∂M/∂T* , the analysis yields  $\Delta c_p = -T_{N2} \Delta (\partial M / \partial T) (dT_{N2} / dB)^{-1} \approx 0.2 \text{ J/(mol K)}$  [\[16\]](#page-6-0). In both cases, the anomaly would be smeared out over ∼1*.*5 K and cannot be resolved by the calorimetric measurements presented. In this respect we mention the ambiguous behavior  $c_p(T)$  at low temperatures. The data suggest an approximately linear behavior  $c_p$  vs  $T$  at around  $5$  K whose exact origin is unclear. Considering the right-bending of  $c_p$  vs  $T$  below 3.5 K, the data are reminiscent of the presence of a hump in the temperature dependence of the specific heat in triangular spin systems such as  $AMn_5(SO_4)_6$  ( $A = Pb$ , Sr) and Li<sub>4</sub>FeSbO<sub>6</sub> which may be associated with the frustrated nature of the spin system [\[17,18\]](#page-6-0). Although less pronounced than in these systems, such a hump in  $MnSb<sub>2</sub>O<sub>6</sub>$  might overlay a possible  $T<sup>n</sup>$  behavior with  $n > 1$  and it prevents clear conclusions about the nature of low-energy magnetic excitations from the specific heat data.

## **IV. ZERO-FIELD MUON-SPIN RELAXATION**

In order to probe the local magnetic fields of the corresponding magnetic phase via the  $\mu^+$  spin precession frequency and relaxation rate, we have performed  $ZF-\mu$ <sup>+</sup>SR spectroscopy [\[19\]](#page-6-0). The ZF- $\mu$ <sup>+</sup>SR asymmetry spectra in Fig. 5 confirm longrange magnetic order at low temperatures. Depending on the temperature, the spectra show two different types of behavior. At  $T \geqslant 9$  K, the data exhibit only slow decay of the asymmetry signal [Fig.  $5(a)$ ]. This is attributed to dipole-dipole interaction between the muon spin and the nuclear and electronic spins in  ${\rm MnSb_2O_6}.$  In the whole temperature range  $9 \leqslant T \leqslant 270$  K (not all spectra are shown), the asymmetries are essentially identical for the first few 100 ns. In contrast, the spectra tails at  $\mu$ s time scales slightly increase upon heating from 9 to 20 K. As will



FIG. 6. Temperature dependence of (a) muon-spin relaxation time, (b) the order parameter, i.e., the oscillation frequency *f*, and (c) relaxation time of the oscillation divided by the frequency,  $\lambda_{\rm T}/f$ . (d) Temperature dependence of the order parameter on a double-logarithmic scale. The vertical (dashed) lines show  $T_{N2}$  ( $T_N$ ) derived from Fig. [1.](#page-1-0) The dashed lines in (b) and (d) represent a phenomenological fit to the experimental data at  $T_{\rm N2} \leqslant T \leqslant T_{\rm N}$  (see text). The dotted line in (d) is an extrapolated guide line for the data at  $T < T_{N2}$ .

be discussed below, these changes of the long-time relaxation may be associated with short-range spin order. Whereas, there are no changes upon further temperature increase from 20 up to 270 K.

Adopting that muon-spin relaxation is dominantly due to the dynamics of electronic moments, a general exponential function  $A(t) \propto \exp(-(\lambda t)^{\beta'}$  was used to describe the  $\mu$ SR spectra above  $T_N$ . Here,  $\lambda = 1/T_1$  is the generalized muon-spin relaxation rate. The exponent  $\beta'$  is a measure of the homogeneity of the system. The data imply only small variation of  $\beta' = 1.15$ (5) in the temperature range  $9 \le T \le 270$  K which suggests a homogeneous system. The obtained *λ* values [see Fig. 6(a)] are rather temperature independent in the temperature range from 9 up to 270 K. In particular, there is no indication of local fields associated with weak ferromagnetism below 41 K. Thus, the  $\mu$ SR data prove the absence of weak ferromagnetism in bulk  $MnSb<sub>2</sub>O<sub>6</sub>$  in contrast to the results in Ref. [\[8\]](#page-6-0).

Upon cooling below  $T_N$ , there is a clear change in the  $ZF-\mu$ <sup>+</sup>SR asymmetry spectra. Above all, the asymmetry signal on the  $\mu$ s time scale is significantly suppressed. This becomes evident when comparing the  $\mu$ SR spectra at 8 and 9 K which are displayed in Fig.  $5(a)$  without any offset on the spectra. The asymmetry at the two temperatures is quite different in the whole time scale under study. This difference implies the presence of a fast relaxation process at  $T = 8$  K, implying the presence of quasistatic internal fields. The presence of long-range spin order is indeed clearly confirmed by a reasonably well-defined damped oscillation behavior at  $T \leq 7.5$  K [Fig.  $5(b)$ ]. Upon further cooling, the damping decreases and the oscillations become more and more pronounced. The decay and the oscillation of the muon polarization imply the evolution of local static magnetic moments in the experimental time window. In the case of a single muon site, the muon ensemble precesses about the mean local magnetic field with the Larmor frequency  $2\pi f_\mu = \gamma_\mu |\mathbf{B}_{loc}|$ , where  $\gamma_\mu \sim 851.4 \text{ MHz/T}$  is the gyromagnetic ratio of the muon.

As displayed in Fig.  $5(b)$ , the damped oscillations in the  $\mu$ SR spectra below  $T_N$  are well described by means of the internal field function

$$
A(t) = \alpha \cos(2\pi ft + \varphi) \exp(-\lambda_{\rm T}t) + (1 - \alpha) \exp(-\lambda_{\rm L}t),
$$
\n(1)

where  $\alpha$  is the ratio of the oscillating term to the nonoscillating term, which is close to 2*/*3 due to the statistic average of the perpendicular orientation of the polycrystal to the direction of polarized muons. *f* is the Larmor frequency related to the averaged local magnetic field at the muon site, and  $\varphi$  is the phase term.  $\lambda_T$  and  $\lambda_L$  are the muon relaxation rates reflecting the static and dynamic effects. From the frequency at  $T = 2$  K, i.e.,  $f(T = 2 K) = 57.7 \text{ MHz}$ , the local magnetic field at the muon site is estimated as  $B_{\text{loc}} = 0.43$  T.

The oscillations are reasonably well defined and hence allow extracting the temperature-dependent antiferromagnetic order parameter by means of fitting of the *μ*SR spectra in the oscillating regime. The order parameter is presented in Figs.  $6(b)$  and  $6(d)$ . It shows the typical development of internal fields associated with long-range magnetic order. In a phenomenological description, the data may be described by

$$
f(t) = f_0 (1 - T/T_N)^{\beta}.
$$
 (2)

The best fitting parameters describing the data at  $T_{\text{N2}} \leqslant T \leqslant T$  $T_N$  are  $\beta = 0.28 \pm 0.02$ ,  $f_0 = 60$  MHz, and  $T_N = 8$  K. At  $T_{N2}$ , there is a slight change in the temperature dependence of *f* which might be associated with  $T_{N2}$  [see Fig. 6(d)].

The transversal relaxation rate divided by the oscillation frequency stays rather constant between 8 and 6 K but clearly decreases for  $T \leq 5$  K [Fig. 6(b)]. This change of behavior coincides with the step-like anomaly observed in the static susceptibility measurements at  $T_{N2}$  and the change in the temperature dependence  $f(T)$ . We note, however, the large error bars of  $\lambda_T$  between  $T_N$  and 6 K. In contrast, the muon relaxation rate  $\lambda_L$  shows no clear feature at  $T_{N2}$  but increases as the transition temperature  $T_N$  is approached from below.

# **V. HIGH-FREQUENCY ELECTRON-SPIN RESONANCE**

Further information on the magnetism in  $MnSb<sub>2</sub>O<sub>6</sub>$  is obtained from HF-ESR measurements. Figure [7](#page-4-0) shows selected spectra and the observed resonance fields, taken well in the long-range ordered phase at  $T = 4$  K, in a frequencymagnetic-field plot. At high frequencies, typical transmission powder spectra with two features are observed. The more pronounced minimum feature appears at the lower magnetic

<span id="page-4-0"></span>

FIG. 7. HF-ESR absorption frequencies vs magnetic field at  $T =$ 4 K, together with representative spectra obtained at 50, 141, 230, and 259 GHz. The inset shows how the resonance features  $\omega_1$  (black circles) and  $\omega_2$  (red squares) were obtained by fitting the resonance by means of a powder spectrum. The diamond represents the resonance field observed in previous X-band ESR measurements in Ref. [\[8\]](#page-6-0).

field which is indicative of an easy-plane-type anisotropy [\[20\]](#page-6-0). Fitting the resonance features by means of powder spectra yields the respective resonance fields  $\omega_1$  and  $\omega_2$  shown in Fig. 7 which can be attributed to the magnetic fields directed parallel and perpendicular to the easy plane, respectively. At low frequencies, due to the small difference of the resonance fields, we only observe single resonance features.

The observed resonance branches in the frequency vs field diagram can be described by means of the antiferromagnetic resonance (AFMR) model with two sublattices in consideration of an easy-plane-type anisotropy field [\[21\]](#page-6-0). In this model, there are two AFMR resonance modes  $\omega_1$  and  $\omega_2$  associated with magnetic fields directed either perpendicular or parallel to the easy plane. Due to the fixation of the powder sample, we expect to observe both modes. The AFMR modes are described as the following:

$$
\omega_1/\gamma = \left(B_1^2 + B_{\text{EA}}^2\right)^{1/2},\tag{3}
$$

$$
\omega_2/\gamma = B_2. \tag{4}
$$

 $\gamma$  is the gyromagnetic ratio. The modified magnetic fields  $B_i =$  $g_i B/2$  ( $i = 1, 2$ ) account for the anisotropy of the *g* factor. The exchange field  $B<sub>E</sub>$  and the anisotropy field  $B<sub>A</sub>$  are combined as  $B_{\text{EA}} = \sqrt{2B_{\text{E}}B_{\text{A}}}$ . The best fit to the data yields the branches  $ω_1$  and  $ω_2$  shown in Fig. 7. The best fitting parameters are  $g_1 =$  $1.97 \pm 0.01$ ,  $g_2 = 2.01 \pm 0.01$ , and  $B_{EA} = 0.59 \pm 0.01$  T.

While the gapless branch  $\omega_2$  fully agrees with the resonance feature from a previous X-band ESR study [\[8\]](#page-6-0), our analysis suggests the presence of small but finite zero-field splitting (ZFS) of  $\omega_1(B = 0 \text{ T}) = 18 \text{ GHz}$ . Since no experimental data have been obtained below 30 GHz in this study due to the limitations of the experimental devices, such a small ZFS cannot be unambiguously derived from the ESR data alone. The absence of any additional resonance at low frequencies down to 30 GHz, however, implies that the ZFS is smaller



FIG. 8. (a) HF-ESR spectra at  $f = 320.2$  GHz at different temperatures between 2 and 175 K. The vertical dashed line represents  $g = 2$ . The data are vertically shifted for clarity. (b) Temperature dependence of the effective *g* factors associated with  $\omega_1$  and  $\omega_2$ . The inset enlarges the low-temperature region with  $T \le T_N$  (11 T) highlighted in grey.

than 30 GHz. Note that our data are not consistent with both  $ω_1$  and  $ω_2$  being gapless because in that case line splitting at 100 GHz would be large enough to be well resolved. In addition, the extracted anisotropy gap perfectly agrees with the thermodynamic spin-flop field. At  $T = 2$  K, the magnetization curve demonstrates  $B_{\rm SF} = 0.72$  T, which corresponds to the anisotropy gap  $\Delta(T = 0 \text{ K}) = g\mu_B B_{\text{SF}} \approx 20 \text{ GHz}$ . This value agrees with the best fit to the HF-ESR branches.

Figure 8 shows the temperature dependence of the two resonance features at  $f = 320.2$  GHz from 2 to 175 K. At high temperatures, the resonance is well described by a single Lorentzian with  $g \sim 1.99$ . Upon cooling, at temperatures not less than 100 K the resonance starts to broaden and shift. The two resonance features can be clearly separated at  $T \leqslant 80$  K and can be fitted with two Lorentzians. This clearly indicates the presence of local magnetic fields implying that short-range spin correlations remain well above the Neel temperatures up to at least  $12T_N$ . As seen by the temperature dependence of the effective *g* factors in Fig. 8(b), local magnetic fields continuously evolve upon cooling and eventually the typical splitting of the resonance features attributed to AFMR modes in the ordered phase is observed. Note that no particular effects appear upon crossing the actual long-range ordering temperature  $T_N$  which, at the resonance field of about 11 T, amounts to ∼6*.*5 K.

### **VI. DISCUSSION**

The  $ZF-\mu+SR$  data confirm the evolution of quasistatic internal magnetic fields, i.e., of long-range AFM order in  $MnSb<sub>2</sub>O<sub>6</sub>$  below  $T<sub>N</sub> = 8.0(4)$  K. Together with the static magnetization and specific heat data this enables constructing the magnetic phase diagram of  $MnSb<sub>2</sub>O<sub>6</sub>$  (see Fig. [9\)](#page-5-0). Note that our data clearly exclude the presence of a potential

<span id="page-5-0"></span>

FIG. 9. Magnetic phase diagram of  $MnSb<sub>2</sub>O<sub>6</sub>$  as derived from  $c<sub>p</sub>$ (open squares), *M* vs *B* and *T* (filled circles).  $T_N$ ,  $T_{N2}$ , and  $B_{SF}$  indicate the onset of long-range antiferromagnetic order, the transition AFM I to AFM II, and the spin-flop transition. The inset shows the phase diagram up to high magnetic fields. All lines are guides to the eye.

weakly ferromagnetic phase below 41 K. The phase boundary  $T_N(B)$  between the long-range antiferromagnetic ordered phase AFM I and the paramagnetic one shows the expected negative slope.

In contrast to DFT predictions [\[8\]](#page-6-0) and different from the isostructural compound  $MnAs<sub>2</sub>O<sub>6</sub>$  [\[6\]](#page-6-0), magnetic order is of commensurate nature as evidenced by well-defined oscillations of the  $\mu$ SR asymmetry spectra. In both materials, DFT+U suggests triangular magnetic substructures in which spin exchange interactions  $J_1$ ,  $J_2$ , and  $J_3$  are weak and comparable in magnitude [\[6,8\]](#page-6-0). Koo and Whangbo point out that in  $MnAs<sub>2</sub>O<sub>6</sub>$ , spin exchange interactions are not the deciding factors favoring the incommensurate spin structure over a commensurate one but suggest dipole-dipole interactions being crucial [\[6\]](#page-6-0). The fact that our data imply that commensurate spin order in the isostructural compound  $MnSb<sub>2</sub>O<sub>6</sub>$  where  $J_1$ ,  $J_2$ , and  $J_3$ from DFT+U is very similar as in  $MnAs<sub>2</sub>O<sub>6</sub>$  confirms that even small effects may decide the actual spin ground state. We conclude that the observed effective anisotropy of 18 GHz should be considered in this respect. In addition, our analysis of the ESR and magnetization data suggests that the spin structure in the SF phase involves not more than two magnetic sublattices. AFMR models with three or more sublattices would imply an additional ZFS of the  $\omega_2$  mode and/or a different intensity distribution of the AFMR spectra.

Analyzing the antiferromagnetic order parameter in terms of a phenomenological model yields the critical exponent  $\beta =$  $0.28 \pm 0.02$ . This value is in between the values for the twodimensional (2D) XY ( $\beta$  = 0.23) and the three-dimensional (3D) Heisenberg ( $\beta$  = 0.36) antiferromagnet which suggests that magnetic order in  $MnSb_2O_6$  is not of a simple two- or threedimensional antiferromagnetic Heisenberg type. This agrees with DFT calculations which yield intralayer interactions which are stronger than the (however finite) interlayer ones and would form 2D AFM networks if the interlayer coupling

was negligible [\[8\]](#page-6-0). Hence, neither would one expect perfect 2D or 3D magnetism in agreement with the observed critical behavior. In contrast to the order parameter extracted from the  $\mu$ SR data, splitting of the HF-ESR line does not reflect a clear change at  $T_N$ . If at all, line broadening and splitting which, in the paramagnetic phase, signals the presence of short-range correlations, stay somehow constant at  $T_N$ . This agrees with the fact that, at  $f = 320$  GHz, the resonance branches are well in the linear regime [\[11\]](#page-6-0).

At small magnetic fields, the phase diagram demonstrates two antiferromagnetic phases (AFM I and AFM II). Our observation of the yet unknown AFM II phase illustrates the presence of two competing antiferromagnetic phases. Thermodynamically, the presence of the phase boundary  $T_{N2}$  is unambiguously derived from the associated jump in the magnetization. In the dynamic response, the AFM II phase may be associated with a kink in the temperature dependence of the transverse relaxation rate. However, no significant anomaly in the order parameter is observed at  $T_{N2}$ . In agreement with  $\Delta M_{N2}$  being positive, the slope of  $T_{N2}(B)$  is positive, too. The spin-flop transition appears in both AFM I and AFM II at around 1 T. The nearly vanishing temperature dependence of  $B_{\rm SF}$  implies negligible entropy changes at the spin-flop transition as compared to the magnetization anomaly. In the spin-flop phase, we do not find evidence for a phase boundary  $T_{N2}(B)$  [\[22\]](#page-6-0).

Magnetic anisotropy appears to be relevant in this high-spin  $Mn^{2+}$  system. The HF-ESR data imply a small but finite planar anisotropy showing up in the zero-field splitting of the associated AFMR mode of approximately 20 GHz. The resulting exchange-anisotropy field which is obtained by analyzing the resonances by means of an easy-plane two-sublattice model yields  $B_{EA} = 0.59 \pm 0.01$  T. Exploiting the saturation field  $B_{\text{sat}} = 2B_E \approx 18$  T allows estimating the planar anisotropy field  $B_A = 0.02 \pm 0.01$  T which is the same as in trigonal P321-MnSb<sub>2</sub>O<sub>6</sub> and similar to CaMnCl<sub>3</sub> · H<sub>2</sub>O [\[23,24\]](#page-6-0). The thermodynamic spin-flop field quantitatively provides the same anisotropy gap as derived from the analysis of the AFMR data. Interestingly, the spin-flop phase seems not to exhibit two AFM states. This enables speculating about the relevance of anisotropy for stabilizing the actual antiferromagnetic ground state. In the region of the phase diagram where the magnetic field overcomes the anisotropy energy and yields a spin-rotated situation, one of the  $B = 0$  spin configurations is destabilized, i.e., it only appears if anisotropy is dominant compared to the external field. We conclude that the magnetic field abrogates the energy difference between AFM I and AFM II and that magnetic anisotropy is crucial for selecting the actual magnetic state from two AFM phases of very similar energy. This conclusion is in line with numerical results which suggest that very small effects are decisive for stabilizing the incommensurate spin structure over a commensurate one in  $MnAs<sub>2</sub>O<sub>6</sub>$  [\[6\]](#page-6-0).

### **VII. SUMMARY**

 $MnSb<sub>2</sub>O<sub>6</sub>$  is a spin frustrated system whose magnetic structure exhibits antiferromagnetically frustrated triangles [\[8\]](#page-6-0). Although analysis of static magnetization data in terms of a Curie-Weiss model only yields a moderate ratio  $\Theta/T_N \approx$ 2*.*6, the presence of local magnetic fields, viz. antiferromagnetic spin fluctuations, is clearly confirmed by shifting and broadening of the resonance HF-ESR resonance lines. The <span id="page-6-0"></span>increase of the  $\mu$ SR spectra tail in the long time scale further confirms the presence of short-range magnetic correlations above  $T_N$ . HF-ESR data show that local magnetic fields persist up to at least  $12T_N$ . Such a wide temperature range of antiferromagnetic fluctuations agrees with the triangular arrangement of  $Mn^{2+}$  ions and the corresponding frustrated magnetism in  $MnSb<sub>2</sub>O<sub>6</sub>$ . Below  $T<sub>N</sub>$ , muon asymmetry exhibits well-defined oscillations indicating a narrow distribution of the local fields which strongly suggests the commensurate nature of spin order. The antiferromagnetic order parameter implies a behavior in between what is expected for the 2D XY and the 3D Heisenberg models. A competing antiferromagnetic phase appearing below  $T_{N2} = 5.3$  K is evidenced by a step in the magnetization and a slight kink of the relaxation rate. We conclude that small but finite anisotropy of  $\Delta \approx 18$  GHz derived is crucial for selecting the actual magnetic ground state from two AFM phases of very similar energy.

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- [1] M. F. Collins and O. A. Petrenko, [Can. J. Phys.](https://doi.org/10.1139/p97-007) **[75](https://doi.org/10.1139/p97-007)**, [605](https://doi.org/10.1139/p97-007) [\(1997\)](https://doi.org/10.1139/p97-007).
- [2] S. Nakatsuji, Y. Nambu, H. Tonomura, O. Sakai, S. Jonas, C. Broholm, H. Tsunetsugu, Y. Qiu, and Y. Maeno, [Science](https://doi.org/10.1126/science.1114727) **[309](https://doi.org/10.1126/science.1114727)**, [697](https://doi.org/10.1126/science.1114727) [\(2005\)](https://doi.org/10.1126/science.1114727).
- [3] O. A. Starykh, [Rep. Prog. Phys.](https://doi.org/10.1088/0034-4885/78/5/052502) **[78](https://doi.org/10.1088/0034-4885/78/5/052502)**, [052502](https://doi.org/10.1088/0034-4885/78/5/052502) [\(2015\)](https://doi.org/10.1088/0034-4885/78/5/052502).
- [4] [L. Seabra, T. Momoi, P. Sindzingre, and N. Shannon,](https://doi.org/10.1103/PhysRevB.84.214418) Phys. Rev. B **[84](https://doi.org/10.1103/PhysRevB.84.214418)**, [214418](https://doi.org/10.1103/PhysRevB.84.214418) [\(2011\)](https://doi.org/10.1103/PhysRevB.84.214418).
- [5] M. Yun and G. S. Jeon, [J. Phys.: Conf. Ser.](https://doi.org/10.1088/1742-6596/592/1/012111) **[592](https://doi.org/10.1088/1742-6596/592/1/012111)**, [012111](https://doi.org/10.1088/1742-6596/592/1/012111) [\(2015\)](https://doi.org/10.1088/1742-6596/592/1/012111).
- [6] H.-J. Koo and M.-H. Whangbo, [Inorg. Chem.](https://doi.org/10.1021/ic500156e) **[53](https://doi.org/10.1021/ic500156e)**, [3812](https://doi.org/10.1021/ic500156e) [\(2014\)](https://doi.org/10.1021/ic500156e).
- [7] A. M. Nakua and J. E. Greedan, [J. Solid State Chem.](https://doi.org/10.1006/jssc.1995.1361) **[118](https://doi.org/10.1006/jssc.1995.1361)**, [402](https://doi.org/10.1006/jssc.1995.1361) [\(1995\)](https://doi.org/10.1006/jssc.1995.1361).
- [8] V. B. Nalbandyan, E. A. Zvereva, A. Y. Nikulin, I. L. Shukaev, M. H. Whangbo, H. J. Koo, M. Abdel-Hafiez, X. J. Chen, C. Koo, A. N. Vasiliev, and R. Klingeler, [Inorg. Chem.](https://doi.org/10.1021/ic502666c) **[54](https://doi.org/10.1021/ic502666c)**, [1705](https://doi.org/10.1021/ic502666c) [\(2015\)](https://doi.org/10.1021/ic502666c).
- [9] [J. N. Reimers, J. E. Greedan, and M. A. Subramanian,](https://doi.org/10.1016/0022-4596(89)90273-9) J. Solid State Chem. **[79](https://doi.org/10.1016/0022-4596(89)90273-9)**, [263](https://doi.org/10.1016/0022-4596(89)90273-9) [\(1989\)](https://doi.org/10.1016/0022-4596(89)90273-9).
- [10] R. D. Johnson, K. Cao, L. C. Chapon, F. Fabrizi, N. Perks, P. Manuel, J. J. Yang, Y. S. Oh, S. W. Cheong, and P. G. Radaelli, [Phys. Rev. Lett.](https://doi.org/10.1103/PhysRevLett.111.017202) **[111](https://doi.org/10.1103/PhysRevLett.111.017202)**, [017202](https://doi.org/10.1103/PhysRevLett.111.017202) [\(2013\)](https://doi.org/10.1103/PhysRevLett.111.017202).
- [11] J. Werner, W. Hergett, M. Gertig, J. Park, C. Koo, and R. Klingeler, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.95.214414) **[95](https://doi.org/10.1103/PhysRevB.95.214414)**, [214414](https://doi.org/10.1103/PhysRevB.95.214414) [\(2017\)](https://doi.org/10.1103/PhysRevB.95.214414).
- [12] R. Klingeler, B. Büchner, K.-Y. Choi, V. Kataev, U. Ammerahl, A. Revcolevschi, and J. Schnack, [Phys. Rev. B](https://doi.org/10.1103/PhysRevB.73.014426) **[73](https://doi.org/10.1103/PhysRevB.73.014426)**, [014426](https://doi.org/10.1103/PhysRevB.73.014426) [\(2006\)](https://doi.org/10.1103/PhysRevB.73.014426).
- [13] P. Comba, M. Großhauser, R. Klingeler, C. Koo, Y. Lan, D. [Müller, J. Park, A. Powell, M. J. Riley, and H. Wadepohl,](https://doi.org/10.1021/acs.inorgchem.5b01673) Inorg. Chem. **[54](https://doi.org/10.1021/acs.inorgchem.5b01673)**, [11247](https://doi.org/10.1021/acs.inorgchem.5b01673) [\(2015\)](https://doi.org/10.1021/acs.inorgchem.5b01673).
- [14] A. Suter and B. Wojek, [Phys. Procedia](https://doi.org/10.1016/j.phpro.2012.04.042) **[30](https://doi.org/10.1016/j.phpro.2012.04.042)**, [69](https://doi.org/10.1016/j.phpro.2012.04.042) [\(2012\)](https://doi.org/10.1016/j.phpro.2012.04.042).
- [15] Different atomic masses have been accounted for by considering a factor of 1.03. See A. Tari, *The Specific Heat of Matter at Low Temperatures* (World Scientific, Singapore, 2003).
- [16] [R. Klingeler, B. Büchner, S.-W. Cheong, and M. Hücker,](https://doi.org/10.1103/PhysRevB.72.104424) *Phys.* Rev. B **[72](https://doi.org/10.1103/PhysRevB.72.104424)**, [104424](https://doi.org/10.1103/PhysRevB.72.104424) [\(2005\)](https://doi.org/10.1103/PhysRevB.72.104424).
- [17] D. V. West, T. M. McQueen, I. D. Posen, X. Ke, Q. Huang, H. W. Zandbergen, A. J. Williams, P. Schiffer, and R. J. Cava, [J. Solid State Chem.](https://doi.org/10.1016/j.jssc.2009.03.001) **[182](https://doi.org/10.1016/j.jssc.2009.03.001)**, [1343](https://doi.org/10.1016/j.jssc.2009.03.001) [\(2009\)](https://doi.org/10.1016/j.jssc.2009.03.001).
- [18] E. A. Zvereva, O. A. Savelieva, Ya. D. Titov, M. A. Evstigneeva, V. B. Nalbandyan, C. N. Kao, J.-Y. Lin, I. A. Presniakov, A. V. Sobolev, S. A. Ibragimov, M. Abdel-Hafiez, Y. Krupskaya, C. Jähne, G. Tan, R. Klingeler, B. Büchner, and A. N. Vasiliev, [Dalton Trans.](https://doi.org/10.1039/C2DT31938A) **[42](https://doi.org/10.1039/C2DT31938A)**, [1550](https://doi.org/10.1039/C2DT31938A) [\(2013\)](https://doi.org/10.1039/C2DT31938A).
- [19] See, e.g., A. Schenck, *Muon Spin Rotation Spectroscopy* (Hilger, London, 1985).
- [20] C. Koo, E. A. Zvereva, I. L. Shukaev, M. Richter, M. I. Stratan, A. N. Vasiliev, V. B. Nalbandyan, and R. Klingeler, J. Phys. Soc. Jpn. **[85](https://doi.org/10.7566/JPSJ.85.084702)**, [084702](https://doi.org/10.7566/JPSJ.85.084702) [\(2016\)](https://doi.org/10.7566/JPSJ.85.084702).
- [21] E. A. Turov, *Physical Properties of Magnetically Ordered Crystals* (Academic, New York, 1965).
- [22] In the spin-flop phase, however, such a feature would be hardly visible if appearing below  $T \sim 5$  K.
- [23] J.Werner, C. Koo, R. Klingeler, A. N. Vasiliev, Y. A. Ovchenkov, [A. S. Polovkova, G. V. Raganyan, and E. A. Zvereva,](https://doi.org/10.1103/PhysRevB.94.104408) Phys. Rev. B **[94](https://doi.org/10.1103/PhysRevB.94.104408)**, [104408](https://doi.org/10.1103/PhysRevB.94.104408) [\(2016\)](https://doi.org/10.1103/PhysRevB.94.104408).
- [24] A. C. Phaff, C. H. W. Swüste, K. Kopinga, and W. J. M. de Jonge, [J. Phys. C](https://doi.org/10.1088/0022-3719/16/34/014) **[16](https://doi.org/10.1088/0022-3719/16/34/014)**, [6635](https://doi.org/10.1088/0022-3719/16/34/014) [\(1983\)](https://doi.org/10.1088/0022-3719/16/34/014).