Supercurrent in ferromagnetic Josephson junctions with heavy metal interlayers

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 \bigcirc (Received 5 March 2018; revised manuscript received 23 May 2018; published 12 June 2018)

The length scale over which supercurrent from conventional BCS, *s*-wave superconductors (*S*) can penetrate an adjacent ferromagnetic (*F*) layer depends on the ability to convert singlet Cooper pairs into triplet Cooper pairs. Spin-aligned triplet Cooper pairs are not dephased by the ferromagnetic exchange interaction and can thus penetrate an *F* layer over much longer distances than singlet Cooper pairs. These triplet Cooper pairs carry a dissipationless spin current and are the fundamental building block for the fledgling field of superspintronics. Singlet-triplet conversion by inhomogeneous magnetism is well established. Here, we describe an attempt to use spin-orbit coupling as an alternative mechanism to mediate singlet-triplet conversion in *S-F-S* Josephson junctions. We report that the addition of thin Pt spin-orbit-coupling layers in our Josephson junctions significantly increases supercurrent transmission, however the decay length of the supercurrent is not found to increase. We attribute the increased supercurrent transmission to Pt acting as a buffer layer to improve the growth of the Co *F* layer.

DOI: [10.1103/PhysRevB.97.214509](https://doi.org/10.1103/PhysRevB.97.214509)

I. INTRODUCTION

In nature there are very few examples of materials simultaneously exhibiting superconducting (*S*) and ferromagnetic (*F*) properties, due to the competition between the order parameters. Breakthroughs in materials engineering and nanolithography techniques in the last two decades have enabled the synthesis of artificial heterostructures, where two or more layers are in direct electronic contact, revealing a wealth of new physics at *S-F* interfaces [\[1–3\]](#page-6-0). Exploitation of this new physics has led to advances in the emerging field of superspintronics, which offers a new class of highly energy-efficient devices, most promisingly cryogenic memory elements based on ferromagnetic Josephson junctions [\[4–13\]](#page-6-0).

In the simplest case of a normal metal (*N*) in *S-N-S* Josephson junctions, the critical current of the junction (I_c) will decay slowly with increasing *N* thickness, on a typical length scale $\xi_N \approx 100$'s nm [\[14,15\]](#page-6-0). When the *N* layer is replaced by a ferromagnet, *S-F-S*, singlet Cooper pairs entering the *F* layer are dephased and gain an oscillatory term with *F* layer thickness, driven by the same physics as the predicted Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) state [\[15–19\]](#page-6-0). This oscillation results in a series of transitions from a zero to *π* ground-state phase difference across the Josephson junction. Experimentally, oscillations in I_c are observed with increasing *F* layer thickness [\[20,21\]](#page-6-0), typically over a length scale $\xi_F \approx$ 1–5 nm for a strong ferromagnet [\[22,23\]](#page-6-0). With the addition of spin-mixing layers on either side of the *F* layer, it is possible to create the so-called long-ranged triplet component (LRTC) [\[24,25\]](#page-6-0). Unlike singlet Cooper pairs, the LRTC is not dephased by the ferromagnet and can therefore penetrate further into the *F* layer than the singlet component, typically $\xi_{LRTC} \approx 10$'s– 100's nm [\[26–30\]](#page-6-0). Experimentally, the LRTC is generated reliably through the addition of *F', F"* ferromagnetic layers in *S-F'-F-F"-S* Josephson junctions, where *F', F"* have either intrinsic magnetic inhomogeneity (for example, Ho [\[27,28\]](#page-6-0)) or magnetic inhomogeneity which is engineered in multilayered structures [\[30–32\]](#page-6-0). It is known theoretically, however, that this spin-mixing layer need not be a ferromagnet and there are several proposals indicating that spin-orbit coupling can act as a source for the LRTC [\[33–](#page-6-0)[40\]](#page-7-0).

Two recent experimental reports study the *S*-*F* proximity effect with the addition of spin-orbit-coupling layers. Banerjee *et al.* measured the $T_c(H)$ characteristics of Nb/Pt(d_{Pt})/Co/Pt multilayers with $0 \leq d_{\text{Pt}} \leq 2 \text{ nm } [41]$ $0 \leq d_{\text{Pt}} \leq 2 \text{ nm } [41]$. The changes in $T_c(H)$ are attributed to spin-orbit coupling mediating singlet-to-triplet conversion. The results are presented in analogy to the triplet spin valve, where the presence of triplet correlations modifies the proximity effect, introducing measurable signatures in *Tc*(*H*) [\[42\]](#page-7-0). Jeon *et al.* study ferromagnetic resonance (FMR) in *N*_{SOC}/Nb/Py/Nb/*N*_{SOC} films, where the *N*_{SOC} layers (normal metals with strong spin-orbit coupling) are Ta, W, and Pt [\[43\]](#page-7-0). With the addition of N_{SOC} layers, an enhancement in the spin pumping into the Nb *S* layers is observed. This is the opposite behavior to what is expected for a superconductor and is attributed to the LRTC. It is clear that the presence of spin-orbit coupling plays an important role in both experiments.

In this work, we describe a different approach to generating the LRTC using a normal metal with strong spin-orbit coupling (N_{SOC}) in Josephson junctions. We compare the transport properties of two sets of Josephson junctions: *S-F-S* and *S*-*N*SOC-*F*-*N*SOC-*S*, where *S* is Nb, *F* is a Co/Ru/Co synthetic antiferromagnet (SAF), and N_{SOC} is Pt (which has been shown in previous works to have strong Rashba spin-orbit coupling with Co due to broken inversion symmetry $[44–46]$). It is our proposal that only the set of samples containing two *N*_{SOC} layers should display properties consistent with the generation of the LRTC. In *N*_{SOC}-containing samples, the decay of supercurrent transmitted through the *F* layer should

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FIG. 1. Magnetic hysteresis loops acquired at a temperature of 10 K, (a),(b) for *(S-F-S*)-type samples with the applied field oriented (a) in and (b) out of the sample plane, and (c),(d) for $[S-Pt(0.5)-F-Pt(0.5)-S]$ -type samples (c) in and (d) out of the sample plane. *F* is a Co(5)/Ru(0.6)/Co(5) multilayer in all cases. The diamagnetic contribution from the substrate has been subtracted and data are normalized by the saturated value of magnetization. Insets show the low-field switching.

take place over a longer length scale than in the non- N_{SOC} samples, which only contain the short-ranged supercurrent components (namely, singlet and $m_s = 0$ triplet Cooper pairs).

II. METHODS

The films are deposited using dc sputtering in a vacuum system with base pressure of 2×10^{-8} Torr and partial water pressure of 3×10^{-9} Torr after liquid-nitrogen cooling. The samples are grown on 0.5-mm-thick Si substrates which have a native oxide layer. A uniform 200 Oe magnetic growth field is applied to the substrates. Growth is performed at an approximate Ar pressure of 2 mTorr, at a typical growth rate of 0.4 nm s−¹ for Nb and 0.1–0.2 nm s−¹ for the other materials. Growth rates are calibrated using an *in situ* crystal film thickness monitor and checked by fitting to Keissig fringes obtained by low-angle x-ray reflectometry on reference samples. All layer thicknesses (in brackets) are in nm. The bottom superconducting electrode is a multilayer $[Nb(25)/A(2.4)]_3/Nb(20)$ which grows considerably smoother than single-layer Nb of comparable total thickness [\[47–49\]](#page-7-0). The bottom electrode, ferromagnetic layers, any normal-metal interlayers, and a capping bilayer Nb(5)/Au(15) are grown without breaking vacuum.

For electrical transport measurements, films are patterned into circular Josephson junctions of diameters 12, 24, and 48 *μ*m using standard photolithography and ion milling methods, described in a previous work [\[47\]](#page-7-0). Once the Josephson junctions are defined, the samples are returned to the dc sputtering system and the top Au(15) layer is ion milled *in situ*, thus recovering a very clean interface before depositing the top superconducting electrode Nb(150).

Magnetization loops of sister sheet film samples are measured using a Quantum Design Magnetic Property Measurement System (MPMS 3) at 10 K. X-ray diffraction (XRD) of sheet film samples is measured using a Bruker D8 diffractometer at room temperature. Electrical transport is performed using a conventional four-point-probe measurement configuration at 4.2 K, employing the low-noise electrical transport system described in Ref. [\[10\]](#page-6-0). Our system can resolve 6 pV, which is taken as a resolution limit where appropriate. For all transport measurements, the field is applied parallel to the sample's plane, and samples are measured in the as-grown magnetic state (which is set by the growth field).

III. MAGNETIC CHARACTERIZATION

The magnetization versus field data are shown in Fig. 1 for *S-F-S* [Figs. 1(a) and 1(b)] and *S-N*_{SOC}-*F-N*_{SOC}-*S* [Figs. 1(c) and $1(d)$] samples at 10 K, where *F* is a Co(5)/Ru(0.6)/Co(5) multilayer in all cases and N_{SOC} is Pt(0.5). The choice of Pt thickness here is dictated by the transport measurements to follow. Both samples behave as synthetic antiferromagnets (SAFs). The application of an applied field in-plane [Figs. $1(a)$] and $1(c)$] causes a spin-flop transition and then rotates the magnetizations into the direction of the applied field, saturating at about 5 kOe. Removing the field causes the Co layers in the SAF to relax antiparallel with respect to each other and perpendicular with respect to the applied field, hence zero remanent magnetization is observed. The spin-flop transition in similar samples was confirmed in previous work by polarized neutron reflectometry $[50]$. In Fig. [1\(c\),](#page-1-0) the addition of the Pt(0.5) interlayers has caused a slight reduction in the low-field susceptibility, between about -1 and 1 kOe (highlighted in the figure inset). This implies that there are magnetic phases present with different coercivities, which we can understand if the surface moments couple with the Pt layer, modifying the local anisotropy of the Co/Pt interface. Or, alternatively, this may be a direct signature of the spin-flop transition in this sample.

The addition of Pt at the Co interface may induce an additional out-of-plane magnetic anisotropy [\[51\]](#page-7-0). The response of both samples to an out-of-plane applied field, as shown in Figs. $1(b)$ and $1(d)$, indicates that the magnetic anisotropy of our samples lies predominantly in-plane as very little out-of-plane remanent magnetization is observed. The sample containing Pt interlayers may have a small out-of-plane component, shown in Fig. $1(d)$ and inset. This is not surprising given the thickness of the Co and Pt layers in this study compared to the previous work of Shepley *et al.* [\[52\]](#page-7-0), where an out-of-plane magnetic anisotropy is achieved for Pt thickness of 2.5 nm and corresponding Co thicknesses in the range 0.85–1.0 nm. The reorientation transition from predominant out-of-plane to in-plane magnetic anisotropy is found at Co thickness of 1.1 nm [\[52\]](#page-7-0).

We do not expect the slight differences in magnetic switching between samples with and without Pt interlayers (Fig. [1\)](#page-1-0) to affect our transport measurements, which are performed in the as-grown magnetic state.

IV. ELECTRICAL TRANSPORT

Typical I-V curves and Fraunhofer *Ic* (*B*) patterns for each Josephson junction size along with the collated *ARN* (area times the normal-state resistance) are shown in the Supplemental Material [\[53\]](#page-7-0).

A. *S***-Pt(***d***Pt)-Co(5)/Ru(0.6)/Co(5)-Pt(***d***Pt)-***S*

We first consider the transport characteristics of the set of samples $S-Pt(d_{Pt})-Co(5)/Ru(0.6)/Co(5)-Pt(d_{Pt})-S$, where $d_{\text{Pt}} = 0-3.5$ nm. A total Co thickness of 10 nm is chosen as it is known from previous works to be a thickness where LRTC and non-LRTC samples show obvious difference in *Ic* (approximately an order of magnitude) [\[30\]](#page-6-0). Figure 2 shows the result of this study, where characteristic junction voltage $I_c R_N$ (the product of the maximum measured I_c in the Fraunhofer pattern times normal-state resistance) is plotted for a series of samples with increasing d_{Pt} . Without the Pt, our Josephson junctions have an expected small $I_c R_N$. With the addition of $d_{\text{Pt}} = 0.5$ nm (less than two monolayers), we see a large enhancement in I_c and no change in R_N , increasing the characteristic junction voltage by approximately an order of magnitude. This high $I_c R_N$ remains approximately constant for

FIG. 2. Product of critical current times normal-state resistance vs Pt interlayer thickness (d_{Pt}) for Josephson junctions of the form *S*-Pt(*d*Pt)-Co(5)/Ru(0.6)/Co(5)-Pt(*d*Pt)-*S*. Each data point represents one Josephson junction and the uncertainty in determining $I_c R_N$ is smaller than the data points.

 $d_{\text{Pt}} = 1.0$ nm Pt interlayers, but for increasing Pt thicknesses beyond this, there is a sharp drop in $I_c R_N$, where the critical current of our Josephson junctions appears to fall back towards the value without any Pt.

B. $S-Pt(0.5)-Co(d_{Co}/2)/Ru(0.6)/Co(d_{Co}/2)-Pt(0.5)-S$

With a fixed Pt thickness of 0.5 nm, guided by Fig. 2, we next vary the thickness of the *F* layer in $S-Pt(0.5)-Co(d_{Co}/2)/Ru(0.6)/Co(d_{Co}/2)-Pt(0.5)-S$ and $S-Co(d_{Co}/2)/Ru(0.6)/Co(d_{Co}/2)$ -*S* samples to compare the decay length of the supercurrent with and without the Pt interlayer. For these samples, $I_c R_N$ as a function of total Co thickness d_{Co} is plotted in Fig. [3.](#page-3-0) Considering first the data for samples without Pt, where we expect to only have short-ranged supercurrent components inside the *F* layer, we observe the expected rapid decay in $I_c R_N$ [\[54\]](#page-7-0). Fitting to a simple exponential decay, the decay length is found to be 1.7 ± 0.2 nm. This decay length is longer than found in our previous study of a Co SAF, where the comparable samples have decay length 1.18 ± 0.05 nm [\[54\]](#page-7-0). The differences between this work and the previous work are discussed later. Samples thicker than $d_{\text{Co}} = 14$ nm were fabricated but show no measurable critical current.

The samples containing Pt(0.5) interlayers can be described in two regimes. In the Co thickness range $10 \leq d_{\text{Co}} \leq 16$ nm, the supercurrent is found to decay exponentially with decay length 1.73 ± 0.07 nm. This is identical within our experimental uncertainty to the decay length of samples without Pt interlayers and suggests that short-ranged supercurrent components dominate transport in our Josephson junctions. The $I_c R_N$ product for the Pt interlayer samples is, however, consistently about one order of magnitude higher than the samples without the Pt interlayer. This suggests that the Pt has a role in the transmission of these short-ranged supercurrent components.

Although the AR_N product of the $d_{\text{Co}} = 18$ nm Josephson junction appears consistent with the other samples measured in

FIG. 3. Product of critical current times normal-state resistance vs total Co thickness (d_{Co}) for Josephson junctions of the following forms: *S*-Pt(0.5)-Co($d_{Co}/2$)/Ru(0.6)/Co($d_{Co}/2$)-Pt(0.5)-*S* (blue triangles) and *S*-Co($d_{Co}/2$)/Ru(0.6)/Co($d_{Co}/2$)-*S* (red inverted triangles). Each data point represents one Josephson junction and where no error bars are shown, the uncertainty in determining $I_c R_N$ is smaller than the data point. The lines are fits to simple exponential decay in the range $8 \leq d_{\text{Co}} \leq 16$ nm, with decay lengths of 1.73 ± 0.07 and 1.7 ± 0.2 nm, respectively.

this work, we believe this data point to be an anomaly. The other five Josephson junctions on this substrate showed electrical shorts when measured, indicating a failure in the lithographic processing. Samples showing electrical shorts were rejected from this study. A junction with an electrical short does not display the characteristic Fraunhofer $I_c(B)$ pattern, rather the *Ic* is found to decay monotonically with *B* (it is not a Josephson junction). While it is included in Fig. 3 for completeness, the $d_{\text{Co}} = 18$ nm sample is not used in the analysis of decay lengths. A second reason for rejecting samples in this study is when the AR_N product is considerably outside of the spread of *AR_N*, presented in Fig. [1](#page-1-0) of the Supplemental Material [\[53\]](#page-7-0). This only happened on one set of samples which had increased R_N , where the microscope later revealed residual resist in the area of the junctions. A $d_{\text{Co}} = 8$ nm sample containing Pt(0.5) interlayers did not survive fabrication processing.

In the second regime, upon increasing the Co thickness further, it is found that unlike the samples without Pt, a small residual supercurrent is observable in Josephson junctions with Co thickness $d_{\text{Co}} = 20$ and $d_{\text{Co}} = 24$ nm. The $d_{\text{Co}} = 20$ nm sample produces a clear critical current and Fraunhofer pattern, giving us confidence that the $I_c R_N$ of this sample is well above what is expected from the decay of short-ranged supercurrent components, depicted by the blue line. The $d_{\text{Co}} = 24 \text{ nm}$ sample shows some evidence for nonzero critical current; however, the Fraunhofer pattern is not well defined and the $I_c R_N$ product is at the resolution of our instrument (approximately 6 pV), leading to a large uncertainty in this value. We have included data from the $d_{\text{Co}} = 20$ and 2[4](#page-4-0) nm samples in Fig. 4 of the Supplemental Material [\[53\]](#page-7-0). The decay length in this regime (where short-ranged supercurrent components are vanishingly small) appears much longer, but we do not have enough data points to place a meaningful quantitative value on the decay.

C. Control samples

As a first control measurement, we consider the properties of a set of samples where we replace the Pt interlayer with a normal metal *N*, Cu. Cu is not expected to contribute much to spin-orbit coupling in our system and the supercurrent carrying properties of Cu are well characterized. It is known that supercurrent decay through Cu is very slow due to to the long electron mean free path [\[14\]](#page-6-0). Additionally, Cu is already widely implemented as a normal-metal interlayer in *S-F* systems, where it is added into multilayer stacks as a buffer layer to improve growth conditions and to decouple multiple *F* layers where independent switching of each *F* layer is desirable $[54–56]$.

Figure [4](#page-4-0) includes $I_c R_N$ for the set of samples $S-Cu(d_{Cu})$ - $Co(5)/Ru(0.6)/Co(5)-Cu(d_{Cu})-S$, where $d_{Cu} = 0$, 0.5, and 2.5 nm (black diamonds). With no interlayer, once again a small $I_c R_N$ is observed. The slightly lower $I_c R_N$ of this sample set (compared to the previous sample set, blue triangles) is most likely a run-to-run variation between samples grown in different vacuum cycles. Adding 0.5 nm of Cu does not significantly improve the transmission of supercurrent through the *F* layer, unlike Pt. With an increase in Cu thickness to 2.5 nm, an increase in $I_c R_N$ to approximately the value of the Pt(0.5) interlayer samples is observed. This increase with thick Cu interlayers is expected from a previous work [\[54\]](#page-7-0) and is due to improved structural properties of the Co, a mechanism outlined further in Sec. V.

The next control samples are asymmetric Josephson junctions containing only one Pt(0.5) interlayer, shown as olive green stars in Fig. [4.](#page-4-0) We find that the interface on which the Pt is grown is of key importance to the observed increase in $I_c R_N$. When the Pt layer is grown only on the top interface $[S-Co(5)/Ru(0.6)/Co(5)-Pt(0.5)-S]$, a small *reduction* in $I_c R_N$ is observed. On the other hand, when the Pt layer is grown only on the bottom interface [*S*-Pt(0.5)-Co(5)/Ru(0.6)/Co(5)-*S*], a large *increase* in $I_c R_N$ is observed, almost recovering the value for the symmetric $Pt(0.5)$ samples (replotted blue triangles in Fig. [4\)](#page-4-0).

We also perform x-ray diffraction measurements on sheet films for each of the selected samples plotted in Fig. [4.](#page-4-0) We simplify the structure of the sheet films so the seed and capping layer is Nb(5) and remove the Ru layer to make the data interpretation easier. The main structural peak for the $Co(10)$ *F* layer is easily visible in the x-ray diffraction pattern and used to determine the Co *c*-plane spacing for each sample. We find that the interlayers used in this work subtly change the growth morphology of the Co layer. The $Pt(0.5)$ and $Cu(2.5)$ interlayers push the Co towards the bulk $fcc(111)$ phase, which corresponds to the Josephson junctions with highest $I_c R_N$. With no interlayers or with Cu(0.5) interlayers, the Co appears to contain a mixture of $fcc(111)$ and $hep(0001)$ phases, which corresponds to the Josephson junctions with lower $I_c R_N$. The asymmetric samples follow the same trend.

V. DISCUSSION

Direct evidence for the presence of a LRTC of superconductivity in a Josephson junction is the slower decay of $I_c R_N$ with increasing *F* layer thickness. This "smoking gun" is reliably

FIG. 4. Product of critical current times normal-state resistance (solid symbols) and Co *c*-plane spacing (open symbols) vs selected sample for the following: symmetric Josephson junctions containing no interlayers, two $Pt(0.5)$ interlayers, or two $Cu(0.5, 2.5)$ interlayers, and asymmetric Josephson junctions which contain only one Pt(0.5) interlayer. Each symbol corresponds to a set of samples grown in the same vacuum cycle, and our run-to-run variation in $I_c R_N$ is visible in the -*F*- only samples. All Josephson junctions contain a Co(5)/Ru(0.6)/Co(5) *F* layer. Each solid data point represents one Josephson junction and the uncertainty in determining $I_c R_N$ is smaller than the data points. The open symbols show the Co *c*-plane spacing obtained by x-ray diffraction measurements on sheet films described in the text.

observed in samples of the form *S-F'-F-F"-S*, where *F', F"* are aligned perpendicular to *F* [\[30–32\]](#page-6-0). This increase in supercurrent decay length is often (but not necessarily) accompanied by an increase in $I_c R_N$ for LRTC samples compared to non-LRTC samples for typical *F* layer thicknesses in experiments. In this work, for the Co thickness range $8 \leq d_{\text{Co}} \leq 16 \text{ nm}$, we observe an increase in $I_c R_N$ without the corresponding increase in decay length. We therefore do not believe the increased transmission of supercurrent into the Co layers for the thickness range $8 \leq d_{\text{Co}} \leq 16$ nm can be attributed to the presence of a LRTC generated by spin-orbit coupling.

For our Josephson junctions with Co thickness $d_{\text{Co}} = 20$ and $d_{\text{Co}} = 24$ nm, we measure a very small residual supercurrent. The measured $I_c R_N$ of these junctions is well above what is expected from the decay of short-ranged supercurrent components, shown as a blue line in Fig. [3.](#page-3-0) The decay length of superconductivity for these Co thicknesses appears to be much longer than for thinner Co. These observations offer the best evidence in this work that spin-orbit coupling can mediate the conversion of Cooper pairs to the LRTC. This residual supercurrent is many orders of magnitude lower than comparable samples with *F', F"* LRTC generating interlayers [\[30\]](#page-6-0). This suggests at a minimum that *if* we attribute these observations to spin-orbit coupling generating a LRTC, then the conversion efficiency of such a mechanism is poor. We must caution that the supercurrent observed in these junctions is only just above the resolution limit of our measurement apparatus.

We next address the values of $I_c R_N$ and supercurrent decay length obtained in this work compared to the previous work of Khasawneh *et al.*, which also considers the transmission of singlet supercurrent through a Co/Ru/Co SAF [\[54\]](#page-7-0). The reported $I_c R_N$ for samples containing no interlayers is approximately an order of magnitude lower in this work compared to the previous work. For Josephson junctions in this work containing either Cu(2.5) or Pt(0.5) interlayers, the $I_c R_N$ is also about an order of magnitude lower, compared to the Cu(5) interlayers of Khasawneh *et al.* The decay length inside the Co for the samples with no interlayers also differs, but in the opposite way to $I_c R_N$. In this work, the decay length is improved to 1.7 ± 0.2 nm compared to the previous study, which reports a decay length of 1.18 ± 0.05 nm. There are three main differences between the Josephson junctions in this work and those studied by Khasawneh *et al.* which could contribute to the lower $I_c R_N$ and longer decay length. First, this work uses the smoother $[Nb(25)/A1(2.4)]_3/Nb(20)$ multilayer and not the thick single-layer Nb(150) as a bottom electrode. One difference of note is that the multilayer has a reduced T_c (8.0 compared to 9.0 K). Second, the capping layers on the initial stack in this work are $Nb(5)/Au(15)$ compared to Nb(25)/Au(15) in the previous work. Third, when we introduce Cu here, we only study 0.5- and 2.5-nm-thick Cu interlayers, whereas in the previous work 5-nm-thick Cu is used. A more detailed comparison is made in the Supplemental Material [\[53\]](#page-7-0). In our future work, we will study these differences systematically, as this might have technological implications for superspintronic devices.

In the previous work of Khasawneh *et al.*, it is found that the addition of Cu(5) on either side of the Co/Ru/Co SAF increases the decay length of supercurrent from 1.18 ± 0.05 to 2.34 ± 0.08 nm, accompanied with an increase in $I_c R_N$ [\[54\]](#page-7-0). In that work, the improvement was attributed to Cu changing the growth characteristic of Co, improving the mean free path. Here, we are able to offer some additional insight into this result. We grow two thicknesses of Cu, i.e., 0.5 and 2.5 nm, and measure both the $I_c R_N$ of the Josephson junction and the Co *c*-plane spacing in corresponding sheet films. It is found that $Cu(0.5)$ interlayers are not thick enough to affect the growth characteristic of Co compared to the samples with no interlayers, and correspondingly no improvement in the transmission of supercurrent is observed (Fig. [4\)](#page-4-0). The Co c -plane spacings for both the Cu (0.5) sample and the no interlayer sample fall between the bulk fcc(111) and hcp(0001) values, which we interpret as the Co initially growing in an fcc phase, before relaxing to hcp. This is a known phenomena for Co and creates stacking faults and dislocations in the Co grains [\[57\]](#page-7-0). In previous high-resolution transmission electron microscopy studies, it was found that Cu will grow in a nonequilibrium bcc phase on bcc Nb for Cu thicknesses up to 1.2 nm [\[58–60\]](#page-7-0). In this bcc phase, the lattice parameter of Cu is 0.328 ± 0.007 nm (close to the bulk bcc Nb lattice parameter of 0.331 nm). This explains why the Cu(0.5) and no interlayer samples behave so similarity. It is possible that the presence of stacking faults and dislocations are responsible for the lower critical current in these samples.

Upon growing Cu(2.5) interlayers, we recover the higher $I_c R_N$ values also found for the Pt(0.5) interlayers samples. By 2.5 nm, the Cu has recovered fcc growth and the positive influence this has on the Co growth is observed in both the improved *IcRN* and *c*-plane spacing. From our XRD measurements, it is clear that both $Pt(0.5)$ and $Cu(2.5)$ interlayers have a similar effect on the growth characteristic of the Co layer (Fig. [4,](#page-4-0) open symbols). In these samples, the Co *c*-plane spacing recovers almost the bulk $fcc(111)$ value. This suggests two things: first, unlike Cu, Pt does not form a nonequilibrium bcc phase for very thin layers grown on bcc Nb $[61,62]$, and second, these fcc interlayers influence the growth of the Co removing the hcp growth phase from the grains. The improved supercurrent in these samples may be due to the lack of stacking faults and dislocations compared to the other samples. An important open question from this work is why the Cu(5) interlayers reported by Khasawneh *et al.* improve both $I_c R_N$ and the decay length of the supercurrent, while the $Pt(0.5)$ interlayers in this work improve only $I_c R_N$. Unfortunately, the structural characterizations performed here do not offer any insight into this question.

To further support our interpretation of the data, consider the asymmetric structures in Fig. [4.](#page-4-0) It is reasonable to assume that a seed layer preceding Co growth is most important to improve the growth condition and atomic structure of the Co. Figure [4](#page-4-0) shows that indeed a higher $I_c R_N$ is only observed in the asymmetric sample with the bottom Pt(0.5) interlayer only. The Co *c*-plane spacing of these samples follows the same trend with $I_c R_N$; however, it is a less definitive result compared to the other samples. It is interesting to note that to recover the highest $I_c R_N$ observed in this work requires both interlayers, and that a decrease in $I_c R_N$ is observed for asymmetric samples with only the top Pt(0.5) interlayer. These observations in *IcRN* and Co *c*-plane spacing suggest some importance of having uniform strain across the Josephson junction, but this hypothesis requires further study.

We next speculate why as the Pt layer is made thicker, the enhanced transmission of the supercurrent decreases towards the value with no Pt interlayer (Fig. [2\)](#page-2-0). We consider what happens to the number of Cooper pairs in the junction as the Pt interlayer is made thicker. This is described by the *S-N* proximity effect. For a metal such as Cu with a very long electron mean free path, the length scale of this proximity effect, *ξ*Cu, can be very long [\[14\]](#page-6-0). Therefore, in Cu interlayer samples, there is little loss of Cooper pairs from the *S-N* proximity effect. In Pt interlayer samples, the three important contributions to *ξ*Pt are the much shorter electron mean free path (compared to Cu), the role of the interfacial Rashba spin-orbit coupling, and the magnetic moment gained by Pt in proximity to Co [\[63,64\]](#page-7-0). The influence of the first may be studied in Josephson junctions containing only Pt; however, we expect the second and third to be more important in our experiment. The exact role of the spin-orbit coupling in our samples is unknown. A theoretical work on Josephson current through a diffusive normal wire with intrinsic Rashba spin-orbit coupling has been studied [\[65\]](#page-7-0), however it is difficult to know how to apply these results to our experiment. The Pt magnetization will contribute to spin-flip scattering, especially if structural roughness propagates into a magnetic roughness or there are competing interface anisotropies between Pt and Co. In any case, our results suggest that *ξ*Pt is short and hence any gain in supercurrent transmission from the addition of Pt interlayers will have to compete with the loss of Cooper pairs

Finally, we discuss our experiment in the context of theoretical predictions. Bergeret *et al.* consider singlet-triplet conversion in the presence of Rashba and/or Dresselhaus spin-orbit coupling [\[35\]](#page-6-0). They provide a criteria for generating the LRTC, namely, that the vector operator $[\hat{\mathcal{A}}_k, [\hat{\mathcal{A}}_k, h^a \sigma^a]]$ is *not* parallel to the exchange field operator $(h^x \sigma^x, h^y \sigma^y, h^z \sigma^z)$. They obtain the former in Eq. (67) of their work, which we simplify here for a metallic system (such as ours) with finite Rashba ($\alpha \neq 0$) and zero Dresselhaus ($\beta = 0$) contribution to the spin-orbit coupling as [\[35\]](#page-6-0)

from this *S-N* proximity effect.

$$
[\hat{\mathcal{A}}_k, [\hat{\mathcal{A}}_k, h^a \sigma^a]] = 4\alpha^2 (2h^x \sigma^x + h^y \sigma^y + h^z \sigma^z), \quad (1)
$$

where α is known in the literature as the Rashba constant and σ is the vector of the Pauli matrices. In other words, (1) has components $(2h^x, h^y, h^z)$. If the direction of the exchange field is perpendicular to the plane ($h^x \neq 0$, $h^y = h^z = 0$), then there is no LRTC as (1) is parallel to the exchange field. Equally, if $h^x = 0$ and $h^y = h^z \neq 0$ (in-plane magnetization), then there is no LRTC by the same logic. If h^x and at least one of h^y or h^z are nonzero, then $(2h^x, h^y, h^z)$ has a component perpendicular to the exchange field (h^x, h^y, h^z) , and hence the LRTC can be created.

To address this limitation, Bergeret *et al.* propose performing the experiment with a magnetization in-plane *F* layer fabricated into a current in-plane (lateral) Josephson junction, which they show can recover LRTC generation [\[35\]](#page-6-0). Lateral Josephson junctions containing half metals are well established [\[26,29,31\]](#page-6-0), however substituting transition-metal *F* layers into this geometry has proved experimentally difficult. Singlecrystal Co nanowires contacted by W electrodes display zero resistivity [\[66\]](#page-7-0) and, recently, a Josephson current has been passed laterally through Co disks when the separation between *S* electrodes is very small [\[67\]](#page-7-0). Polycrystalline Co wires show promise, however a zero-resistance state is not observed [\[68,69\]](#page-7-0). Jacobsen *et al.* suggest alternatively to use the current perpendicular-to-plane geometry (employed in this work) with a ferromagnetic alloy which has both in- and out-of-plane magnetization components together with a source of spin-orbit coupling [\[40\]](#page-7-0). This is closer to our experiment, where a small out-of-plane remanent magnetization is observed in Fig. [1\(d\).](#page-1-0) This out-of-plane anisotropy, however, is most likely limited to the Co/Pt interface as our samples have predominant in-plane anisotropy. This may explain why LRTC generation in our samples appears (at best) to be very poor. In future works, we will replace the Co/Ru/Co SAF with a multilayer such as $[Pd/Co]_n$ $[10]$, $[Pt/Co]_n$, or $[Ni/Co]_n$ $[70]$ where careful engineering of the layer thicknesses can promote the required canted magnetization [\[52\]](#page-7-0).

VI. CONCLUSIONS

The major conclusions of this work may be summarized as follows. The growth of 0.5 nm Pt interlayers in Josephson junctions containing Co/Ru/Co ferromagnetic layers significantly enhances the transmission of supercurrent through the junction. The origin of this enhanced transmission is believed to be primarily from the fcc Pt being an effective seed layer for the growth of fcc Co, which we confirm with complementary x-ray diffraction measurements. Although most of our junctions displayed a supercurrent decay length consistent with singlet superconductivity, for the thickest Co layers a small residual supercurrent is present which may have a longer decay length. This small residual supercurrent is the best evidence in this work for spin-obit coupling mediating singlet-triplet conversion.

The data associated with this paper are openly available from the University of Leeds data repository [\[71\]](#page-7-0).

ACKNOWLEDGMENTS

We thank G. Burnell and F. S. Bergeret for many helpful discussions, B. Bi for help with fabrication using the Keck Microfabrication Facility, and R. Loloee, J. Glick, and V. Aguilar for assistance with sample growth, fabrication, magnetometry, and transport measurements, particularly in the early stages of this project. This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie Action (MSCA-IF-GF Grant No. 743791-SUPERSPIN).

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